Homework_3

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Question 7.1 Describe a situation or problem from your job, everyday life, current events, etc., for which exponential smoothing would be appropriate. What data would you need? Would you expect the value of (the first smoothing parameter) to be closer to 0 or 1, and why?

At my job the production of our product requires a lot of materials. We make diagnostic tests for food pathogens, so the amount of product we make on a monthly basis can be different based on the holiday season, time of farmer's harvest, or on random food outbreaks. If we could see the potential growth along with the seasonal need of each product, we can make sure we can secure the right amount of materials before we hit peaks in demand. We could use exponential smoothing with a alpha value closer to 0 because we tend to get a lot of randomness in the system due to random outbreaks or other factors like farmers needing to harvest quicker due to weather.

Question 7.2 Using the 20 years of daily high temperature data for Atlanta (July through October) from Question 6.2 (file temps.txt), build and use an exponential smoothing model to help make a judgment of whether the unofficial end of summer has gotten later over the 20 years. (Part of the point of this assignment is for you to think about how you might use exponential smoothing to answer this question. Feel free to combine it with other models if you'd like to. There's certainly more than one reasonable approach.)

To start I clear the environment, call the forecast package, then bring in the data.

3

```
rm(list = ls())
library(forecast)
## Registered S3 method overwritten by 'quantmod':
##
##
     as.zoo.data.frame zoo
library(stats)
temps_data <- read.table("C:/Users/phan_/Documents/R/temps.txt", stringsAsFactors = F, header = T)
head(temps_data)
##
       DAY X1996 X1997 X1998 X1999 X2000 X2001 X2002 X2003 X2004 X2005 X2006 X2007
                                                 84
                                                        90
## 1 1-Jul
               98
                      86
                             91
                                   84
                                          89
                                                               73
                                                                     82
                                                                            91
                                                                                   93
                                                                                         95
## 2 2-Jul
               97
                      90
                             88
                                   82
                                                 87
                                                        90
                                                                            89
                                                                                   93
                                                                                         85
                                          91
                                                               81
                                                                     81
## 3 3-Jul
               97
                      93
                             91
                                   87
                                          93
                                                 87
                                                        87
                                                               87
                                                                     86
                                                                            86
                                                                                   93
                                                                                         82
               90
                             91
                                   88
                                          95
## 4 4-Jul
                      91
                                                 84
                                                        89
                                                               86
                                                                     88
                                                                            86
                                                                                   91
                                                                                         86
## 5 5-Jul
               89
                      84
                             91
                                   90
                                          96
                                                 86
                                                        93
                                                               80
                                                                     90
                                                                            89
                                                                                   90
                                                                                         88
## 6 6-Jul
               93
                             89
                      84
                                   91
                                          96
                                                 87
                                                        93
                                                               84
                                                                     90
                                                                            82
                                                                                   81
                                                                                         87
##
     X2008 X2009 X2010 X2011 X2012 X2013 X2014
                                                    X2015
                                                 90
## 1
         85
               95
                      87
                             92
                                   105
                                          82
                                                        85
## 2
         87
               90
                      84
                             94
                                   93
                                          85
                                                 93
                                                        87
```

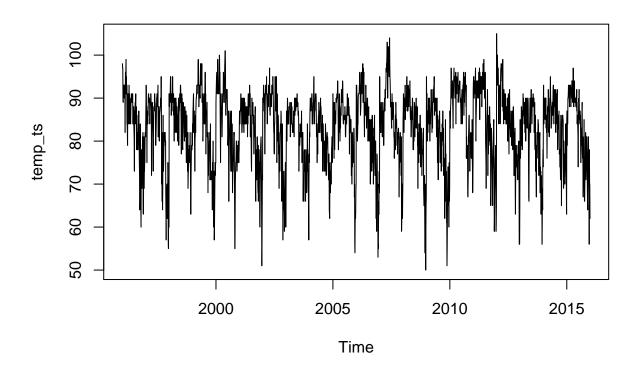
```
## 4
          90
                 91
                         85
                                92
                                        98
                                                77
                                                       84
                                                               85
## 5
          88
                 80
                         88
                                90
                                       100
                                                83
                                                       86
                                                              84
## 6
          82
                 87
                         89
                                        98
                                                83
                                                       87
                                                               84
```

