# Homework 2 - Week 2 - Karthick Krishna

#### Question 4.1

Describe a situation or problem from your job, everyday life, current events, etc., for which a clustering model would be appropriate. List some (up to 5) predictors that you might use.

I am an Analyst at Mindtree Limited. Currently, I work on Marketing Analytics and Ad Analytics. I work for one of the world's largest Search Engine Platforms providers on the Advertise r level data and User level data. I use Python for analysis and used the Scikit Learn packag e in Python. In my current project, as one of the early steps, I segregate the Customers(als o known as Advertisers) into different groups before I perform Quasi-experimental design to find a treatment group for my test advertisers. After trying out lots of different clustering methods such as K-means, Partitioning Around Medoids(PAM), Hierarchical Clustering, DBSCA N, K-prototype, and K-Modes. I ended up using K-Modes since it gave good cluster separation for my dataset and I could also use Categorical data as my feature.

Few of the KPI's(predictors) are as follows,

- 1. The Impression gained by the advertiser using the platform (Integer datatype)
- 2. Click gained by the advertiser using the platform (Integer datatype)
- 3. Spend/Revenue of the Advertiser on the Platform (Doubble datatype)
- 4. Vertical (Example: Travel and Transport, Retail, B2C Services, et cetera) (Categorical d ata)
- 5. Country on the Advertiser has performed (Categorical data)

#### Question 4.2

Problem Statement: Use the R function kmeans to cluster the points as well as possible. Report the best combination of predictors, your suggested value of k, and how well your best clustering predicts flower type.

On an overall output of k = 3 and using Petals as Predictors gave 96% accuracy

# My approach to the given problem:

The problem is very straightforward, we have to Cluster the data into k numbers. In this problem, *After the TA call(Mr. Siawpeng Er) I've scalled my data*, I've used ggplot to identify which feature (Sepal or Petal) can get better clustering of iris Dataset followed by identifying the number of clusters using the elbow curve, later I performed k-means using the number of k that we obtain from elbow curve and feature that I select. In the end, I use the output value to find the Accuracy.

# My understanding of the output

The Petal feature looks good to separate the data into k clusters, later k=3 for the petal predictors looked good from the elbow curve. At last, the accuracy looks extremely good, i.e k-means (for the selected feature and k value) has given a good output of separating the Spe cies into different types.

I used the following link for this question:

- 1. https://rpubs.com/AnanyaDu/361293
- 2. http://rstudio-pubs-static.s3.amazonaws.com/227726\_134741628338405eaebcff73cc63abc6.html

```
In [25]: install.packages("dplyr", repos='http://cran.us.r-project.org')
          install.packages("tidyverse", repos='http://cran.us.r-project.org')
          install.packages("cluster", repos='http://cran.us.r-project.org')
          install.packages("fpc", repos='http://cran.us.r-project.org')
          install.packages("factoextra", repos='http://cran.us.r-project.org')
          Installing package into 'C:/Users/v-balkar.REDMOND/Documents/R/win-library/3.6'
          (as 'lib' is unspecified)
          Installing package into 'C:/Users/v-balkar.REDMOND/Documents/R/win-library/3.6'
          (as 'lib' is unspecified)
  In [4]: | oldw <- getOption("warn")</pre>
          options(warn = -1)
          library(dplyr)
          library(tidyverse)
          library(cluster)
          library(fpc)
          library(factoextra)
          require(gridExtra)
          library(ggplot2)
In [189]: # Loading the iris text dataset into a dataframe
          iris <- read.table("iris.txt",header = TRUE)</pre>
In [190]: head(iris)
           Sepal.Length Sepal.Width Petal.Length Petal.Width Species
                              3.5
                   5.1
                                         1.4
                                                    0.2
                                                         setosa
                   4.9
                              3.0
                                         1.4
                                                    0.2
                                                         setosa
                   4.7
                              3.2
                                         1.3
                                                    0.2
                                                         setosa
                   4.6
                              3.1
                                         1.5
                                                    0.2
                                                         setosa
                   5.0
                                                    0.2
                              36
                                         14
                                                         setosa
                              3.9
                                         1.7
                                                    0.4
                                                         setosa
In [191]: length(unique(iris$Species))
          3
In [192]: |dim(iris)
          150 5
In [193]: | summary(iris)
            Sepal.Length
                             Sepal.Width
                                             Petal.Length
                                                             Petal.Width
           Min. :4.300
                            Min. :2.000
                                            Min. :1.000
                                                            Min. :0.100
           1st Ou.:5.100
                            1st Qu.:2.800
                                            1st Qu.:1.600
                                                            1st Ou.:0.300
           Median :5.800
                            Median :3.000
                                            Median :4.350
                                                            Median :1.300
           Mean :5.843
                           Mean :3.057
                                            Mean :3.758
                                                            Mean :1.199
           3rd Qu.:6.400
                            3rd Qu.:3.300
                                            3rd Qu.:5.100
                                                            3rd Qu.:1.800
           Max.
                  :7.900
                           Max. :4.400 Max. :6.900
                                                            Max. :2.500
                 Species
           setosa
                    :50
           versicolor:50
           virginica:50
```

```
In [196]: normalize <- function(x){
    return ((x-min(x))/(max(x)-min(x)))
}

iris$Sepal.Length<- normalize(iris$Sepal.Length)
    iris$Sepal.Width<- normalize(iris$Sepal.Width)
    iris$Petal.Length<- normalize(iris$Petal.Length)
    iris$Petal.Width<- normalize(iris$Petal.Width)
    head(iris)</pre>
```

