

Discussion Problems

Name: _____

Worksheet 5: Product Rule and Differentiation

Math 408C:

Instructor: Athil George

Problem 1. Suppose you have a function $f(x)$, $g(x)$, and $h(x)$, where $h(x)$ is the product of f and g . You also know that the function f at $x=2$, its derivative and value is 7 and 4, respectively. You also know that $g(x)$ is $f(x)$ reflected over the x -axis, or $f(x) = -g(x)$. What is derivative of h at $x=2$, or $h'(2)$?

Problem 2. Consider the function $f(x) = ax^2$. Find a so that the tangent line $y = 2x + 1$ exists on $f(x)$.

Problem 3. A tangent line is drawn to the hyperbola $x^2y = c$ for all $x \geq 0$. Show that the triangle formed by this tangent line and the coordinate axes are the same for all tangent lines.