

Name: Atharva Bilonikar

Uid no: 2021700011

CSE DS D1

DAA EXP 5

Aim:

Matrix Chain multiplication using Dynamic Programming

Algorithm:

MATRIX-CHAIN-ORDER (p)

```
1   $n = p.length - 1$ 
2  let  $m[1 \dots n, 1 \dots n]$  and  $s[1 \dots n - 1, 2 \dots n]$  be new tables
3  for  $i = 1$  to  $n$ 
4       $m[i, i] = 0$ 
5  for  $l = 2$  to  $n$            //  $l$  is the chain length
6      for  $i = 1$  to  $n - l + 1$ 
7           $j = i + l - 1$ 
8           $m[i, j] = \infty$ 
9          for  $k = i$  to  $j - 1$ 
10              $q = m[i, k] + m[k + 1, j] + p_{i-1} p_k p_j$ 
11             if  $q < m[i, j]$ 
12                  $m[i, j] = q$ 
13                  $s[i, j] = k$ 
14  return  $m$  and  $s$ 
```

PRINT-OPTIMAL-PARENS (s, i, j)

```
1  if  $i = j$ 
2      then print " $A_i$ "
3  else print "("
4      PRINT-OPTIMAL-PARENS ( $s, i, s[i, j]$ )
5      PRINT-OPTIMAL-PARENS ( $s, s[i, j] + 1, j$ )
6      print ")"
```

In the example of Figure 15.3, the call **PRINT-OPTIMAL-PARENS**($s, 1, 6$) prints the parenthesization $((A_1(A_2A_3))((A_4A_5)A_6))$.

Code:

```

#include <bits/stdc++.h>
using namespace std;

void printParenthesis(int i, int j, int n, int* bracket,
                     char& name)
{
    if (i == j) {
        cout << name++;
        return;
    }

    cout << "(";

    printParenthesis(i, *((bracket + i * n) + j), n,
                     bracket, name);

    printParenthesis(*((bracket + i * n) + j) + 1, j, n,
                     bracket, name);
    cout << ")";
}

void matrixChainOrder(int p[], int n)
{
    int m[n][n];

    int bracket[n][n];

    for (int i = 1; i < n; i++)
        m[i][i] = 0;

    // L is chain length.
    for (int L = 2; L < n; L++)
    {
        for (int i = 1; i < n - L + 1; i++)
        {
            int j = i + L - 1;
            m[i][j] = INT_MAX;
            for (int k = i; k <= j - 1; k++)
            {

```

```

        int q = m[i][k] + m[k + 1][j]
                + p[i - 1] * p[k] * p[j];
        if (q < m[i][j])
        {
            m[i][j] = q;

            bracket[i][j] = k;
        }
    }
}

char name = 'A';

cout << "Optimal Parenthesization is : ";
printParenthesis(1, n - 1, n, (int*)bracket, name);
cout << "\nOptimal Cost is : " << m[1][n - 1];
}

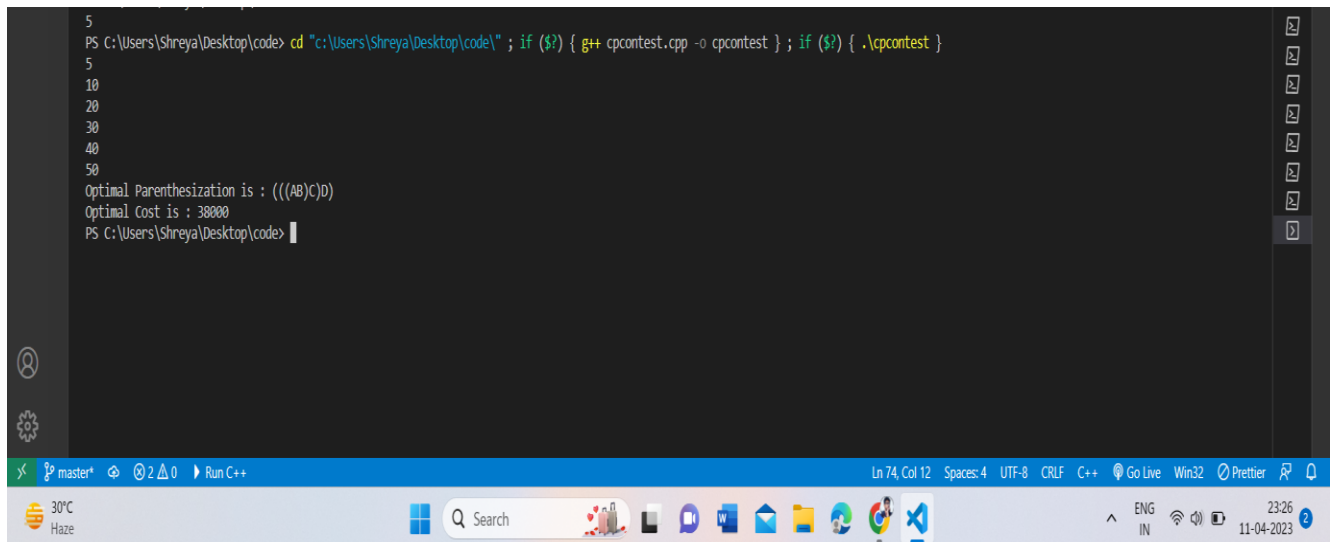
int main()
{
    int N;
    cin>>N;
    int arr[N];
    for(int i=0;i<N;i++)cin>>arr[i];

    matrixChainOrder(arr, N);
    return 0;
}

```

Output:

```
5
PS C:\Users\Shreya\Desktop\code> cd "c:\Users\Shreya\Desktop\code\" ; if ($?) { g++ cpcontest.cpp -o cpcontest } ; if ($?) { .\cpcontest }
5
10
20
30
40
50
Optimal Parenthesization is : (((AB)C)D)
Optimal Cost is : 38000
PS C:\Users\Shreya\Desktop\code> |
```



Conclusion:

In this experiment, I understood how to implement MCM algorithm using dynamic programming technique.