Scientific Programming With Modern Fortran

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History of FORTRAN

One of the earliest of the high-level programming languages, FORTRAN (short for Formula Translation) was developed by John Backus at IBM in the 1950s (circa 1953 for the 704, first released in 1957):

- FORTRAN 66, ANSI standard (X3.9-1966) based on FORTRAN IV
- FORTRAN 77, X3.9-1978, improved I/O
- Fortran 90, ISO/IEC 1539:1991(E), FORTRAN becomes Fortran
- Fortran 95, ISO/IEC 1539-1:1997, minor revisions
- Fortran 2003, ISO/IEC 1539:2004, command line arguments, more intrinsics, IEEE exception handling, C interoperability
- Fortran 2008, revision to Fortran 2003, to include BIT type and Co-array parallel processing (starting to become better supported)

Part I

Fortran Basic Operations

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Why Is This Language Still Used?

So why is Fortran still in use?

- Efficiency has always been a priority, in the sense that compilers should produce efficient code. Fortran data are generally not allowed to be aliased (e.g. pointers) making life easier on the compiler
- Designed from the outset as the tool for numerically intensive programming in science and engineering
- Backward compatibility most modern compilers can still compile old (as in decades!) code

Come On, Fortran is 50 Years Old!

Indeed, Fortran celebrated its 50th birthday in 2007. How many other high-level languages can you say that about? Think of it this way - it is arguably the most efficient, compact, portable high-level language available. And you will likely still be able to use programs written today until you retire (unmodified, at that) ...

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The Rest of This Talk

In this presentation I will focus almost entirely on Fortran >=90/95 (a.k.a Modern Fortran) features, with some side notes on FORTRAN 77 (mostly for contrast). This talk is not intended to be exhaustive in its coverage of Fortran syntax, but should be enough to yield a "rough and ready" knowledge for HPC.

Some Fortran Compilers

Fortran compilers are easy to find, some are freely available (including compiler source code):

- gfortran, part of the GNU toolchain (gcc/g++), supplanted g77 as of version 4.0
- q95, another freebie
- open64, open sourced by SGI (derived from their MIPSPro compiler suite), further developed by Intel and the Chinese Academy of Sciences (Gnu Public License), intended mainly for compiler research (includes C/C++) on the IA64 platform
- ifort, Intel's commercial compiler
- pqf95, PGI's commercial compiler
- Other commercial compilers: IBM, Qlogic/Pathscale, Lahey/Fujitsu, Sun, NAGWare, ...

Source Code Format

While FORTRAN 77 used by default a fixed format for its source code, the default with modern Fortran is now a free format, in which lines can be up to 132 columns long, with a maximum of 39 continuation lines, indicated by the & character.

Statement labels are still in fashion, and consist of 1-5 digits (leading

Source Format Summary

```
characters per line
2
          initiates comment
3
          continuation character
          statement separator (multiple per line)
   print*,''You need two continuation &
2
            &characters when splitting a token &
            & or string across lines"
```

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Introduction

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Introduction

Source Format

Statement Labels

zeros are neglected), e.g.

READ (*, 2) runid format (a9)

WRITE(6,*) 'Enter runid:(<=9chars) '</pre>

Most commonly used for FORMAT statements.

Source Format

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Names

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In Fortran, names must:

- Start with a letter (a-z)
- Contain only letters, digits, and underscore
- Must not be longer than 31 characters

More Resources

Good reference material on all things Fortran:

- M. Metcalf and J. Reid, Fortran 90/95 Explained, 2nd Ed., (Oxford, Great Britain, 2000)
 - Fortran 95/2003 Explained, 3rd Ed., (Oxford, Great Britain, 2004), with M. Cohen
 - Modern Fortran Explained, (Oxford, Great Britain, 2011), with M. Cohen
- Metcalf's online tutorial:

http://wwwasdoc.web.cern.ch/wwwasdoc/WWW/f90/f90.html

• Alan Miller's Fortran Resources:

http://jblevins.org/mirror/amiller/

Language Elements Implicit Types

Implicit Types

Implicit None

Unfortunately FORTRAN historically allowed implicit types, which by default were:

FORTRAN 77

implicit real (a-h,o-z) implicit integer (i-n)

Thanks to backward compatibility, this feature is still present:

Language Elements

Fortran

implicit type (letter-list) [,type (letter-list) ...]

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Intrinsic Types

Basic Declarations

Declarative Syntax

<type> [,<attribute-list>] :: <variable-list> & [=<value>]

The attribute is usually one of PARAMETER, DIMENSION, or POINTER.

I would recommend starting every declaration block with the following:

Implicit Types

Language Elements

Fortran

implicit none

which will turn all implicit typing off, and save a lot of potential errors (misspelled variable names just being one of them). Use implicit types at your own risk!

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Language Elements

Intrinsic Types

Fortran Intrinsic Types

We have five different intrinsic types, integer, real, logical, complex, and character. The syntax looks like:

```
integer :: i
real :: x
complex :: z
logical :: beauty
character :: c
```

These are all of default kind ... (Note that integers can also be represented in binary (base 2), octal (base 8), and hex (base 16)) Language Elements Intrinsic Types

Kind

There is an intrinsic function KIND that returns an integer and can be used to guery (or set) the "kind type" of a variable

Fortran

KIND(x) returns default integer whose value is the kind type parameter value of x

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Language Elements

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Intrinsic Types

Best illustrated by example - this is a chunk of code that use in all of my Fortran codes:

```
integer, parameter :: si=KIND(1), sp=KIND(1.0), sc=KIND((1.0,1.0)), &
2
           di=SELECTED_INT_KIND(2*RANGE(1_si)), &
3
           dp=SELECTED_REAL_KIND(2*PRECISION(1.0_sp)), &
           dc=SELECTED_REAL_KIND (2*PRECISION (1.0_sc))
```

Note the use of underscores in literal constants to indicate kind type, which is guite generally applicable:

```
real(kind=dp) :: a,b,c
complex(kind=dc) :: zi=(0.0_dp,1.0_dp)
```

Language Elements Intrinsic Types

Example: Declarative Use of KIND

These are two of the very handy "transformational" functions:

SELECTED REAL KIND/SELECTED INT KIND

SELECTED REAL KIND([p][,r])

p:: integer, decimal precision (intrinsic PRECISION)

r :: integer, decimal exponent range (RANGE) (at least one of p or r must be present)

SELECTED INT KIND(r)

r :: integer, decimal exponent range

the return values of both functions are default integers whose values can be used in the KIND intrinsic function. -1 is returned if the desired precision is unavailable (-2 for the range in SELECTED_REAL_KIND, -3 if both).

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Intrinsic Types

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Language Elements PARAMETER Attribute

Instead of the old FORTRAN 77 PARAMETER statement, one can use the parameter attribute:

REAL, **PARAMETER** :: E = 2.71828, PI = 3.141592

Language Elements Intrinsic Types

Intrinsic Type Arrays

Arrays can be indicated by the old-type DIMENSION attribute, or simply in the declaration itself:

```
real,dimension(3) :: a
real :: b(3)
<u>real</u> :: c(-1:1)
```

are all arrays of rank 1, shape 3.

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Intrinsic Types

Initializing Arrays

There is some special syntax for initialization arrays:

Language Elements

```
a(1:4) = 0.0
2
   a(1:4) = (/1.1, 1.2, 1.3, 1.4/)
   a(1:4) = (/ i, i=1,7,2 /)
                                    ! implied do loop with stride 2
```

Note that the RESHAPE function can also be used to initialize an array of rank greater than 1.

Note that arrays can be **sectioned**:

```
! rank 1 array, size j-i+1
2
              ! rank 1 array, size n
   b(k,1:n)
   c(1:m,1:n,k) ! rank 2 array, extent m by n
```

Intrinsic Types

Language Elements

and **vector subscripts** can be used:

```
x(ivector)
           ! ivector is an integer array
```

which makes for a very flexible (essentially arbitrary) indexing scheme.

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Language Elements

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Intrinsic Types

Character Arrays

Better known as **strings**, Fortran is not the best for string handling (it is intended for number crunching, after all), but modern Fortran is considerably improved in this regard:

```
character, dimension(120) :: line1
character(len=120) :: line2
character(len=120),dimension(80) :: page
```

Substrings can be handled in several ways:

```
character(len=1200) :: line
   character(len=12) :: words,term*8 ! term has length 8, alternate length spec
3
   line(:i)
                              ! same as line(1:i)
4
   line(i:)
                              ! same as line(i:120)
   line(:)
                              ! same as line(1:120)
```

and we will come back later to some of the intrinsic string handling functions and subroutines.

