# Homework 4

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# Question 9.1

### Question 9.1

Using the same crime data set uscrime.txt as in Question 8.2, apply Principal Component Analysis and then create a regression model using the first few principal components. Specify your new model in terms of the original variables (not the principal components), and compare its quality to that of your solution to Question 8.2.

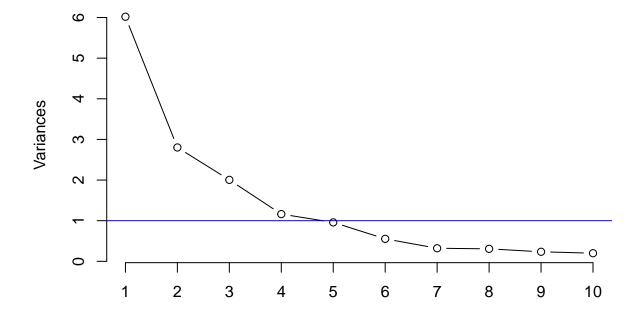
Answer: Using an estimation using both 4 and 5 PCAs(assumption based on scree plot), the results were worse than the original regression. This may be due to overtraining on the original regression.

```
setwd("D:/ernie/self-study/GTxMicroMasters/Introduction to Analytics Modeling/week4/homework")
library(tidyverse)
crime <- read.table("uscrime.txt",header = T) %>%
  data.frame()
#original model from 8.2 with 9 variables
model <- lm (data = crime , Crime ~ Ed + Ineq + LF + M + M.F +Po1 + Pop + Prob
summary(model)
##
## Call:
## lm(formula = Crime ~ Ed + Ineq + LF + M + M.F + Po1 + Pop + Prob +
##
       Time, data = crime)
##
## Residuals:
##
       Min
                10 Median
                                 3Q
                                        Max
                     -6.44
##
  -468.62 -100.73
                            139.91
                                     520.35
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
##
  (Intercept) -5189.5782
                           1460.9341
                                      -3.552 0.001063 **
## Ed
                 140.9730
                             57.8900
                                        2.435 0.019823 *
## Ineq
                  68.7477
                             15.8765
                                        4.330 0.000109 ***
                           1065.0117
## LF
                                      -0.572 0.570751
                -609.2340
## M
                  68.3357
                             35.3331
                                        1.934 0.060784 .
## M.F
                             15.2790
                                        1.169 0.249738
                  17.8666
## Po1
                 126.5215
                             17.3893
                                        7.276 1.22e-08 ***
                                      -0.513 0.610833
## Pop
                  -0.6526
                              1.2716
## Prob
               -4006.6838
                           2033.8562
                                      -1.970 0.056359
                              6.6248
                                        0.270 0.788995
## Time
                   1.7858
```

```
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 213.8 on 37 degrees of freedom
## Multiple R-squared: 0.7543, Adjusted R-squared: 0.6945
## F-statistic: 12.62 on 9 and 37 DF, p-value: 7.275e-09
pca <- prcomp(formula = ~ So + Ed + Ineq + LF + M + M.F +Po1 + Pop + Prob + Time + Po2 + NW + U1 +U
pca
## Standard deviations (1, .., p=15):
    [1] 2.45335539 1.67387187 1.41596057 1.07805742 0.97892746 0.74377006
    [7] 0.56729065 0.55443780 0.48492813 0.44708045 0.41914843 0.35803646
## [13] 0.26332811 0.24180109 0.06792764
##
## Rotation (n x k) = (15 \times 15):
##
                           PC1
                                             PC2
                                                                  PC3
                                                                                    PC4
                                                                                                      PC5
## So
              0.12061130
## Ed
                0.33962148 - 0.21461152 - 0.0677396249 - 0.07974375
                                                                                            0.02442839
              -0.36579778 0.02752240 0.0002944563 0.08066612
## Ineq
                                                                                            0.21672823
## LF
                0.17617757 - 0.31943042 - 0.2715301768 0.14326529
                                                                                            0.39407588
## M
               -0.30371194 -0.06280357 -0.1724199946 0.02035537
                                                                                            0.35832737
## M.F
                0.57877443
## Po1
                0.23527680
                0.11307836 0.46723456 -0.0770210971 0.03210513
## Pop
                                                                                           0.08317034