Sepal.Length	Sepal.Width	Petal.Length	Petal.Width	Species
0.2222222	0.6250000	0.06779661	0.04166667	setosa
0.16666667	0.4166667	0.06779661	0.04166667	setosa
0.11111111	0.5000000	0.05084746	0.04166667	setosa
0.08333333	0.4583333	0.08474576	0.04166667	setosa
0.19444444	0.6666667	0.06779661	0.04166667	setosa
0.3055556	0.7916667	0.11864407	0.12500000	setosa

# Preprocessing the data

Clustering falls under Unsupervised Learning, so we don't need the output variable during execution of our algorithm. We will, therefore, remove Output variable "Species" and store it in another variable.

```
In [197]: # Seperate the independent variables from the dependent variabe
    df <- iris[,1:4]
    df_Class <- iris[,"Species"]
    head(df)</pre>
```

Sepal.Length	Sepal.Width	Petal.Length	Petal.Width
0.2222222	0.6250000	0.06779661	0.04166667
0.16666667	0.4166667	0.06779661	0.04166667
0.11111111	0.5000000	0.05084746	0.04166667
0.08333333	0.4583333	0.08474576	0.04166667
0.19444444	0.6666667	0.06779661	0.04166667
0.3055556	0.7916667	0.11864407	0.12500000

Now I see how different combinations have splitted.

```
In [198]: # plotting the petal and sepal features separately to view the different features.

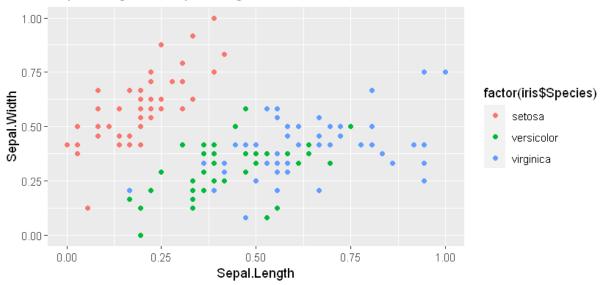
plot1 <- ggplot(df, aes(x = df[,1], y = df[,2]))+geom_point(aes(color = factor(iris$Species)))+labs(x

plot2 <- ggplot(df, aes(x = df[,3], y = df[,4]))+geom_point(aes(color = factor(iris$Species)))+labs(x

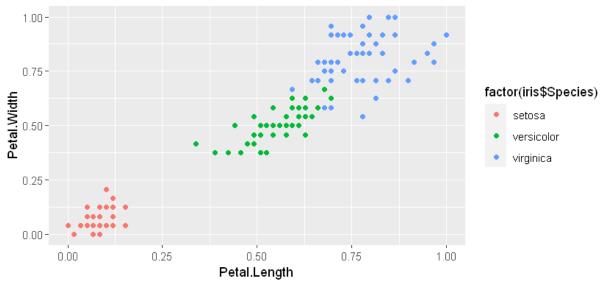
grid.arrange(plot1, plot2, ncol=1)

# It is clear the petal features can get a better clustering of the iris dataset</pre>
```

