

# DEDS Summer School Presentation

## ESR#2.4 Analytic Operators for Trajectories

7 July 2023

Song WU

Home Supervisors (ULB): Esteban Zimányi, Mahmoud Sakr  
Host Supervisors (AAU): Kristian Torp



AALBORG UNIVERSITY  
DENMARK



# Agenda

## Current Status

## Scientific Content

Semantic segmentation of AIS trajectories

Evaluation of Vessel CO<sub>2</sub> Emissions Methods

Fusion of trajectories from AIS and Camera (ongoing secondment)



# Current Status: where & progress

## Courses

- ▶ all ECTS are finished

## Relocation

- ▶ (home) ULB, 1 Sep 2021 - 31 Aug 2022
- ▶ (host) AAU, 1 Sep 2022 - 31 May 2023
- ▶ Secondment at MarineTraffic in Athens, 01 June 2023 - 31 Aug 2023 (ongoing)

## Research Output

- ▶ one 6-page workshop paper at the MDM'2022 conference (before DPP)  
Semantic Segmentation of AIS Trajectories for Detecting Complete Fishing Activities
- ▶ one 10-page research paper accepted at SSTD'2023 conference (after DPP)  
Evaluation of Vessel CO<sub>2</sub> Emissions Methods using AIS Trajectories



# Semantic segmentation of AIS trajectories

## Motivation

Illegal, unreported and unregulated (IUU) fishing is becoming an increasing concern<sup>1</sup>.  
*So it is important to know when & where a ship may have performed fishing activities.*

## Definition

trajectory  $T$ :  $(p_1, t_1), (p_2, t_2), \dots, (p_{n-1}, t_{n-1}), (p_n, t_n)$ , an ordered sequence of timestamped points where  $p_i$  is the coordinate of a moving object at the timestamp  $t_i$ .

## Problem Statement

Given a trajectory  $T$ , this work aims to split  $T$  into a sequence of labelled segments  $\langle (S_1, l_1), \dots, (S_k, l_k) \rangle$ , where  $S_i$  is a continuous sequence of points in  $T$ , and  $l_i$  is the label of segment  $\in \{\text{fishing, non-fishing}\}$ .

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<sup>1</sup>[https://ec.europa.eu/oceans-and-fisheries/fisheries/rules/illegal-fishing\\_en](https://ec.europa.eu/oceans-and-fisheries/fisheries/rules/illegal-fishing_en)



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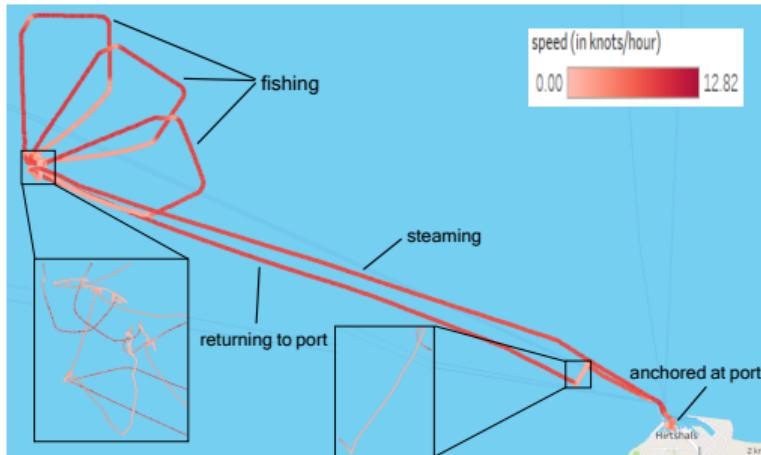
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# Semantic segmentation of AIS trajectories

## Limitations of existing approaches

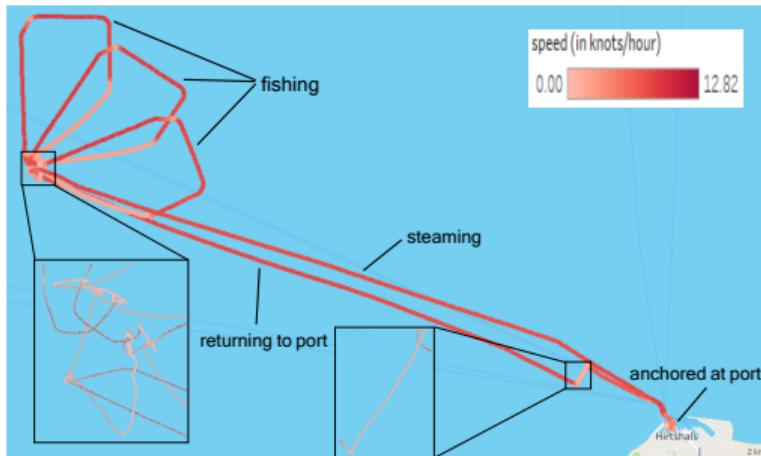
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- ▶ segments are returned without labels, such as W-Kmeans[6], SWS[1].
- ▶ Many studies assume that returned segments should have high homogeneity w.r.t. some spatiotemporal criteria or features of points, such as GRASP-UTS[13].



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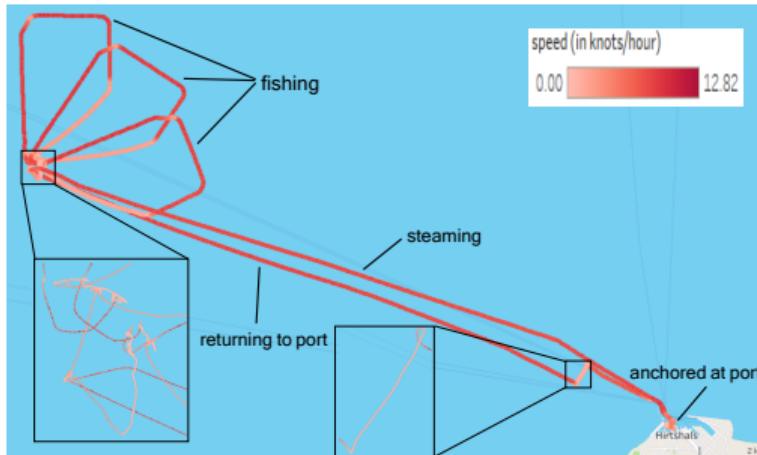
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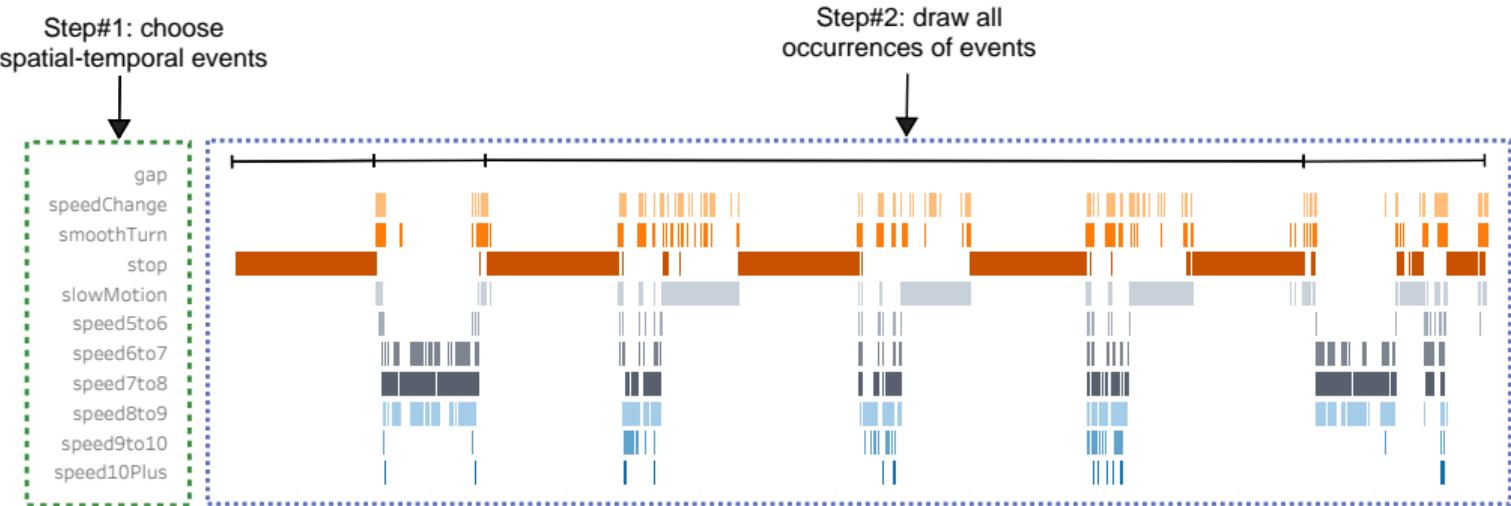
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# Semantic segmentation of AIS trajectories

