Analytic Solution