

PROLOG

(PROGRAMMING IN LOGIC)

ARTIFICIAL INTELLIGENCE

INTRODUCTION TO PROLOG

○ Exercises Teaching Material

- Learn Prolog Now!
<https://sites.google.com/site/prologsite/home>
- SWI Prolog interpreter <http://www.swi-prolog.org/>
- Book: The Art of Prolog by Leon Sterling and Ehud Shapiro.

SWI PROLOG

- *Sociaal-Wetenschappelijke Informatica* ("Social Science Informatics")
- Freely available Prolog interpreter
- Works with
 - Linux,
 - Windows, or
 - Mac OS
- There are many more Prolog interpreters

LECTURE 1

- Theory
 - Introduction to Prolog
 - Facts, Rules and Queries
 - Prolog Syntax

AIM OF THIS LECTURE

- Give some simple examples of Prolog programs
- Discuss the three basic constructs in Prolog:
 - Facts
 - Rules
 - Queries
- Introduce other concepts, such as
 - the role of logic
 - unification with the help of variables
- Begin the systematic study of Prolog by defining terms, atoms, and variables

PROLOG

- "Programming with Logic"
- Declarative
- Very different from other (procedural) programming languages
- Good for knowledge-rich tasks

BASIC IDEA OF PROLOG

- Describe the situation of interest
- Ask a question
- Prolog logically deduces new facts about the situation we described
- Prolog gives us its deductions back as answers

CONSEQUENCES

- Think declaratively, not procedurally
 - Challenging
 - Requires a different mindset
- High-level language
 - Not as efficient as, say, C
 - Good for rapid prototyping
 - Useful in many AI applications

LOGIC PROGRAMS

- A logic program is a set of axioms, or rules, defining relations between objects.
 - There are 3 basic constructs which define logic programming.
-
1. Facts
 2. Queries
 3. Rules

FACTS

- The simplest kind of statement is called a fact.
- Relation holds between objects → Facts
- **Example: father(abraham, isaac).**
- This fact says that **Abraham** is the father of **Isaac**, or that the relation father holds between the individuals named **abraham** and **isaac**.
- **Predicate:** Another name for a relation is a predicate.
- **Atoms:** Names of individuals are known as atoms. Example: **abraham** and **isaac**.
- **Program:** A finite set of facts constitutes a program.

QUERIES

- Queries are a means of retrieving information from a logic program.
- Example: `father(abraham, isaac)?`
- Given the facts of previous slide, the answer to this query is **true/yes**.

ATOMS

- A sequence of characters of upper-case letters, lower-case letters, digits, or underscore, **starting with a lowercase letter**.
 - *Examples:* **abraham**, **big_kahuna_burger**, **hamSandwich** etc.
- An arbitrary sequence of characters enclosed in single quotes
 - *Examples:* **'Vincent'**, **'Suarez's bite'**, **'@\$%'**
- A sequence of special characters
 - *Examples:* **:** **,** **;** **.** **:-**

NUMBERS

- 0-9
- Integers: 12, -34, 22342
- Floats: 34573.3234

VARIABLES

- A sequence of characters of upper-case letters, lower-case letters, digits, or underscore, ***starting with*** either an **uppercase letter** or an **underscore**.

- Examples:

X, Y, Variable, Vincent, _tag etc.

THE LOGICAL VARIABLE, SUBSTITUTIONS, AND INSTANCES

- Suppose we want to know of whom **abraham** is the father.
- `father(abraham, lot)?`
- `father(abraham, milcah)?`
- `,...,`
- `father (abraham, isaac)?` until an answer **yes** is given.
- Better way to use variable logically ☺
- `father (abraham, X)?`
- **X=isaac.**

TERMS

- Variables. Example: X, Y, etc.
- Constants Example: abraham, isaac, etc.

Compound Terms: (functor)

- A functor is characterized by its name, which is an **atom**, and its **arity**, or number of arguments.
- Example: $f(t_1, t_2, \dots, t_n)$
- Atom $\rightarrow f$
- Arity $\rightarrow n$
- t_i are arguments.

