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# Multi-Layered Dictionary Learning for Face Spoofing Detection

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# Introduction

- ❑ Ease of availability of silicone masks has increased the crime related to face spoofing.
- ❑ Spoofing is difficult to be identified by single-layered pre-defined dictionaries.
- ❑ Adaptive multi-layered dictionaries for sparse approximation provide a superior performance for such applications.
- ❑ Motivation: Improve the face spoofing detection using multi-layered dictionaries.



# Problem Statement

*“Face Spoofing Detection in unconstrained environment”*

- ❑ Given an image, compute the sparse approximation and classify if the image is spoofed.
- ❑ How to compute the sparse approximation?  
Learn the dictionary and sparse approximation of the input dataset of images.
- ❑ How to classify?  
Train the classifier using the sparse representation of the input data.

- ❑ Presentation Attack Detection (PAD) algorithms rely on domain knowledge.
- ❑ Properties like Motion, Texture, Reflectance and Image Quality are considered by PAD.
- ❑ Image Spoofing is difficult to incorporate texture in Boltzmann machines.
- ❑ Regularized Sparse Coding is also used for Image Representation

# Multi-layered Dictionary Learning

- Let  $D_1$  be the Dictionary at the first level,  $X$  be the input data and  $Z$  be the sparse representation.

$$X = D_1 Z$$

This is similar to the shallow one-level dictionary learning problem

- Extending the shallow set-up to the second layer, we get

$$X = D_1 \varphi(D_2 Z)$$

Here,  $\varphi$  is the activation function

- The full optimization for the  $N$  layers can be written as:

$$X = D_1 \varphi(D_2 \varphi(\dots (D_N Z) \dots))$$

- Hence, the minimization problem becomes

$$\min_{D_1, D_2, \dots, D_N} \|X - D_1 \varphi(D_2 \varphi(\dots (D_N Z) \dots))\|_F^2$$

# Multi-layered Dictionary Learning via Greedy Algorithm – 1st Layer

- ❑ The entire problem can be divided into a smaller bunch of greedy problems.
- ❑ For the first layer,

$$\mathbf{Z}_1 = \varphi(\mathbf{D}_2 \varphi(\dots (\mathbf{D}_N \mathbf{Z})))$$

$$\min_{\mathbf{D}_1, \mathbf{Z}_1} \|\mathbf{X} - \mathbf{D}_1 \mathbf{Z}_1\|_F^2$$

- ❑ This can be solved by Method of Alternating Directions

$$\mathbf{Z}_k \leftarrow \min_{\mathbf{Z}} \|\mathbf{X} - \mathbf{D}_{k-1} \mathbf{Z}\|_F^2$$

$$\mathbf{D}_k \leftarrow \min_{\mathbf{D}} \|\mathbf{X} - \mathbf{D} \mathbf{Z}_k\|_F^2$$

# Multi-layered Dictionary Learning via Greedy Algorithm – Continuing it with other layers

- After formulating the coefficients for the first layer, we formulate that of second layer as:

$$\varphi^{-1}(Z_1) = D_2 Z_2$$

$$Z_1 = \varphi(D_3 \varphi(\dots (D_N Z)))$$

- Method of alternating directions is invoked again to find to solve the optimization at every level