Language Elements **Derived Types**

Derived Types

Assigning Derived Types

It is often advantageous to define your own data types:

```
TYPE Coords_3D
    real :: r, theta, phi ! spherical coordinates
END TYPE Coords_3D
TYPE (Coords_3D) :: point1, point2
```

You can reference the internal components of a structure:

```
x1 = point1%r * SIN(point1%theta) * COS(point1%phi)
y1 = point1%r * SIN(point1%theta) * SIN(point1%phi)
z1 = point1%r * COS(point1%theta)
x2 = point2%r * SIN(point2%theta) * COS(point2%phi)
y2 = point2%r * SIN(point2%theta) * SIN(point2%phi)
z2 = point2%r * COS(point2%theta)
```

N.B. Derived type components can not be ALLOCATABLE (but they can be POINTERS).

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Language Elements

Pointers

Fortran finally has the capability (often best left unused) of using pointers. Along with ALLOCATABLE and automatic arrays, pointers make up the 3 types of dynamic data in Fortran 90/95. Pointers can be members of derived types, most useful for implementation of linked lists:

```
real, pointer, dimension(:,:) :: a
real,pointer :: x,y
NULLIFY (x, y, a)
                              ! Point to nothing
                              ! Fortran 95 only
ALLOCATE (x, y, a (100:100))
                             ! Fresh storage allocation
```

We will talk a bit more about pointers later when dealing with other aspects of dynamic memory.

Derived types can be assigned either by component or using a constructor:

Language Elements

```
point1%r = 1.0
point1%theta = 0.0
point1%phi = 0.0
point1 = Coords_3D(1.0, 0.0, 0.0)
point2 = point1
```

Derived Types

Note that two variables of the same type can be handled very simply. Derived types should always be placed in a **MODULE**.

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DATA Statement

The DATA statement can be used to initialize values:

```
DATA object-list /value-list/ [[,] object-list /value-list/] ...
```

Language Elements

Values initialized in DATA statements automatically have the SAVE attribute.

```
real :: a,b,c
integer :: i, j, k
DATA a,b,c/1.0,2.0,3.0/,i,j,k/3\star0/
<u>real</u> :: diag(100,100)
! sets diagonal elements by implied do
DATA (diag(i,i), i=1,100) / 100*5.0 /
! sets the upper and lower triangles to 0, diagonal to 1
DATA ((matA(i,j),matA(j,i),j=i+1,100),i=1,100)/ 9900*0.0 /
DATA (matA(i,i),i=1,100) / 100*1.0 /
```

Expressions & Operators

Scalar Expressions

Expressions & Operators

Scalar Expressions

Scalar Expressions

Scalar expressions use operators **, *, /, +, -. The following table summarizes the result KIND for all but exponentiation (**)

а	b	used(a)	used(b)	result
I	ı	а	b	
I	R	real(a,kind(b))	b	R
I	С	cmplx(a, 0, kind(b))	b	С
R	- 1	a	real(b,kind(a))	R
R	R	a	b	R
R	С	cmplx(a, 0, kind(b))	b	С
С	1	a	cmplx(b, 0, kind(a))	С
С	R	a	cmplx(b, 0, kind(a))	С
С	С	a	b	С

(I = integer, R = real, C = complex)

and for exponentiation (**):

а	b	used(a)	used(b)	result
	ı	а	b	
- 1	R	real(a,kind(b))	b	R
- 1	С	cmplx(a, 0, kind(b))	b	С
R	- 1	а	b	R
R	R	a	b	R
R	С	cmplx(a, 0, kind(b))	b	С
С	-1	a	b	С
С	R	a	cmplx(b, 0, kind(a))	С
С	С	a	b	С

(I = integer, R = real, C = complex)

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Scalar Expressions

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Expressions & Operators **Logical Operators**

Relational Operators

Fortran supports the old-style FORTRAN 77 relational operators as well as more modern syntax (which most compilers were supporting by extension anyway):

77	Modern
.lt.	<
.le.	<=
.eq.	==
.ne.	/=
.gt.	>
.ge.	>=

The logical operators are simply:

logical negation .not.

logical intersection .and.

logical union .or.

logical equivalence .eqv.

logical non-equivalence .neqv.

Expressions & Operators

Scalar Expressions

Expressions & Operators

Scalar Expressions

Character Operations

Substrings are easy using the same syntax as for arrays:

```
character(len=*),parameter :: alphabet1='abcdefghijklm' &
                                  alphabet2='nopqrstuvwxyz'
    character(len=*),parameter :: numerals='0123456789'
5
   print*, '`First four letters: '`,alphabet1(1:4)
   print*, '`alphanumeric: '`,alphabet1//alphabet2//numerals
```

where we also made use of the "//" concatenation operator.

Arrays can be assigned using expressions that involve arrays of the same shape, or by scalar (in which case the scalar is applied to all elements of the array), e.g.

```
real :: a(20,20),b(10)
3
   a(1,11:20) = b
   a = a + 1 0
```

This flexible syntax makes for much more compact code.

Control Constructs

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Array Assignment

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DO Loops

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Control Constructs

IF Conditional

IF Construct

```
[name:] if (expr) then
          block
        [else if (expr) then [name]
          block] ...
        [else [name]
          blockl
        end if [name]
```

Note that the optional name is only for program clarity (especially for nested loops), and needs to be unique. Also note the single statement variation:

```
if (expr) single-statement
```

DO Loops

Old style loop syntax:

```
[name:] do var=expr1,expr2[,expr3]
2
               block
            end do [name]
```

where the loop is executed MAX(0,(expr2-expr1+expr3)/expr3) times, and var is a named scalar integer variable, and expr1, expr2, and expr3 are scalar integer expressions (expr3 must be nonzero if used). Control Constructs

DO Loops

Control Constructs

termination, it is not really worth talking about ...

Infinite DO Loop

One important variation on the DO construct is the endless do loop, which has a simple means to exit:

```
i = i+1
if (i >= enough) exit
end do
```

Note that the exit statment is also handy for early termination in bounded loops. The cycle statement is similar, but just drops execution to the next iteration.

2

is exactly the same as

DO WHILE (a /= b)

END DO

DO-WHILE Loop?

```
if (a == b) exit
3
    END DO
```

There is a DO-WHILE construct, but with the exit option for early loop

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Control Constructs

Control Constructs Do Loops **Using Named and Nested Loops**

The GOTO Statement

Ah, the bane of FORTRAN 77 programmers everywhere - the infamous GOTO statement. Still supported in Fortran 90/95, be wary of using the GOTO. If you have to use it, make it as clear as you possibly can.

```
WRITE (6, *) 'Enter runid: (<=9chars) '
2
          READ (*,'(a9)') runid
3
          i=INDEX(runid,' ')-1
          INQUIRE (file=runid(1:i) //".in", exist=ifex)
5
          if(.not.ifex) goto 101
6
          OPEN(unit=iunit, file=runid(1:i)//'.in', status='old', &
               form=' formatted')
```

Here is an example of when using named loops comes in handy:

```
outa: DO
     inna: DO
3
       IF (a.GT.b) EXIT outa ! jump to line 10
       IF (a.EQ.b) CYCLE outa ! jump to line 1
       IF (c.GT.d) EXIT inna ! jump to line 9
7
       IF (c.EQ.a) CYCLE inna ! jump to line 2
     END DO inna
    END DO outa
```

Control Constructs

CASE Construct

Control Constructs

CASE Construct

The CASE Construct

Somewhat like the C switch statement ...

```
[name:] select case (expr)
            [case selector [name]
2
3
              block] ...
            end select [name]
```

The CASE construct can be used as an efficient substitute for a more elaborate IF ... THEN ... ELSEIF ... ELSE ... IF construct.

