

# THE EXAM- SCHEDULING PROBLEM

## EXAMS

AI

FINANCE

STATISTICS

PHYSICS

AGRI. ENGG

## EXAM - SLOTS

3:00 pm – 5:00 pm

5:00 pm – 7:00 pm

7:00 pm – 9:00 pm

9:00 pm – 11:00 pm

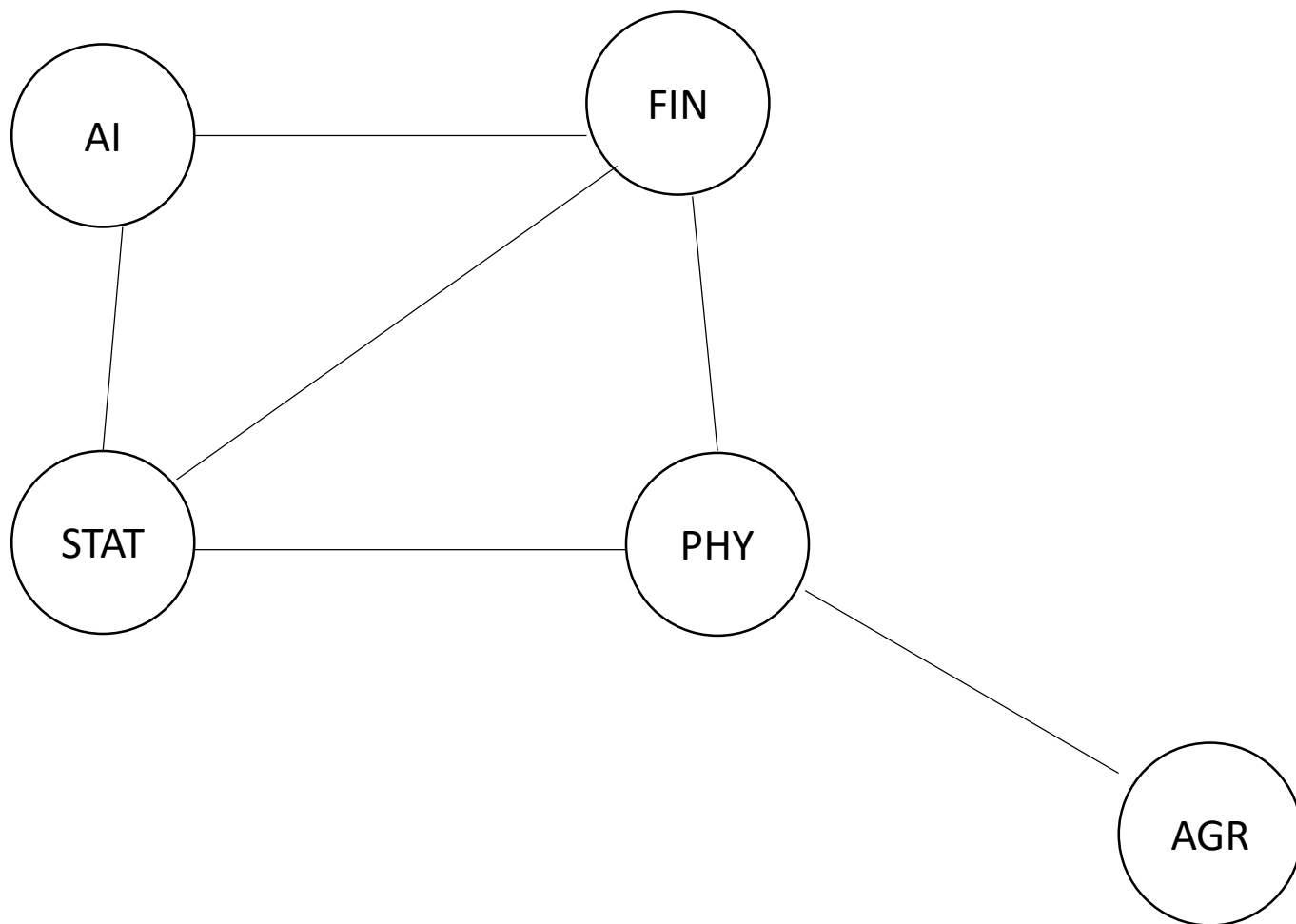
11:00 pm – 1:00 am

# Student – Overlap Matrix

	AI	FIN	STAT	AGR	PHY
AI	-	Yes	Yes	No	No
FIN	Yes	-	Yes	No	Yes
STAT	Yes	Yes	-	No	Yes
AGR	No	No	No	-	Yes
PHY	No	Yes	Yes	Yes	-

# Objective

- All exams must be held.
- No student should miss an exam.
- The exams must be wrapped up ASAP.



# Colour – Slot Mapping

- Imagine 5 distinct colours – {Col.1 , Col.2, Col.3, Col.4, Col.5}
- Each colour is associated with one unique slot.

EXAM - SLOTS	Colour
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3:00 pm – 5:00 pm	COL.1
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5:00 pm – 7:00 pm	COL.2
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7:00 pm – 9:00 pm	COL.3
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9:00 pm – 11:00 pm	COL.4
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11:00 pm – 1:00 am	COL.5
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# Graph – Colouring Problem

- Imagine 5 distinct colours – {Col.1 , Col.2, Col.3, Col.4, Col.5}
- Each colour is associated with one unique slot.
- Assign a colour to each node.
- No two adjacent nodes should have the same colour.
- Colour all nodes using minimum number of colours.

# Chromatic Number

- ***GT Problem***: Given a graph  $G$  and ' $k$ ' colours assign a colour to each node such that no two adjacent nodes have the same colour.
- The minimum value of ' $k$ ' for which such a colouring scheme exists for a graph  $G$  is called the **chromatic number** of graph  $G$

# Basic Colouring Algorithm

Given a graph G

- i. Order the *vertices* in some order:  $v_1, v_2, v_3, v_4, \dots, v_n$
- ii. Order the *colours* in some order:  $COL_1, COL_2, COL_3, \dots, COL_n$
- iii. For  $i = 1, 2, 3, \dots, n$   
Assign the lowest legal colour to  $v_i$



# Theorem

If every node in a graph  $G$  has degree  $\leq d$ , the basic algorithm will require AT MOST  $(d+1)$  colours, **no matter what the ordering is.**