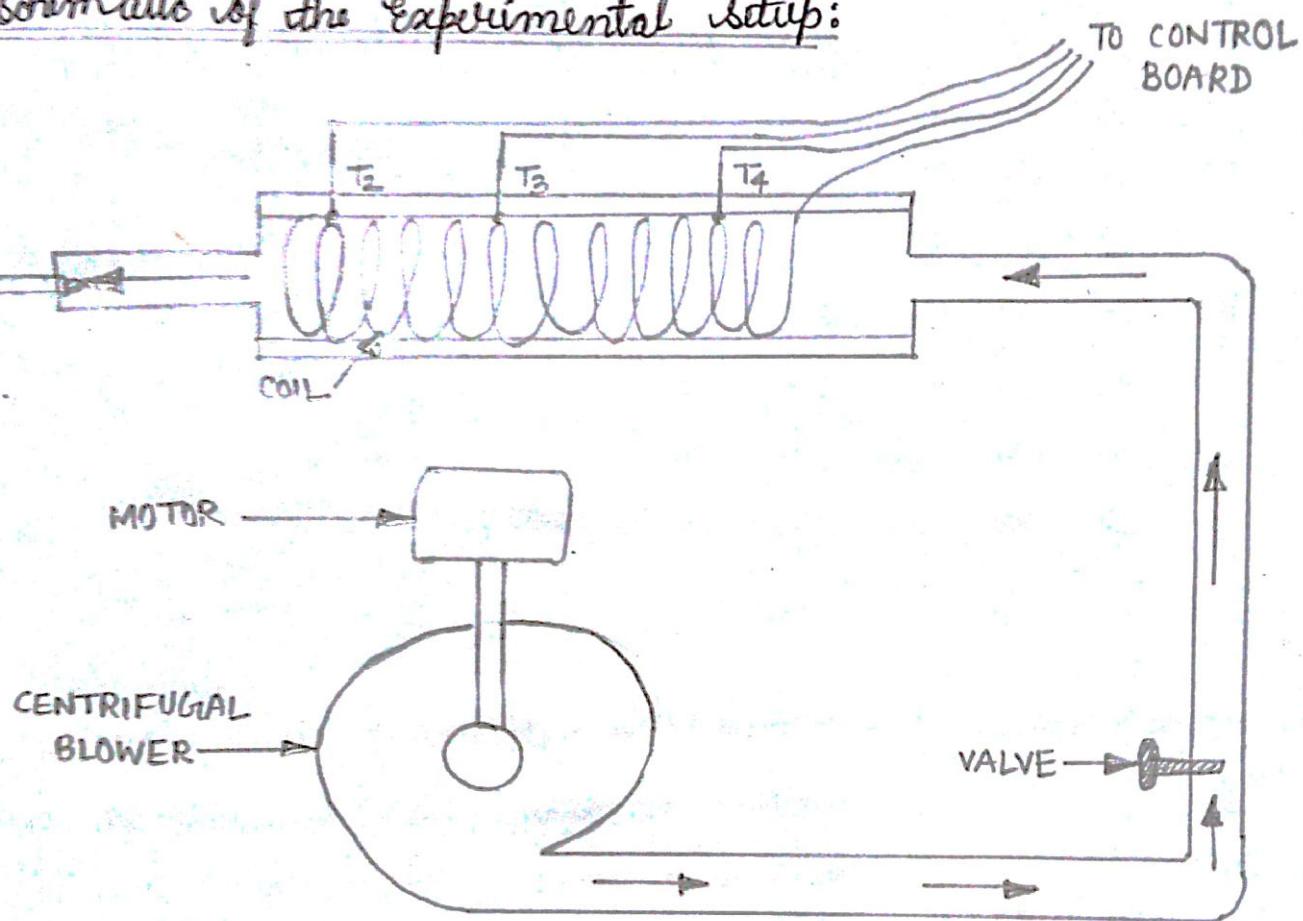


FORCED CONVECTION HEAT TRANSFER

① Objectives: Determination of average Nusselt number for forced convection in a heated circular pipe at various Reynolds numbers, and correlation for Nusselt number