## Proposed solution

part#1: feature design by TPoSTE (Temporal Profiling of Spatio-Temporal Events)



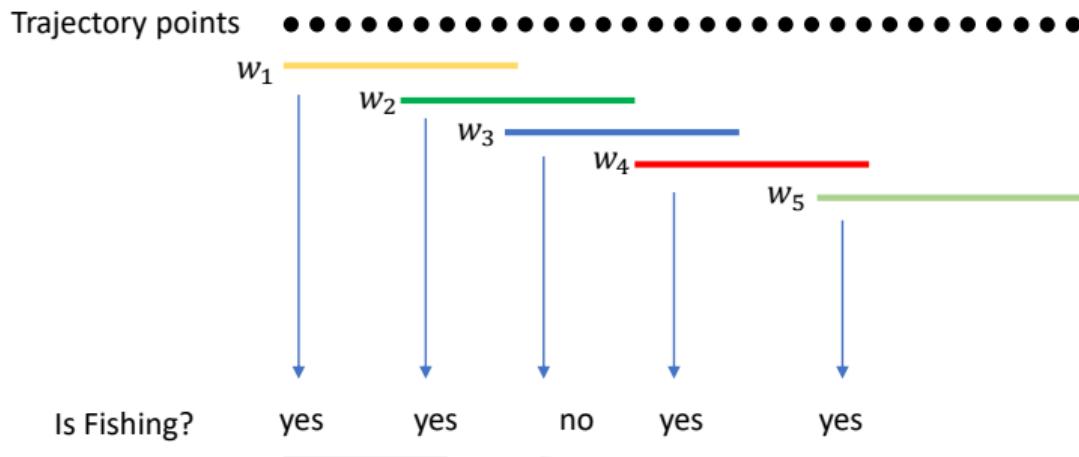
Step#3: gain some insights that help design features capturing movement patterns

# Semantic segmentation of AIS trajectories

## Proposed solution

### part#2: Window-Based Trajectory Segmentation using Run-Length Encoding

- ▶ a window is required to contain at least  $size_w$  points and its duration is larger than a time threshold  $t_w$ .
- ▶ two adjacent windows have some overlap indicated by  $ratio$ .



# Semantic segmentation of AIS trajectories

## Proposed solution

part#2: Window-Based Trajectory Segmentation using Run-Length Encoding  
(an alternating sequence of counts  $\dots, a_{fishing}, b_{sailing}, c_{fishing}, \dots$  is obtained.)

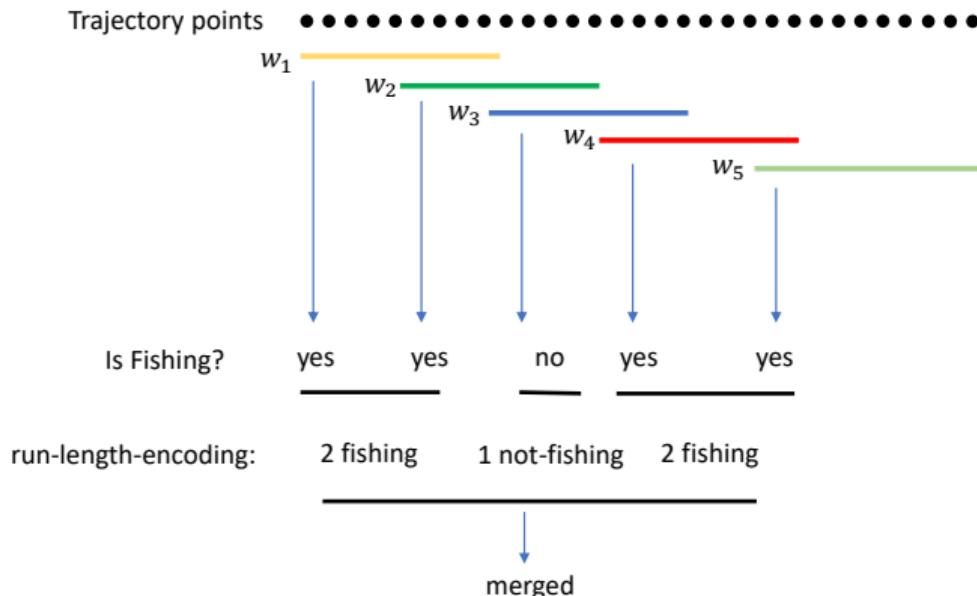
**A complete fishing activity A is a maximal subsequence of counts that:**

- ▶ A starts and ends with fishing counts.
- ▶ each triplet  $\langle a_{fishing}, b_{sailing}, c_{fishing} \rangle$  in A fulfills  $a \geq b$  and  $b \leq c$  to correct occasional classification errors.