              ## Prob
## Time
              0.14764767
## Po2
                \hbox{-0.29358647} \quad \hbox{0.22801119} \ \hbox{-0.0788156621} \ \hbox{-0.23925971}
## NW
                                                                                            0.36079387
## U1
                0.04050137 - 0.00807439 \ 0.6590290980 \ 0.18279096
                                                                                            0.13136873
## 112
                ## Wealth 0.37970331 0.07718862 -0.0100647664 -0.11781752 -0.01167683
                            PC6
                                              PC7
                                                                PC8
                                                                                   PC9
##
                                                                                                   PC10
                                                                                                                     PC11
               -0.100500743 0.19649727 -0.22734157
                                                                       0.65599872 -0.06141452 -0.23397868
## So
## Ed
              -0.008571367 \ -0.23943629 \ \ 0.14644678 \ \ 0.44326978 \ -0.51887452 \ \ 0.11821954
                0.272027031 \quad 0.37483032 \ -0.07184018 \quad 0.02494384 \quad 0.01390576 \quad 0.18278697
## Ineq
                0.504234275 \ -0.15931612 \ -0.25513777 \ -0.14393498 \ -0.03077073 \ -0.385328279 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.03077073 \ -0.0307707073 \ -0.0307707073 \ -0.0307707070 \ -0.0307707070 \ -0.03077070 \ -0.03077070 \ -0.03077070 \ -0.03077070 \ -0.03077070 \ -0.03077070 \ -0.03077070 \ -0.03077070 \ -0.03077070 \ -0.03077070 \ -0.03077070 \ -0.03077070 \ -0.030770 \ -0.030770 \ -0.030770 \ -0.030770 \ -0.030770 \ -0.030770 \ -0.030770 \ -0.030770 \ -0.030770 \ -0.030770 \ -0.030770 \ -0.030770 \ -0.030770 \ -0.030770 \ -0.030770 \ -0.030770 \ -0.030770 \ -0.030770 \ -0.030770 \ -0.030770 \ -0.030770 \ -0.030770 \ -0.030770 \ -0.030770 \ -0.030770 \ -0.030770 \ -0.030770 \ -0.030770 \ -0.030770 \ -0.030770 \ -0.030770 \ -0.030770 \ -0.030770 \ -0.030770 \ -0.030770 \ -0.030770 \ -0.030770 \ -0.030770 \ -0.030770 \ -0.030770 \ -0.03070 \ -0.03070 \ -0.03070 \ -0.03070 \ -0.03070 \ -0.03070 \ -0.03070 \ -0.03070 \ -0.03070 \ -0.03070 \ -0.03070 \ -0.03070 \ -0.03070 \ -0.03070 \ -0.03070 \ -0.03070 \ -0.03070 \ -0.03070 \ -0.03070 \ -0.03070 \ -0.03070 \ -0.03070 \ -0.03070 \ -0.03070 \ -0.03070 \ -0.03070 \ -0.03070 \ -0.03070 \ -0.03070 \ -0.03070 \ -0.03070 \ -0.03070 \ -0.03070 \ -0.03070 \ -0.03070 \ -0.03070 \ -0.03070 \ -0.03070 \ -0.03070 \ -0.03070 \ -0.03070 
## LF
## M
               -0.449132706 -0.15707378 0.55367691 -0.15474793 0.01443093 -0.39446657
              -0.074501901 0.15548197 0.05507254 0.24378252 0.35323357 0.28029732
## M.F
## Po1
              -0.095776709 0.08011735 -0.04613156 -0.19425472 0.14320978 0.13042001
## Pop
                0.547098563 0.09046187 0.59078221
                                                                       0.20244830 0.03970718 -0.05849643
## Prob
                0.283535996 -0.56159383 0.08598908 0.05306898 0.42530006 0.08978385
## Time
              -0.148203050 -0.44199877 -0.19507812 0.23551363 0.29264326 0.26363121
## Po2
              -0.119524780 0.09518288 -0.03168720 -0.19512072 0.05929780 0.13885912
## NW
                0.051219538 -0.31154195 -0.20432828 -0.18984178 -0.49201966
                0.017385981 \ -0.17354115 \quad 0.20206312 \ -0.02069349 \ -0.22765278 \quad 0.17857891
## U1
## U2
                0.048155286 \ -0.07526787 \ -0.24369650 \ -0.05576010 \ \ 0.04750100 \ -0.47021842
## Wealth -0.154683104 -0.14859424 -0.08630649
                                                                      0.23196695 0.11219383 -0.31955631
##
                         PC12
                                           PC13
                                                              PC14
                                                                                   PC15
## So
                0.05753357 -0.29368483 0.29364512 0.0084369230
              ## Ed
## Ineq
              -0.43762828 -0.12181090 -0.59279037 0.0177570357
## LF
               -0.02705134 -0.27742957 0.15385625
                                                                      0.0336823193
## M
              -0.16580189 -0.05142365 -0.04901705
                                                                     0.0051398012
## M.F
```