An example of using CASE when parsing an input file:

```
select case (cterms(1))
2
         case ("MODEL")
3
            select case (cterms(2))
              case ("XBMC", "xbmc")
5
                MCflg=.true.
6
              case ("NRL", "nrl")
              case ("NN2", "nn2")
8
              case default
9
            end select
```

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Modules, Functions & Subroutines

Part II

Fortran Essentials

Modules

Modules provide a way to package together commonly used code (similar to the old common blocks in FORTRAN 77) and have distinct advantages:

- Can be used to hide internal data and routines through PRIVATE and PUBLIC declarations
- Can contain common subroutines and functions with explicit interfaces which can be changed without affecting calling code
- Modules can (and often should) be compiled separately, before the program units that use them

Module Syntax

```
module module-name
      [specification statements]
3
     [contains
       module - subprograms]
    end [module [module-name]]
```

and a very simple example:

```
MODULE TBconst
2
       implicit none
      integer, parameter :: sp=KIND(1.0),
3
          & dp=SELECTED_REAL_KIND(2*PRECISION(1.0_sp)),
           & sc=KIND((1.0,1.0)),
6
          & dc=SELECTED_REAL_KIND(2*PRECISION(1.0_sc))
     real (kind=dp),parameter :: pi=3.141592653589793238462643_dp
    END MODULE TBconst
```

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Modules, Functions & Subroutines

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Modules, Functions & Subroutines

Modules

Using Modules

Modules encapsulate code that can be made accessible to other program units through the USE statement:

```
MODULE TBatoms
2
     USE TBconst
```

Modules are free to load other modules, but not themselves.

Module Data Visibility

You can allow or prevent access to the internal workings of a module using the PRIVATE and PUBLIC attributes:

```
PRIVATE :: pos, store, stack_size ! hidden
2
        PUBLIC :: pop, push
                                          ! not hidden
or
                              ! set default visibility
2
        INTEGER, PRIVATE, SAVE :: store(stack_size), pos
        INTEGER, PRIVATE, PARAMETER :: stack_size = 100
```

Renaming/USE ONLY

You can rename a module entity in a local context:

```
USE TBconst, local_dp => dp ! dp becomes local_dp in current scope
```

or you can restrict access by

```
USE TBconst, ONLY:dp,dc
                              ! only load dp and dc from module TBconst
```

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Modules, Functions & Subroutines Subroutines

Subroutine Syntax

The syntax for a subroutine call is given by

SUBROUTINE

[recursive] subroutine *subroutine-name*[([dummy arguments])]

Module Summary

```
MODULE modname
     ... type defs
3
     ... Global data
     CONTAINS
      SUBROUTINE sub_1
8
      CONTAINS
        SUBROUTINE internal_1
9
10
11
         END SUBROUTINE internal_1
12
         SUBROUTINE internal_2
13
14
         END SUBROUTINE internal_2
15
      END SUBROUTINE sub_1
16
17
      FUNCTION fun_1
18
19
      CONTAINS
20
21
      END FUNCTION fun_1
    END MODULE modname
```

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Modules, Functions & Subroutines

Subroutines

Argument Intent

You can provide information to the compiler (always a good idea!) about the dummy arguments to a routine by:

```
REAL, INTENT (IN) :: arg1
                               ! passing in value
REAL, INTENT(OUT) :: arg2
                               ! returning value only
REAL, INTENT(INOUT) :: arg3
                               ! both apply
```

You should always make use of the INTENT attribute - it allows the compiler to do extensive error checking and optimization (remember, the more that your compilers knows about your code, the better it will be able to perform).

Modules, Functions & Subroutines

Subroutines

Modules, Functions & Subroutines

Function Call Syntax

SAVE Attribute

The SAVE attribute can be applied to a specified entity, or all of the local entities in a procedure:

```
SUBROUTINE sub_1 (arg1, arg2)
       integer, save :: number_calls = 0
2
3
       number_calls = number_calls +1
    SUBROUTINE sub_1 (arg1, arg2)
3
     SAVE
```

SAVE acts to preserve values between calls to the subroutine/function.

The syntax for a function call is given by

FUNCTION

type [recursive] function function-name[([dummy arguments])] & [result(result-name)]

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Modules, Functions & Subroutines

Explicit Interfaces

Explicit Interfaces

External subprograms have an implicit interface by default (even if one uses the external statement to indicate that a subunit is outside the current code, the arguments and their types remain unspecified), and an INTERFACE block is necessary to specify an explicit interface of an external subprogram; as mentioned above, this allows type-checking of actual and formal arguments in a reference to a subprogram

Explicit Interface Example

```
INTERFACE
           SUBROUTINE resid(m, n, x, fvec, iflag)
3
             USE TBatoms
             USE TBconst
             USE TBfitdata
             USE TBflags
7
             USE TBmat
8
             USE TBopt
             USE TBparams
10
11
             implicit none
12
             integer, intent(in) :: m, n
13
             integer, intent(in out) :: iflag
14
             \underline{real}(\underline{kind} = dp), \underline{intent}(\underline{in}) :: x(n)
15
             real(kind=dp), intent(in out) :: fvec(m)
16
           END SUBROUTINE resid
       END INTERFACE
```

Note that the syntax of the interface-body is just an exact copy of the subprogram's header, argument specifications, function result, and END statement.

Modules, Functions & Subroutines

Explicit Interfaces

INTERFACE Properties

- Can not use both EXTERNAL and INTERFACE
- Explicit interfaces required for POINTER or TARGET dummy arguments in a procedure, or pointer-valued function result
- Explicit interfaces also required for OPTIONAL, KEYWORD, and procedural arguments
- Even when not required, explicit interfaces are a good idea (usually placed inside a MODULE)

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Recursion

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Modules, Functions & Subroutine

Modules, Functions & Subroutines Procedures as Arguments

Procedures as Arguments

When using a procedure as an argument, an explicit interface is required (as it is for POINTER, optional, and keyword arguments):

```
REAL FUNCTION minimum(a, b, func)
      ! returns the minimum value of the function func(x)
      ! in the interval (a,b)
           \underline{\mathtt{REAL}}, \underline{\mathtt{INTENT}} (\underline{\mathtt{in}}) :: a, b
               REAL FUNCTION func(x)
                  REAL, INTENT(IN) :: x
               END FUNCTION func
9
            END INTERFACE
10
           REAL f,x
11
12
            f = func(x)! invocation of the user function.
13
        END FUNCTION minimum
```

Optional & Keyword Arguments

Dummy arguments can be optional - using OPTIONAL:

```
SUBROUTINE optargs(a,b)

REAL, INTENT(IN), OPTIONAL :: a

INTEGER, INTENT(IN), OPTIONAL :: b

REAL :: ay; INTEGER :: by

ay = 1.0; bee = 1 ! defaults

IF(PRESENT(a)) ay = a

IF(PRESENT(b)) bee = b

...
```

```
CALL optargs()
CALL optargs(1.0,1); CALL optargs(b=1,a=1.0) ! same, using keywords
CALL optargs(1.0); CALL optargs(a=1.0) ! keywords handier still for long lists
CALL optargs(b=1)
```

Note that optional and keyword arguments need explicit interfaces, and should come after positional arguments.

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Modules, Functions & Subroutines

Recursion

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Recursion is supported in Fortran >=90/95; we can illustrate it best by example:

```
1
2
2
    INTEGER res, n
3
3    IF(n.EQ.1) THEN
4    res = 1
5    ELSE
6    res = n*factorial(n-1)
7
8    END IF
8    END FUNCTION factorial
```

this would be an example of direct recursion ...

Modules, Functions & Subroutines

Recursion

Input/Output

and an example of **indirect** recursion:

```
volume = integrate(func, bounds)
2
    RECURSIVE FUNCTION integrate(f, bounds)
    ! Integrate f(x) from bounds(1) to bounds(2)
5
      REAL integrate
      INTERFACE
         FUNCTION f(x)
            REAL f, x
         END FUNCTION f
      END INTERFACE
11
      REAL, DIMENSION (2), INTENT (IN) :: bounds
12
13
    END FUNCTION integrate
14
15
    FUNCTION func(x)
16
      USE MODfunc
                         ! module MODfunc contains function f
17
      REAL func, x
18
         xval = x
19
         func = integrate(f, bounds)
20
    END FUNCTION func
```

Generally indirect recursion is of the form 'A calls B calls A ...' - in this case integrate calls func which calls integrate ...

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OPEN Examples

number.