DAY X1996 X1997 X1998 X1999 X2000 X2001 X2002 X2003 X2004 X2005 X2006 X2007 X2008 X2009 X2010 X2011 X20

 $11-Jul \ 98 \ 86 \ 91 \ 84 \ 89 \ 84 \ 90 \ 73 \ 82 \ 91 \ 93 \ 95 \ 85 \ 95 \ 87 \ 92 \ 105 \ 2 \ 2-Jul \ 97 \ 90 \ 88 \ 82 \ 91 \ 87 \ 90 \ 81 \ 81 \ 89 \ 93 \ 85 \ 87 \ 90 \ 84 \ 94 \ 93 \ 3 \ 3-Jul \ 97 \ 93 \ 91 \ 87 \ 87 \ 87 \ 86 \ 86 \ 93 \ 82 \ 91 \ 89 \ 83 \ 95 \ 99 \ 4 \ 4-Jul \ 90 \ 91 \ 91 \ 88 \ 95 \ 84 \ 89 \ 86 \ 88 \ 86 \ 91 \ 80 \ 90 \ 90 \ 88 \ 88 \ 90 \ 100 \ 6 \ 6-Jul \ 93 \ 84 \ 89 \ 91 \ 96 \ 87 \ 93 \ 84 \ 90 \ 82 \ 81 \ 87 \ 82 \ 87 \ 89 \ 90 \ 98 \ X2013 \ X2014 \ X2015 \ 1 \ 82 \ 90 \ 85 \ 2 \ 85 \ 93 \ 87 \ 3 \ 76 \ 87 \ 79 \ 4 \ 77 \ 84 \ 85 \ 5 \ 83 \ 86 \ 84 \ 68 \ 87 \ 84$

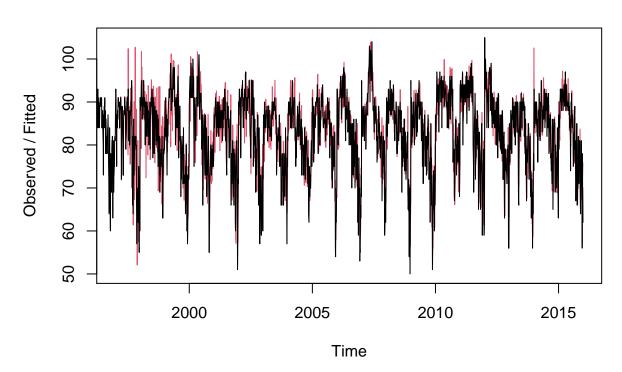
To create a time series I first only want the years and temperature of each day, I created a vector and unlisted the data to get all the atomic components, and also removed the first column as well. I created a time series object using ts, making the frequency 123 (days in the data set) and set the start point at 1996.

```
temp_vector <- as.vector(unlist(temps_data[,2:21]))
temp_ts <- ts(data = temp_vector, frequency = 123, start = 1996)
ts.plot(temp_ts)</pre>
```



Now we will use the Holtswinter model onto the timeseries data to help smooth it out. From how I understood from reading the details in the HoltWinters details page, the function will filter a timeseries and find the optimal values for our parameters, which is the default of the function. I just had to indicate that it is seasonality type, inserting the "multiplicitive" in the function. I was not sure if the seasonality was additive or multiplicitive, so I tried multiplicative first since the amplitude does not look too constant. You can see in the plot the red line represents the fitted values (xhat) of the model.