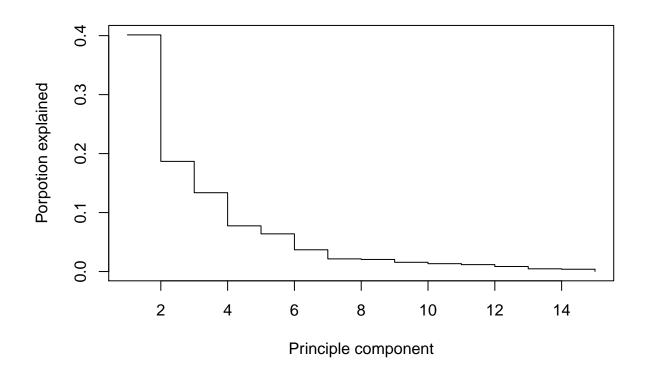
```
## Po1
        -0.22611207 -0.18592255 0.09490151 -0.6894155129
## Pop
         ## Prob
        -0.15567100 -0.03547596 -0.04761011 0.0293376260
        -0.13536989 -0.05738113 0.04488401 0.0376754405
## Time
## Po2
        -0.19088461 -0.13454940 0.08259642 0.7200270100
         ## NW
## U1
         0.09314897 - 0.59039450 \ 0.02335942 \ 0.0111359325
## U2
        -0.28440496 0.43292853 0.03985736 0.0073618948
## Wealth 0.32172821 -0.14077972 -0.70031840 -0.0025685109
#Plotting Scree plot
# Kaiser eigenvalue-greater-than-one rule
Scree <- plot(pca,</pre>
            type="line",
            main="Scree Plot for crime factors")%>%
            abline(h=1, col="blue")
```

# **Scree Plot for crime factors**

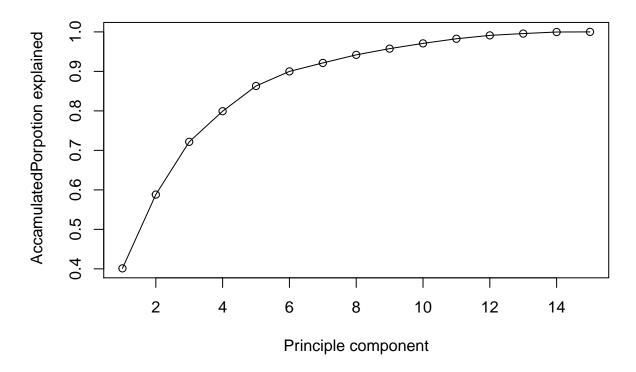


# Calculate and Plot the variances and proportion of variances

```
var <- pca$sdev^2</pre>
propvar <- var/sum(var)</pre>
#plotting
```



