

3)

a) Design Variables  $d, t$

Objective

$$\text{Min} : C_1 w + C_2 d$$

$$C_1 = 4 \quad C_2 = 2$$

$$4w + 2d$$

$$w = \frac{0.0025 \times \pi \times 275}{4} [(d^2 + 2t)^2 - d^2]$$

Useful 'H', 'E', 'I', 'P', 'Yield Stress'

Constraints

$$\textcircled{1} d \geq d_1 = 1 \Rightarrow d - 1 \geq 0$$

$$\textcircled{2} d \leq d_2 = 10 \Rightarrow d - 10 \leq 0$$

$$\textcircled{3} t \geq t_1 = 0.1 \Rightarrow t - 0.1 \geq 0$$

$$\textcircled{4} t \leq 1 \Rightarrow t - 1 \leq 0$$

$$\textcircled{5} \sigma < \sigma_b \Rightarrow \frac{P}{\pi d t} - \frac{\pi E I}{H^2 d t} \leq 0$$

$$\frac{P}{\pi d t} - \frac{\pi \times E}{8 H^2} (d^2 + t^2) \leq 0$$

$$\textcircled{6} \sigma < \text{Yield Stress}$$

$$\sigma - \text{Yield Stress} \leq 0$$

b) Constraints

$$-d + 1 \leq 0$$

$$d - 10 \leq 0$$

$$-t + 0.1 \leq 0$$

$$t - 1 \leq 0$$

$$\frac{2000}{\pi d t} - \frac{\pi^2 \times 9 \times 10^5}{8 \times (275)^2} \times (d^2 + t^2) \leq 0$$

$$\frac{2000}{\pi d t} - 550 \leq 0$$

Min

$$4 \left( \frac{0.0025 \times \pi \times 275}{4} \left[ (d^2 + t^2)^2 - d^2 \right] \right)$$

The d, t values are:

6.117589

0.189207

c) Please check the matlab files in q3 folder

mainscript → Run

confun → function for non- linear inequality

objecfun → function for linear inequality

x = 3.4269 0.9938

fval = 44.8104

d) Please check the same files again

x2 = 6.1176 0.1892

fval2 = 22.5445

(e) Yes results agree except for Active-Set

After changing initial values to 5 and 0.9

**Excel does not change answer**

6.117589

0.189207

**Active set becomes better**

$x_3 = 6.1176 \quad 0.1892$

$fval_3 = 22.5445$

**SQP remains same**

$x_4 = 6.1176 \quad 0.1892$

$fval_4 = 22.5445$