Holt-Winters filtering



summary(temp_holtw)

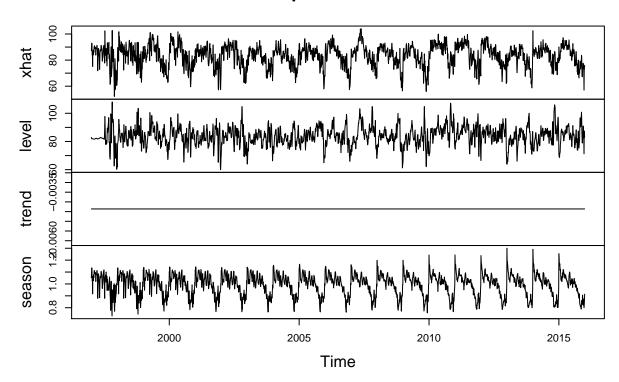
##		Length	Class	Mode
##	fitted	9348	mts	numeric
##	x	2460	ts	numeric
##	alpha	1	-none-	numeric
##	beta	1	-none-	numeric
##	gamma	1	-none-	numeric
##	${\tt coefficients}$	125	-none-	numeric
##	seasonal	1	-none-	${\tt character}$
##	SSE	1	-none-	numeric
##	call	6	-none-	call

fitted 9348 mts numeric x 2460 ts numeric alpha 1 -none- numeric beta 1 -none- numeric gamma 1 -none- numeric coefficients 125 -none- numeric seasonal 1 -none- character SSE 1 -none- numeric call 6 -none- call

when I looked at the fitted version of the filtered data, it confirmed the seasonality as multiplicative for me. You can see that for the season parameter, the amplitude is increasing as time passes, specifically around 2010. I noticed that trend seems to be a horizontal straight line, but that makes sense, the global temperature should be oscillating over time as the season changes, having minimal changes in yearly temperature change in terms of degrees, so there is not much change in trend and dampening needed there.

plot(temp_holtw\$fitted)

temp_holtw\$fitted



I then converted the smoothed data back into a matrix and gave the rows and columns back their names. I then exported the data as a csv so I could use excel to do cusum.

```
temps_holtw_smoothed <- matrix(temp_holtw$fitted[,1], nrow = 123)
head(temps_holtw_smoothed)</pre>
```

```
[,2]
##
            [,1]
                               [,3]
                                        [,4]
                                                 [,5]
                                                           [,6]
                                                                    [,7]
                                                                             [,8]
  [1,] 87.23653 65.04516 90.29613 83.39938 87.68863 78.07509 73.10059 87.27074
   [2,] 90.42182 84.87634 85.44878 86.44444 84.78855 86.02384 72.13247 85.01878
   [3,] 92.99734 89.61560 85.65942 92.85774 88.70570 90.23022 77.77739 82.68648
   [4,] 90.94030 88.47600 84.80741 91.55309 86.98750 87.27931 83.52416 83.37312
   [5,] 83.99917 83.11178 81.14293 88.80208 81.40681 86.06745 83.86090 83.64904
       84.04496 88.00054 85.21673 91.04477 81.83758 87.87757 78.93483 86.79140
##
                                                                   [,15]
            [,9]
                    [,10]
                              [,11]
                                       [,12]
                                                [,13]
                                                          [,14]
##
                                                                            [,16]
  [1,] 92.29714 78.50826 81.58696 84.72917 79.51855 86.74604 93.88371 82.30605
  [2,] 92.85614 88.18138 88.52648 80.39548 85.65722 81.47324 87.43846 92.55001
  [3,] 92.33884 92.43570 86.72311 84.53380 88.31357 82.29310 90.24836 91.18746
```

```
## [4,] 87.29596 92.69774 83.30574 89.62822 88.56597 82.90566 93.69353 95.13130
  [5,] 84.25223 90.58916 84.18954 89.27001 89.12501 80.92784 90.14667 94.60910
## [6,] 85.75665 86.91496 82.21750 84.28967 79.32562 84.52016 88.67069 96.75445
##
           [,17]
                     [,18]
                               [,19]
## [1,] 84.88750 102.54643 90.07756
## [2,] 76.18707
                  89.57468 85.16854
## [3.] 81.46207
                  88.15080 82.09161
## [4,] 76.56780
                  87.11605 79.49314
## [5,] 75.42085
                  85.20682 83.69666
## [6,] 78.42462 83.25423 82.08838
colnames(temps_holtw_smoothed) <- colnames(temps_data[,3:21])</pre>
rownames(temps_holtw_smoothed) <-temps_data[,1]</pre>
write.csv(temps_holtw_smoothed, file = "C:/Users/phan_/Documents/smoothed_temp_data.csv")
```