3

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Note that UNIT 1-7 are typically reserved (6, or *, is almost always the

standard output, for example), and each file stream needs a unique

OPEN (17, FILE='output.dat', ERR=10, STATUS='REPLACE', &

write (unit = iounit, fmt = "(a) ", iostat = badunit) title if (badunit > 0) call error_handler(ERR_IO)

OPEN (14, FILE='input.dat', ERR=10, STATUS='OLD', RECL=iexp, &

ACCESS='SEQUENTIAL', ACTION='WRITE')

ACCESS='DIRECT', ACTION='READ')

File Handling

Input/Output

Too large a topic to cover in its entirety here - we will focus on the

basics required to familiarize you with basic Fortran I/O functionality.

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Input/Output File Handling

OPEN

```
OPEN ([UNIT=integer,] FILE=filename, [ERR=label,] &
2
          [STATUS=status,] [ACCESS=method,] [ACTION=mode,] &
          [RECL=int-expr)
```

- filename is a string
- status is 'OLD', 'NEW', 'REPLACE', 'SCRATCH' or 'UNKNOWN'
- method is 'DIRECT' or 'SEQUENTIAL'
- mode is 'READ', 'WRITE' or 'READWRITE'
- RECL (record length) needs to be specified for DIRECT access files

Fortran I/O

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Input/Output File Handling

A very handy statement for querying the status of a file by unit number

 EXIST=log_exist returns a logical on the existence of the file • OPENED=log_opened returns a logical on whether the file is

and there are many possible entries in ilist, of which the most

INQUIRE

or filename:

handy are:

open

INQUIRE Example

2 Open input file - fail gracefully if not found. 3 4 INQUIRE (file=runid(1:len_runid)//'.in',exist=exist_in) 5 if (.not.exist_in) then 6 write (*,*) '<readin> Unable to open input file: ', & runid(1:len_runid)//'.in' 8

OPEN(file=runid(1:len_runid)//'.in',status='old',unit=inunit)

Input/Output

File Handling

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Input/Output File Handling

Other I/O Statements

INQUIRE ([UNIT=]unit | FILE=filename, ilist)

• IOSTAT=ios as in the OPEN syntax

CLOSE unattach specified unit number REWIND place file pointer back to start of file BACKSPACE place file pointer back one record **ENDFILE** force writing end-of-file

```
REWIND (11)
BACKSPACE (UNIT=27)
ENDFILE (19)
CLOSE(13, IOSTAT=io_value)
```

endif

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Input/Output Read & Write

READ

```
READ ([UNIT=unit,] [FMT=format,] [IOSTAT=int-variable,] &
2
          [ERR=label,] [END=label,] [EOR=label,] &
3
          [ADVANCE=adv-mode,] [REC=int-expr,] &
          [SIZE=num-chars]) <output-list>
```

where the non-obvious entries are:

- unit is an integer (some lower values are reserved) or * for standard input
- format is a string of FORMAT statement label number
- label is a statement label
- adv-mode is 'YES' or 'NO'
- IOSTAT returns zero for no error

Read & Write Input/Output

Read & Write Input/Output

WRITE

```
READ (14, FMT=' (3(F10.7,1x))', REC=iexp) a,b,c
READ (14, '(3(F10.7,1x))', REC=iexp) a,b,c
READ (*,'(A)', ADVANCE='NO', EOR=12, SIZE=nch) str
```

WRITE ([UNIT=unit,] [FMT=format,] [IOSTAT=int-variable,] & 2 [ERR=label,] [ADVANCE=adv-mode,] & [REC = int-expr) <output-list>

where the entries are as in the READ case.

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READ Example

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Read & Write

Input/Output

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Input/Output

Read & Write

FORMAT

Fortran does have quite an elaborate formatting system. Here are the highlights.

> w chars of integer data lw

w chars of real data, d decimal places w chars of real data, d decimal places

w chars of logical data Lw

w chars of CHARACTER data Aw

n**X** skip n spaces

Note that:

• The **E** descriptor is just the **F** with scientific notation

FORMAT Example

```
WRITE(*,FMT='(2X,2(I4,1X),''name'',A4,F13.5,1X,E13.5)') &
        77778,3,'abcdefghi',14.45,14.5666666
         3 name abcd
                         14.45000
                                    0.14567E+02
```

Note that are quite a few other format descriptors, much less commonly used.

Read & Write

Arrays and Array Syntax

Assumed-shape & Automatic Arrays

Unformatted I/O

Unformatted I/O is simpler (no FORMAT statements) and involves less overhead, less chance of roundoff error), but is inherently non-portable, since it relies on the detailed numerical representation. A file must be either entirely formatted or unformatted, not a mix of the two.

```
WRITE (15, IOSTAT=ios, ERR=2001) B
```

Note that unformatted i/o is generally quite a lot faster than formatted so unless you are concerned with moving your files from one platform to another, you will be much better off using unformatted i/o.

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Automatic Arrays

Local arrays whose extent is determined by dummy arguments are called automatic objects. Example:

```
SUBROUTINE stubbv1(b,m,n)
 integer, intent(in) :: m, n
 real, intent(inout) :: b(:,:)
 REAL :: b1(m,n)
                                  ! automatic
 REAL :: b2(SIZE(b,1),SIZE(b,2)) ! automatic
```

Note that both assumed-shape arrays and automatic objects are likely to be placed on the **stack** in terms of memory storage.

Assumed-shape Arrays

Arrays passed as dummy arguments should generally be what are called **assumed-shape** arrays, meaning that the dimensions are left to the actual (calling arguments):

```
SUBROUTINE stubby (a,b)
      implicit none
3
      real, intent(in) :: a(:),b(:,:)
```

- Note that the default bounds (1) apply
- Actual arguments can not be vector subscripted or themselves assumed-shape

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Arrays and Array Syntax Dynamic(Allocatable) Arrays

Allocatable Arrays

Finally, dynamic data storage elements for Fortran! An array that is **not** a dummy argument or function can be given the ALLOCATABLE attribute:

```
real, allocatable :: a(:,:)
2
3
    ALLOCATE (a (ntypes, 0:ntypes+2)) ! ntypes is an integer
    ! lots of work
    DEALLOCATE (a)
```

Note that originally ALLOCATABLE arrays could not be part of a derived type (have to use a POINTER to get the same functionality) that oversight was fixed in Fortran 2003.

Arrays and Array Syntax Dynamic(Allocatable) Arrays

Arrays and Array Syntax

More Pointers

ALLOCATE & DEALLOCATE

The syntax for ALLOCATE and DEALLOCATE are given by:

```
ALLOCATE ( list [, stat=istat] )
DEALLOCATE( list [, stat = istat]
```

The optional stat= specifier can be used to test the success of the (de)allocation through the scalar integer istat. As usual, zero for success. Leaving out "stat=" should result in a termination if the (de)allocation was unsuccessful.

C), instead the variables must be declared using the target attribute: real, target :: x, y(100), z(4,4)

```
integer, target :: m, n(10), k(10,10)
    real, pointer :: ptr1, ptr2, ptr_y(:), ptr_z1(:), ptr_z2(:,:)
5
                       ! simple pointer assignment
    alpha = exp(ptrl) ! pointer shares memory location with x,
                       ! but used like any value
    nullify (ptr1)
                      ! frees up pointer
10
11
    if (associated(ptrl)) then
12
       print*, 'ptrl is associated'
13
       if (associated(ptrl, target=x)) then
14
          print*, 'ptrl is associated with "x"'
15
    endif
```

Note that you can not associate pointers with just any variable (as in

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Pointer Flexibility

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More Pointers

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Arrays and Array Syntax More Pointers

More Fun With Pointers

array-associated pointers have considerable flexibility:

```
ptr_y => y
                      ! can use ptr_y(i) just as y(i)
ptr_y => y(11:20)
                    ! ptr_y(1) is now y(11) ...
ptr_y => z(2,1:4)
                   ! loads row 2 of z intro ptr_y(:)
ptr z2 \Rightarrow z(2:4,2:4) ! ptr z2 is 3x3 submatrix of z
ALLOCATE (ptr_z1(16)) ! direct allocation
```

Note that pointers can also be used as components of derived types, making for very flexible data structures.