acc.por.explained <- plot(cumsum(propvar) , xlab = "Principle component" , ylab = " AccamulatedPorpotion")</pre>



```
#choose 4 new variables(variance > 1)
pca.chosen <- pca$x[, 1:4]
pca.chosen</pre>
```

```
PC2
                                     PC3
             PC1
                                                  PC4
##
      -4.1992835
                  1.09383120
                              1.11907395 -0.67178115
       1.1726630 -0.67701360
                              0.05244634
                                          0.08350709
##
##
  3
      -4.1737248 -0.27677501
                              0.37107658 -0.37793995
                  2.57690596 -0.22793998 -0.38262331
## 4
       3.8349617
## 5
       1.8392999 -1.33098564 -1.27882805 -0.71814305
##
       2.9072336
                  0.33054213 -0.53288181 -1.22140635
##
       0.2457752
                  0.07362562 0.90742064 -1.13685873
                  1.35985577 -0.59753132 -1.44045387
      -0.1301330
      -3.6103169
                  0.68621008 -1.28372246 -0.55171150
       1.1672376 -3.03207033 -0.37984502
                                           0.28887026
## 11
       2.5384879
                  2.66771358 -1.54424656
                                           0.87671210
       1.0065920
                  0.06044849 -1.18861346
       0.5161143 -0.97485189 -1.83351610
                                           1.59117618
       0.4265556 -1.85044812 -1.02893477
                                           0.07789173
  15 -3.3435299 -0.05182823
                              1.01358113 -0.08840211
  16 -3.0310689
                  2.10295524
                              1.82993161 -0.52347187
## 17 -0.2262961 -1.44939774
                              1.37565975 -0.28960865
  18 -0.1127499
                  0.39407030
                              0.38836278 -3.97985093
  19
       2.9195668
                  1.58646124 -0.97612613 -0.78629766
  20
       2.2998485
                  1.73396487
                              2.82423222
                                           0.23281758
## 21
       1.1501667 -0.13531015 -0.28506743
                                          2.19770548
```

```
## 22 -5.6594827 1.09730404 -0.10043541 0.05245484
## 23 -0.1011749 0.57911362 -0.71128354 0.44394773
## 24 1.3836281 -1.95052341 2.98485490 0.35942784
## 25 0.2727756 -2.63013778 -1.83189535 -0.05207518
## 26 4.0565577 -1.17534729 0.81690756 -1.66990720
## 27 0.8929694 -0.79236692 -1.26822542 0.57575615
## 28 0.1514495 -1.44873320 -0.10857670 0.51040146
## 29 3.5592481 4.76202163 -0.75080576 -0.64692974
## 30 -4.1184576  0.38073981 -1.43463965 -0.63330834
## 31 -0.6811731 -1.66926027 2.88645794 1.30977099
## 32 1.7157269 1.30836339 0.55971313 0.70557980
## 33 -1.8860627 -0.59058174 -1.43570145 -0.18239089
## 34 1.9526349 -0.52395429 0.75642216 -0.44289927
## 35 1.5888864 3.12998571 1.73107199 1.68604766
## 36 1.0709414 1.65628271 -0.79436888 1.85172698
## 37 -4.1101715 -0.15766712 -2.36296974
                                         0.56868399
## 38 -0.7254706 -2.89263339 0.36348376 0.50612576
## 39 -3.3451254 0.95045293 -0.19551398 0.27716645
## 40 -1.0644466 1.05265304 -0.82886286 0.12042931
      1.4933989 -1.86712106 -1.81853582
                                         1.06112429
## 42 -0.6789284 -1.83156328 1.65435992 -0.95121379
## 43 -2.4164258   0.46701087 -1.42808323 -0.41149015
## 44  2.2978729  -0.41865689  0.64422929
                                        0.63462770
## 45 -2.9245282 1.19488555 3.35139309
                                         1.48966984
## 46 1.7654525 -0.95655926 -0.98576138 -1.05683769
## 47 2.3125056 -2.56161119 1.58223354 -0.59863946
#Combining PCAs with crime
new.crime <- cbind(pca.chosen, crime[,16]) %>%
  data.frame()
colnames(new.crime)[5] <- "Crime"</pre>
new.model <- lm ( Crime ~ PC1 + PC2 + PC3 + PC4 ,data = new.crime )</pre>
summary(new.model)
##
## Call:
## lm(formula = Crime ~ PC1 + PC2 + PC3 + PC4, data = new.crime)
##
## Residuals:
##
      Min
               1Q Median
                               30
                                      Max
## -557.76 -210.91 -29.08 197.26 810.35
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
                            49.07 18.443 < 2e-16 ***
## (Intercept)
                905.09
## PC1
                 65.22
                            20.22
                                    3.225 0.00244 **
## PC2
                 70.08
                            29.63
                                    2.365 0.02273 *
## PC3
                -25.19
                            35.03 -0.719 0.47602
                            46.01 -1.509 0.13872
## PC4
                -69.45
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 336.4 on 42 degrees of freedom
## Multiple R-squared: 0.3091, Adjusted R-squared: 0.2433
## F-statistic: 4.698 on 4 and 42 DF, p-value: 0.003178
```

```
#Transforming new data back to original variable
PCAs <- new.model$coefficients[2:5]
intercept <- new.model$coefficients[1]</pre>
original <- pca$rotation[,1:4] %*% PCAs
original
##
                [,1]
## So
           10.223091
## Ed
           14.352610
## Ineq
          -27.536348
          -14.005349
## LF
## M
          -21.277963
## M.F
          -24.437572
## Po1
           63.456426
           39.830667
## Pop
## Prob
            3.295707
## Time
           -6.612616