See the attached excel to see the cusum results. Based on the results the end of summer seems to not be really getting later according to the data. The end of summer just seems to be going up and down from year to year, not really having an upward trend or downward trend so far.

Question 8.1

Describe a situation or problem from your job, everyday life, current events, etc., for which a linear regression model would be appropriate. List some (up to 5) predictors that you might use.

A way to use regression is to find out how much rent varies in Seattle and I can compare it against the square footage of the place, how many rooms it has, distance from downtown Seattle, what part of Seattle, or age of the place.

Question 8.2

6 20.9995

682

Using crime data from http://www.statsci.org/data/general/uscrime.txt (file uscrime.txt, description at http://www.statsci.org/data/general/uscrime.html), use regression (a useful R function is lm or glm) to predict the observed crime rate in a city with the following data.

First I will clear the environment. Call the data and any packages I may be using.

```
rm(list = ls())
set.seed(1)
library(ggplot2)
crime_data <- read.table("C:/Users/phan_/Documents/R/uscrime.txt", stringsAsFactors = F, header = T)</pre>
View(crime data)
head(crime_data)
##
               Ed
                  Po1
                        Po2
                                LF
                                     M.F Pop
                                               NW
                                                     U1 U2 Wealth Ineq
                                                                             Prob
## 1 15.1
              9.1
                   5.8
                        5.6 0.510
                                    95.0
                                          33 30.1 0.108 4.1
                                                               3940 26.1 0.084602
           1
           0 11.3 10.3
                        9.5 0.583 101.2
## 2 14.3
                                          13 10.2 0.096 3.6
                                                               5570 19.4 0.029599
## 3 14.2
           1 8.9
                  4.5
                        4.4 0.533
                                    96.9
                                          18 21.9 0.094 3.3
                                                               3180 25.0 0.083401
           0 12.1 14.9 14.1 0.577
                                    99.4 157
                                              8.0 0.102 3.9
                                                               6730 16.7 0.015801
                                    98.5
           0 12.1 10.9 10.1 0.591
                                                               5780 17.4 0.041399
## 5 14.1
                                          18
                                              3.0 0.091 2.0
  6 12.1
           0 11.0 11.8 11.5 0.547
                                    96.4
                                          25
                                              4.4 0.084 2.9
                                                               6890 12.6 0.034201
        Time Crime
##
## 1 26.2011
               791
## 2 25.2999
              1635
## 3 24.3006
               578
## 4 29.9012
              1969
## 5 21.2998
              1234
```

```
test<-data.frame(M = 14.0,So = 0,Ed = 10.0, Po1 = 12.0,Po2 = 15.5,

LF = 0.640, M.F = 94.0,Pop = 150,NW = 1.1,U1 = 0.120,

U2 = 3.6, Wealth = 3200,Ineq = 20.1,Prob = 0.04, Time = 39.0)
```