# Semantic segmentation of AIS trajectories

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part#2: Window-Based Trajectory Segmentation using Run-Length Encoding

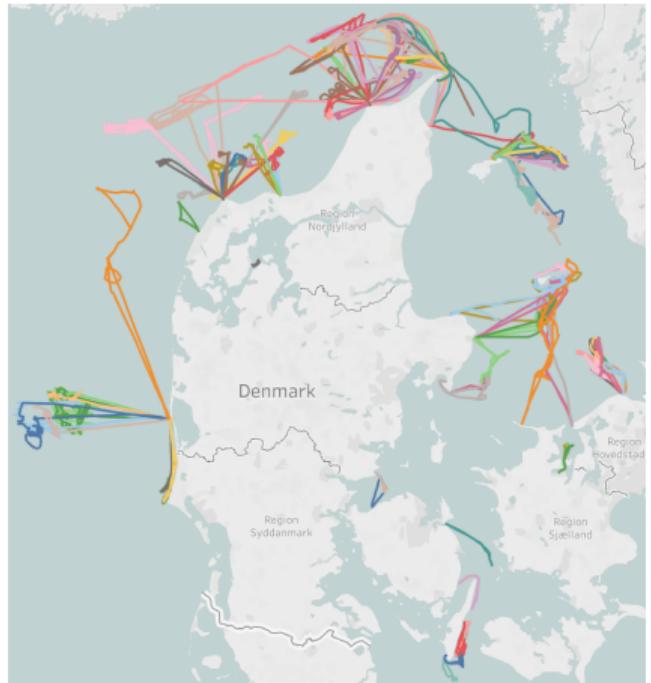


# Semantic segmentation of AIS trajectories

## Datasets

We manually labeled 128 trajectories that are likely to contain fishing activities.

- ▶ publicly available from [Danish Maritime Authority](#)
- ▶ average sampling frequency: 10.63 seconds
- ▶ # of points: 1,080,220
- ▶ 31 trajs for training, 97 trajs for testing

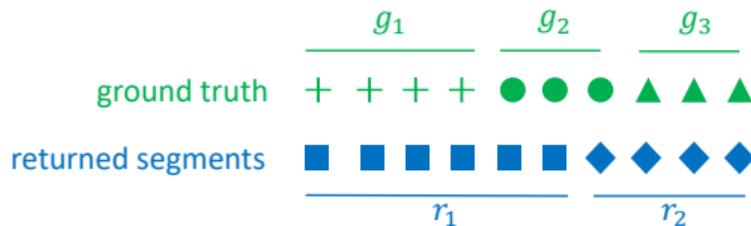


# Semantic segmentation of AIS trajectories

three state-of-the-art for comparison: CB-SMoT, W-Kmeans, SWS

Four metrics are used:

- ▶ Purity (introduced in [13])
- ▶ Coverage (introduced in [13])
- ▶ Harmonic Mean of Purity and Coverage
- ▶ # of returned segments



$$\text{Purity} = (4/6 + 3/4) / 2$$

$$\text{Coverage} = (4/4 + 2/3 + 3/3) / 3$$

# Semantic segmentation of AIS trajectories

## Results

WBS-RLE achieves:

- ▶ the highest harmonic mean
- ▶ the closest number of segments w.r.t ground truth, except WKMeans ( $k=3$ )

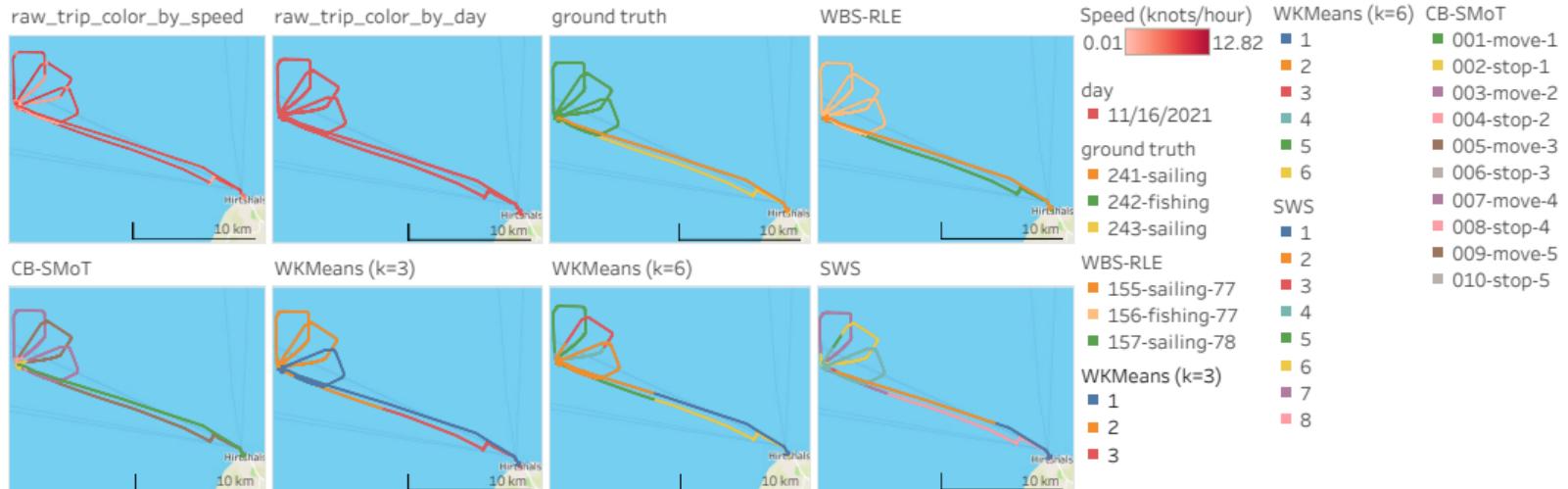
method	purity	coverage	harmonic mean	# of segments
WBS-RLE	0.890	0.974	0.927	2.670
CB-SMoT	0.859	0.885	0.859	5
WKMeans ( $k=3$ )	0.878	0.840	0.855	3
WKMeans ( $k=6$ )	0.932	0.619	0.741	6
SWS	0.954	0.759	0.837	9.855

Table: average performance on the 97 trajectories

\* all segmentation results are available [online](#)

# Semantic segmentation of AIS trajectories

Segmentation result for the trajectory #220051000-2



# Evaluation of Vessel CO<sub>2</sub> Emissions Methods

## Motivation

1. growing interest of society in environmental friendliness and sustainability
2. about **90%** of global trade is fulfilled by shipping
3. In 2018, shipping CO<sub>2</sub> emissions were estimated to be **1,056 million tons** by IMO
4. accurate estimation of shipping CO<sub>2</sub> emissions is important for developing regulations

## Research gap:

- ▶ None of the review studies [2, 15, 14] does a quantitative comparison of models
- ▶ The comparative studies [8, 9] are limited to a small area near the Strait of Gibraltar

## Contribution

- ▶ a general data-driven framework to compare/validate ship emission models
- ▶ extensive experiments are conducted and insights are presented