GROUND VS. NONGROUND

- queries, goals or terms without variable is ground.
- Example: `foo(a, b)` is ground.
- queries, goals or terms with variable is a ground.
- Example: `bar(X)` is nonground.

PROLOG AND LOGIC

- Clearly Prolog has something to do with logic
- Operators
 - Implication :-
 - Conjunction ,
 - Disjunction ;
- Use of modus ponens
- Negation

RULES

- Rules are statements of the form:

$A :- B_1, B_2, \dots, B_n.$ where $n \geq 0$.

- ❖ Note that a fact is just a special case of a rule when $n = 0$. Facts are also called unit clauses.
- ❖ Example: A rule expressing the son relationship is

$\text{son}(X, Y) :- \text{father}(Y, X), \text{male}(X).$

- ❖ Similarly one can define a rule for the daughter relationship:

$\text{daughter}(X, Y) :- \text{father}(Y, X), \text{female}(X).$

KNOWLEDGE BASE

- A collection of facts and rules is called a knowledge base (KB) (or a database) and Prolog programming is all about writing knowledge bases.

KNOWLEDGE BASE 1

woman(mia).
woman(jody).
woman(yolanda).
playsAirGuitar(jody).
party.

KNOWLEDGE BASE 1

```
woman(mia).  
woman(jody).  
woman(yolanda).  
playsAirGuitar(jody).  
party.
```

```
?- woman(mia).  
yes  
?- playsAirGuitar(jody).
```

KNOWLEDGE BASE 1

```
woman(mia).  
woman(jody).  
woman(yolanda).  
playsAirGuitar(jody).  
party.
```

```
?- woman(mia).  
yes  
?- playsAirGuitar(jody).  
yes  
?-
```

KNOWLEDGE BASE 1

```
woman(mia).  
woman(jody).  
woman(yolanda).  
playsAirGuitar(jody).  
party.
```

```
?- woman(mia).  
yes  
?- playsAirGuitar(jody).  
yes  
?- playsAirGuitar(mia).  
no
```


KNOWLEDGE BASE 1

```
woman(mia).  
woman(jody).  
woman(yolanda).  
playsAirGuitar(jody).  
party.
```

```
?- tattooed(jody).
```

KNOWLEDGE BASE 1

```
woman(mia).  
woman(jody).  
woman(yolanda).  
playsAirGuitar(jody).  
party.
```

```
?- tattooed(jody).  
no  
?-
```

KNOWLEDGE BASE 1

```
woman(mia).  
woman(jody).  
woman(yolanda).  
playsAirGuitar(jody).  
party.
```

```
?- tattooed(jody).  
ERROR: predicate tattooed/1 not defined.  
?-
```

KNOWLEDGE BASE 1

```
woman(mia).  
woman(jody).  
woman(yolanda).  
playsAirGuitar(jody).  
party.
```

```
?- party.
```

KNOWLEDGE BASE 1

```
woman(mia).  
woman(jody).  
woman(yolanda).  
playsAirGuitar(jody).  
party.
```

```
?- party.  
yes  
?-
```

KNOWLEDGE BASE 1

```
woman(mia).  
woman(jody).  
woman(yolanda).  
playsAirGuitar(jody).  
party.
```

```
?- rockConcert.
```

KNOWLEDGE BASE 1

```
woman(mia).  
woman(jody).  
woman(yolanda).  
playsAirGuitar(jody).  
party.
```

```
?- rockConcert.  
no  
?-
```

KNOWLEDGE BASE 2

```
happy(yolanda).  
listens2music(mia).  
listens2music(yolanda):- happy(yolanda).  
playsAirGuitar(mia):- listens2music(mia).  
playsAirGuitar(yolanda):- listens2music(yolanda).
```


KNOWLEDGE BASE 2

fact

happy(yolanda).

listens2music(mia).

listens2music(yolanda):- happy(yolanda).

playsAirGuitar(mia):- listens2music(mia).

playsAirGuitar(yolanda):- listens2music(yolanda).

KNOWLEDGE BASE 2

happy(yolanda).

fact

listens2music(mia).