Pointer Considerations

Some things to think about when using pointers in Fortran:

Arrays and Array Syntax

- Can create complex (and difficult to maintain) code
- Easy to create bugs that only arise at run-time
- Inhibit compiler optimization (difficult to predict data patters and disjoint memory structures)

Elemental Operations

We have already seen **elemental** operations in which conformable operands can be used with intrinsic operators, e.g.

```
real :: a(100,100)
2
   a = SQRT(a)
```

will apply the square root operator individually to all of the elements of a. Not only intrinsics can be elemental, and you can also use the elemental declaration in user-defined functions (Requires Fortran >=95) as well.

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Arrays and Array Syntax Array-valued Functions

WHERE Statement

Useful for performing array operations only on certain elements of an array, but preserving the compact syntax:

```
WHERE (logical-array-expr)
 array-assignments
WHERE (pressure <= 1.0)
pressure = pressure + increment
ELSEWHERE
 pressure = pressure + check_pressure
END WHERE
```

in the example all arrays are of the same shape, and the assignment is said to be *masked* using the comparison (which is done element by element). Fortran >=95 also provides for masks in additional ELSEWHERE statements.

Array-valued Functions

Functions can return arrays - just be careful that you ensure that the interface is an explicit one. An example:

```
PROGRAM arrfunc
       implicit none
3
      integer,parameter :: ndim=36
      integer, dimension (ndim, ndim) :: m1, m2
      m2 = funky(m1, 4)
7
      CONTAINS
      FUNCTION funky (m, scal)
10
        integer, intent(in) :: ima(:,:)
11
         integer, intent(in) :: scal
12
         integer :: funky(SIZE(m,1),SIZE(m,2))
13
        funky(:,:) = m(:,:)*scal
14
      END FUNCTION funky
    END PROGRAM arrfunc
```

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FORALL Construct (Fortran 95)

Fortran 95 introduced the concept of a FORALL statement which is basically an array assignment with some explicit indexing:

```
FORALL (i = 1:M) grid(i,i) = diag(i)
FORALL (i = 1:M, j = 1:N) grid(i, j) = u(i) *v(j)
FORALL (i = 1:M, j = 1:N, eps(i.j) /= 0.0) grid(i,j) = 1.0/eps(i,j)
```

Implied is that the assignment is trivially data-parallel, i.e. it can be carried out in any order, and therefore can be more efficient than a more traditional loop. Construct form:

```
FORALL (i = 2:N-1, j = 2:N-1)
 U(i,j) = U(i,j-1) + U(i,j+1) + U(i-1,j) + U(i+1,j)
 V(i,j) = U(i,j)
END FORALL
```

where the results are executed in any order, held in temporary storage (to avoid indeterminate results), and then updated in arbitrary order.

Arrays and Array Syntax

Array-valued Functions

PURE Procedures (Fortran >=95)

Complete FORALL construct syntax:

```
[name:] FORALL(index=lower:upper[:stride] [,index2=lower2:upper2[:stride2]] ... &
2
                      [,scalar-logical-expr])
3
              [body]
            END FORALL [name]
```

The body of a FORALL construct can be quite general (containing statements, additional FORALL or WHERE statements/constructs, etc.), but must not branch (e.g. goto) out of the construct. Any included subprograms must be pure, in the sense of inducing no undesired side-effects in the sense of inducing an order dependence that would impede parallel processing.

Programmer can assert that a function or subroutine is PURE: by adding the PURE keyword to the function/subroutine statement:

- a pure function does not alter its dummy arguments (must be INTENT (IN))
- INTENT of dummy arguments must be declared (IN for functions)
- does not alter variables accessed by host or use association
- contains no local variables with SAVE attribute

Arrays and Array Syntax

- contains no operations on external file
- contains no STOP statements
- any internal procedures must also be pure all intrinsic functions are pure.

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Intrinsics For Arrays

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Arrays and Array Syntax Intrinsics For Arrays

Array Functions

Array Intrinsics

Fortran is designed around the notion of data manipulation, so it is not a great surprise that it has a number of built-in functions for array manipulation, some of which we have already seen (elemental operations, masking).

Set of operations that involve common extractions from arrays:

ALL(MASK [,dim]) ANY(MASK [,dim]) COUNT(MASK [,dim]) MAXLOC(ARRAY [,mask]) MINLOC(ARRAY [,dim[,mask]]) MAXVAL(ARRAY [,dim[,mask]]) MINVAL(ARRAY [,dim[,mask]]) PRODUCT(ARRAY [,dim[,mask]]) SUM (ARRAY [,dim[,mask]])

all relations in mask are true [along dimension dim] if any elements of mask are true [along dimension dim] number of elements of mask that are true location of element with maximum value location of element with minimum value maximum value [of true elements in mask, along dim] minimum value [of true elements in mask, along dim] products [of true elements in mask, along dim] of values sum [of true elements in mask, along dim] of values

Example of Array Extraction Intrinsics

```
integer :: i, j, max_element(2), max_element_2(2)
    real :: Amax, Amax_2, Amat(100, 100)
3
     Amat = RESHAPE( (/ ((100*(i-1)+j,j=1,100),i=1,100) /), (/ 100, 100 /), ORDER=(/2,1/))
    max_element = MAXLOC( Amat )
                                             ! finds the element of Amax with
                                             ! max value [A(100,100) =
8
    Amax = MAXVAL ( Amat )
9
10
    max_element_2 = MAXLOC( Amat, Amat<66) ! finds element in Amax</pre>
                                             ! that's < 66 [ A(1,65) =
11
                                                                        65 ]
    Amax_2 = MAXVAL(Amat, Amat<66)
```

Very useful array inquiry functions:

Array Inquiry Functions

ALLOCATED(ARRAY) LBOUND(ARRAY [,dim]) SHAPE(ARRAY) SIZE(ARRAY [,dim]) UBOUND(ARRAY [,dim])

logical if A has been allocated lower bound for dimension dim of A (integer vector if no dim) returns integer vector of shape of A size of dimension dim of A (else all of A) upper bound for dimension dim of A (integer vector if no dim)

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Arrays and Array Syntax Intrinsics For Arrays

Array Reshaping

RESHAPE is a general intrinsic function which delivers an array of a specific shape:

```
RESHAPE(source, shape [,pad][,order])
```

returns an array whose shape is given by the constant rank-1 integer array (nonnegative elements) shape derived from the array source. If order is absent, elements of pad are used to fill out remaining elements in the result (whose size may then exceed that of source. order can be used to pad the result in non-element order.

```
real :: A2(2,2)
A2 = RESHAPE(((/1,2,3,4/),(/2,2/)))
                                          ! create a 2x2 matrix from 1x4 vector
print*, 'A2: 1,1 1,2 = ',A2(1,1),A2(1,2)
print*, 'A2: 2,1 2,2 = ',A2(2,1),A2(2,2)
```

produces (recall that Fortran is column-ordered):

```
A2: 1,1 1,2 =
                                3.000000
                 2.000000
                                4.000000
A2: 2,12,2 =
```

Arrays and Array Syntax

Intrinsics For Arrays

Vector/Matrix Intrinsics

Fortran 90 has several intrinsics for vector dot products matrix multiplication and transposition:

DOT PRODUCT(vector 1, vector 2) MATMUL(matrix_1,matrix_2) TRANSPOSE(matrix)

dot product of two rank-1 equal length vectors matrix multiplication transposition of any rank-2 array

Fortran Intrinsics

Fortran Intrinsics

Mathematical Intrinsics

Intrinsics Categories

There are roughly 75 new intrinsic routines (versus FORTRAN 77), but they roughly fall into 4 categories:

- Elemental procedures
- Inquiry functions
- Transformational functions
- Nonelemental subroutines

I am going to group them a bit differently, and only cover the more common ones. Consult a good reference¹ for a thorough list.

¹Metcalf, Reid, and Cohen *Modern Fortran Explained*, (Oxford, Great Britain, 2011).