② Schematic of the Experimental setup:



Observations

Room Temperature = 30°C

least count = 1°C for temperature, 0.001A for current, 1V for voltage

Run No. : 1 (volume flow rate = $4.976 \times 10^{-3} \text{ m}^3/\text{s}$, Heater Power = 66.5W)

| SL. No. | TIME (min) | VOLTAGE V (V) | CURRENT I (A) | POWER P (W) | MANOMETER READING ₁ | | | T_1 ($^{\circ}\text{C}$) | T_2 ($^{\circ}\text{C}$) | T_3 ($^{\circ}\text{C}$) | T_4 ($^{\circ}\text{C}$) | T_5 ($^{\circ}\text{C}$) | T_6 ($^{\circ}\text{C}$) |
|------------|---------------|---------------------|---------------------|-------------------|--------------------------------|---------------|-----------|---------------------------------|---------------------------------|---------------------------------|---------------------------------|---------------------------------|---------------------------------|
| | | | | | LEFT (mm) | RIGHT (mm) | H (mm) | | | | | | |
| 1 | 0 | 94 | 0.692 | 65.05 | 180 | 38 | 142 | 37 | 53 | 63 | 70 | 64 | 48 |
| 2 | 10 | 92 | 0.675 | 62.10 | 180 | 38 | 142 | 38 | 61 | 73 | 77 | 76 | 53 |
| 3 | 20 | 92 | 0.672 | 61.82 | 180 | 38 | 142 | 40 | 65 | 78 | 89 | 82 | 57 |
| 4 | 30 | 91 | 0.667 | 60.70 | 180 | 38 | 142 | 41 | 67 | 80 | 90.5 | 84 | 58 |
| 5 | 35 | 92 | 0.674 | 62.01 | 180 | 38 | 142 | 41 | 68 | 80 | 85.5 | 85 | 59 |
| 6 | 40 | 92 | 0.672 | 61.82 | 180 | 38 | 142 | 42 | 68 | 81 | X | 85 | 59 |

Run No. : 2 (volume flow rate = $4.351 \times 10^{-3} \text{ m}^3/\text{s}$, Heater Power = 62.38W)

| SL. No. | TIME (min) | VOLTAGE V (V) | CURRENT I (A) | POWER P (W) | MANOMETER READING ₁ | | | T_1 ($^{\circ}\text{C}$) | T_2 ($^{\circ}\text{C}$) | T_3 ($^{\circ}\text{C}$) | T_4 ($^{\circ}\text{C}$) | T_5 ($^{\circ}\text{C}$) | T_6 ($^{\circ}\text{C}$) |
|------------|---------------|---------------------|---------------------|-------------------|--------------------------------|---------------|-----------|---------------------------------|---------------------------------|---------------------------------|---------------------------------|---------------------------------|---------------------------------|
| | | | | | LEFT (mm) | RIGHT (mm) | H (mm) | | | | | | |
| 1 | 0 | 92 | 0.678 | 62.38 | 163 | 55 | 108 | 41 | 68 | 82 | 89 | 86.5 | 60 |
| 2 | 10 | 91 | 0.670 | 60.97 | 163 | 55 | 108 | 42 | 68 | 83 | X | 88 | 61 |
| 3 | 15 | 91 | 0.665 | 60.51 | 163 | 55 | 108 | 41.5 | 68 | 82 | X | 88 | 61 |
| 4 | 20 | 89 | 0.654 | 58.21 | 163 | 55 | 108 | 42 | 68 | 82 | X | 88 | 62 |

DATE

SHEET NO.