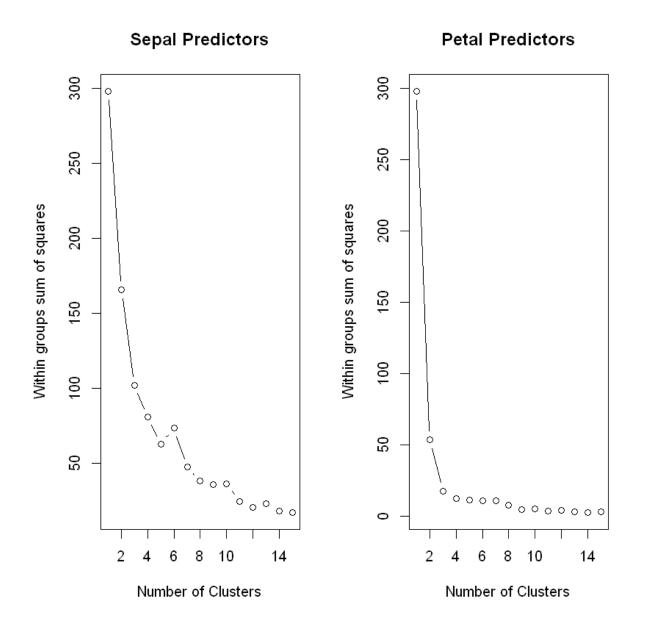
# Sepal.Length vs Sepal.Length



# Petal.Length vs Petal.Width



```
In [199]: # For the next step, I am going to try to determine the number of clusters using the elbow method.
           # FROM THE ELBOW METHOD, I am going to be using 3 clusters as input to kmeans function.
           sepals_df = df[,1:2]
           petals_df = df[,3:4]
          par(mfrow=c(1,2))
                                                # used to set or query graphical parameters (Get the 2 graphs sid
          # Elbow method on Sepals
           sepals_df <- scale(sepals_df)</pre>
           wss <- (nrow(sepals_df)-1)*sum(apply(sepals_df,2,var))</pre>
           for (i in 2:15) wss[i] <- sum(kmeans(sepals_df, centers=i)$withinss)</pre>
           plot1 <- plot(1:15, wss, type="b", xlab="Number of Clusters", ylab="Within groups sum of squares", ma
          # Elbow method on Petals
          petals_df <- scale(petals_df)</pre>
          wss <- (nrow(petals_df)-1)*sum(apply(petals_df,2,var))</pre>
           for (i in 2:15) wss[i] <- sum(kmeans(petals_df, centers=i)$withinss)</pre>
          plot2 <- plot(1:15, wss, type="b", xlab="Number of Clusters", ylab="Within groups sum of squares", ma
```

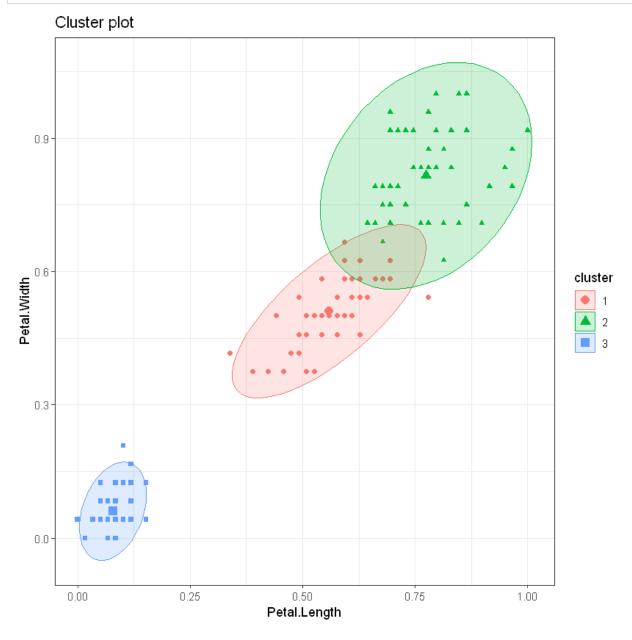


```
In [200]: # ?kmeans

set.seed(123)
model <- kmeans(petals_df, 3, nstart = 25, iter.max = 10)
cluster_centroids <- aggregate(petals_df,by=list(model$cluster),FUN=mean)
cluster_centroids</pre>
```

Group.1	Petal.Length	Petal.Width
1	0.3048515	0.1648655
2	1.0245672	1.1242119
3	-1.3006301	-1.2507035

Showing the output graphically along with the cluster centroid



Now to check how well the model has predicted

```
In [202]: model$size # gives no. of records in each cluster
```

52 48 50

```
In [203]: table(model$cluster,df_Class)
```

```
df_Class
  setosa versicolor virginica
1     0     48     4
2     0     2     46
3     50     0     0
```

The above result of table shows that Cluster 1 corresponds to Virginica, Cluster 2 corresponds to Versicolor and Cluster 3 to Setosa.

Total number of correctly classified instances are: 46 + 48 + 50= 144

Total number of incorrectly classified instances are: 2 + 4= 6

Accuracy = 144/(144+6) = 0.96 meaning our model has achieved 96% accuracy

### Question 5.1

Problem Statement: Using crime data from the file uscrime.txt, test to see whether there are any outliers in the last column (number of crimes per 100,000 people). Use the grubbs.test function in the outliers package in R.