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Numerical Intrinsics

Numerical Intrinsics

The list of numerical intrinsics (with syntax and usage):

INT(a[,KIND]) REAL(a[,KIND]) CMPLX(x[,y][,KIND]) AINT(a[,KIND]) ANINT(a[,KIND]) NINT(a[,KIND]) ABS(a) MOD(a,p) MODULO(a,p) FLOOR(a[,kind]) CEILING(a[,KIND]) SIGN(a,b) DIM(x,y)MAX(a1,a2[,a3,...]) MIN(a1,a2[,a3,...]) AIMAG(z) CONJG(z)

convert to integer, type KIND convert to real, type KIND convert x or (x,y) to complex, type KIND truncate real to lowest whole number, type KIND returns nearest whole number real, type KIND integer (type KIND) value nearest a absolute value of a, same KIND as a remainder of a modulo p, a-int(a/p)*p (has sign of a) a-floor(a/p)*p (has sign of p) greatest integer less than or equal to a, type KIND least integer greater than or equal to a, type KIND absolute value of a times sign of b max(x-y,0.0)maximum of two or more numbers minimum of two or more numbers imaginary part of complex number z, type real, KIND(z) conjugate of complex number z

Mathematical Intrinsics

Far too many to enumerate here - you can find a handy reference for the full set in other references. Note that almost all support a generic interface supporting available KIND types, and that most are elemental.

SQRT, EXP, LOG, LOG10, SIN, COS, TAN, ASIN, ACOS, ATAN, SINH, COSH, TANH

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Fortran Intrinsics

String Functions

String Functions

Yes, Fortran does have string handling capability! And in fact, it is much improved. The following table gives a brief synopsis:

> ACHAR(I) ADJUSTL(STRING) ADJUSTR(STRING) CHAR(I, kind) IACHAR(C) ICHAR(C) INDEX(STRING, SUBSTRING, back) LEN(STRING) LEN TRIM(STRING) REPEAT(STRING, NCOPIES) SCAN(STRING, SET, back) TRIM(STRING) VERIFY(STRING, SET, back)

Adjusts to the left Adjusts to the right Returns character of number I ASCII number of char C Number of char C Starting pos of substring in string Length of STRING Length of string without trailing blanks String concatnation

ASCII character of number I

Position of 1st occurrence of any char in SET in STRING Returns string without trailing blanks

Position of 1st char in STRING not in SET

Fortran Intrinsics

String Functions

Fortran Intrinsics

Bitwise Intrinsics

The following functions can be used for ASCII lexical string comparisons:

```
1 LGE(STRING_A, STRING_B)
2 LGT(STRING_A, STRING_B)
3 LLE(STRING_A, STRING_B)
4 LLT(STRING_A, STRING_B)
```

Note that if the strings are of differing length, the shorter will be padded with blanks for comparative purposes. All return default logical results.

Bitwise Intrinsics

Modern Fortran added support for quite a few bitwise operations:

BIT_SIZE(I) BTEST(I, POS) IAND(I, J) IBCLR(I, POS) IBITS(I, POS, LEN)

ISHIFTC(I, SHIFT, size)

NOT(I)

number of bits in a word .true. if POS number of I is 1 logical addition of bit chars in I and J puts a zero in the bit in POS

puts a zero in the bit in POS uses LEN bits of word I beginning at POS, additional

bits are set to zero. POS + LEN <= BIT_SIZE(I)

IBSET(I, POS) puts the bit in position POS to 1

IEOR(I, J) performs logical exclusive OR

IOR(I, J) performs logical OR

ISHIFT(I, SHIFT) performs logical shift (to the right if the number of steps SHIFT < 0 and to the left if SHIFT > 0).

Positions that are vacated are set to zero. performs logical shift a number of steps

circularly to the right if SHIFT < 0, circularly to the left if SHIFT > 0. If SIZE

is given, it is required that 0 < SIZE <= BIT_SIZE(I)

Timing & Random Numbers

logical complement

Fortran Intrinsics

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Fortran Intrinsic

Timing & Random Numbers

Real-time Clock

Modern Fortran provides a pair of routines to access the real-time clock:

DATE AND TIME

DATE_AND_TIME([date] [,time] [,zone] [,values])

date character string in form ccyymmdd

time character string in form hhmmss.sss

zone character string in form Shhmm, difference between local

and UTC

values integer vector of size at least 8 with year, month, day, difference from UTC in minutes, hour, minutes, seconds, milliseconds

Random Numbers

Modern Fortran also has a built-in pseudorandom generator:

```
1 CALL RANDOM_NUMBER(harvest)
2 CALL RANDOM_SEED([size] | [put] | [get])
```

harvest can be an array, and the range of the random numbers are the interval [0,1). size is intent OUT and returns the size of the integer seed array, which can be input (put) or returned (get).

Fortran Intrinsics Timing & Random Numbers

CPU Time

SYSTEM_CLOCK

SYSTEM_CLOCK([count][,count_rate][,count_max])

count processor-dependent value of processor clock
 (-huge (0) if no clock)

count_rate clock counts per second (0 if no clock)

count_max maximum for count (0 if no clock)

CPU TIME

CPU_TIME(time)

Fortran >=95 only:

time real assigned to processor-dependent time in seconds (negative value if no clock)

```
real :: t1,t2

CALL CPU_TIME(t1) ! Fortran>=95 only

CALL CPU_TIME(t2)

CALL CPU_TIME(t2)

Print*, 'Time spent in code: ',t2-t1,' seconds'
```

Fortran Intrinsics

In my experience the CPU_TIME intrinsic is not very precise, however, and depends rather strongly on the compiler ...

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Fortran Intrinsics

Timing & Random Numbers

Fortran Intrinsics

Array Functions

STOPWATCH

STOPWATCH is not part of standard Fortran, but is a nice little package written by William Mitchell at NIST:

http://math.nist.gov/StopWatch

which supports a more full featured set of timing routines (including wall time, cpu time, and system time).

Array Functions

The array intrinsic functions will be discussed in a special section devoted to arrays ...

Part III

Fortran Advanced Operations

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Numerics in Modern Fortran

Inquiry Functions

The floating-point model is given by

$$x = sb^e \sum_{k=1}^p f_k b^{-k},$$

where

x real value

s sign (+,-)

b base (b > 1)

e exponent (q > 1)

p number mantissa digits (p > 1)

 f_k k-th digit, $(0 < f_k < b)$

Numerical Inquiry Functions

There are a bunch of numerical inquiry functions in Fortran 90/95. First, the integer representation model is given by

$$i = s \sum_{k=0}^{q-1} d_k r^k,$$

where

i integer value

sign (+,-)

r radix (r > 1)

q number of digits (q > 1)

 d_k k-th digit, $(0 \le d_k < r)$

Numerics in Modern Fortran Inquiry Functions

Inquiry Functions

The inquiry functions are given in the following table:

digits(x) value of (q, p) for (integer, real)

epsilon(x) b^{1-p}

huge(x) largest value in model

minexponent(x) minimum e maxexponent(x) maximum e

precision(x) decimal precision radix(x) base b of integers

range(x) decimal exponent range tiny(x) smallest positive value (real)

Note that all of these functions are generic, and can be used with any supported KIND.

Numeric Manipulation Functions

Using the same representational model as the inquiry functions. Designed to return values related to components of real type.

exponent(x)	value of <i>e</i> in real model
fraction(x)	fractional part in real model

value nearest x in direction of sign of s nearest(x,s) reciprocal of relative spacing, $|xb^{-e}|b^p$ rrspacing(x)

xbi scale(x,i) xb^{i-e} set exponent(x,i)

 b^{e-p} if x/=0 and in range, else TINY spacing(x)

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IEEE Exceptions

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IEEE Exceptions

IEEE Arithmetic in Fortran

The Fortran 2003 (and later) standard contains facilities for IEEE exception handling. The IEEE¹/ ISO² standard for floating-point arithmetic greatly helped in developing portable numeric code. The goal is to allow for a portable way to test and set the five floating-point exception flags in the IEEE standard.

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IEEE Arithmetic IEEE Intrinsics

IEEE Intrinsics

IEEE exceptions:

Overflow the result of an operation exceeds the data format Division by Zero finite numerator, zero denominator (result is $\pm \infty$) Invalid operation invalid (e.g. $\infty \times 0$) - result is NaN Underflow result of operation too small for data representation Inexact result of operation can not be represented without rounding

Three intrinsic modules are provided:

- IEEE EXCEPTIONS
- IEEE ARITHMETIC, itself loads IEEE EXCEPTIONS
- IEEE FEATURES

Inability to load one of these modules will indicate a non-compliant compiler. For detailed usage, see, for example, Metcalf & Reid. At this point there are relatively few compilers that have explicit support for these modules.