Run No. : 3 (Volume flow Rate = $3.722 \times 10^{-3} \text{ m}^3/\text{s}$, Heater Power = 59.22 W)

| SL. NO. | TIME (min) | VOLTAGE V (v) | CURRENT I (A) | POWER P (W) | MANOMETER READING | | | T ₁ (°C) | T ₂ (°C) | T ₃ (°C) | T ₄ (°C) | T ₅ (°C) | T ₆ (°C) |
|------------|---------------|---------------------|---------------------|-------------------|-------------------|---------------|-----------|------------------------|------------------------|------------------------|------------------------|------------------------|------------------------|
| | | | | | LEFT (mm) | RIGHT (mm) | H (mm) | | | | | | |
| 1. | 0 | 90 | 0.658 | 58.22 | 149 | 70 | 79 | 41.5 | 68 | 82.5 | X | 88 | 61 |
| 2. | 10 | 90 | 0.659 | 59.31 | 149 | 70 | 79 | 42 | 69.5 | 84 | X | 90 | 62 |
| 3. | 20 | 90 | 0.660 | 59.40 | 149 | 70 | 79 | 42 | 70.5 | 86 | X | 91.5 | 63 |
| 4. | 30 | 88 | 0.645 | 56.76 | 149 | 70 | 79 | 42 | 70 | 85 | X | 91 | 62.5 |

Run No. 4 (volume flow Rate = Same as Before, Heater Power = 88.22 W)

| SL. NO. | TIME (min) | VOLTAGE V (v) | CURRENT I (A) | POWER P (W) | MANOMETER READING | | | T ₁ (°C) | T ₂ (°C) | T ₃ (°C) | T ₄ (°C) | T ₅ (°C) | T ₆ (°C) |
|------------|---------------|---------------------|---------------------|-------------------|-------------------|---------------|-----------|------------------------|------------------------|------------------------|------------------------|------------------------|------------------------|
| | | | | | LEFT (mm) | RIGHT (mm) | H (mm) | | | | | | |
| 1 | 0 | 110 | 0.802 | 88.22 | 149 | 70 | 79 | 42 | 71 | 86.5 | X | 92 | 63 |
| 2 | 10 | 112 | 0.819 | 91.73 | 149 | 70 | 79 | 42 | 80 | 100.5 | X | 107 | 70 |
| 3 | 20 | 114 | 0.832 | 94.85 | 149 | 70 | 79 | 42 | 84.5 | 106 | X | 113 | 73 |
| 4 | 25 | 112 | 0.817 | 91.50 | 149 | 70 | 79 | 42 | 86 | 108 | X | 115 | 74.5 |
| 5 | 30 | 113 | 0.827 | 93.45 | 149 | 70 | 79 | 42 | 86 | 108 | X | 116 | 75 |

④ Sample Calculation :

Density of water, $\rho_w = 1000 \text{ kg/m}^3$

Gravitational accn., $g = 9.81 \text{ m/s}^2$

Average surface temperature, $T_s = (T_2 + T_3 + T_4 + T_5)/4$
 $= 78^\circ\text{C}$

Average temperatures of water, $T_a = (T_1 + T_6)/2$
 $= 50.5^\circ\text{C}$

Density of air at T_a and P_{atm} , $\rho_{air} = P_{atm}/(RT_a)$
 $= 1.091 \text{ kg/m}^3$

Volume flow rate of air through orifice = $c_d \left(\frac{\pi d^2}{4}\right) \sqrt{2gH (\rho_w/\rho_{air}-1)}$

Mass flow rate of air through pipe, $\dot{Q}_{flow} = 4.976 \times 10^{-3} \text{ m}^3/\text{s}$

$$m = \rho_{air} \dot{Q}_{flow}$$

$$= 5.429 \times 10^{-3} \text{ kg/s}$$

Rate of Heat transfer to the air,

$$\dot{Q}_a = m c_p (T_6 - T_1)$$

$$= 92.71 \text{ W}$$

Power Input to the heater, $P = VI$
 $= 61.82 \text{ W}$

Surface area of heated section, $\pi D_i L = 0.04398 \text{ m}^2$

Average heat flux

$$\dot{q}_a = \dot{Q}_a/A = 2108 \text{ W/m}^2$$

$$\dot{q}_i = P/A = 1405.64 \text{ W/m}^2$$

Average heat transfer coefficient, $h_a = \dot{q}_a/(T_s - T_a)$
 $= 76.65 \text{ W/m}^2\text{K}$