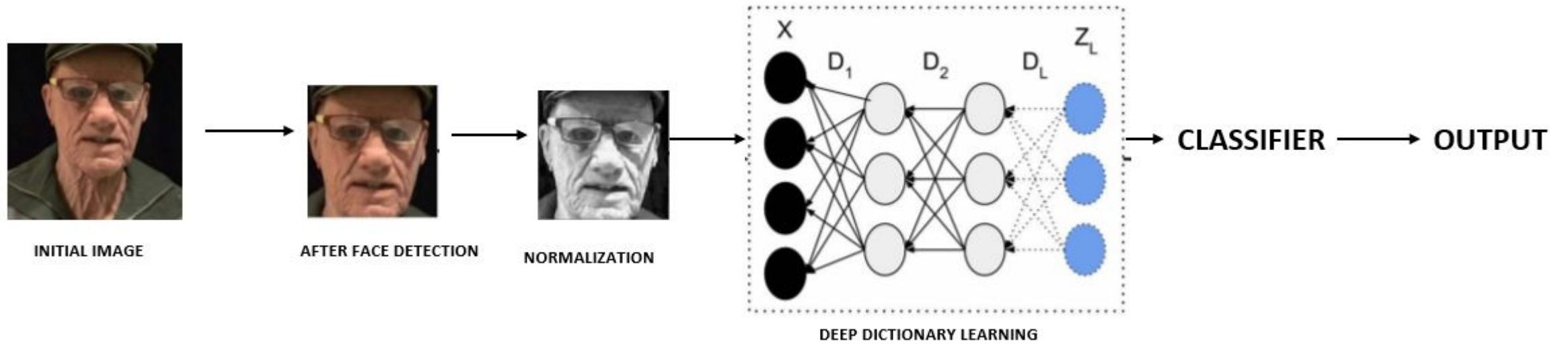
- Sparsity can be introduced to this optimization problem by re-writing it as:

$$\min_{D_1, D_2, \dots, D_N} \|X - D_1 \varphi(D_2 \varphi(\dots (D_N Z)))\|_F^2 + \lambda \|Z\|_1$$

- This can be imposed at the final layer as:

