



**SECI1013: DISCRETE STRUCTURE  
SESSION 20242025 – SEMESTER 1  
ASSIGNMENT 3**

**INSTRUCTIONS:**

1. This assignment must be conducted in a group (**3 or 4 students**).  
Please clearly write the **group members name and matric number** in the front-page of the submission.
2. Solutions for each question must be readable and neatly written on plain A4 paper. Every step or calculation should be properly shown.  
Failure to do so will result in rejection of the submission of assignment.  
**(Due date : 2 January 2024)**

**QUESTION 1**

**[15 Marks]**

You are conducting a study on the choice of university among Sijil Pelajaran Malaysia (SPM) leavers in Malaysia. Your data includes a **sample of 500 students** who have recently enrolled in universities across the country. Specifically, you are interested in whether these students chose to study in **private universities or local public universities**. The data you collected is as follows:

- **175** students chose **private** universities.
  - **325** students chose **local public** universities
- a) Calculate the **probability** that a randomly selected student from your sample chose to **study in a private university**. (1 Mark)
  - b) Determine the **probability** that a randomly selected student from your sample chose to **study in a local public university**. (1 Mark)
  - c) Are these two events **mutually exclusive**? Explain your reasoning. (3 Marks)

Now, let's consider additional factors that may influence the choice of university. You have gathered the following information:

- Among the students who chose **private universities**, **60%** majored in **business-related** fields, while the **rest majored in other disciplines**.

- Among the students who chose local public universities, 40% majored in business-related fields, while the rest majored in other disciplines.
- 70% of the students who majored in business-related fields chose private universities.

d) Calculate the probability that a student chosen at random for the following :

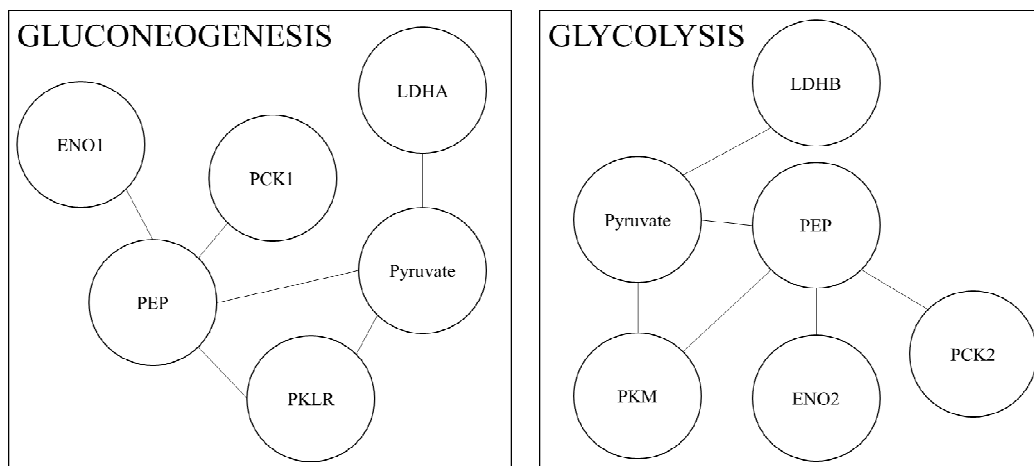
- Majored in a business-related field and chose a private university (3 Marks)
- Majored in a business-related field (3 Marks)
- Majored in a business-related field but chosen a local public university (4 Marks)

## QUESTION 2

10 MARKS

For the following pair of graphs GLUCONEOGENESIS and GLYCOLYSIS, show that both graphs are isomorphic by

- Define the one-to-one and onto functions from the vertices of graph GLUCONEOGENESIS and the vertices of graph GLYCOLYSIS.
- Construct the adjacency matrix.