M So Ed Po1 Po2 LF M.F Pop NW U1 U2 Wealth Ineq Prob Time Crime

 $1\ 15.1\ 1\ 9.1\ 5.8\ 5.6\ 0.510\ 95.0\ 33\ 30.1\ 0.108\ 4.1\ 3940\ 26.1\ 0.084602\ 26.2011\ 791\ 2\ 14.3\ 0\ 11.3\ 10.3\ 9.5\ 0.583$ $101.2\ 13\ 10.2\ 0.096\ 3.6\ 5570\ 19.4\ 0.029599\ 25.2999\ 1635\ 3\ 14.2\ 1\ 8.9\ 4.5\ 4.4\ 0.533\ 96.9\ 18\ 21.9\ 0.094\ 3.3\ 3180$ $25.0\ 0.083401\ 24.3006\ 578\ 4\ 13.6\ 0\ 12.1\ 14.9\ 14.1\ 0.577\ 99.4\ 157\ 8.0\ 0.102\ 3.9\ 6730\ 16.7\ 0.015801\ 29.9012$ $1969\ 5\ 14.1\ 0\ 12.1\ 10.9\ 10.1\ 0.591\ 98.5\ 18\ 3.0\ 0.091\ 2.0\ 5780\ 17.4\ 0.041399\ 21.2998\ 1234\ 6\ 12.1\ 0\ 11.0\ 11.8$ $11.5\ 0.547\ 96.4\ 25\ 4.4\ 0.084\ 2.9\ 6890\ 12.6\ 0.034201\ 20.9995\ 682$

I tried building a model using all the features and it gave a high adjust R-squared and low overall p-value, but since there are also so many features and insignificant features, the p=value and r-squared may not be accurate. I tested it on the test data set and got 155, lower than the min of the data. The best way to figure this out is to pick the best features from the 15 we are given. Of note I did not split the data into a training and validation. I thought our data set was already small, and splitting it may have been more detrimental.

```
lm_model_1 <- lm(Crime~.,data = crime_data)
summary(lm_model_1)</pre>
```

```
##
## Call:
## lm(formula = Crime ~ ., data = crime_data)
##
## Residuals:
##
       Min
                1Q
                   Median
                                3Q
                                       Max
  -395.74 -98.09
                    -6.69
##
                           112.99
                                    512.67
##
##
  Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept) -5.984e+03 1.628e+03 -3.675 0.000893 ***
                                       2.106 0.043443 *
## M
                8.783e+01
                          4.171e+01
## So
                          1.488e+02
               -3.803e+00
                                     -0.026 0.979765
## Ed
                1.883e+02
                           6.209e+01
                                       3.033 0.004861 **
                1.928e+02 1.061e+02
## Po1
                                       1.817 0.078892 .
## Po2
               -1.094e+02 1.175e+02
                                     -0.931 0.358830
## LF
               -6.638e+02
                          1.470e+03
                                      -0.452 0.654654
## M.F
                1.741e+01
                          2.035e+01
                                       0.855 0.398995
## Pop
               -7.330e-01
                          1.290e+00
                                      -0.568 0.573845
## NW
                4.204e+00
                           6.481e+00
                                       0.649 0.521279
## U1
               -5.827e+03
                           4.210e+03
                                      -1.384 0.176238
## U2
                          8.234e+01
                1.678e+02
                                       2.038 0.050161 .
## Wealth
                9.617e-02
                          1.037e-01
                                       0.928 0.360754
## Ineq
                7.067e+01
                           2.272e+01
                                       3.111 0.003983 **
               -4.855e+03
                           2.272e+03
                                      -2.137 0.040627 *
## Prob
## Time
               -3.479e+00 7.165e+00
                                     -0.486 0.630708
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 209.1 on 31 degrees of freedom
## Multiple R-squared: 0.8031, Adjusted R-squared: 0.7078
## F-statistic: 8.429 on 15 and 31 DF, p-value: 3.539e-07
```

```
Residuals: Min 1Q Median 3Q Max -395.74 -98.09 -6.69 112.99 512.67
Coefficients: Estimate Std. Error t value Pr(>|t|)
(Intercept) -5.984e+03\ 1.628e+03\ -3.675\ 0.000893 M 8.783e+01\ 4.171e+01\ 2.106\ 0.043443
So -3.803e+00 1.488e+02 -0.026 0.979765
Ed 1.883e+02 6.209e+01 3.033 0.004861 Pol 1.928e+02 1.061e+02 1.817 0.078892.
Po2 -1.094e+02 1.175e+02 -0.931 0.358830
LF -6.638e+02 1.470e+03 -0.452 0.654654
M.F 1.741e+01 2.035e+01 0.855 0.398995
Pop -7.330e-01 1.290e+00 -0.568 0.573845
NW 4.204e+00 6.481e+00 0.649 0.521279
U1 -5.827e+03 4.210e+03 -1.384 0.176238
U2\ 1.678e + 02\ 8.234e + 01\ 2.038\ 0.050161.
Wealth 9.617e-02\ 1.037e-01\ 0.928\ 0.360754
Ineq 7.067e+01\ 2.272e+01\ 3.111\ 0.003983 ** Prob -4.855e+03\ 2.272e+03\ -2.137\ 0.040627 *
Time -3.479e+00 7.165e+00 -0.486 0.630708
— Signif. codes: 0 '' 0.001 '' 0.01 '' 0.05 '' 0.1 '' 1
Residual standard error: 209.1 on 31 degrees of freedom Multiple R-squared: 0.8031, Adjusted R-squared:
0.7078 F-statistic: 8.429 on 15 and 31 DF, p-value: 3.539e-07
predict(lm_model_1, test)
##
## 155.4349
#155.4349
min(crime_data$Crime)
## [1] 342
#[1] 342
```