$$\min_{D_N, Z} \|\varphi^{-1}(Z_{N-1}) - D_N Z\|_F^2 + \lambda \|Z\|_1$$

# Architecture



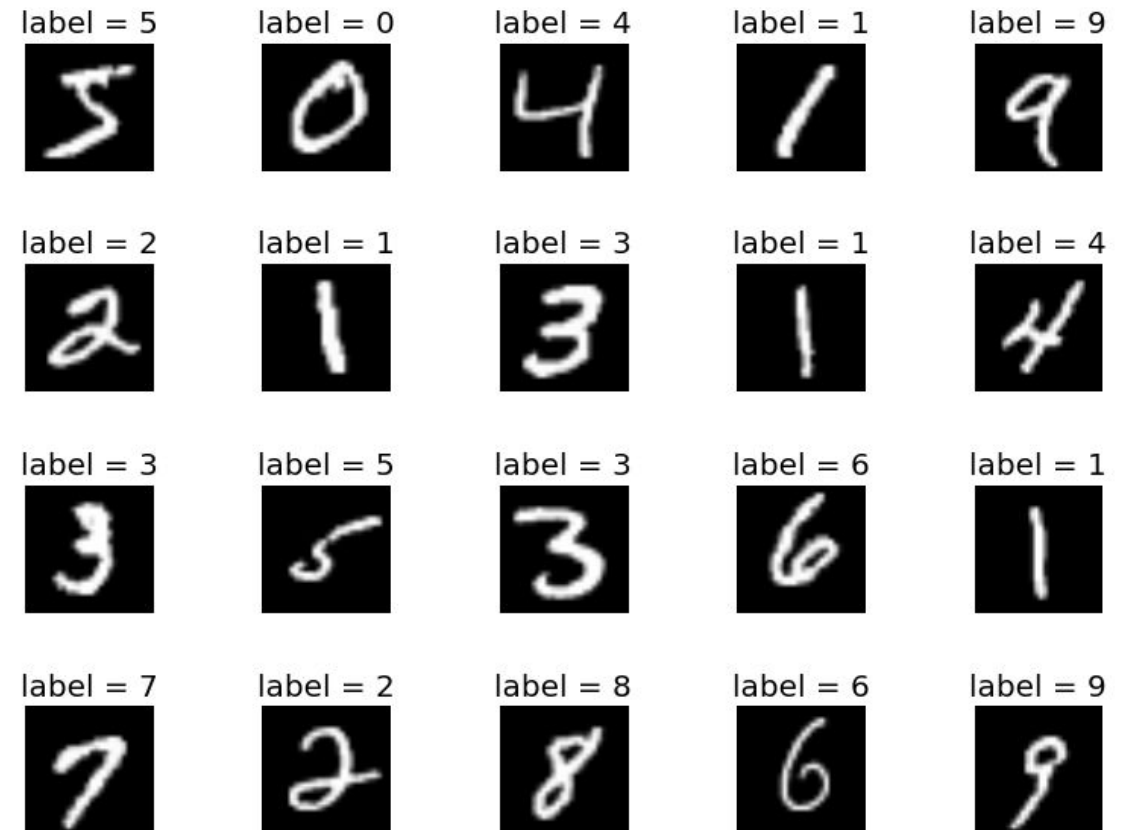


# Dataset - Evaluation on MNIST

❑ Dataset of handwritten digits provided by Yann Lecun\*.

❑ 28 x 28 images for 10 classes

Training	Test
40,000	8,000



\* <http://yann.lecun.com/exdb/mnist/>

# Dataset - Training on MNIST

- ❑ First we tried with **all features**.