**QUESTION 3****[31 Marks]**

Suppose Amina needs to spread a message among friends. Because of a restriction in the flow of communications, her 6 friends can only talk to specified friend as in Table 1:

Table 1

| Friends | Can Talk to       |
|---------|-------------------|
| Heidi   | Nadia             |
| Nadia   | Heidi, Adam       |
| Ali     | Faiz, Bara,Adam   |
| Faiz    | Bara, Ali         |
| Amina   | Heidi, Faiz       |
| Bara    | Faiz, Ali         |
| Adam    | Heidi, Nadia, Ali |

- Draw a **directed graph** to represent the flow of communications for Amina and her friends. (4 Marks)
- If **Amina initiates the message** and a continuous path is created, is there a path that will possible the **message delivered to everybody exactly once**? If so, execute the path flow of the communication. (4 Marks)
- What **theorem** in graph theory implemented to solved **problem in (b)** (2 Marks)
- Towns on a mountainous island are linked by railway lines as shown Figure 1. The distances (in kilometres) between stations are shown on the map

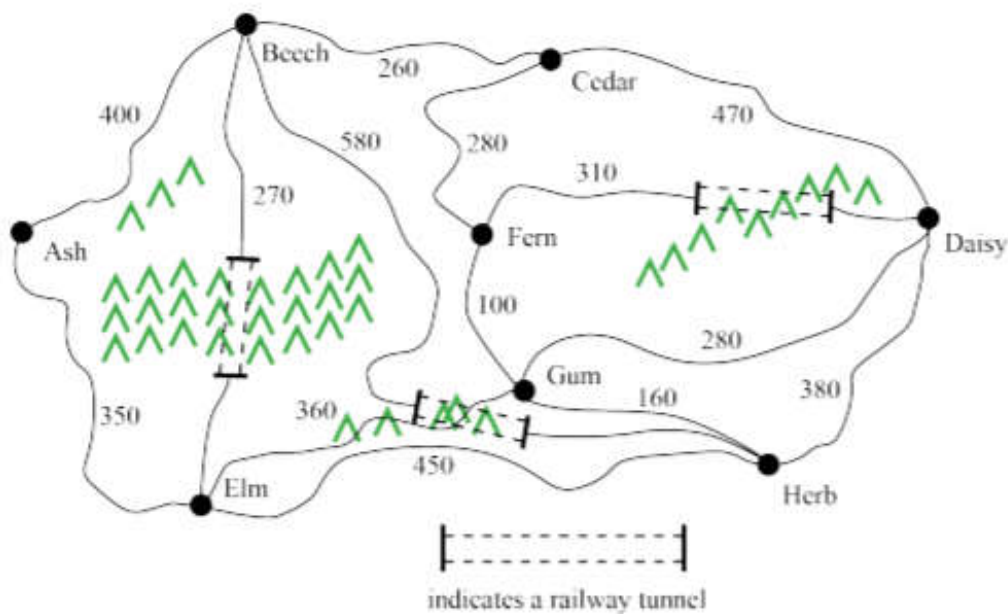


Figure 1

- Construct a graph for the network of the railway system. Label the stations with the first letter and show the distances on the lines. (3 Marks)
- Determine the degrees of the vertices in the graph. (3 Marks)
- It is possible to plan a trip that travels all sections of the railway line without travelling on any section of the line more than once. (You may have to visit towns more than once.). If so, determine the specific station to start and end the trip? Explain. (3 Marks)
- The railway company decides to close one line to reduce the maintenance cost but the tourist still possible to travel all sections of the railway line once from any station and return back to the same station. Identify which line that can be closed? Explain (2 Marks)

- v) Determine the shortest route and the minimum total length of track to travel from Ash to Daisy using Dijkstra algorithm by completing Table 2. (10 Marks)

Table 2

| S   | N                         | L(A) | L(B)     | L(C)     | L(D)     | L(E)     | L(F)     | L(G)     | L(H)     |
|-----|---------------------------|------|----------|----------|----------|----------|----------|----------|----------|
| { } | {A,B,C,D,E,F,G,H,I,J,K,L} | 0    | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ |
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