#### **Grubbs Test:**

It is a statistical test to identify Outliers. The value could be smallest or largest in the data. Grubbs test works by assuming that data is normally distributed, so we have to check the normality assumption first.

#### My approach to the given problem:

First I checked whether my data is normally distributed or not to perform Grubbs test. Later I used grubbs.test() function to perform the test. Later I removed those values and I performed the grubb test again and checked the P-value.

#### My understanding of the output

342 and 1993 are outliers, i.e these values are separated maximum from the mean. The p-value measures how much evidence there is that the tested point is an Outlier or not (Values Near 0 - Stronger evidence of an Outlier, Values Near 1 - Weaker evidence of an Outlier). Since I got P-value output of 1 this means the tested point should not be considered as an Outlie r.

I continued the process till the value was some what near  $\boldsymbol{\theta}$ 

That was not happening so as TA(Mr. Siawpeng Er) mentioned during the cass time if we continue to do this we will end up in removing all the data.

I used the following link for this question:

- rdocumentation.org/packages/outliers/versions/0.14/topics/grubbs.test
- 2. https://www.youtube.com/watch?v=kc905XfV2pc

In [64]: crime\_df <- read.table("uscrime.txt", header = TRUE)</pre>

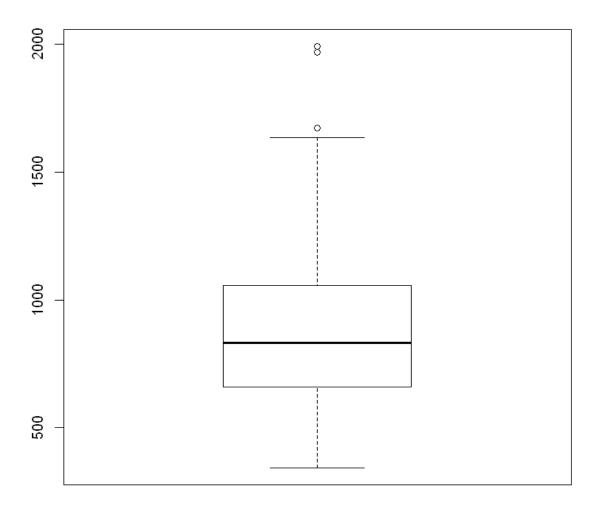
In [65]: head(crime\_df,2)

М	So	Ed	Po1	Po2	LF	M.F	Pop	NW	U1	U2	Wealth	Ineq	Prob	Time	Crime
15.1	1	9.1	5.8	5.6	0.510	95.0	33	30.1	0.108	4.1	3940	26.1	0.084602	26.2011	791
14.3	0	11.3	10.3	9.5	0.583	101.2	13	10.2	0.096	3.6	5570	19.4	0.029599	25.2999	1635

In [172]: dim(crime\_df)

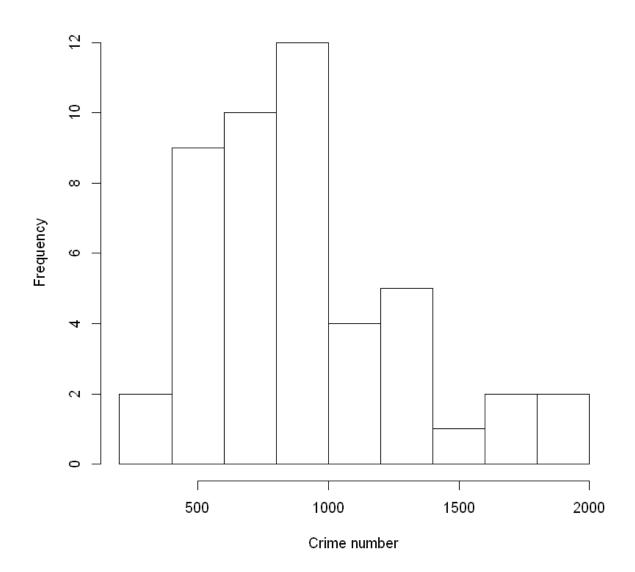
47 16

In [168]: # Using boxplot to visualize the Outliers
boxplot(crime\_df\$Crime)



```
In [83]: # Checking Normality with Histogram
hist(crime_df$Crime, xlab = "Crime number", main = "Crime Dataset")
```