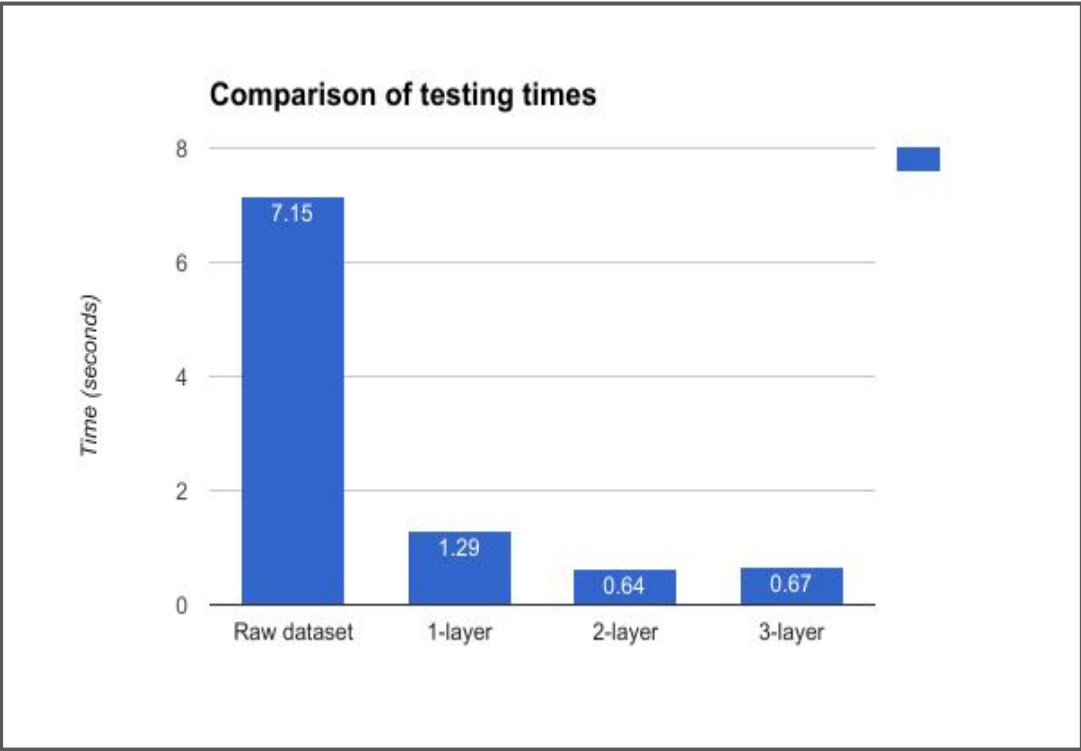
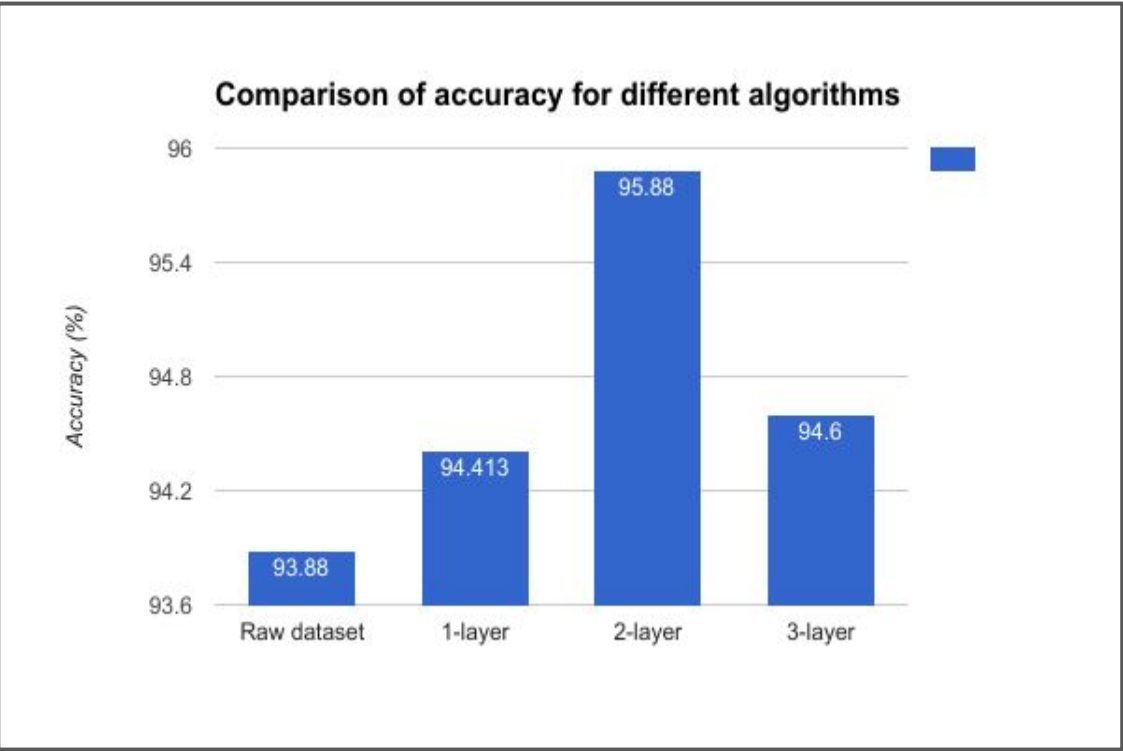
Dataset	Feature Size	Training Size	Test Size
MNIST	784	40,000	8,000

- ❑ Dimensionality Reduction with **Dictionary learning**.

Dataset	Feature Size (1 Layer)	Feature Size (2 Layer)	Feature Size (3 Layer)	Training Size	Test Size
MNIST	100	200 - 100	400 - 200 - 100	40,000	8,000