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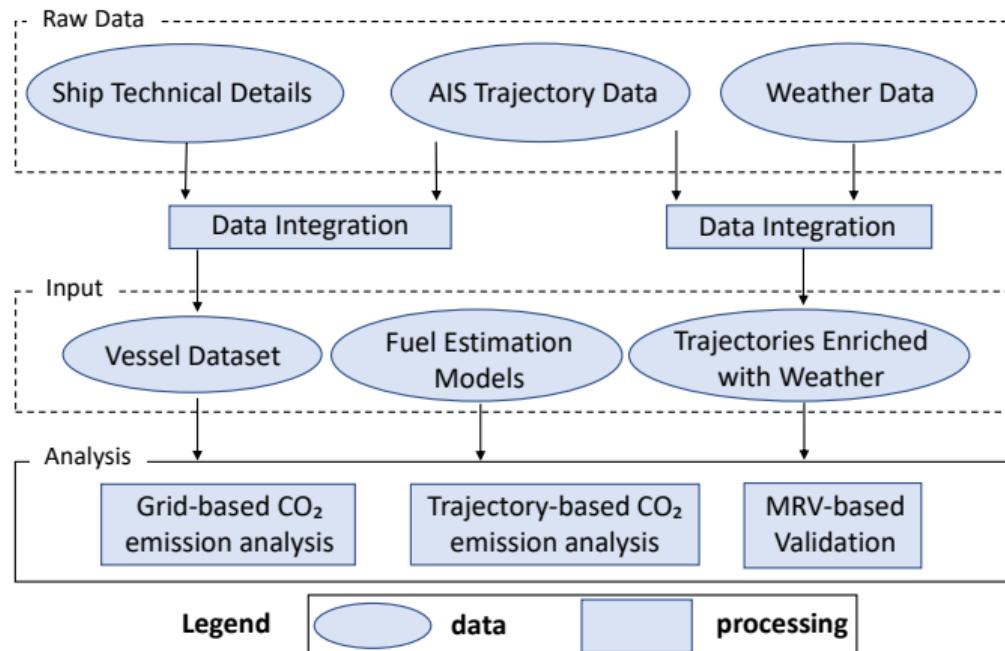


Figure: Overview of the Evaluation Framework

# Evaluation of Vessel CO<sub>2</sub> Emissions Methods

Currently, five models are considered in our framework.

- ▶ **Baseline**: assumes a certain amount of CO<sub>2</sub> are emitted per metric ton of cargo per kilometer of transport, 3 grams CO<sub>2</sub> / (ton · km) [3].
- ▶ **GrossTonnage** [7]: The daily fuel consumption  $C$  is linearly related to the gross tonnage of a ship, and the CO<sub>2</sub> emissions per ton of fuel depends on operation mode.
- ▶ **SpeedCubic** [4]: speed is considered, and the emission factor (gCO<sub>2</sub>/kWh) depends on engine type and fuel type.
- ▶ **IMO** [10]: speed and draught are considered. The emission factor (gCO<sub>2</sub>/kWh) depends on engine type/load/generation and fuel type.
- ▶ **STEAM** [5]: speed is considered. A speed penalty is added based on wave conditions.

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# Evaluation of Vessel CO<sub>2</sub> Emissions Methods

summary of required input by the five models

Models	TPC	DWT	D	P	S	GT	RPM	Year	Length	Beam	Wave
Baseline	✓	✓	✓								
GrossTonnage					✓	✓					
SpeedCubic				✓	✓		✓				
IMO			✓	✓	✓		✓	✓			
STEAM				✓	✓				✓	✓	✓

TPC: tons per centimeter

D: maximum draught

S: maximum speed

RPM: revolutions per minute

DWT: deadweight

P: maximum power

GT: gross tonnage

# Evaluation of Vessel CO<sub>2</sub> Emissions Methods

## AIS data

One-month data from May 2022 was downloaded from the Danish Maritime Authority<sup>2</sup>. 41,024,724 records from 1,571 cargo ships were used.

## Ship Technical Details

Public information in six websites were collected.

- ① BalticShipping ② Bureau Veritas ③ FleetMon
- ④ MarineTraffic ⑤ ShipAtlas ⑥ VesselTracker

## Wave Data (wave height and direction)

Two products were used from the Copernicus Marine Service.

- Baltic Sea<sup>3</sup>: spatial res. 1nm × 1nm ; temporal res. 1 hour
- North Sea<sup>4</sup>: spatial res. 3km × 1.5km ; temporal res. 1 hour

<sup>2</sup><https://web.ais.dk/aisdata/>

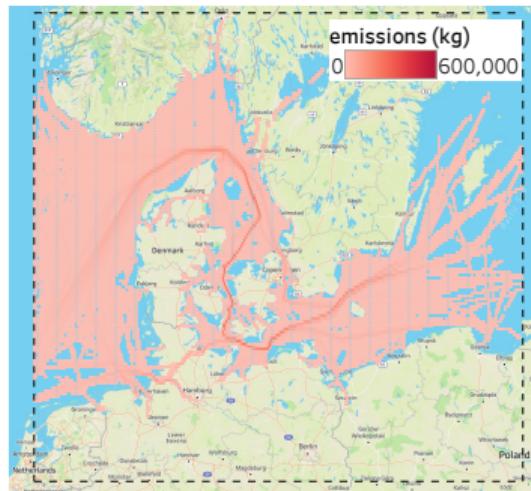
<sup>3</sup><https://goo.by/FKzLj>

<sup>4</sup><https://goo.by/vPwnP>

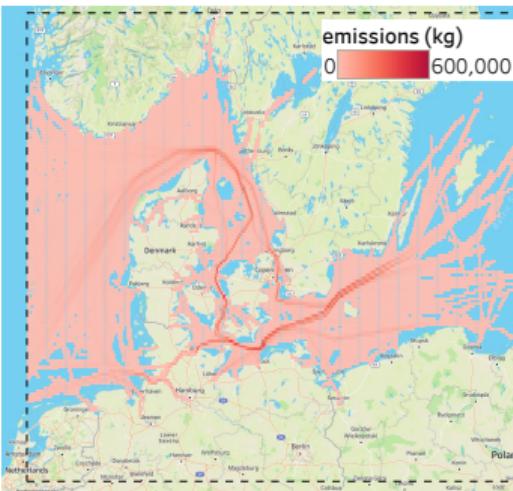
# Evaluation of Vessel CO<sub>2</sub> Emissions Methods

Grid-based analysis

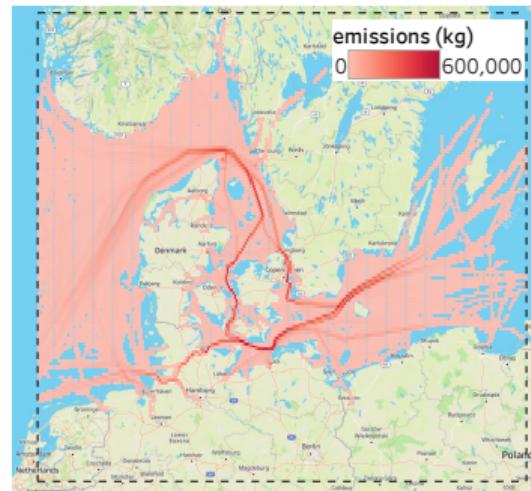
The area of interest in divided into 0.05° by 0.05° grids