This looks fine, but if our data had more than a single peak then Grub test cannot be used. Now I'm continueing with the grub test.

```
In [84]: library(outliers)
crime <- crime_df$Crime</pre>
```

```
In [188]: # ?grubbs.test
          grubbs.test(crime, type = 11, opposite = FALSE, two.sided = FALSE)
                  Grubbs test for two opposite outliers
          data: crime
          G = 4.26877, U = 0.78103, p-value = 1
          alternative hypothesis: 342 and 1993 are outliers
          p-value near 1 - Weaker evidence of an Outlier
In [239]: crime_df <- crime_df[(!(crime_df$Crime == 342) & !(crime_df$Crime == 1993)),]</pre>
In [240]: dim(crime_df)
          45 16
In [241]: | grubbs.test(crime_df$Crime, type = 11, opposite = FALSE, two.sided = FALSE)
                  Grubbs test for two opposite outliers
          data: crime df$Crime
          G = 4.56671, U = 0.73301, p-value = 0.6893
          alternative hypothesis: 373 and 1969 are outliers
In [242]: crime df <- crime_df[(!(crime_df$Crime == 373) & !(crime_df$Crime == 1969)),]</pre>
In [243]: |dim(crime_df)
          43 16
In [244]: | grubbs.test(crime_df$Crime, type = 11, opposite = FALSE, two.sided = FALSE)
                  Grubbs test for two opposite outliers
          data: crime_df$Crime
          G = 4.03257, U = 0.78992, p-value = 1
          alternative hypothesis: 439 and 1674 are outliers
```

Kindly read "My understanding of the output" for this question as why I performed the process again

## **Question 6.1**

Describe a situation or problem from your job, everyday life, current events, etc., for which a Change Detection model would be appropriate. Applying the CUSUM technique, how would you choose the critical value and the threshold?

As an Analyst at Mindtree, I worked on a churn analytics project for my client where I had to analyze the Customers who tend to churn out of the system. For this I use lots of different performance metrics across a time period. One important note is that I consider the seasonality since some customers prefer to invest in the platform during a certain time of the yar. Depending on the importance of the metric, I vary the time window from weeks to months. After tabulating the time-weighted values, I compare the values to the threshold, which I decide on the data that is provided. The main objective of this project is to identify the time when the customer might leave the system, by doing so my client will get in touch with the customer and makes sure that the customer doesn't leave the system. So for this problem statement it's not definitive on selecting a Critical value or threshold.

## Question 6.2 (a)

Problem Statement: Using July through October daily-high-temperature data for Atlanta for 1996 through 2015, use a CUSUM approach to identify when unofficial summer ends (i.e., when the weather starts cooling off) each year.

First I viewed the sum and average of temperatures by year and by month to see trends,if present, in this data.

In the Daily Temperature by Year output we want to see if climate has generally changed for the warmer as time goes on. It looks like temperature is stable throughout the years, but from 2010 there are a few abnormally with high mean temperatures. The mean temperatures for 2010 and 2011 are high.

In the Daily Temperature by Month output we want to see when we start transitioning out of summer. The output clearly explains what was expected. Starting in September temperatures start to cool down. CUSUM model would start to pick up changes as early as late August that temperatures are decreasing.

I set up a loop to run a cusum model on each individual year to determine which day start a string of temperature changes. To do this I set up a cusum model using the mean of all summer days as the center value, the standard deviation of all summer days as the target standard deviation. Detection standard deviation is set to 1.96 times the summer day standard deviation. Any value greater than 1.96 times the standard deviation will add to the cumulative sum model.

The dates for each year are listed in a data frame below. The earliest end of summer was 2013-08-15. The latest end of summer was 2005-10-06. Most end of summer days occur in early to mid-September.

```
In [118]: # load libraries
          # if (!require(lubridate)) install.packages("lubridate")
          # library(lubridate)
          # if (!require(qcc)) install.packages("qcc")
          # library(qcc)
          # if (!require(changepoint)) install.packages("changepoint")
          # library(changepoint)
          # if (!require(bda)) install.packages("bda")
          # library(bda)
In [97]: # setup cusum algorithm for changes over time
          temps_df = read_delim('temps.txt', delim = '\t') %>%
                  as_tibble() %>%
                  gather(year, temp, -DAY) %>%
                  mutate(year = as.factor(year),
                         date = paste(DAY,year, sep = '-')) %>%
                  mutate(date_val = dmy(date),
                         color = ifelse(temp > mean(.$temp), 'Above', 'Below'),
                         month = month(date_val),
                         day = day(date_val)) %>%
                  dplyr::select(date_val, DAY, year, temp,color, month, day)
          Parsed with column specification:
          cols(
            .default = col_double(),
            DAY = col_character()
          See spec(...) for full column specifications.
```

```
In [133]: # Truncating the data
head(temps_df)
```