¹IEEE 754-1985, Standard for floating-point arithmetic

²IEC 559:1989, Binary floating-point arithmetic for microprocessor systems

Generic Interfaces

Modules for OO Programming

Note that Fortran modules can be used as objected oriented programming (OOP) constructs:

- Creation of derived types that behave just like intrinsic types
- Intrinic types and operators can be overloaded
- Data can be hidden (encapsulated)
- In such a way one can create semantic extensions

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Object-Oriented Fortran? Generic Interfaces

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argument:

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User-supplied functions, like most of the intrinsics, can have **generic**

interfaces. For example, consider the intrinsic ABS (x) - behind the

scenes, the function actually called depends on the KIND of the

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CABS for x complex

ABS for x real

IABS for x integer

Object-Oriented Fortran? Generic Interfaces

Generic Interface Procedure Example

You can also make use of generic interfaces, of course:

```
MODULE useful_1
     IMPLICIT NONE
     INTERFACE exemplify
      MODULE PROCEDURE exemplify_int
                                          ! Fortran 95 allows separated
      MODULE PROCEDURE exemplify_real
                                          ! module procedure statements
      MODULE PROCEDURE exemplify_complex
     END INTERFACE exemplify ! only Fortran >=95 allows specification at END
8
     CONTAINS
9
     SUBROUTINE exemplify_int(x)
10
      integer, dimension(:), intent(inout) :: x
11
     END SUBROUTINE exemplify_real(x)
12
13
     SUBROUTINE exemplify_real(x)
14
      real, dimension(:), intent(inout) :: x
15
16
      END SUBROUTINE exemplify_complex(x)
17
      SUBROUTINE exemplify_complex(x)
18
      complex, dimension(:), intent(inout) :: x
19
     END SUBROUTINE exemplify_complex(x)
    END MODULE useful_1
```

Generic Interface Example (cont'd)

```
PROGRAM Main
IMPLICIT NONE
USE useful 1
 real :: rx(1000)
 integer :: ix(1000)
 CALL exemplify(rx) ! generic call
CALL exemplify(ix) ! generic call
END PROGRAM Main
```

The rule being that the argument list makes the actual choice of routine unambiguous.

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Object-Oriented Fortran?

Operator Overloading

Operator Overloading

Operator Overloading Example

```
MODULE useful 2
      IMPLICIT NONE
      TYPE frac ! type for integer fractions
        integer :: numerator, denominator
      END TYPE frac
      INTERFACE OPERATOR (*)
      MODULE PROCEDURE frac_int, int_frac, frac_frac
     CONTAINS
10
      FUNCTION frac_int(left,right)
11
       type(frac), intent(in) :: left
       integer, intent(in) :: right
12
13
14
      END FUNCTION frac_int
      FUNCTION int_frac(left, right)
      integer, intent(in) :: left
16
17
      type (frac), intent (in) :: right
18
19
      END FUNCTION int_frac
20
      FUNCTION frac_frac(left, right)
21
      type(frac), intent(in) :: left
22
      type (frac), intent (in) :: right
23
```

Note that operator precedence remains unaffected, however.

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Object-Oriented Fortran?

User Defined Operators

User Defined Assignment

END FUNCTION frac_frac END MODULE useful 2

The assignment operator (=) is a little special - overloading it requires an INTERFACE ASSIGNMENT with a SUBROUTINE:

- The first argument has INTENT (OUT) and represents the left-hand side of the assignment
- The second argument has INTENT (IN) and represents the right-hand side
- The subroutine must be "pure," i.e. not alter global data, or produce any output

Operators can be overloaded using the INTERFACE OPERATOR statement:

- Specify the MODULE PROCEDURE/ to deal with the implementation
- Useful (if not required) for derived types
- Operator name/symbox can be any of the intrinsics or any sequence of 31 characters or less in length enclosed in periods (other than .true. and .false)
- Be wary when overloading intrinsic operators binary operators can not be made unary, etc.
- Can not redefine intrinsically defined operations (must remain unambiguous)

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User Defined Operators

User Defined Operators

and in a similar way, you can define your own operators:

Object-Oriented Fortran?

```
MODULE useful_2
    IMPLICIT NONE
    INTERFACE OPERATOR (.converged.) ! new op
     MODULE PROCEDURE testconv
    END INTERFACE
6
   END MODULE useful_2
```

User Defined Assignment Example

```
MODULE useful 3
     IMPLICIT NONE
     INTERFACE ASSIGNMENT (=)
       MODULE PROCEDURE frac_eq
     END INTERFACE
     PRIVATE frac_eq
    CONTAINS
     SUBROUTINE frac_eq(lhs,rhs)
      type(frac), intent(out) :: lhs
10
      type(frac),intent(in) :: rhs
11
      : ! body has to have an assignment to lhs
12
     END SUBROUTINE frac_eq
13
    END MODULE useful_3
```

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CAF Execution Model

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Coarray Fortran

CAF Execution Model

CAF Execution Model

CAF can be used in shared and distributed memory systems (as long as the runtime system supports it),

- **image** refers to each copy of the program in CAF, with
 - $1 \le \text{this_image}() \le \text{num_images}()$
- Co-array syntax uses usual () to refer to local data, [] to refer to remote data
- An image moves remote data to local data through co-array syntax
- Programmer handles synchronization

Coarray Fortran Basics

Coarray Fortran (CAF, requires Fortran >=2008) follows the PGAS (partitioned global address space) model. It is composed of simple extensions to "regular" Fortran, similar to UPC (Unified Parallel C) and Titanium (Java).

- Designed to follow SPMD (Single Program Multiple Data)
- Fixed number of processes/threads/images
- Explicit data decomposition and synchronization, data and computing are local
- One-sided communciations through co-dimensions
- Current CAF design is very "minimalist," introduced as few extensions to Fortran as possible

CAF Coarrays

Data stored in other CAF images are referenced through cosubscripts (enclosed in square brackets), mapped to an image index (one to num images()).

- Images have their own data, accessed in the standard Fortran way
- Data with codimensions (square brackets) has corank (at decalaration) and cobounds/coextent (at declaration or allocation)
- Coarray data has the same size and shape on each image

```
real, dimension(100), codimension[*] :: a,b ! array coarrays
2
      real, codimension[*] :: c
                                                     ! scalar coarray
3
      a(:) = b(:)[i]
                                                     ! coarray b in image i copied to a
                                                       on executing image
```

sync all

Each CAF image executes on its own without regard to others until image control statements are reached, the simplest of which is sync all, which forces a barrier synchronization.

```
real :: a[*] ! scalar coarray
svnc all
if (this_image() == 1) then
  read(*,*) a ! from stdin
  do image=2, num_images()
     a[image] = a
   end do
end if
sync all
! Broadcasts a to all images
```

The above code snippet forms a broadcast, the first sync all ensures that image 1 does not interfere with any other image's use of a, the second that no image uses the old value of a before its update by image one.

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Coarray Fortran CAF Examples

Coarray Fortran Simple Example

Once again, our favorite "Hello, world" example:

```
program hello_caf
      ! Simple Hello World for CAF
      use ifport ! intel specific
6
      implicit none
      integer :: istat,len
      character(len=max_hostnam_length+1) :: myhostname
10
      ! intel specific call for host name
11
     istat = hostnam (myhostname)
12
     len = len_trim(myhostname)
13
14
      write(*,'(a26,i4,a4,i4,a17,a)') "Hello, world, I am image ",this_image(), &
15
           & " of ", num_images(), " total images on ", myhostname(1:len)
    end program hello_caf
```

More Synchronization

- sync images (image set) Synchronizes calling image with all others in the image set - sync all is equivalent to sync images (*)
- lock/unlock Requires scalar lock variable of type lock_type defined by intrinsic module iso fortran env
- critical/end critical restricts execution to one image at a time
- sync memory Gives the ability to define boundaries on image between segments (statements between two image control statements), allows user-defined ordering (very flexible, but also very difficult to debug)

All synchronization statements have optional stat= and errmsq= arguments (as with allocate/deallocate).