(a) Baseline



(b) IMO



(c) GrossTonnage

Figure: Spatial distribution of CO<sub>2</sub> emissions by each model

# Evaluation of Vessel CO<sub>2</sub> Emissions Methods

Grid-based analysis

Comparison of absolute emissions by each model

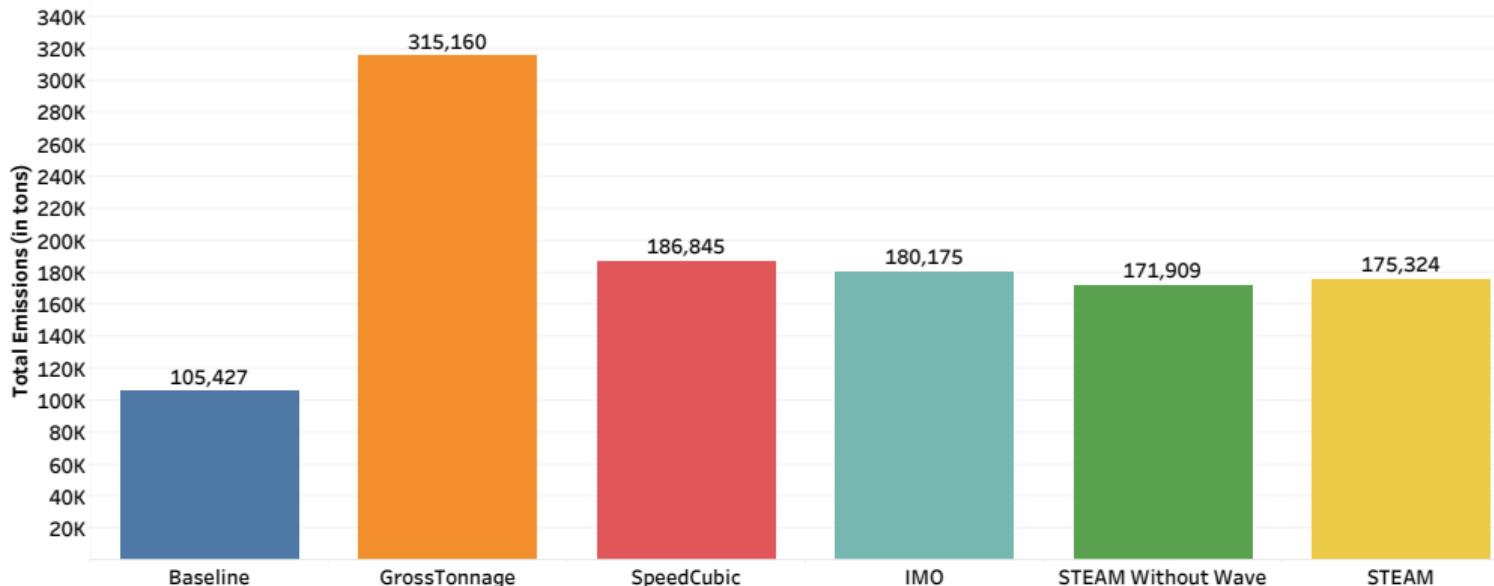
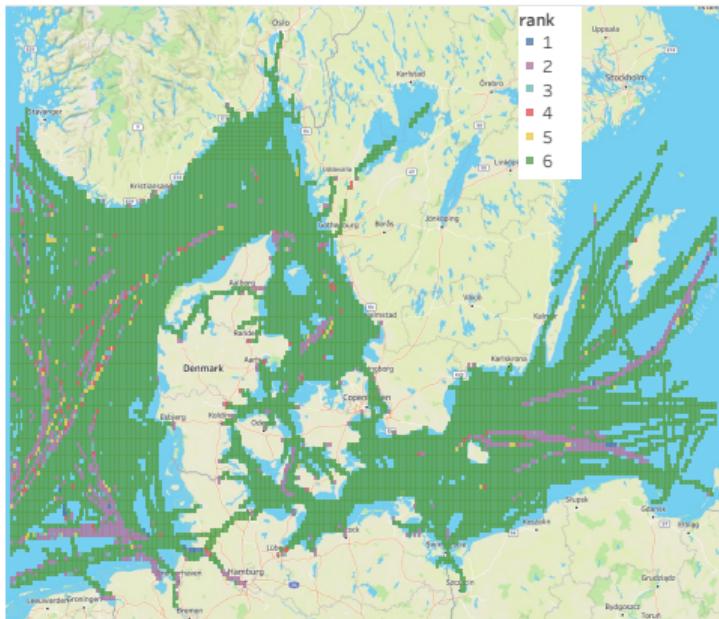


Figure: Total CO<sub>2</sub> emissions of the 1,571 ships by each model

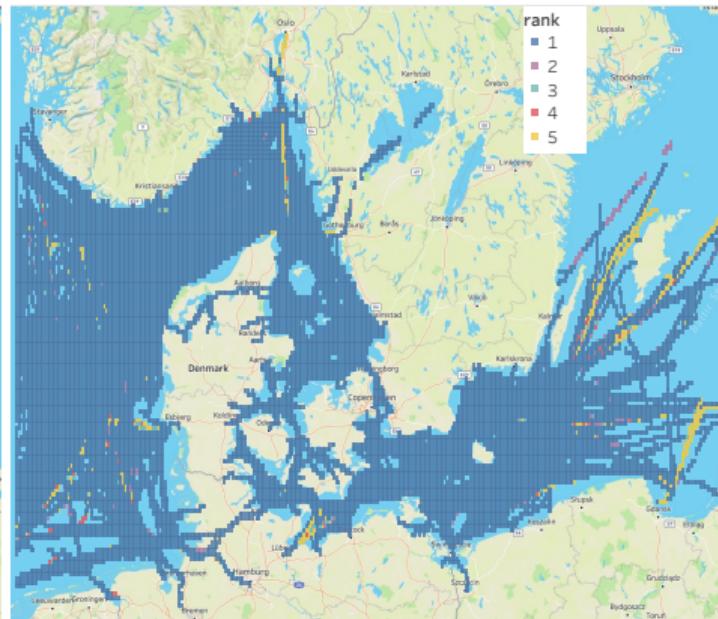
# Evaluation of Vessel CO<sub>2</sub> Emissions Methods