date_val	DAY	year	temp	color	month	day	
1996-07-01	1-Jul	1996	98	Above	7	1	
1996-07-02	2-Jul	1996	97	Above	7	2	
1996-07-03	3-Jul	1996	97	Above	7	3	
1996-07-04	4-Jul	1996	90	Above	7	4	
1996-07-05	5-Jul	1996	89	Above	7	5	
1996-07-06	6-Jul	1996	93	Above	7	6	

```
In [99]: dim(temps_df)
           2460 7
In [222]: # This is the Standard Deviation of the whole output
           sd(temps_df$temp)
           8.62025319888611
In [218]: # Group the data by year and summing it
           aggregate(temps_df$temp ~ temps_df$year, temps_df, sum)
            temps_df$year temps_df$temp
                    1996
                                 10297
                    1997
                                 10046
                    1998
                                 10364
                    1999
                                 10253
                   2000
                                 10336
                   2001
                                 10031
                   2002
                                 10281
                   2003
                                 10022
                   2004
                                 10057
                    2005
                                 10253
                   2006
                                 10215
                   2007
                                 10504
                   2008
                                 10149
                   2009
                                  9962
                   2010
                                 10727
```

```
In [213]: # The mean temperaature across all the years
mean(temps_df$temp)
```

83.3390243902439

# In [220]: # Group the data by months and averaging it aggregate(temps\_df\$temp ~ temps\_df\$year, temps\_df, mean)

temps_df\$year	temps_df\$temp
1996	83.71545
1997	81.67480
1998	84.26016
1999	83.35772
2000	84.03252
2001	81.55285
2002	83.58537
2003	81.47967
2004	81.76423
2005	83.35772
2006	83.04878
2007	85.39837
2008	82.51220
2009	80.99187
2010	87.21138
2011	85.27642
2012	84.65041
2013	81.66667
2014	83.94309
2015	83.30081

temps_df\$month	temps_df\$temp
7	55025
8	54942
9	49603
10	45444

In [217]: # Group the data by months and averaging it

aggregate(temps\_df\$temp ~ temps\_df\$month, temps\_df, mean)

temps_df\$month	temps_df\$temp
7	88.75000
8	88.61613
9	82.67167
10	73.29677

```
In [226]: ## Cusum Model
          # setup cusum algorithm for changes over time
          temps_model_df <- read_delim('temps.txt', delim = '\t') %>%
                  as_data_frame() %>%
                  gather(year, temp, -DAY) %>%
                  mutate(year = as.factor(year),
                          date = paste(DAY,year, sep = '-')) %>%
                  mutate(date_val = dmy(date),
                         color = ifelse(temp > mean(.$temp), 'Above', 'Below'),
                         month = month(date_val),
                          day = day(date_val)) %>%
                   dplyr::select(date_val, DAY, year, temp,color, month, day)
          print("Head of temp data")
          head(temps_model_df)
          print('Unique Years: ',)
          unique(temps_model_df$year)
          # grab only the summer dates for the cusum model
          summer_df = temps_model_df %>%
                  filter(month %in% c(as.Date(7), as.Date(8)))
          # summer_df
          # determine baseline mean and sd metrics in the summer months only
          summer_mean = mean(summer_df$temp)
          summer_sd = sd(summer_df$temp)
          # summer_mean
          # summer_sd
          # list of years to loop through
          years = as.list(unique(as.character(temps_model_df$year)))
          # years
          # empty list to store values of the for loop into
          store_days <- list()</pre>
          # cusum for loop
          for (i in seq_along(years)) {
                  # take a year subset
                  year_index <- years[[i]]</pre>
                  df <- temps_model_df %>%
                           filter(as.character(year) == year_index) %>%
                           dplyr::select(temp)
                  # fit a cusum model to that year
                  qsum <- qcc::cusum(</pre>
                           data = df$temp,
                           centervalue = summer_mean,
                           std.dev = summer_sd,
                           se.shift = 1.96,
                           plot = F
                  # extract the first day that starts at least 4 consecutive days of temperature flagged by cus
                  qsum_results <- qsum$neg %>%
                           as_tibble() %>%
                           rownames_to_column() %>%
                           cbind(date = temps_model_df$DAY) %>%
                           mutate( # current cusum value times the next and the fourth value cannot be 0!
                                   consecutive = value * lead(value,1) * lead(value, 4) == 0
                                   ) %>%
                           filter(consecutive == F) %>%
                           .[1,] %>%
                           cbind(year_index) %>%
                           dplyr::select(., -consecutive)
                  # store the first day of a string of flagged temperatures into a list
                  store_days[[i]] = qsum_results
          }
```

```
# reduce the list of stored temperatures and format into a readable format
end_summer <- reduce(store_days, rbind) %>%
        mutate(date = paste(date, year_index, sep = '-')) %>%
        mutate(date_val = dmy(date)) %>%
        dplyr::select(date_val, 'cusum_val' = value) %>%
        mutate(year_date = year(date_val)) %>%
        dplyr::select(year_date, date_val, cusum_val) %>%
        mutate(month_val = month(date_val),
                day_val = day(date_val))
# end_summer
# find the earliest end of summer
earliest_end <- end_summer %>%
        filter(month_val == min(month_val))
# earliest_end
# find the latest end of summer
latest_end <- end_summer %>%
        filter(month_val == max(month_val))
# Latest_end
# print outputs
print("Outputs:")
print(paste('Earliest Summer End: ', earliest_end$date_val))
print(paste('Latest Summer End: ', latest_end$date_val))
end summer
Parsed with column specification:
cols(
  .default = col_double(),
  DAY = col_character()
See spec(...) for full column specifications.
[1] "Head of temp data"
```