Call: $lm(formula = Crime \sim ., data = crime data)$

I decided to pick the best features by using the ggpairs function in the GGally package. This allows me to plot variables against each other and give me a correlation. I made vectors that split the data into 3 groups so we can visually see the scatter plots better. From this method I narrowed down the features with the strongest correlation to be Po1 and Po2.

```
library(GGally)

## Registered S3 method overwritten by 'GGally':

## method from

## +.gg ggplot2

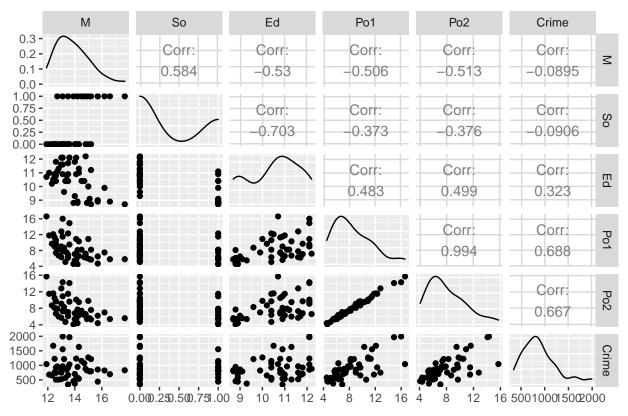
crime_plot_1 <- ggpairs(data=crime_data, columns = c(1:5, 16), title = "Crime Data")

crime_plot_2 <- ggpairs(data=crime_data, columns = c(6:10, 16), title = "Crime Data")

crime_plot_3 <- ggpairs(data=crime_data, columns = c(10:15, 16), title = "Crime Data")

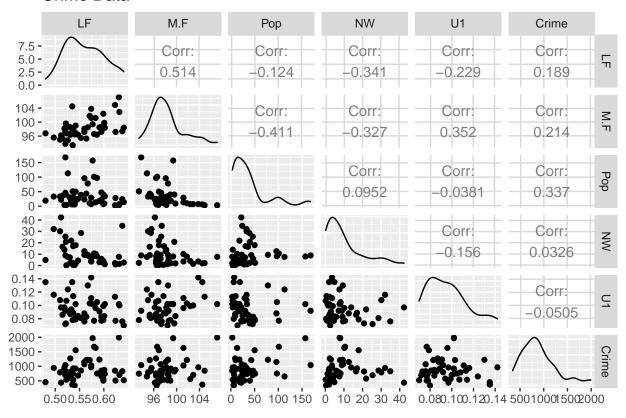
crime_plot_1</pre>
```