Grid-based analysis

Grid-level ranking of each model: "1" highest ("6" lowest) emissions



(a) Baseline

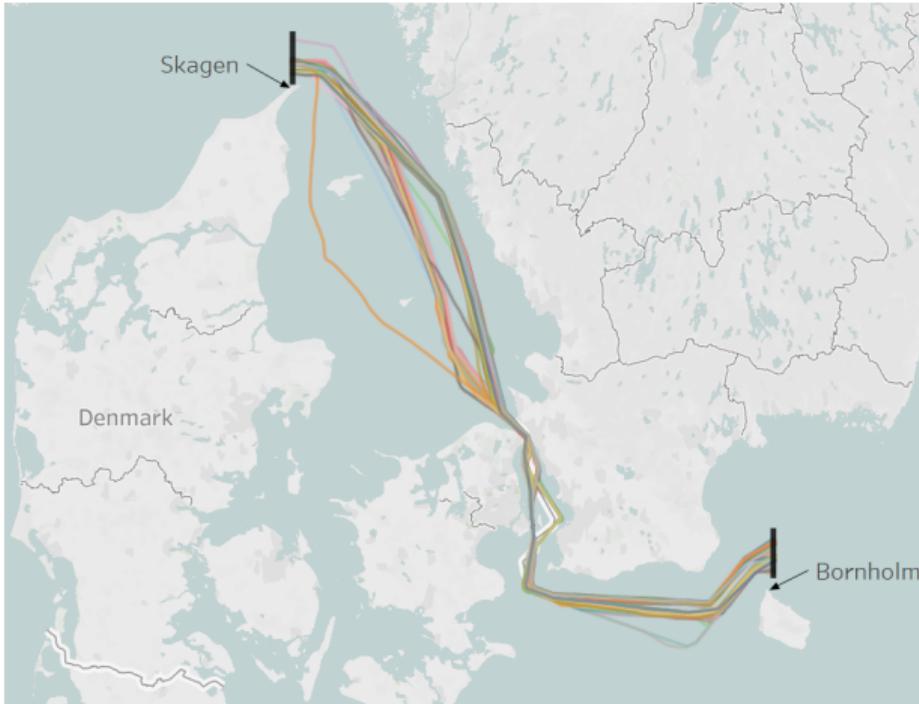


(b) GrossTonnage

# Evaluation of Vessel CO<sub>2</sub> Emissions Methods

Trajectory-based analysis

192 trips are selected travelling between Skagen and Bornholm



# Evaluation of Vessel CO<sub>2</sub> Emissions Methods

## Trajectory-based analysis

### Statistic of the 192 trips

min. / avg. / max. length (km)	478.4 / 488.8 / 507.9
min. / avg. / max. duration (hours)	13.8 / 23.3 / 32.9
min. / avg. / max. passing speed (knots/hour)	8.0 / 11.7 / 19.0

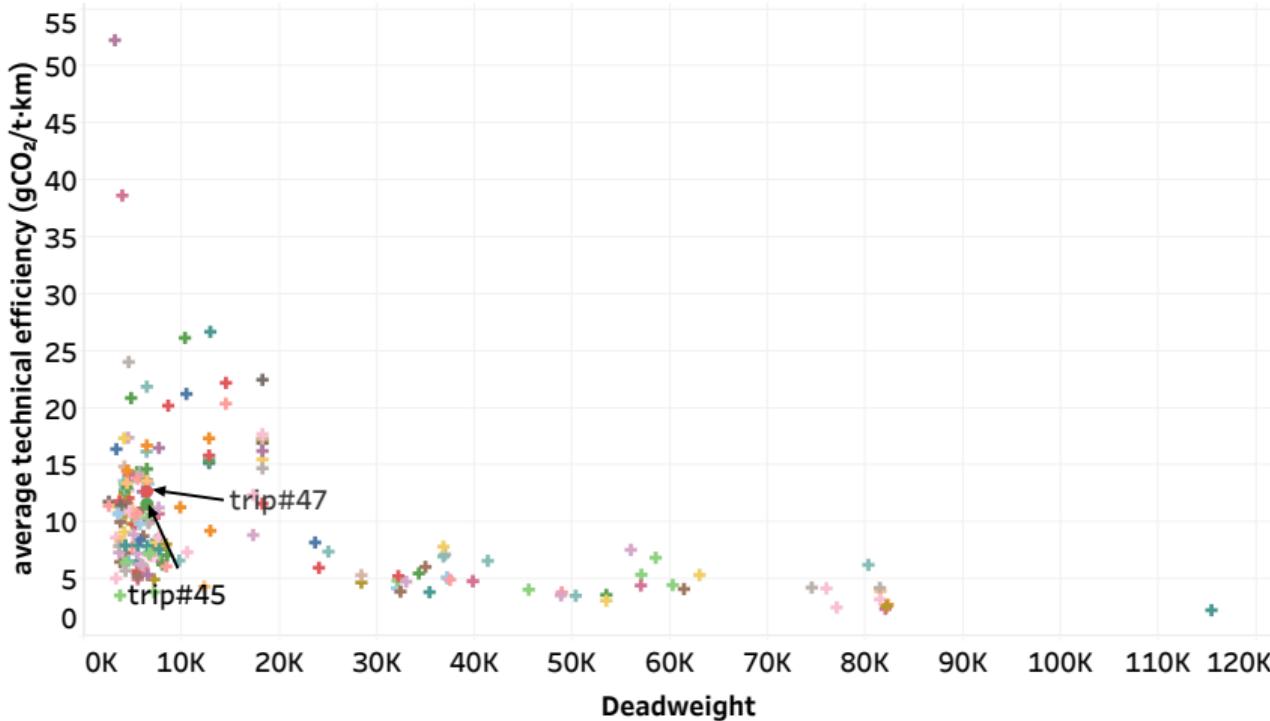
### Equivalent CO<sub>2</sub> efficiency for each trip

$$E_{CO_2,i} = \frac{CO_2\_IMO}{Cargo_i * Length_i}, 1 \leq i \leq 192$$

# Evaluation of Vessel CO<sub>2</sub> Emissions Methods

Trajectory-based analysis

Equivalent CO<sub>2</sub> efficiency of the 192 trips



# Evaluation of Vessel CO<sub>2</sub> Emissions Methods

## Trajectory-based analysis

trip#45 and trip#47 by the same ship ( $DWT = 6,410\text{ t}$ ,  $S = 19\text{ knots/h}$ )

	trip#45	trip#47
length (km)	489.8	489.6
avg. passing speed (knots/hour)	13.17	14.15
CO <sub>2</sub> emissions (kg)	36,372	39,798
CO <sub>2</sub> efficiency (gCO <sub>2</sub> /t·km)	11.58	12.68

A 5.2% decrease in speed leads to a 8.7% increase in CO<sub>2</sub> efficiency

- it suggests that shipowners can probably improve CO<sub>2</sub> efficiency of their fleet by speed optimization.

# Evaluation of Vessel CO<sub>2</sub> Emissions Methods

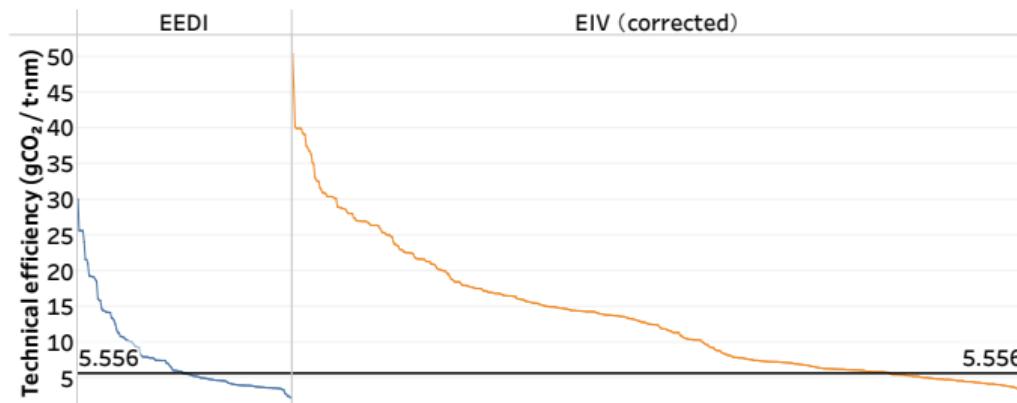
MRV-based validation

## The EU's Monitoring, Reporting and Verification (MRV) system

- ship above 5,000 gross tonnage should report CO<sub>2</sub> emissions data for their maritime transport activities in the EU waters.
- 760 out of the 1,571 ships have matching entries in the MRV dataset.