date_val	DAY	year	temp	color	month	day	
1996-07-01	1-Jul	1996	98	Above	7	1	
1996-07-02	2-Jul	1996	97	Above	7	2	
1996-07-03	3-Jul	1996	97	Above	7	3	
1996-07-04	4-Jul	1996	90	Above	7	4	
1996-07-05	5-Jul	1996	89	Above	7	5	
1996-07-06	6-Jul	1996	93	Above	7	6	

[1] "Unique Years: "

1996 1997 1998 1999 2000 2001 2002 2003 2004 2005 2006 2007 2008 2009 2010 2011 2012 2013 2014 2015

## ► Levels:

- [1] "Outputs:"
- [1] "Earliest Summer End: 2013-08-15" [1] "Latest Summer End: 2005-10-06"

year_date	date_val	cusum_val	month_val	day_val
1996	1996-09-18	-0.2128955	9	18
1997	1997-09-22	-1.4566970	9	22
1998	1998-09-29	-0.9527283	9	29
1999	1999-09-20	-2.2253764	9	20
2000	2000-09-06	-2.7836448	9	6
2001	2001-09-24	-1.6399583	9	24

year_date	date_val	cusum_val	month_val	day_val
2002	2002-09-24	-1.2293172	9	24
2003	2003-09-28	-0.7898293	9	28
2004	2004-09-15	-0.8492196	9	15
2005	2005-10-06	-1.3905193	10	6
2006	2006-09-21	-1.8172197	9	21
2007	2007-09-16	-0.9815750	9	16
2008	2008-09-17	-1.8401883	9	17
2009	2009-09-29	-0.8967318	9	29
2010	2010-09-26	-1.3599757	9	26
2011	2011-09-04	-0.1212649	9	4
2012	2012-09-30	-1.6603207	9	30
2013	2013-08-15	-0.8288572	8	15
2014	2014-09-23	-0.4691220	9	23
2015	2015-09-12	-0.1263554	9	12

# Question 6.2 (b)

Use a CUSUM approach to make a judgment of whether Atlanta's summer climate has gotten warmer in that time (and if so, when).

To answer this question we will use the a cusum model to see if any year's summer days have been hotter than the overall average of the summer months. To do this we will filter the data set to only the summer months, then set up a cusum model with center value as the mean temperature of all summer months. We will use the standard deviation for the same time period.

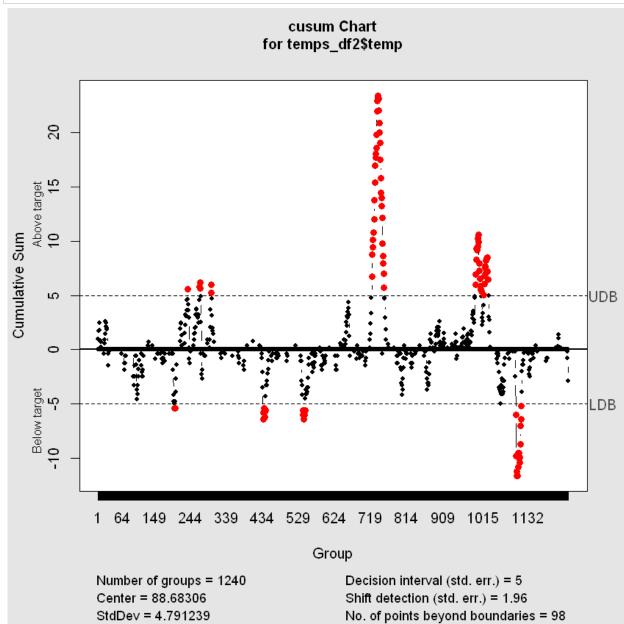
Examining the cusum plot - there is an extreme amount of positive change around the mid 2000s, with another run of hot summers following close to the end of our data set.