## Po2
           64.557974
## NW
           15.434545
## U1
          -27.222281
## U2
            1.425902
## Wealth 38.607855
PCAs
                              PC3
##
         PC1
                   PC2
                                        PC4
## 65.21593 70.08312 -25.19408 -69.44603
These are the variables used, expressed in original form.
# un-scaling data
origi.var <- original/sapply(crime[,1:15],sd)</pre>
origi.inter <- intercept - sum(original*sapply(crime[,1:15],mean)/sapply(crime[,1:15],sd))
origi.var
##
                   [,1]
## So
             8.13445978
## Ed
            29.96524916
## Ineq
           -24.61459872
## LF
            -4.71259516
## M
            -7.60978529
## M.F
          -604.71355665
## Po1
            21.53447549
## Pop
             1.04621551
## Prob
             0.32050426
## Time
          -366.78104113
            76.44113075
## Po2
## NW
             0.01599585
            -6.82330056
## U1
## U2
            62.71293220
            5.44778133
## Wealth
```

```
#Trying with 5 PCAs
#choose 4 new variables(variance > 1)
pca.chosen2 <- pca$x[, 1:5]
pca.chosen2</pre>
```

```
##
            PC1
                       PC2
                                   PC3
                                              PC4
                                                          PC5
     -4.1992835
                 1.09383120
                            1.11907395 -0.67178115 -0.055283376
      1.1726630 -0.67701360
                           0.05244634 0.08350709 1.173199821
     -4.1737248 -0.27677501 0.37107658 -0.37793995 -0.541345246
## 4
      3.8349617
                2.57690596 -0.22793998 -0.38262331 1.644746496
## 5
      1.8392999 -1.33098564 -1.27882805 -0.71814305 -0.041590320
## 6
      ## 7
      ## 8
     -0.1301330
                1.35985577 -0.59753132 -1.44045387
                                                   0.222781388
## 9
     -3.6103169
                0.68621008 -1.28372246 -0.55171150
                                                   0.324292990
     1.1672376 -3.03207033 -0.37984502 0.28887026 0.646056610
      2.5384879
                2.66771358 -1.54424656 0.87671210 0.324083561
## 12
      1.0065920
                0.06044849 -1.18861346
                                       1.31261964 -0.358087724
      0.5161143 -0.97485189 -1.83351610
  13
                                      1.59117618 -0.599881946
      0.4265556 - 1.85044812 - 1.02893477 0.07789173 - 0.741887592
## 15 -3.3435299 -0.05182823 1.01358113 -0.08840211 -0.002969448
## 16 -3.0310689
                2.10295524
                           1.82993161 -0.52347187
                                                   0.387454246
## 17 -0.2262961 -1.44939774 1.37565975 -0.28960865 -1.337784608
## 18 -0.1127499 0.39407030
                           0.38836278 -3.97985093 -0.410914404
                1.58646124 -0.97612613 -0.78629766 -1.356288600
      2.9195668
                1.73396487 2.82423222
      2.2998485
                                       0.23281758
                                                   0.653038858
      1.1501667 -0.13531015 -0.28506743
                                      2.19770548 -0.084621572
## 22 -5.6594827 1.09730404 -0.10043541 0.05245484 0.689327990
## 23 -0.1011749 0.57911362 -0.71128354
                                       0.44394773 -0.689939865
## 24
      1.3836281 -1.95052341 2.98485490 0.35942784
                                                   0.744371276
      0.2727756 - 2.63013778 - 1.83189535 - 0.05207518 - 0.803692524
      4.0565577 -1.17534729 0.81690756 -1.66990720 2.895110075
      0.8929694 -0.79236692 -1.26822542 0.57575615 -1.830793964
      0.1514495 -1.44873320 -0.10857670 0.51040146 1.023229895
  28
      3.5592481 4.76202163 -0.75080576 -0.64692974 -0.309946510
## 30 -4.1184576  0.38073981 -1.43463965 -0.63330834
                                                   0.254715638
## 31 -0.6811731 -1.66926027
                           2.88645794
                                       1.30977099
                                                   0.470913997
     1.7157269 1.30836339 0.55971313
                                       0.70557980 -0.331277622
## 33 -1.8860627 -0.59058174 -1.43570145 -0.18239089 -0.291863659
      1.9526349 -0.52395429 0.75642216 -0.44289927 -0.723474420
                3.12998571 1.73107199
                                       1.68604766 -0.665406182
      1.5888864
## 36
      1.0709414 1.65628271 -0.79436888
                                       1.85172698 -0.020031154
## 37 -4.1101715 -0.15766712 -2.36296974
                                       0.56868399 2.469679496
## 38 -0.7254706 -2.89263339 0.36348376
                                       0.50612576 -0.028157162
## 39 -3.3451254 0.95045293 -0.19551398
                                       0.27716645 -0.487259213
## 40 -1.0644466 1.05265304 -0.82886286 0.12042931 0.645884788
     1.4933989 -1.86712106 -1.81853582
                                       1.06112429 -0.009855774
## 42 -0.6789284 -1.83156328 1.65435992 -0.95121379 -2.115630145
## 43 -2.4164258   0.46701087 -1.42808323 -0.41149015   0.867397522
     2.2978729 -0.41865689 0.64422929 0.63462770 0.703116983
## 45 -2.9245282 1.19488555 3.35139309 1.48966984 -0.806659622
      1.7654525 -0.95655926 -0.98576138 -1.05683769 -0.542466034
      2.3125056 -2.56161119 1.58223354 -0.59863946 1.140712406
```