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Coarray Fortran

CAF Examples

Note that Intel's ifort has CAF support, and an extra environment variable for controlling the number of images, and it is pretty simple to run in *shared* mode (i.e., on a single node):

```
[rush:~/d_fortran/d_caf]$ ifort -o hello_caf -coarray hello_caf2.f90
[rush:~/d_fortran/d_caf]$ export FOR_COARRAY_NUM_IMAGES=8
[rush:~/d_fortran/d_caf]$ ./hello_caf2
Hello, world, I am image 1 of 8 total images on k07n14
                                 8 total images on k07n14
Hello, world, I am image 2 of
Hello, world, I am image 3 of
                                 8 total images on k07n14
Hello, world, I am image 4 of
                                  8 total images on k07n14
Hello, world, I am image
                          5 of
                                 8 total images on k07n14
Hello, world, I am image 6 of
                                8 total images on k07n14
Hello, world, I am image 7 of
                                  8 total images on k07n14
Hello, world, I am image
                          8 of
                                  8 total images on k07n14
```

Note that running CAF in shared mode does not require jumping through any extra hoops (not so in the distributed case).

```
#!/bin/bash
     #SBATCH --nodes=2
     #SBATCH --ntasks-per-node=8
     #SBATCH --constraint=CPU-L5520|CPU-L5630
     #SBATCH --partition=debug
     #SBATCH --mail-type=END
     #SBATCH --mail-user=jonesm@buffalo.edu
     #SBATCH --output=slurmQ.out
     #SBATCH --job-name=caf-test
     #export | grep SLURM
13
14
     module load intel-mpi intel
     module list
     ifort -o hello_caf.dist -coarray=distributed hello_caf.f90
     export MY_NODEFILE=tmp.$$
    srun -1 hostname -s | sort -n | awk '{print $2}' | uniq > $MY_NODEFILE
NNODES='cat $MY_NODEFILE | wc -1'
     export FOR_COARRAY_CONFIG_FILE=caf.$$
     NODES= 'cat $MY_NODEFILE | awk '{printf "%s ", $1}''
     echo "-n $SLURM_NTASKS_PER_NODE -host $node $EXEC " >> $FOR_COARRAY_CONFIG_FILE
     #export I_MPI_DEBUG=4 # enable to see detailed placement info
     mpdboot -n $NNODES -f $MY_NODEFILE -v
     mpdtrace
     SEXEC
      -e $MY_NODEFILE ] && \rm $MY_NODEFILE
     [ -e $FOR_COARRAY_CONFIG_FILE ] && \rm $FOR_COARRAY CONFIG FILE
```

Note the use of mpds and the MPI subsystem for distributing tasks, although the MPI task launcher is not itself being used.

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Simple Fortran Examples Strings/Internal Files

Example 1, Build/Use Strings and Internal Files

It is fairly common to want to convert to a string, in C/C++ you can cast or use sprintf, and in Fortran you can use an internal file to write to a string.

In the following example we use an internal file (basically a string) to convert an integer to a string, and then build a file name incorporating that string (suppose, for example, that you wanted to write out a separate file for each rank in an MPI application).

```
[rush:~/d_fortran/d_caf]$ cat slurmQ.out
    Currently Loaded Modulefiles:
                                              5) intel-mpi/5.0.1
     2) modules
                         4) intel/15.0
    running mpdallexit on d16n32
    LAUNCHED mpd on d16n32 via
    RUNNING: mpd on d16n32
    LAUNCHED mpd on d16n34 via d16n32
    RUNNING: mpd on d16n34
    d16n32
11
    d16n34
12
     Hello, world, I am image 3 of 16 total images on d16n32
     Hello, world, I am image
                              4 of 16 total images on d16n32
     Hello, world, I am image 9 of 16 total images on d16n34
     Hello, world, I am image 5 of 16 total images on d16n32
     Hello, world, I am image 10 of 16 total images on d16n34
     Hello, world, I am image 6 of 16 total images on d16n32
     Hello, world, I am image 11 of 16 total images on d16n34
     Hello, world, I am image 7 of 16 total images on d16n32
     Hello, world, I am image 12 of
                                     16 total images on d16n34
     Hello, world, I am image
                              8 of 16 total images on d16n32
     Hello, world, I am image 13 of 16 total images on d16n34
     Hello, world, I am image 1 of 16 total images on d16n32
     Hello, world, I am image 14 of 16 total images on d16n34
25
     Hello, world, I am image 2 of 16 total images on d16n32
     Hello, world, I am image 15 of 16 total images on d16n34
     Hello, world, I am image 16 of 16 total images on d16n34
```

Simple Fortran Examples

Strings/Internal Files

```
program testchar
      implicit none
      ! convert integer to string for use in file name
      character(len=*),parameter :: alphabet1='abcdefghijklm', &
                                  alphabet2='nopqrstuvwxyz'
      character(len=*),parameter :: numerals='0123456789'
      character(len=12) :: cstring
8
      integer :: testint
10
      print*, 'First four letters: ',alphabet1(1:4)
11
      print*, 'alphanumeric: ',alphabet1//alphabet2//numerals
13
      ! test convert int to string
14
      testint=123
      write (cstring, '(i12)') testint
      print*," test string = ",TRIM(ADJUSTL(cstring)),"."
17
      print*," filename test = ","outfile_"//TRIM(ADJUSTL(cstring))//".dat"
    end program testchar
```

[rush:~/d_fortran]\$ ifort -o testchar testchar.f90

alphanumeric: abcdefghijklmnopqrstuvwxyz0123456789

[rush:~/d fortran]\$./testchar

filename test = outfile_123.dat

First four letters: abcd

test string = 123.

Example 2, Command Line Arguments

New to Fortran >=2003, command line arguments are now supported. The following example illustrates the use of get command, command_argument_count, and get_command_argument to process command line arguments to a Fortran program.

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Simple Fortran Examples

Command Line Arguments

Simple Fortran Examples

Command Line Arguments

```
cmdline.f90 -- simple command-line argument parsing example
         test fortran2003 support for get_command_argument, get_command,
           and command_argument_count
4
5
6
7
       program cmdline
implicit none
          character(len=255) :: cmd
          character(len=*), parameter :: version = '1.0'
character(len=32) :: arg,date*8,time*10,zone*5
9
          logical :: do_time = .false.
11
12
13
14
15
16
17
18
19
20
21
22
23
24
25
26
27
28
29
30
31
32
          integer :: i
          call get command(cmd)
          write (*,*) 'Entire command line:'
          write (*,*) trim(cmd)
          do i = 1, command_argument_count()
    call get_command_argument(i, arg)
             select case (arg)
case ('-v', '--version')
                 print '(2a)', 'cmdline version ', version
             stop
case ('-h', '--help')
                 call print_help()
              case default
                 print '(a,a,/)', 'Unrecognized command-line option: ', arg
call print_help()
              end select
```

```
34
      ! Print the date and, optionally, the time
35
      call date_and_time(DATE=date, TIME=time, ZONE=zone)
36
       write (*, '(a,"-",a,"-",a)', advance='no') date(1:4), date(5:6), date(7:8)
37
      if (do_time) then
38
         <u>write</u> (*, '(x,a,":",a,x,a)') time(1:2), time(3:4), zone
      <u>else</u>
40
         write (*, '(a)') ''
41
       end if
42
43
     contains
44
45
       subroutine print_help()
        print '(a)', 'usage: cmdline [OPTIONS]'
        print '(a)', ''
47
48
        print '(a)', 'Without further options, cmdline prints the date and exits.'
49
         print '(a)', ''
50
         print '(a)', 'cmdline options:'
        print '(a)', ''
51
        print '(a)', ' -v, --version
                                           print version information and exit'
        print '(a)', ' -h, --help
                                           print usage information and exit'
        print '(a)', ' -t, --time
54
55
      end subroutine print_help
56
     end program cmdline
```

Simple Fortran Examples Command Line Arguments

```
[rush:~/d_fortran]$ ifort -o cmdline cmdline.f90
    [rush:~/d_fortran]$ ./cmdline
3
    Entire command line:
     ./cmdline
    2014-09-29
    [rush:~/d_fortran]$ ./cmdline -v
     Entire command line:
     ./cmdline -v
    cmdline version 1.0
    [rush:~/d_fortran]$ ./cmdline --help
    Entire command line:
    ./cmdline --help
13
    usage: cmdline [OPTIONS]
    Without further options, cmdline prints the date and exits.
    cmdline options:
                       print version information and exit
     -v, --version
                  print usage information and exit print time
     -h, --help
     -t, --time
    [rush:~/d_fortran]$ ./cmdline --time
     Entire command line:
     ./cmdline --time
    2014-09-29 14:13 -0400
```

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10

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14 15

16 17

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