2007 looks to be the peak of the hot summers shown in the cusum chart. In particular, 8-25-2007, shows the highest cummulative sum total of any of the years summer days.

To get the CUSUM chart I used :

```
1.https://cran.r-project.org/web/packages/qcc/vignettes/qcc_a_quick_tour.html
2.http://www.stat.unipg.it/luca/misc/Rnews_2004-1-pag11-17.pdf
3. https://rdrr.io/cran/qcc/man/qcc.html
```

```
Parsed with column specification:
cols(
   .default = col_double(),
   DAY = col_character()
)
See spec(...) for full column specifications.
```



```
In [231]: # extract the cusum results to see exactly when summers get hotter than normal
          cusum_results <- qcc::cusum(</pre>
                  data = temps_df2$temp,
                  centervalue = summer_center2,
                  std.dev = summer_sd2 ,
                  se.shift = 1.96,
                  plot = F
                  )
In [232]: cusum_results
          List of 14
                             : language qcc::cusum(data = temps_df2$temp, std.dev = summer_sd2, se.shift = 1.
           $ call
          96,
                  plot = F, centervalue = summer_center2)
                             : chr "cusum"
           $ type
                             : chr "temps_df2$temp"
           $ data.name
                             : num [1:1240, 1] 98 97 97 90 89 93 93 91 93 93 ...
           $ data
            ... attr(*, "dimnames")=List of 2
           $ statistics : Named num [1:1240] 98 97 97 90 89 93 93 91 93 93 ...
            ... attr(*, "names")= chr [1:1240] "1" "2" "3" "4" ...
                         : int [1:1240] 1 1 1 1 1 1 1 1 1 1 ...
           $ sizes
           $ center
                            : num 88.7
           $ std.dev
                            : num 4.79
           $ pos
                             : num [1:1240] 0.965 1.72 2.476 1.771 0.857 ...
                            : num [1:1240] 0 0 0 0 0 0 0 0 0 0 0 ...
           $ neg
                             : num 0
           $ head.start
           $ decision.interval: num 5
           $ se.shift : num 1.96
           $ violations
                             :List of 2
           - attr(*, "class")= chr "cusum.qcc"
In [233]: | cusum_positive <- cusum_results$pos %>%
                  as_tibble() %>%
                  rownames_to_column() %>%
                  cbind(date = temps_df2$date_val) %>%
                  left_join(., temps_df2, by = c('date' = 'date_val')) %>%
                  dplyr::select(date, value, temp) %>%
                  filter(value != 0) %>%
                  arrange(date)
```

## In [234]: head(cusum\_positive,15)

```
date
                value temp
1996-07-01 0.96457762
1996-07-02 1.72044094
                         97
1996-07-03 2.47630427
1996-07-04 1.77116753
                         90
1996-07-05 0.85731649
                         89
1996-07-06 0.77832264
                         93
1996-07-07 0.69932878
                         93
1996-07-08 0.20290634
                         91
1996-07-09 0.12391248
                         93
1996-07-10 0.04491863
                         93
1996-07-17 0.54714903
                         96
1996-07-18 0.88558376
1996-07-19 1.43273279
                         96
1996-07-20 2.60602471
                         99
1996-07-21 2.10960226
                         91
```

```
In [236]: highest_cusum
```

date

2007-08-25

)

```
date
                value temp
2007-08-03
            0.1297204
2007-08-04
            0.8855838
                          97
2007-08-05
            1.4327328
                          96
2007-08-06
            2.3973104
                          98
2007-08-07
            3.3618880
                          98
2007-08-08
            4.7438942
                         100
2007-08-09
            6.7520433
                         103
2007-08-10
            8.7601924
                         103
2007-08-11 10.1421986
                         100
2007-08-12
            9.4370619
2007-08-13 10.8190681
                         100
2007-08-14 11.9923600
                          99
2007-08-15 13.7917948
                         102
2007-08-16 15.3825153
                         101
2007-08-17 16.9732358
                         101
2007-08-18 17.7290991
                          97
2007-08-19 18.0675339
                          95
2007-08-20 18.6146829
                          96
2007-08-21 19.7879748
2007-08-22 22.0048382
                         104
2007-08-23 22.9694158
                          98
2007-08-24 23.3078506
                          95
2007-08-25 23.4375710
                          94
2007-08-26 23.1498628
                          92
2007-08-27 22.0272975
                          88
2007-08-28 20.9047322
                          88
2007-08-29 19.9908811
                          89
2007-08-30 19.0770301
                          89
2007-08-31 17.5370362
                          86
```