Average Nusselt Number, $Nu = h_a D_i / k = 78.36$

Average velocity, $v = Q/(\pi D_i^2/4) = 8.08 \text{ m/s}$

Reynolds number, $Re = v D_i / \nu = 12556.76$

① Results:

| RUN No. | FLOW RATE (m^3/s) | Re_{Di} | ρ_a (w) | P (w) | T_s ($^{\circ}C$) | T_a ($^{\circ}C$) | h (W/m^2K) | Nu |
|---------|------------------------|-----------|--------------|-------|-----------------------|-----------------------|------------------|-------|
| 1 | 4.976×10^{-3} | 12557 | 92.71 | 61.82 | 78 | 50.5 | 76.65 | 78.36 |
| 2 | 4.351×10^{-3} | 10885 | 94.85 | 58.21 | 79.33 | 52 | 78.91 | 80.34 |
| 3 | 3.722×10^{-3} | 9301 | 83.12 | 56.76 | 82 | 52.25 | 63.52 | 64.64 |
| 4 | 3.758×10^{-3} | 9084 | 132.5 | 93.45 | 103.33 | 58.5 | 67.22 | 67.28 |

② Determination of correlation for Nusselt Number

We did least square fit analysis to obtain the correlation

| Nu | Re | X $\log_{10}(Re)$ | Y $\log_{10}(Nu)$ | XY | X^2 |
|-------|-------|----------------------|----------------------|---------|---------|
| 78.36 | 12557 | 4.0988 | 1.8940 | 7.7636 | 16.8008 |
| 80.34 | 10885 | 4.0368 | 1.9049 | 7.6898 | 16.2959 |
| 64.64 | 9301 | 3.9685 | 1.8105 | 7.1850 | 15.7492 |
| 67.28 | 9084 | 3.9582 | 1.8278 | 7.2352 | 15.6679 |
| Sum = | | 16.0625 | 7.4374 | 29.8738 | 64.5140 |