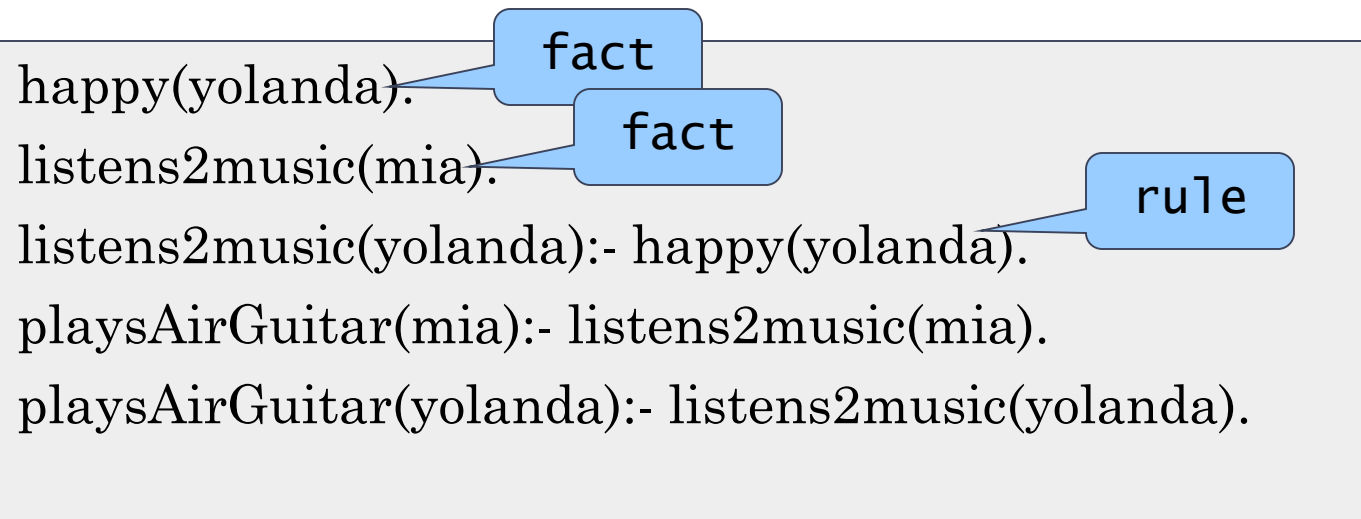
fact

listens2music(yolanda):- happy(yolanda).

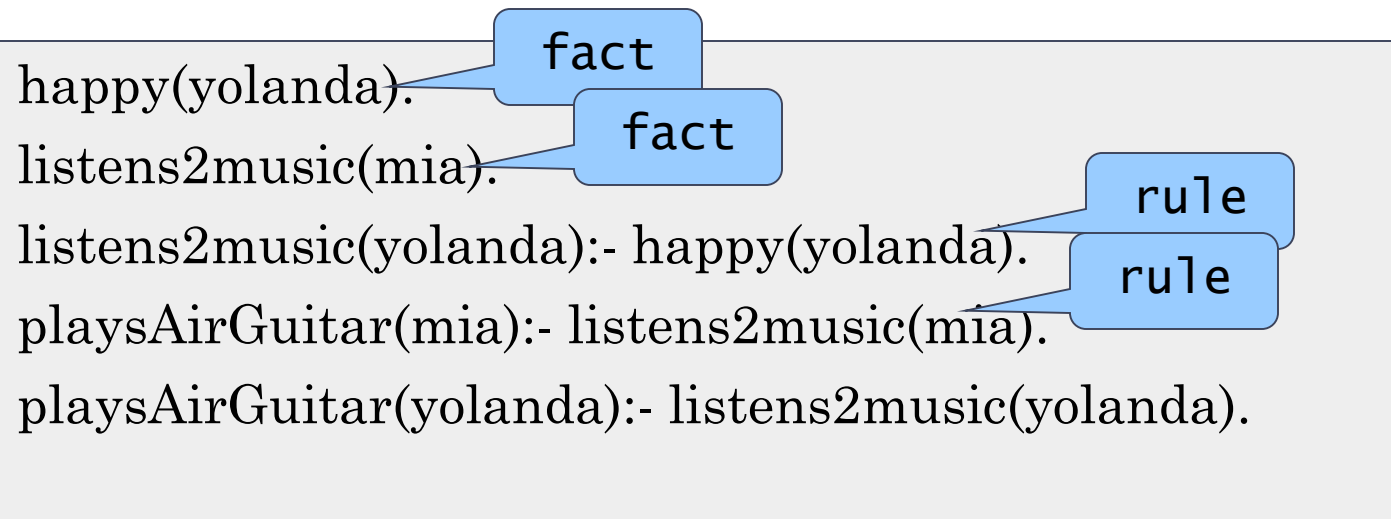
playsAirGuitar(mia):- listens2music(mia).