# Testing and Results on MNIST

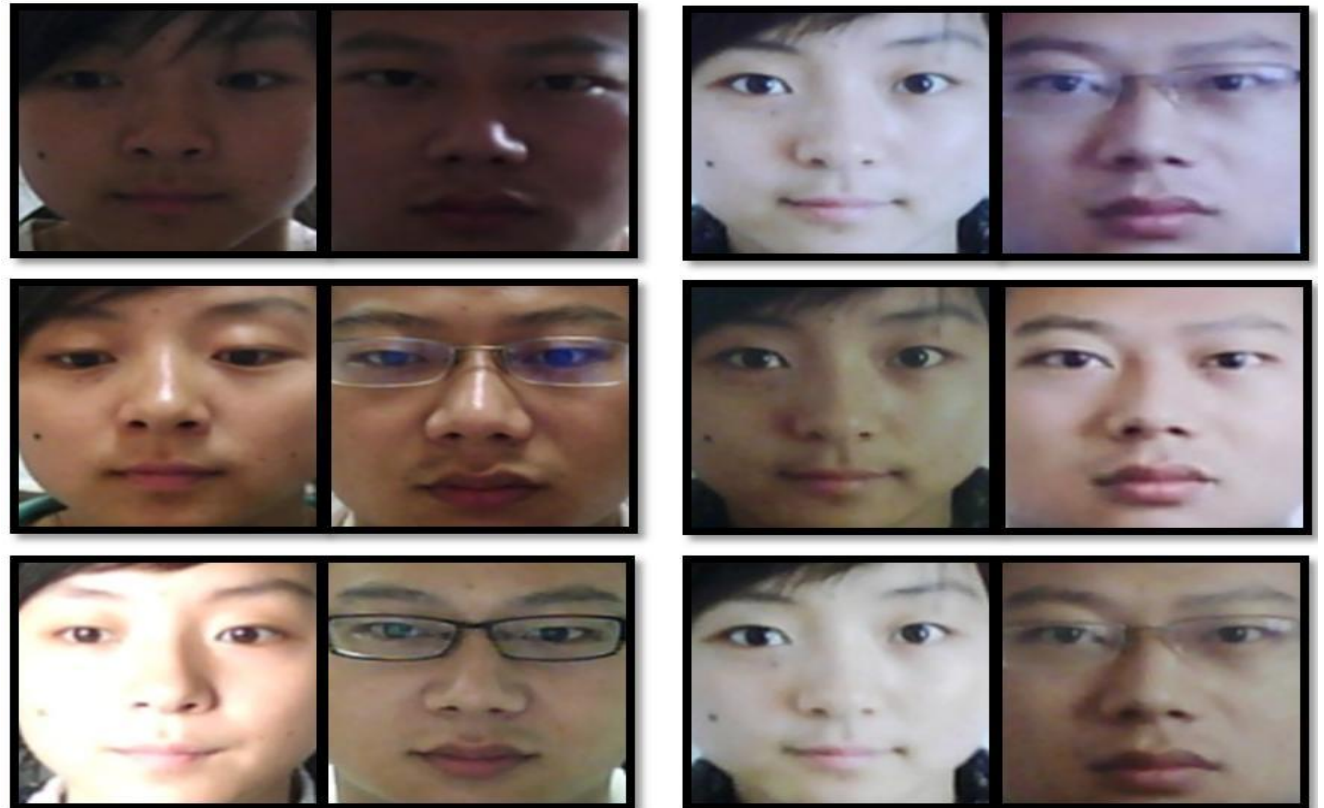
MNIST Dataset	Raw Dataset	Shallow (1-layer)	2-layer	3-layer
Accuracy (%)	93.58	94.413	95.88	94.6
Testing Time (sec.)	7.15	1.29	0.64	0.67



# Dataset - NUAA

- ❑ Database of photograph imposters collected with cheap webcams.
- ❑ 64 x 64 images of 2 classes (client or impostor).

Training	Test
3491	9123



- ❑ We extract the face using Viola Jones face detection algorithm.



- ❑ After detecting the face, the image is converted to grayscale and is normalized
- ❑ All the cropped images are 64 x 64. Hence, every image is represented as a vector of length 4096

# Training on NUAA

- ❑ First we tried with **all features**.

