

HA-3

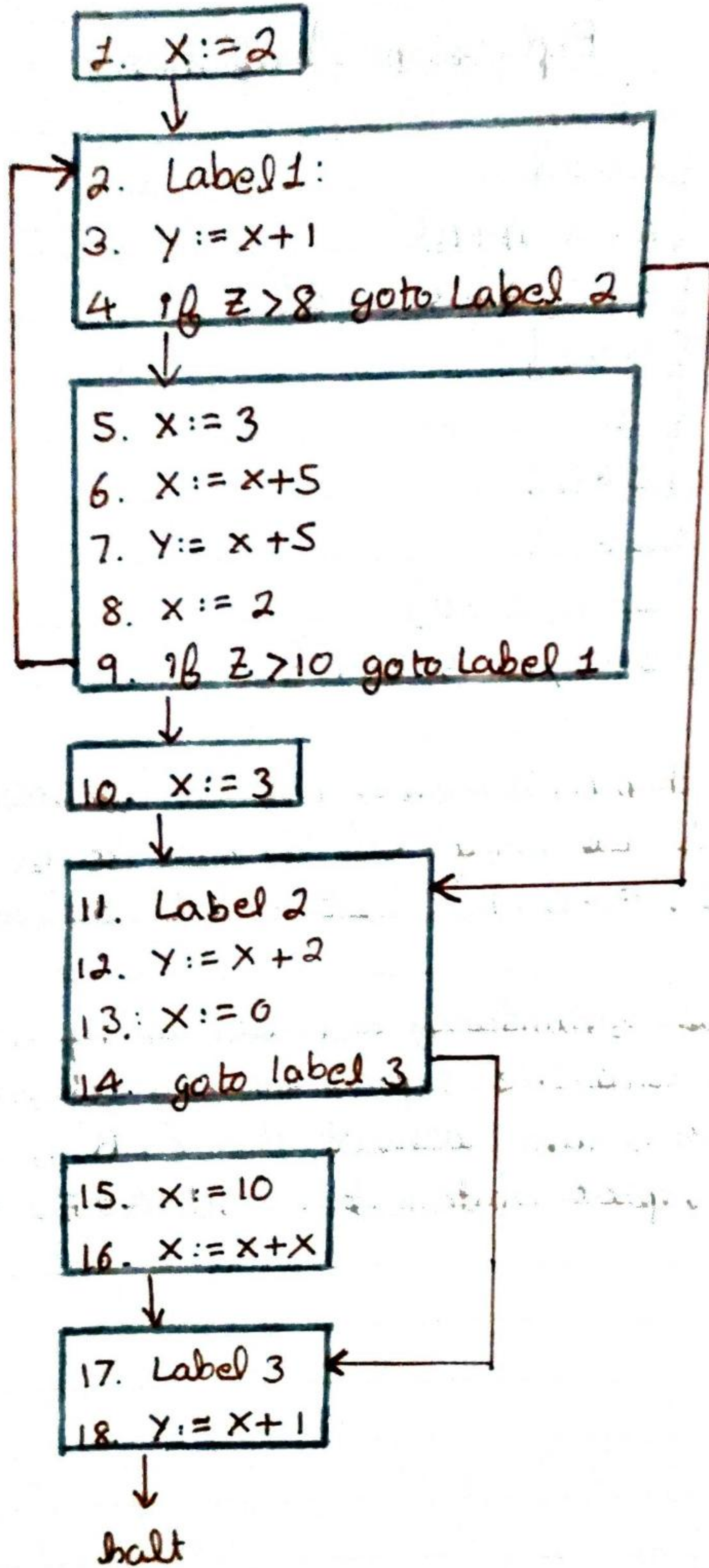
1)
a)

Statement	Expressions Available
1. $A = 7;$	$\{ \}$
2. $B = A + 2;$	$\{A + 2\}$
3. $C = A + B;$	$\{A + 2, A + B\}$
4. $D = C + B;$	$\{A + 2, A + B, C + B\}$
5. $B = D; / B = C + B;$	$\{A + 2\}$
6. $A = A + B;$	$\{ \}$
7. $E = C + D;$	$\{C + D\}$
8. $F = E; / F = C + D;$	$\{C + D\}$
9. $G = C + B;$	$\{C + D, C + B\}$
10. $H = E + F;$	$\{C + D, C + B, E + F\}$

b) If E & C were aliased, then $C + D$ would not be available after statement 7 ($E = C + D$), & we would not be able to perform CSE on statement 8 ($F = E / F = C + D$). Result will be the same.

c) Aliasing might increase redundancy because an expression that looks different than an available expression may actually be redundant. ~~But~~ If B & D were aliased, then $C + B$ is the same as $C + D$, & we could replace statement 9 with $G = E$.