## CO<sub>2</sub> efficiency of the 760 ships based on MRV

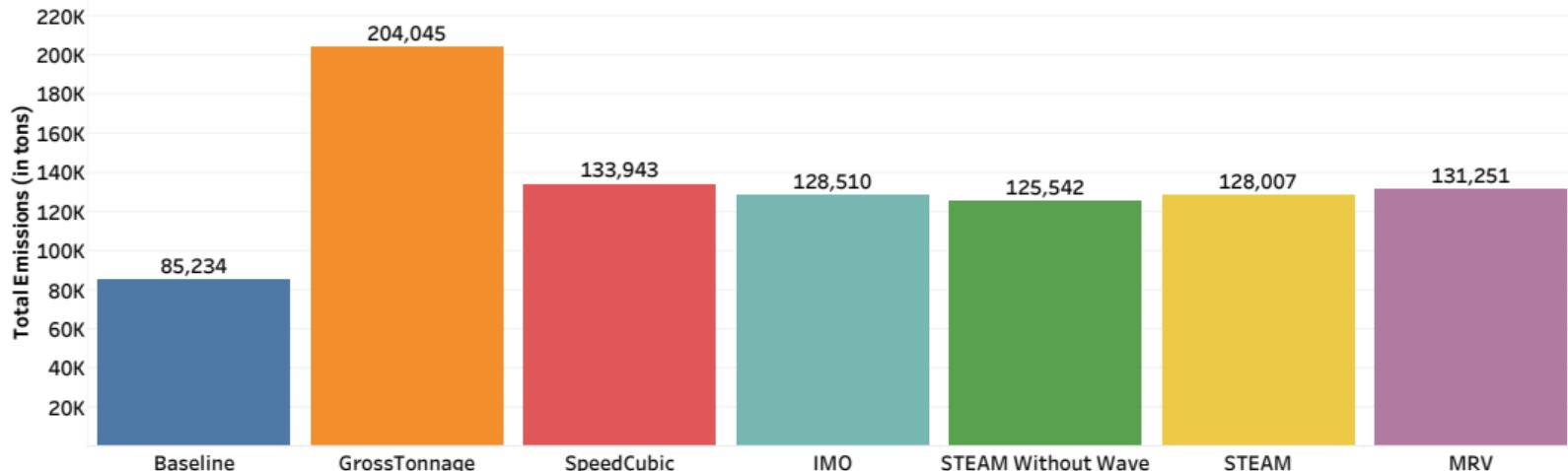
- ▶ - EEDI: Energy Efficiency Design Index
- ▶ - EIV: Estimated Index Values



# Evaluation of Vessel CO<sub>2</sub> Emissions Methods

MRV-based validation

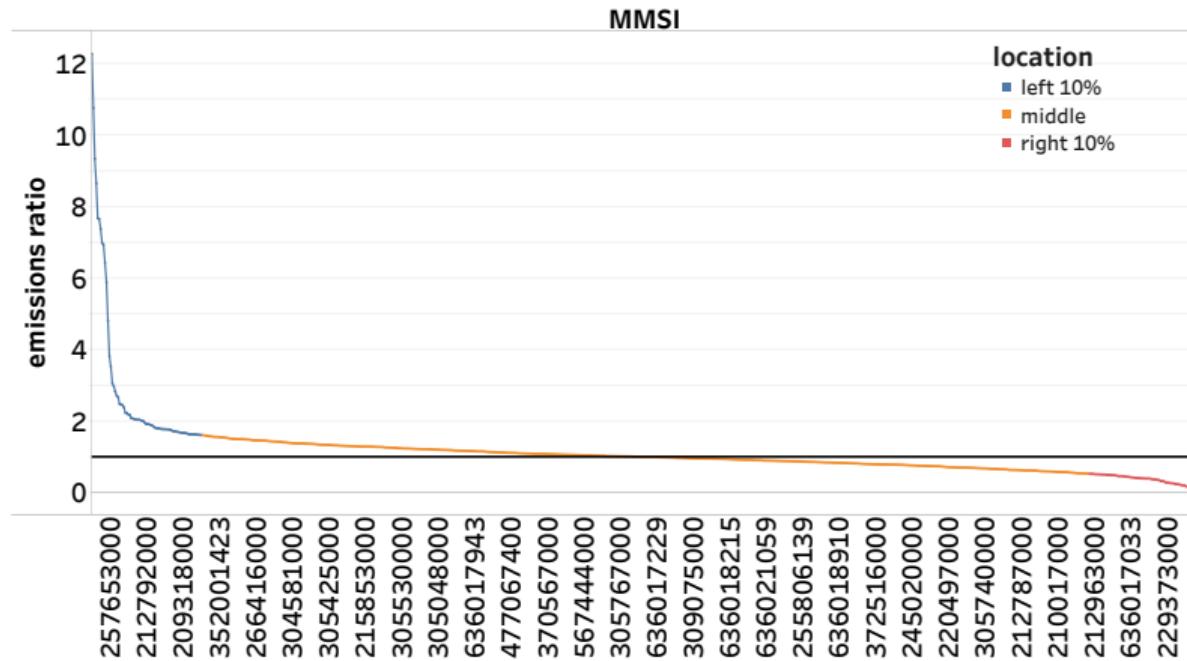
Total CO<sub>2</sub> emissions of the 760 ships by each model



# Evaluation of Vessel CO<sub>2</sub> Emissions Methods

MRV-based validation

Ship-level CO<sub>2</sub> efficiency ratio between the IMO method and MRV dataset





# Fusion of trajectories from AIS and Camera

## Motivation

- ▶ Installation of AIS devices is not mandatory for small boats
- ▶ AIS can be manually switched off by crew onboard. (dark vessels)
- ▶ Different sensors have their own pros and cons:
  - AIS: vessel identify, position, speed, etc
  - Camera images: visual appearance of vessels, but without identify and so on
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# Fusion of trajectories from AIS and Camera

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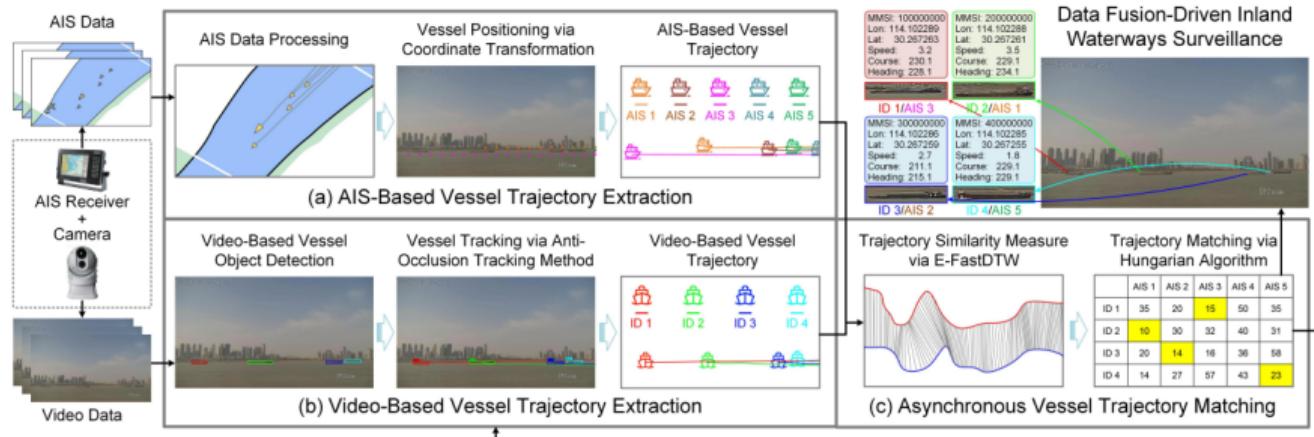