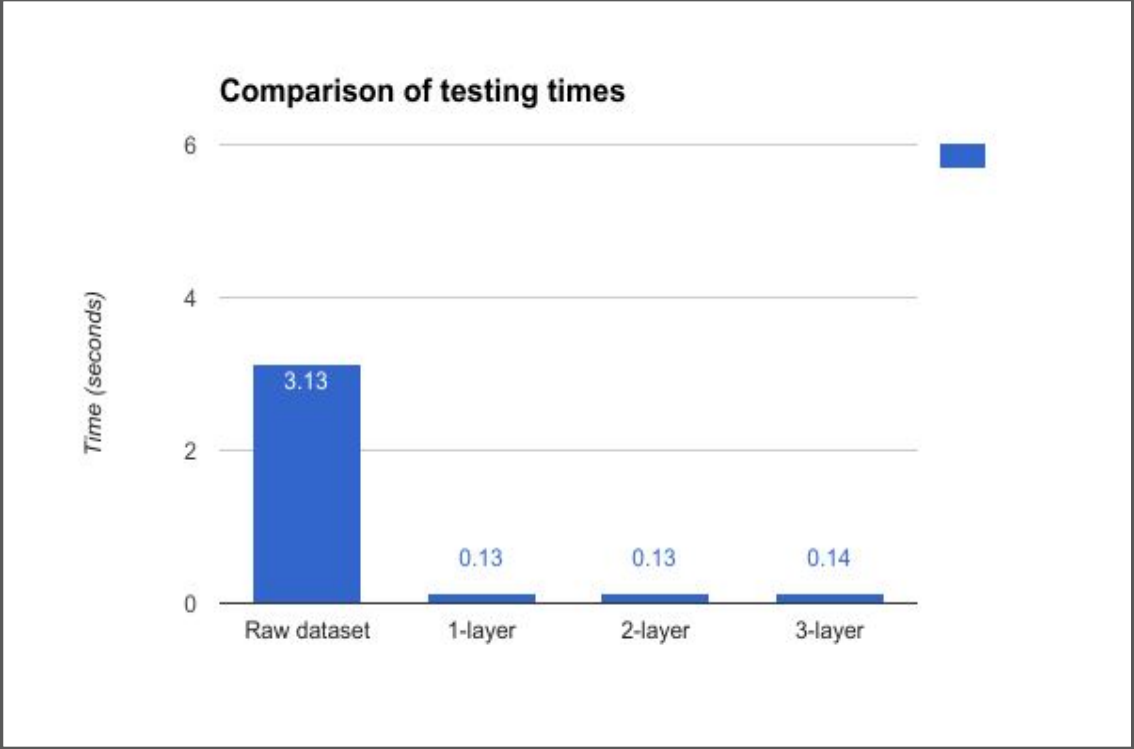
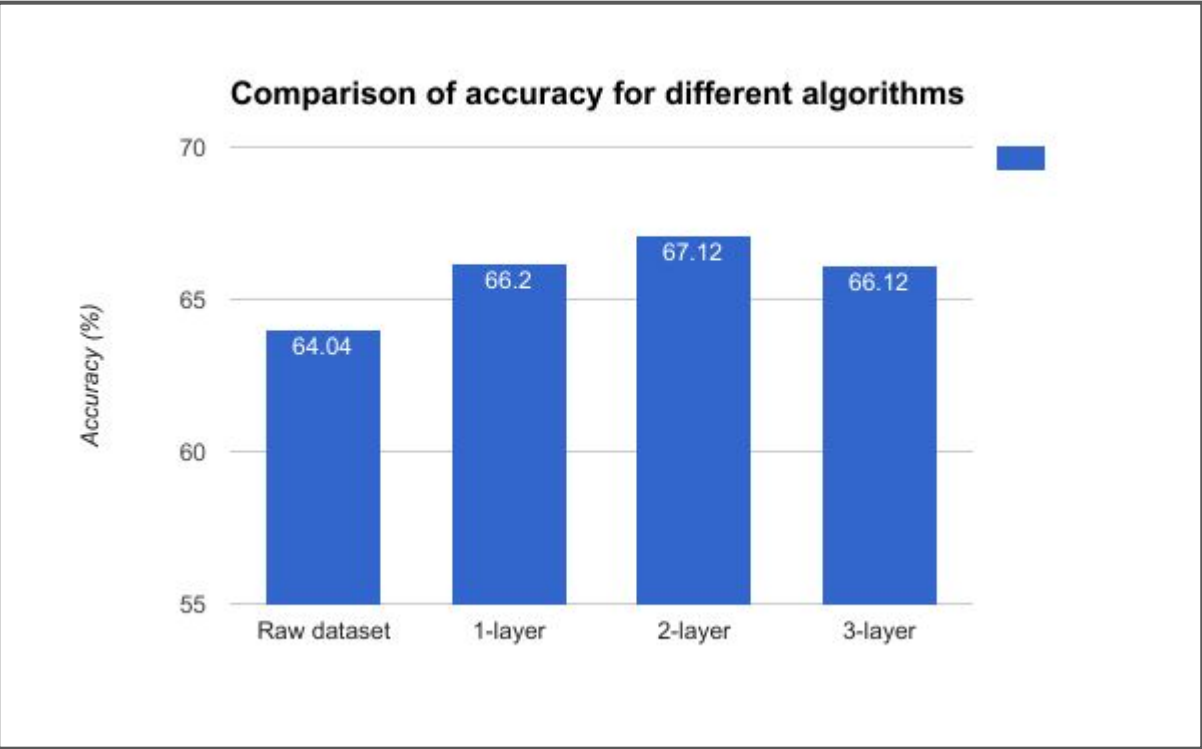
Dataset	Feature Size	Training Size	Test Size
MNIST	784	40,000	8,000
NUAA	4096	3,491	9123