2)



Leaders $\Rightarrow \{1, 2, 5, 10, 11, 15, 17\}$

3) Code after constant propagation 1st time =>

1. $x := 2$
2. Label 1
3. $y := 2 + 1$
4. if $z > 8$ goto label 2
5. $x := 3$
6. $x := 3 + 5$
7. $y := x + 5$
8. $x := 2$
9. if $z > 10$ goto label 1
10. $x := 3$
11. Label 2
12. $y := x + 2$
13. $x := 0$
14. goto label 3
15. $x := 10$
16. $x := 10 + 10$
17. Label 3
18. $y := 0 + 1$

Code after 2nd
constant propagation =>

1. $x := 2$
2. Label 1
3. $y = 3$
4. if $z > 8$ goto label 2
5. $x := 3$
6. $x := 8$
7. $y := 8 + 5$
8. $x := 2$
9. if $z > 10$ goto label 1
10. $x := 3$
11. Label 2
12. $y := x + 2$
13. $x := 0$
14. goto label 3
15. $x := 10$
16. $x := 20$
17. Label 3
18. $y := 1$

Code after 1st constant folding =>

1. $X := 2$
2. Label 1
3. $Y := 3$
4. if $Z > 8$ goto Label 2
5. $X := 3$
6. $X := 8$
7. $Y := X + 5$
8. $X := 2$
9. if $Z > 10$ goto Label 1
10. $X := 3$
11. Label 2
12. $Y := X + 2$
13. $X := 0$
14. goto Label 3
15. $X := 10$
16. $X := 20$
17. Label 3
18. $Y := 1$

Code after 2nd constant folding =>

1. $X := 2$
2. Label 1
3. $Y := 3$
4. if $Z > 8$ goto Label 2
5. $X := 3$
6. $X := 8$
7. $Y := 13$
8. $X := 2$
9. if $Z > 10$ goto Label 1
10. $X := 3$
11. Label 2
12. $Y := X + 2$
13. $X := 0$
14. goto Label 3
15. $X := 10$
16. $X := 20$
17. Label 3
18. $Y := 1$

4) a) $\left. \begin{array}{l} \text{Loop Def} = \{z, y, x\} \\ \text{Loop Use} = \{x, z, c, y\} \end{array} \right\} \text{Variables}$

$$\begin{aligned} \text{Invariant variables} &= \text{Loop Use} - \text{Loop Def} \\ &= \{x, z, c, y\} - \{z, y, x\} \\ &= \{c\} \end{aligned}$$

Invariant expression \Rightarrow ~~$2 * c$~~ in line 5. \Rightarrow $2 * c$

Yes, it can be factored out of the loop body.

~~temp = 2 * c~~ temp = 2 * c

~~temp~~ z = temp

But if the loop is never executed, then factoring it out might become overhead.

b) Basic induction variables $\{I = I \pm S\}$ \therefore Here $\boxed{7 \mid x := x + 1}$ is III
 $= \{x\}$

Mutual induction variables $\{J = I * E \pm D\}$ c, D are loop invariants
 $= \{y\}$ \therefore Here $\boxed{6 \mid y = z * x}$ is III

c) After code motion \Rightarrow

1. $x = a * a$
2. $c = -1 * x$
3. $z = 2 * c$
4. L1:
5. if ($x > 100$) goto L2
6. $y = z * x$
7. $x = x + 1$
8. goto L1
9. L2:

4 c) After strength reduction \Rightarrow

1. $x = a * a$

2. $c = -1 * x$

3. $z = 2 * c$

4. $t1 = z * x$

5. $t2 = z * 100$

6. $L1:$

7. $\text{if } (t1 \geq t2) \text{ goto } L2$

8. $y = t1$

9. $t1 = t1 + z$

10. $\text{goto } L1$

11. $L2$

5)

Block	LineIn	LineOut
b1	$\{y, z, w\}$	$\{y, z, w\}$
b2	$\{y, z, w\}$	$\{y, z, w\}$
b3	$\{y, z, w\}$	$\{y, z, w\}$
b4	$\{y, z\}$	$\{w, y, z\}$
b5	$\{w, y\}$	$\{\}$