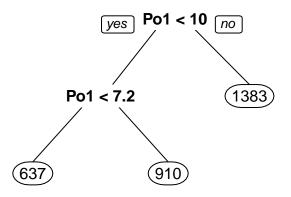
```
#Combining PCAs with crime
new.crime2 <- cbind(pca.chosen2, crime[,16]) %>%
  data.frame()
colnames(new.crime2)[6] <- "Crime"</pre>
new.model2 <- lm ( Crime ~ PC1 + PC2 + PC3 + PC4 + PC5 ,data = new.crime2 )
summary(new.model2)
##
## Call:
## lm(formula = Crime ~ PC1 + PC2 + PC3 + PC4 + PC5, data = new.crime2)
## Residuals:
##
      Min
               1Q Median
                                30
                                      Max
## -420.79 -185.01
                    12.21 146.24 447.86
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                905.09
                            35.59 25.428 < 2e-16 ***
## PC1
                 65.22
                            14.67
                                    4.447 6.51e-05 ***
## PC2
                 70.08
                            21.49
                                    3.261 0.00224 **
                            25.41 -0.992 0.32725
## PC3
                -25.19
## PC4
                -69.45
                            33.37 -2.081 0.04374 *
## PC5
                229.04
                            36.75
                                    6.232 2.02e-07 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 244 on 41 degrees of freedom
## Multiple R-squared: 0.6452, Adjusted R-squared: 0.6019
## F-statistic: 14.91 on 5 and 41 DF, p-value: 2.446e-08
```