Crime Data



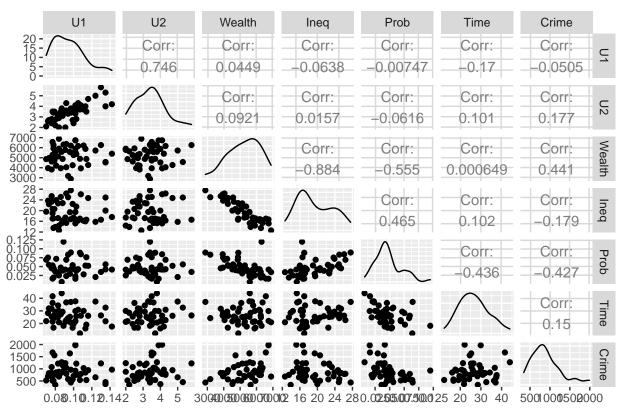
 ${\tt crime_plot_2}$

Crime Data



 ${\tt crime_plot_3}$

Crime Data



I made a new model using those 2 features and got a better result when I ran it on the test.

```
set.seed(1)
lm_model_2 <- lm(Crime ~ Po1 + Po2,data = crime_data)
summary(lm_model_2)</pre>
```

```
##
## Call:
## lm(formula = Crime ~ Po1 + Po2, data = crime_data)
##
## Residuals:
##
      Min
                10 Median
                                3Q
                                      Max
## -636.09 -168.62
                     35.44 141.80
                                   532.10
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
                             125.9
                                     1.257
                                             0.2155
## (Intercept)
                  158.3
                 256.2
                             123.4
                                     2.076
                                             0.0438 *
## Po1
## Po2
                             131.2 -1.359
                 -178.3
                                             0.1810
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 281.3 on 44 degrees of freedom
## Multiple R-squared: 0.494, Adjusted R-squared: 0.471
## F-statistic: 21.48 on 2 and 44 DF, p-value: 3.094e-07
```

```
Call: lm(formula = Crime \sim Po1 + Po2, data = crime data)
Residuals: Min 1Q Median 3Q Max -636.09 -168.62 35.44 141.80 532.10
Coefficients: Estimate Std. Error t value Pr(>|t|)
(Intercept) 158.3 125.9 1.257 0.2155
Po1 256.2 123.4 2.076 0.0438 * Po2 -178.3 131.2 -1.359 0.1810
— Signif. codes: 0 '' 0.001 '' 0.01 '' 0.05 '' 0.1 '' 1
Residual standard error: 281.3 on 44 degrees of freedom Multiple R-squared: 0.494, Adjusted R-squared:
0.471 F-statistic: 21.48 on 2 and 44 DF, p-value: 3.094e-07
predict(lm_model_2, test)
##
          1
## 468.632
468.632
I decided I wanted to try out a package that automatically evaluates each feature. This method is from the
caret package. It uses a random forest algorithm on each iteration to evaluate the model. It explores all
possible subsets of attributes and gives the top attributes.
library(randomForest)
## randomForest 4.6-14
## Type rfNews() to see new features/changes/bug fixes.
##
## Attaching package: 'randomForest'
## The following object is masked from 'package:ggplot2':
##
##
       margin
library(caret)
## Loading required package: lattice
set.seed(1)
control <- rfeControl(functions = rfFuncs, method = "cv", number = 10, repeats = 25)</pre>
results <- rfe(crime_data[,1:15], crime_data[,16], sizes = c(1:15), rfeControl = control)
print(results)
##
## Recursive feature selection
##
## Outer resampling method: Cross-Validated (10 fold)
##
## Resampling performance over subset size:
##
```

```
Variables RMSE Rsquared
                               MAE RMSESD RsquaredSD MAESD Selected
##
##
            1 341.3
                      0.4705 269.7 133.98
                                               0.2978 117.90
                                               0.3473 125.09
##
            2 371.5
                      0.4407 289.8 124.33
##
            3 320.6
                      0.5945 248.4
                                               0.2962 88.42
                                    93.51
##
            4 275.6
                      0.6830 209.1
                                    84.61
                                               0.2776
                                                       76.81
            5 290.1
                                               0.2783 81.47
##
                      0.6734 217.6
                                    91.39
            6 294.9
##
                      0.6413 220.4
                                    89.95
                                               0.2834
                                                       87.64
##
            7 291.7
                      0.6617 214.9
                                    90.56
                                               0.2986
                                                       89.87
##
            8 280.9
                      0.7162 208.8
                                    87.60
                                               0.3093
                                                       86.10
##
            9 290.0
                      0.6652 215.5
                                    93.05
                                               0.3127
                                                       86.20
##
           10 280.3
                      0.6850 207.0
                                    89.16
                                               0.2772 76.45
                      0.6898 214.5
           11 284.1
                                               0.3133
##
                                    88.28
                                                       78.63
##
           12 276.5
                      0.7094 211.4
                                    91.58
                                               0.3063 80.59
           13 277.4
                      0.7068 211.6
##
                                    77.14
                                               0.2960 70.15
##
           14 279.9
                                               0.3149 72.44
                      0.7146 211.5
                                    80.69
##
           15 284.8
                      0.6894 216.2
                                    76.83
                                               0.3209
                                                       68.48
##
## The top 4 variables (out of 4):
      Po1, Po2, NW, Prob
##
```

