

$$-1 \leq \text{Corr}(X, Y) = \frac{\sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\sum_{i=1}^n (x_i - \bar{x})^2} \sqrt{\sum_{i=1}^n (y_i - \bar{y})^2}} \leq 1 \quad \text{Post Hoc Ergo Propter It}$$

Selfselection Bias \rightarrow poorly designed experiments

Voluntary Response Bias \rightarrow Not rep of population

Non Response bias - Non-respondents differ from respondents

$$b_{OLS} = b_1 + \frac{\text{Cov}(e, X)}{\text{Cov}(X, X)} = \frac{\text{Cov}(X, Y)}{\text{Cov}(X, X)} \quad \text{Orthogonality Assumption } \text{Cov}(e, X) = 0$$

When X and e are uncorrelated b_{OLS} is a good estimate of b_1

If X is a dummy variable $b_{OLS} = b_1 + (\bar{e}_1 - \bar{e}_0)$

b_1 is called treatment effect & $(\bar{e}_1 - \bar{e}_0)$ is selection bias

Randomized control Exp (Random (0,1)) \rightarrow < 0.5 (Control group)

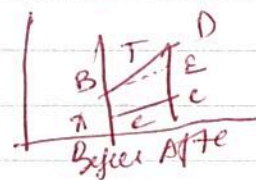
$$\text{OLS} \Rightarrow \text{difference estimator} = \bar{y}_1 - \bar{y}_0 = \frac{\sum_{i=1}^{N_1} y_i}{N_1} - \frac{\sum_{i=1}^{N_0} y_i}{N_0}$$

N_1 = Obs in Treatment group

N_0 = Obs in Control group

Counterfactual \rightarrow comparing outcome with treatment vs without treatment

Difference in Difference $= (D-B) - (C-A) = D-E$



Stock Return = ~~12%~~ $\frac{\text{After} - \text{Before}}{\text{Before}}$

$$r_t = \frac{P_t f_t + d_t}{P_{t-1}} - 1$$

$$\text{Compound return} = (r_{t+1})(r_{t+2}) \dots (r_{nt+1}) - 1$$

$$s = \sqrt{\frac{\sum (x - \bar{x})^2}{n-1}}$$

$$r_i = \alpha + \beta r_{m,t} + \epsilon$$

r_i = Risk factor β = measure of stock return to overall market move

Draw Down (DD) is cumulative losses $DD_t = \frac{(HWM_t - P_t)}{HWM_t}$

P_t = Current price of asset

Abnormal return = Actual return - Expected return

$$\text{Sharpe Ratio} = \frac{(R - R^f)}{\sigma(R - R^f)} \rightarrow R = \text{Risk } R^f = \text{Risk free}$$

$$\text{Treynor Ratio} = \frac{(R - R^f)}{\beta} \rightarrow \text{Indicates higher rewards/unit risk}$$

$$\text{Jensen Ratio} = r_{i,t} - r_{f,t} = \alpha_i + \beta_i (r_{m,t} - r_{f,t}) + \epsilon_{i,t}$$