### Question 10.1

Using the same crime data set uscrime.txt as in Questions 8.2 and 9.1, find the best model you can using(a) a regression tree model, and (b) a random forest model.

```
#Question 10.1
library(rpart)
library(rpart.plot)
library(randomForest)
library(caret)
library(modelr)
#CART
# set up train and testing split
train <- createDataPartition(crime$Crime, p = .85, list = F)</pre>
# set up test and train datasets
crime.train <- crime[train,]</pre>
crime.test <- crime[-train,]</pre>
# check splits
dim(crime.train); dim(crime.test)
## [1] 43 16
## [1] 4 16
```

```
#Regression Tree
crime.tree <- train(</pre>
  Crime ~ .,
  data = crime.train,
 method = 'rpart',
 trControl = trainControl(method = 'boot_all', number = 10),
 metric = 'RMSE'
)
## Warning in nominalTrainWorkflow(x = x, y = y, wts = weights, info = trainInfo, :
## There were missing values in the apparent performance measures.
## Warning in nominalTrainWorkflow(x = x, y = y, wts = weights, info = trainInfo, :
## There were missing values in resampled performance measures.
crime.tree$finalModel
## n = 43
##
## node), split, n, deviance, yval
        * denotes terminal node
## 1) root 43 6601051.0 910.2791
## 2) Po1< 10 32 1534630.0 747.8438
       4) Po1< 7.15 19 654085.2 637.2105 *
##
       5) Po1>=7.15 13 308103.2 909.5385 *
##
     3) Po1>=10 11 1765868.0 1382.8180 *
##
prp(crime.tree$finalModel)
```



```
#Random Forest
crime.forest <- train(</pre>
  Crime ~ .,
  data = crime.train,
  method = 'rf',
  trControl = trainControl(method = 'boot_all', number = 10),
  metric = 'RMSE')
crime.forest$finalModel
##
   randomForest(x = x, y = y, mtry = param$mtry)
##
##
                  Type of random forest: regression
##
                        Number of trees: 500
## No. of variables tried at each split: 8
##
##
             Mean of squared residuals: 82700.7
##
                       % Var explained: 46.13
#Testing
crime.res1 <- crime.test %>%
  add_predictions(., crime.tree) %>%
  select('observations' = Crime, pred) %>%
  as.data.frame()
crime.res2 <- crime.test %>%
  add_predictions(., crime.forest) %>%
  select('observations' = Crime, pred) %>%
```

```
as.data.frame()
crime.res1
##
      observations
                        pred
## 19
               750 1382.8182
## 28
              1216 909.5385
               923 909.5385
## 34
## 46
               508 1382.8182
crime.res2
##
      observations
                        pred
## 19
               750 1245.2786
## 28
              1216 993.0923
## 34
               923 1021.4021
## 46
               508 1131.4758
postResample(obs = crime.res1$observations, pred = crime.res1$pred)
          RMSE
                  Rsquared
                                    MAE
## 561.2186717
                 0.7287986 456.8898601
postResample(obs = crime.res2$observations, pred = crime.res2$pred)
##
          RMSE
                  Rsquared
                                    MAE
## 416.3513502
                 0.4659483 360.0160583
```

### Question 10.2

Describe a situation or problem from your job, everyday life, current events, etc., for which a logistic regression model would be appropriate. List some (up to 5) predictors that you might use.