Recursive feature selection

Outer resampling method: Cross-Validated (10 fold)

Resampling performance over subset size:

```
Variables RMSE R<br/>squared MAE RMSESD R<br/>squared
SD MAESD Selected 1 347.4 0.4851 273.1 161.0 0.3692 124.1 2<br/> 308.5\ 0.5293\ 256.5\ 143.6\ 0.3471\ 122.3
```

3 272.6 0.6149 224.5 140.3 0.3199 118.8 4 236.7 0.7032 190.4 133.2 0.2688 109.7

 $5\ 228.8\ 0.6988\ 184.6\ 131.6\ 0.2672\ 107.6$

 $6\ 228.2\ 0.7232\ 180.2\ 125.1\ 0.2397\ 103.6\ *\ 7\ 228.9\ 0.7123\ 181.9\ 133.5\ 0.2439\ 111.3$

 $8\ 237.2\ 0.6981\ 188.7\ 129.2\ 0.2642\ 108.5$

 $9\ 235.3\ 0.6912\ 189.3\ 124.8\ 0.2356\ 108.2$

 $10\ 234.6\ 0.6884\ 188.5\ 128.2\ 0.2344\ 107.0$

11 231.6 0.6897 187.5 128.7 0.2313 108.3

 $12\ 233.4\ 0.6832\ 186.8\ 129.1\ 0.2424\ 112.1$

 $13\ 230.5\ 0.7058\ 183.9\ 123.9\ 0.1997\ 106.9$

 $14\ 234.2\ 0.7113\ 186.3\ 126.0\ 0.2132\ 107.0$

 $15\ 232.4\ 0.7033\ 186.3\ 126.2\ 0.2185\ 109.0$

The top 5 variables (out of 6): Po1, Po2, NW, Prob, Wealth

```
lm_model_3 <- lm(Crime ~ Po1 + Po2 + NW + Prob + Wealth + Ed,data = crime_data)
predict(lm_model_3, test)</pre>
```

```
## 1
## 458.752
```

458.752

In the end when I ran the model on the test, I got a similar result to the second model.