- ❑ Dimensionality Reduction with **Dictionary learning**.

Dataset	Feature Size (1 Layer)	Feature Size (2 Layer)	Feature Size (3 Layer)	Training Size	Test Size
MNIST	100	200 - 100	400 - 200 - 100	40,000	8,000
NUAA	512	1024 - 512	1024 - 512 - 256	3,491	9123

# Testing and Results on NUAA

MNIST Dataset	Raw Dataset	Shallow (1-layer)	2-layer	3-layer
Accuracy (%)	64.04	66.2	67.12	66.12
Testing Time (sec.)	3.13	0.13	0.13	0.14



# Effect of various activation functions

- ❑ The reference paper [2] uses only linear activation functions in all the layers.
- ❑ We tried with other activation functions also like tanh and sigmoid.
- ❑ In the algorithm, inverse of the activation functions have to be used.
- ❑ At each layer we project the values to a specified interval (e.g.  $[-1, +1]$  for  $\text{arctanh}$ ).

<b>Layers</b>	200, 100	400, 200	50, 25
<b>Accuracy</b>	63.86	51.31	60.61



# Challenges for multi-layered dictionary learning

- ❑ Studies have proven the convergence guarantees for single level dictionary learning. These proofs are very hard to replicate for multiple layers.
- ❑ The number of parameters required to be solved increases when multiple layers of dictionaries are learned simultaneously. With limited training data, this could lead to overfitting.

# Conclusion

- ❑ Multi-layered dictionary gives better results and testing times than shallow dictionary learning.
- ❑ Learning different levels of dictionaries along with the coefficients is not the same as learning a single (collapsed) dictionary and its corresponding features (even with linear activation functions).
- ❑ The single-level problem (single level) is a bi-linear problem and 2-level problem is a tri-linear problem
- ❑ Greedy approach for layer-wise learning ensures the convergence of each layer.
- ❑ Regularization at final layer can be used to control sparsity and prevent overfitting.

## Future Work

- ❑ Using images in 2D format instead of a vector. The data will then become multi-dimensional which calls for multi-dimensional dictionary learning.
- ❑ Using other kind of sparsity measures and comparing performance.
- ❑ Improving performance for nonlinear activation functions.

# References

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- [7] X.Tan, Y.Li, J.Liu and L.Jiang “Face Liveness Detection from a single image with sparse low rank bilinear discriminative model ” *Proceedings of 11th European Conference on Computer Vision (ECCV 10), Crete, Greece. September 2010*

Thank You!