

### Outline

- 1 First Section
  - Section 1 Subsection 1
  - Section 1 Subsection 2
  - Section 1 Subsection 3
- 2 Second Section
  - Section 2 Subsection 1
  - Section 2 Last Subsection

1 First Section

#### Section 1 - Subsection 1

Section 1 - Subsection 2

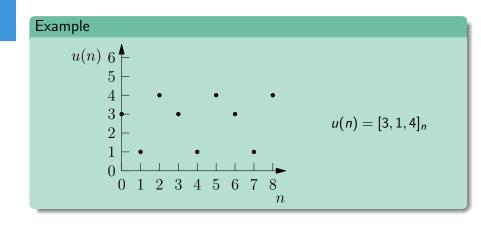
Section 1 - Subsection 3

### 2 Second Section

Section 2 - Subsection 1

Section 2 - Last Subsection







#### Definition

Let n be a discrete variable, i.e.  $n \in \mathbb{Z}$ . A 1-dimensional periodic number is a function that depends periodically on n.

$$u(n) = [u_0, u_1, \dots, u_{d-1}]_n = \begin{cases} u_0 & \text{if } n \equiv 0 \pmod{d} \\ u_1 & \text{if } n \equiv 1 \pmod{d} \\ \vdots & \\ u_{d-1} & \text{if } n \equiv d-1 \pmod{d} \end{cases}$$

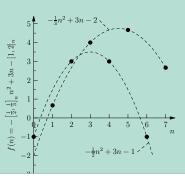
d is called the period.



### Example

$$f(n) = -\left[\frac{1}{2}, \frac{1}{3}\right]_n n^2 + 3n - [1, 2]_n$$

$$= \begin{cases} -\frac{1}{3}n^2 + 3n - 2 & \text{if } n \equiv 0 \pmod{2} \\ -\frac{1}{2}n^2 + 3n - 1 & \text{if } n \equiv 1 \pmod{2} \end{cases}$$





#### Definition

A polynomial in a variable x is a linear combination of powers of x:

$$f(x) = \sum_{i=0}^{g} c_i x^i$$



#### **Definition**

A polynomial in a variable x is a linear combination of powers of x:

$$f(x) = \sum_{i=0}^{g} c_i x^i$$

### Definition

A quasi-polynomial in a variable *x* is a polynomial expression with periodic numbers as coefficients:

$$f(n) = \sum_{i=0}^{g} u_i(n)n^i$$

with  $u_i(n)$  periodic numbers.



1 First Section

Section 1 - Subsection 1

Section 1 - Subsection 2

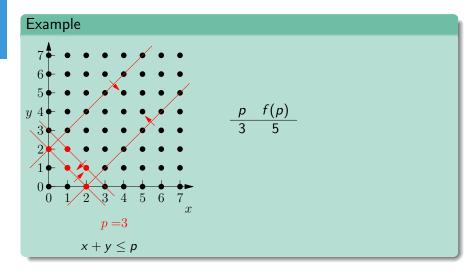
Section 1 - Subsection 3

2 Second Section

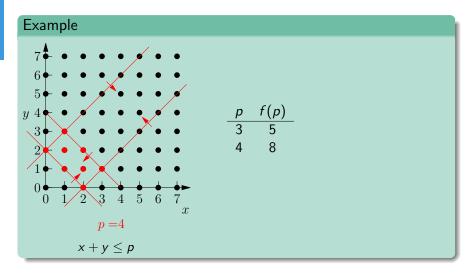
Section 2 - Subsection 1

Section 2 - Last Subsection

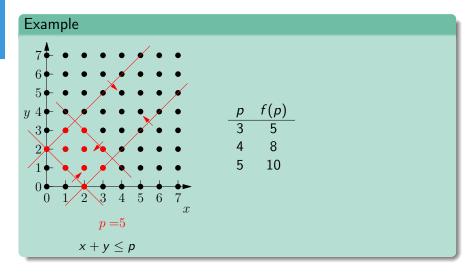




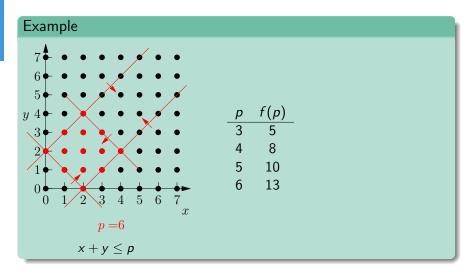




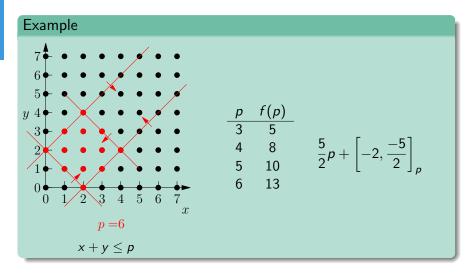














• The number of integer points in a parametric polytope  $P_p$  of dimension n is expressed as a piecewise a quasi-polynomial of degree n in p (Clauss and Loechner).



- The number of integer points in a parametric polytope  $P_p$  of dimension n is expressed as a piecewise a quasi-polynomial of degree n in p (Clauss and Loechner).
- More general polyhedral counting problems:
   Systems of linear inequalities combined with ∨, ∧, ¬, ∀, or ∃
   (Presburger formulas).

- The number of integer points in a parametric polytope  $P_p$  of dimension n is expressed as a piecewise a quasi-polynomial of degree n in p (Clauss and Loechner).
- More general polyhedral counting problems:
   Systems of linear inequalities combined with ∨, ∧, ¬, ∀, or ∃
   (Presburger formulas).
- Many problems in static program analysis can be expressed as polyhedral counting problems.

1 First Section

Section 1 - Subsection 1

Section 1 - Subsection 2

Section 1 - Subsection 3

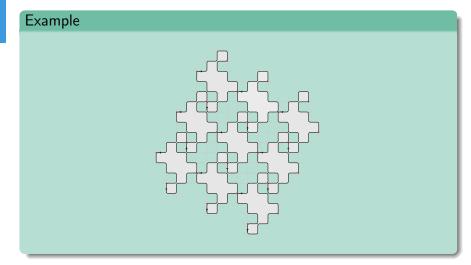
2 Second Section

Section 2 - Subsection 1

Section 2 - Last Subsection



A picture made with the package TiKz





- 1 First Section
  - Section 1 Subsection 1
  - Section 1 Subsection 2
  - Section 1 Subsection 3
- 2 Second Section
  - Section 2 Subsection 1
  - Section 2 Last Subsection



#### Alertblock

This page gives an example with numbered bullets (enumerate) in an "Example" window:

### Example

Discrete domain  $\Rightarrow$  evaluate in each point

Not possible for

parametric domains



#### Alertblock

This page gives an example with numbered bullets (enumerate) in an "Example" window:

### Example

Discrete domain  $\Rightarrow$  evaluate in each point Not possible for

- parametric domains
- 2 large domains (NP-complete)

- first Section
  - Section 1 Subsection 1
  - Section 1 Subsection 2
  - Section 1 Subsection 3
- 2 Second Section
  - Section 2 Subsection 1
  - Section 2 Last Subsection





# Last Page

### Summary

End of the beamer demo with a *tidy* TU Delft lay-out. Thank you!