$$\bar{X} = 4.0156 \quad \bar{Y} = 1.8593$$

∴ The eqn of line is $\bar{Y} = a + b\bar{X}$

$$b = \frac{n \sum xy - \sum x \sum y}{n \sum x^2 - (\sum x)^2} = 0.61792$$

$$\therefore a = -0.62201$$

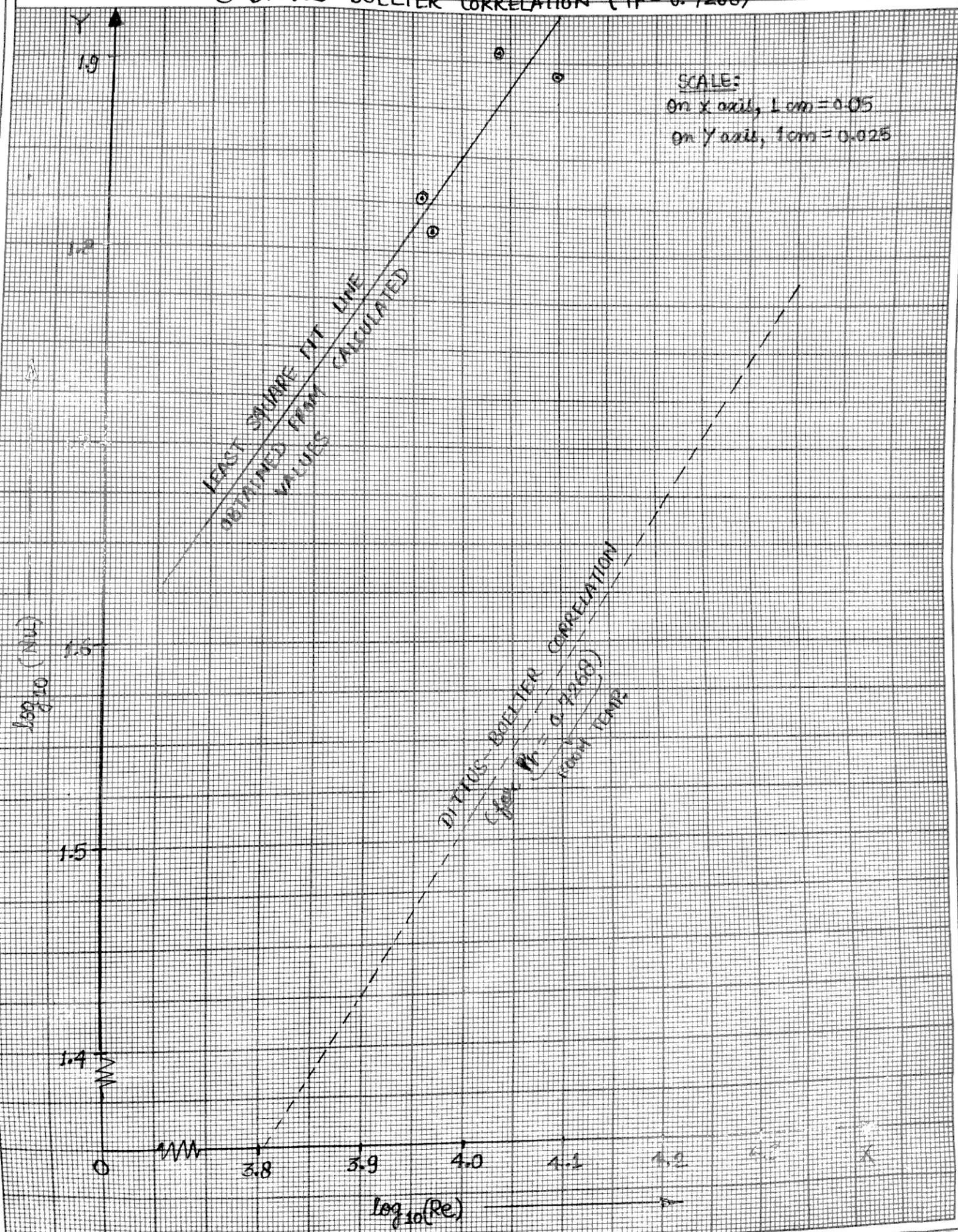
∴ Obtained correlation is $\log_{10}(Nu) = -0.62201 + 0.61792 \log_{10}(Re)$
 $\Rightarrow \log_{10}(Nu) = \log(0.23878) + \log_{10}(Re^{0.61792})$