I would consider logisite regession useful in predicting customer behavior on EC sites. The results would be buy (0) and don't buy(1). As for predictors, age, occupation, time spent on site would be considered good predictors.

# Question 10.3

Using the GermanCredit data set germancredit.txt, use logistic regression to find a good predictive model for whether credit applicants are good credit risks or not.

```
set.seed(101)
credit <- read.table("germancredit.txt", header = FALSE)</pre>
str(credit)
##
  'data.frame':
                    1000 obs. of 21 variables:
   $ V1 : chr
                "A11" "A12" "A14" "A11" ...
##
   $ V2 : int
               6 48 12 42 24 36 24 36 12 30 ...
##
   $ V3 : chr
                "A34" "A32" "A34" "A32" ...
   $ V4 : chr "A43" "A43" "A46" "A42" ...
##
##
   $ V5 : int 1169 5951 2096 7882 4870 9055 2835 6948 3059 5234 ...
##
   $ V6 : chr
                "A65" "A61" "A61" "A61" ...
                "A75" "A73" "A74" "A74" ...
##
   $ V7 : chr
##
   $ V8 : int
               4 2 2 2 3 2 3 2 2 4 ...
                "A93" "A92" "A93" "A93" ...
   $ V9 : chr
   $ V10: chr "A101" "A101" "A101" "A103" ...
```

```
## $ V11: int 4 2 3 4 4 4 4 2 4 2 ...
## $ V12: chr "A121" "A121" "A121" "A122" ...
## $ V13: int 67 22 49 45 53 35 53 35 61 28 ...
## $ V14: chr "A143" "A143" "A143" "A143" ...
## $ V15: chr "A152" "A152" "A152" "A153" ...
## $ V16: int 2 1 1 1 2 1 1 1 1 2 ...
## $ V17: chr "A173" "A173" "A172" "A173" ...
## $ V18: int 1 1 2 2 2 2 1 1 1 1 ...
   $ V19: chr "A192" "A191" "A191" "A191" ...
## $ V20: chr "A201" "A201" "A201" "A201" ...
## $ V21: int 1 2 1 1 2 1 1 1 1 2 ...
credit$V21[credit$V21==1] <- 0</pre>
credit$V21[credit$V21==2] <- 1</pre>
#Dividing data
credit.part <- createDataPartition(credit$V21, times = 1, p = 0.7, list=FALSE)</pre>
head(credit.part)
##
       Resample1
## [1,]
## [2,]
                2
## [3,]
                3
## [4,]
                4
## [5,]
               5
## [6,]
                6
credit.train <- credit[credit.part,]</pre>
credit.valid <- credit[-credit.part,]</pre>
#model
credit.log <- glm(V21 ~ ., data = credit.train, family=binomial(link="logit"))</pre>
summary(credit.log)
##
## Call:
## glm(formula = V21 ~ ., family = binomial(link = "logit"), data = credit.train)
## Deviance Residuals:
                    Median
##
      Min
                1Q
                                   3Q
                                           Max
## -2.6141 -0.6484 -0.3327 0.5806
                                        2.5401
##
## Coefficients:
                Estimate Std. Error z value Pr(>|z|)
##
## (Intercept) -3.569e-01 1.342e+00 -0.266 0.790318
               -2.958e-01 2.809e-01 -1.053 0.292252
## V1A12
## V1A13
              -5.582e-01 4.807e-01 -1.161 0.245532
## V1A14
              -1.507e+00 2.820e-01 -5.346
                                                9e-08 ***
## V2
               4.587e-02 1.215e-02 3.774 0.000160 ***
              8.164e-02 6.777e-01 0.120 0.904113
## V3A31
## V3A32
              -3.752e-01 5.371e-01 -0.699 0.484776
## V3A33
              -1.110e+00 5.813e-01 -1.909 0.056260 .
## V3A34
              -1.857e+00 5.579e-01 -3.329 0.000872 ***
## V4A41
              -1.848e+00 4.817e-01 -3.836 0.000125 ***
## V4A410
              -2.417e+00 9.679e-01 -2.497 0.012511 *
## V4A42
              -9.125e-01 3.323e-01 -2.746 0.006029 **
```

```
## V4A43
              -1.039e+00 3.116e-01 -3.334 0.000855 ***
              -8.163e-01 9.009e-01 -0.906 0.364883
## V4A44
## V4A45
              -3.390e-01 6.401e-01 -0.530 0.596388
## V4A46
               1.099e-01 4.737e-01
                                      0.232 0.816452
## V4A48
              -1.674e+00 1.210e+00 -1.384 0.166426
## V4A49
              -1.163e+00 4.208e-01 -2.764 0.005718 **
## V5
               1.454e-04 5.535e-05
                                     2.628 0.008594 **
## V6A62
              -1.776e-01 3.428e-01 -0.518 0.604336
## V6A63
               4.524e-01 4.577e-01
                                     0.988 0.322956
## V6A64
              -9.605e-01 6.456e-01 -1.488 0.136846
## V6A65
              -8.524e-01 3.235e-01 -2.635 0.008419 **
## V7A72
              -4.012e-01 5.588e-01 -0.718 0.472762
## V7A73
              -6.514e-01 5.339e-01 -1.220 0.222457
## V7A74
              -1.503e+00 5.815e-01 -2.585 0.009750 **
## V7A75
              -8.686e-01 5.445e-01 -1.595 0.110686
## V8
               3.831e-01
                          1.136e-01
                                      3.372 0.000747 ***
## V9A92
              -1.445e-01 5.564e-01
                                     -0.260 0.795099
## V9A93
              -6.374e-01 5.467e-01
                                    -1.166 0.243694
## V9A94
              -4.908e-01 6.419e-01 -0.765 0.444459
## V10A102
               3.868e-01 4.966e-01
                                     0.779 0.436073
## V10A103
              -5.953e-01 4.893e-01 -1.217 0.223718
## V11
              -2.731e-02 1.083e-01 -0.252 0.800898
## V12A122
                                      1.597 0.110233
               5.001e-01 3.131e-01
## V12A123
               2.743e-01 2.899e-01
                                      0.946 0.344022
## V12A124
               6.561e-01 5.220e-01
                                     1.257 0.208747
## V13
              -1.923e-02 1.155e-02 -1.665 0.095899
## V14A142
              -4.130e-01 5.260e-01 -0.785 0.432343
## V14A143
              -8.298e-01 2.938e-01 -2.824 0.004744 **
## V15A152
              -3.803e-01 2.869e-01 -1.326 0.184883
## V15A153
              -6.739e-01 5.884e-01 -1.145 0.252124
## V16
               7.446e-01
                          2.530e-01
                                      2.944 0.003245 **
## V17A172
               7.947e-01 8.275e-01
                                      0.960 0.336845
## V17A173
               5.865e-01
                          7.953e-01
                                      0.737 0.460850
## V17A174
               3.465e-01
                         8.183e-01
                                      0.423 0.671940
## V18
               1.495e-01
                          3.242e-01
                                      0.461 0.644658
              -3.794e-02 2.494e-01 -0.152 0.879062
## V19A192
## V20A202
              -1.223e+00 9.110e-01 -1.343 0.179377
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
      Null deviance: 848.32 on 699 degrees of freedom
## Residual deviance: 592.81 on 651 degrees of freedom
## AIC: 690.81
##
## Number of Fisher Scoring iterations: 5
#Confusion Matrix
creditPredict <- predict(credit.log, newdata=credit.valid[,-21], type="response")</pre>
Confusion.mat <- table(credit.valid$V21, round(creditPredict))</pre>
```

We can see that although sensitivity is quite high, Specifity isn't

```
Sensitivity <- Confusion.mat[1,1]/sum(Confusion.mat[1,])
Sensitivity

## [1] 0.8786408

Specfitity <-Confusion.mat[2,2]/sum(Confusion.mat[2,])
Specfitity
## [1] 0.4787234</pre>
```

Then we change the threshold

```
#setting second thresh hold
threshold <- 0.7
thres <- as.matrix(table(round(creditPredict > threshold), credit.valid$V21))
names(dimnames(thres)) <- c("Predicted", "Observed")
thres

## Observed
## Predicted 0 1
## 0 197 76
## 1 9 18</pre>
```

Below are the results for a different threshold, there is an obvious rise in specifity but also a slight loss in sensitivity.

```
Sensitivity2 <- thres[1,1]/sum(thres[1,])
Sensitivity2

## [1] 0.7216117

Specfitity2 <-thres[2,2]/sum(thres[2,])
Specfitity2</pre>
```

## [1] 0.6666667