Fig. 1. The architecture of the proposed deep learning-based simple online and real-time vessel data fusion method (termed DeepSORVF). The DeepSORVF consists of AIS-based vessel trajectory extraction, video-based vessel trajectory extraction, and asynchronous vessel trajectory matching.

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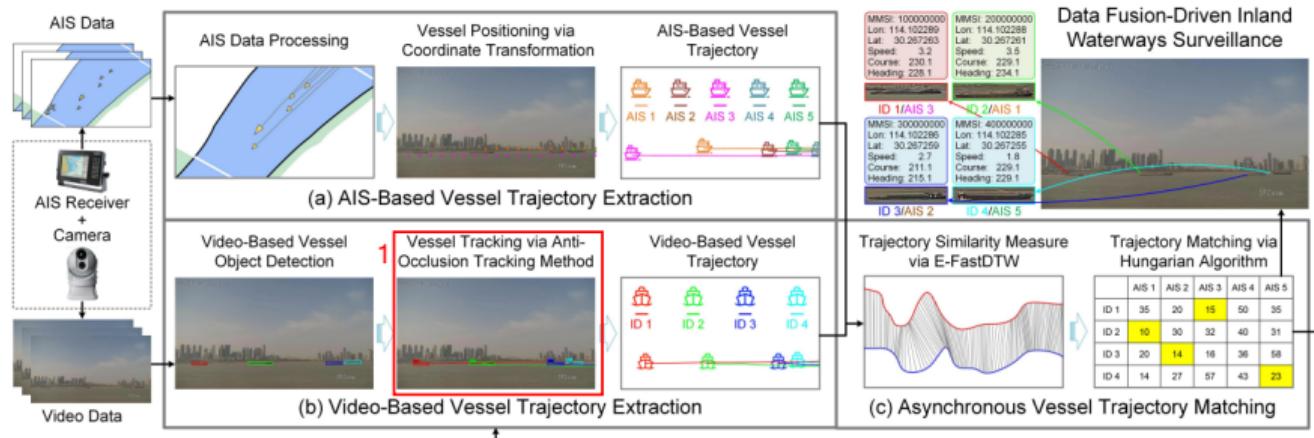


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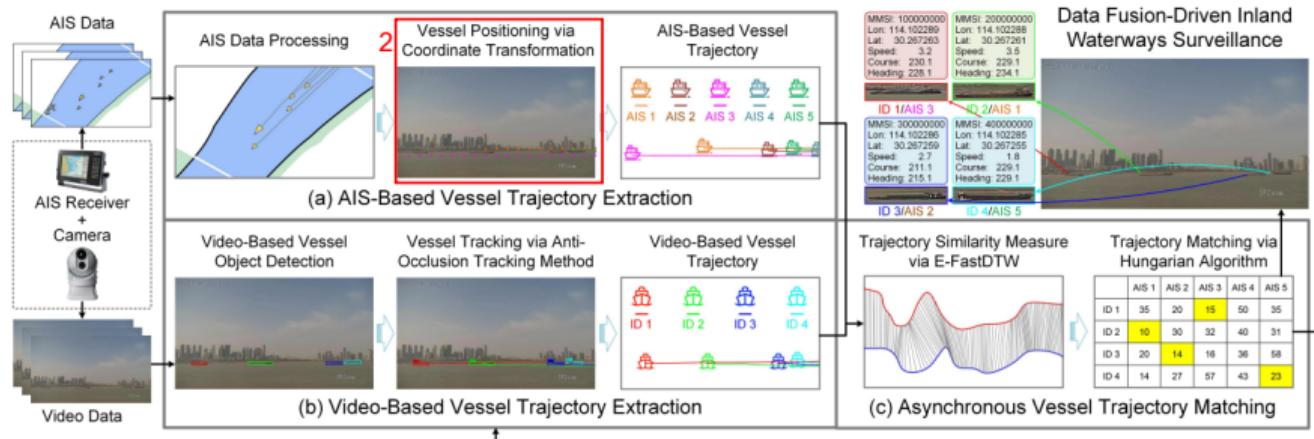


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## State of the art

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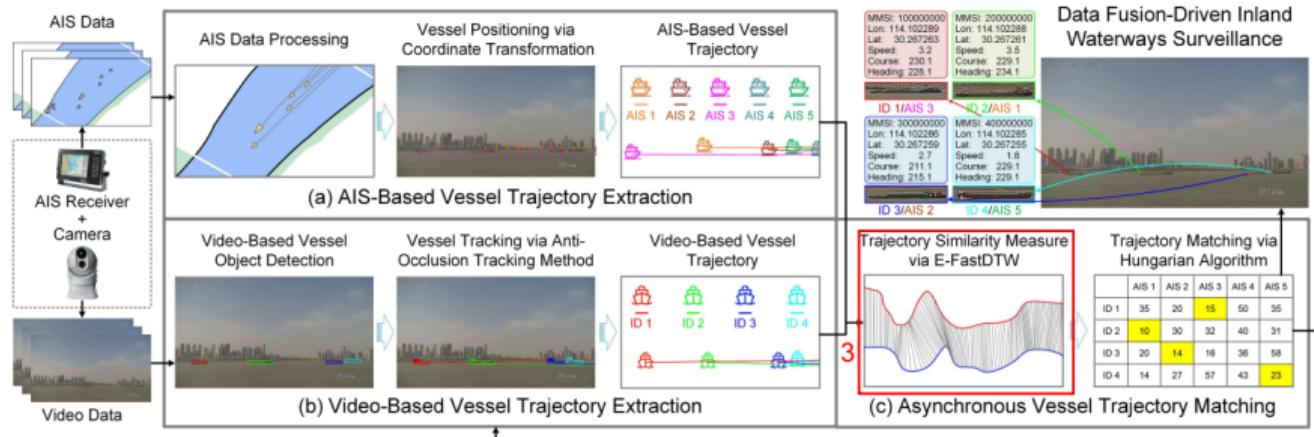


Fig. 1. The architecture of the proposed deep learning-based simple online and real-time vessel data fusion method (termed DeepSORVF). The DeepSORVF consists of AIS-based vessel trajectory extraction, video-based vessel trajectory extraction, and asynchronous vessel trajectory matching.

Thank for your attention! Feel free to ask any questions.



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