$$\Rightarrow Nu = 0.23878 Re^{0.61792}$$

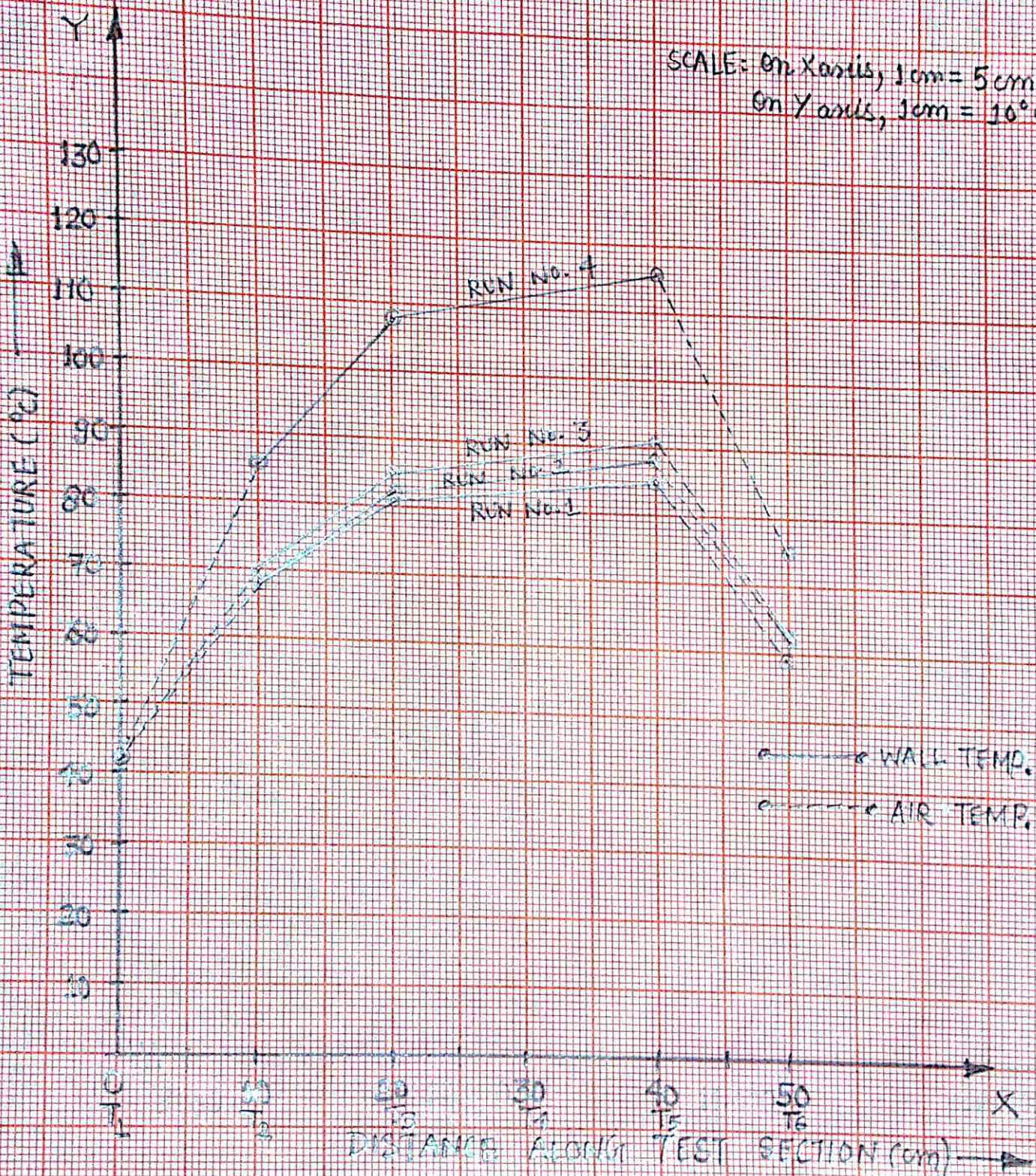
Assuming $Nu \propto Pr^{0.4}$ and $Pr = 0.7268$, $\therefore Nu = 0.27128 Re^{0.61792} Pr^{0.4}$

$$\Rightarrow Nu = 0.271 Re^{0.618} Pr^{0.4}$$

PLOT OF $\log_{10}(\text{Nu})$ VS $\log_{10}(\text{Re})$ FROM CALCULATED VALUES
① DITTUS-BOELTER CORRELATION ($\Pr = 0.7268$)



PLOT OF THE WALL TEMPERATURE DISTRIBUTION



8) Discussion of Results and Sources of error.

Ans for high Reynolds number value i.e $Re = 10393$

the nusselt number is high i.e $Nu = 26.2$ because the flow is turbulent. For a pipe if $Re > 2000$ then the flow is turbulent.

But for $Re = 2698$, the flow is in transition zone and hence the value of Nusselt number corresponds close to that of laminar flow.

Also only for high value of Re ; $Re > 10,000$, dittes boelter relation is valid and hence $\log(Nu)$ via $\log(\text{Nu}_{\text{D}}$) converges for $Re > 10,000$.

Sources of error:

- 1) For high Reynolds number, flow is turbulent but the nusselt no. is calculated ~~for~~ assuming laminar flow which results in error.
- 2) leakage and losses may also cause error in readings.
- 3) Error in taking down readings of manometer & measuring temperature.