playsAirGuitar(yolanda):- listens2music(yolanda).

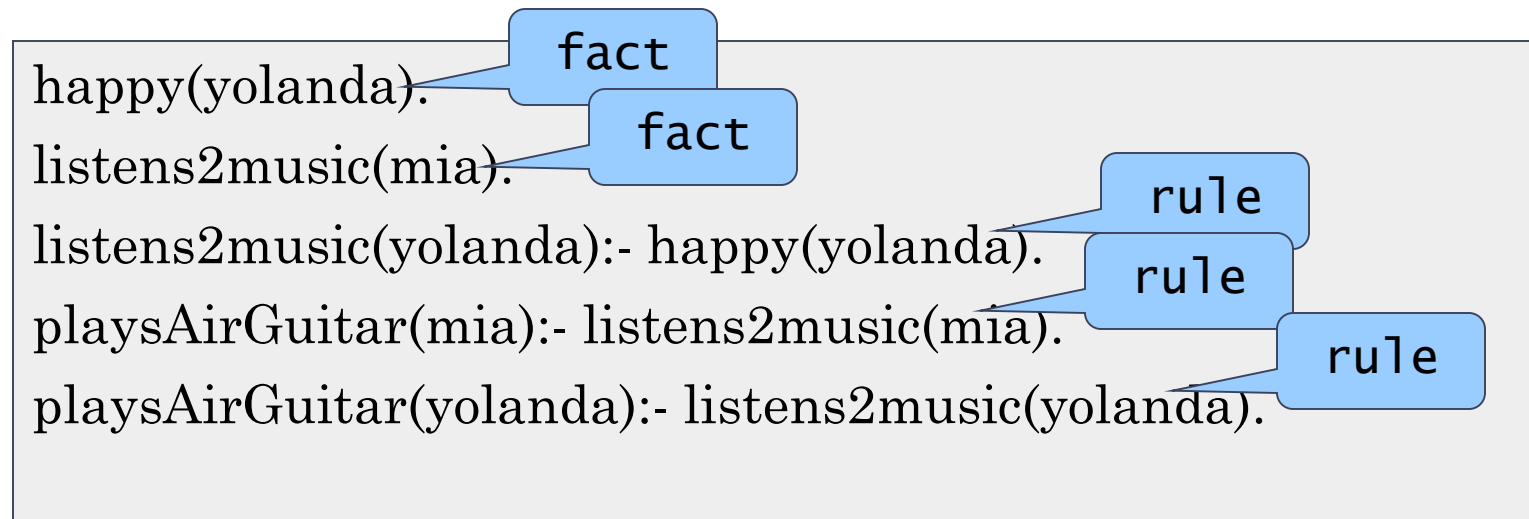
KNOWLEDGE BASE 2



KNOWLEDGE BASE 2



KNOWLEDGE BASE 2



KNOWLEDGE BASE 2

```
happy(yolanda).  
listens2music(mia).  
listens2music(yolanda):- happy(yolanda).  
playsAirGuitar(mia):- listens2music(mia).  
playsAirGuitar(yolanda):- listens2music(yolanda).
```

head

body

KNOWLEDGE BASE 2

```
happy(yolanda).  
listens2music(mia).  
listens2music(yolanda):- happy(yolanda).  
playsAirGuitar(mia):- listens2music(mia).  
playsAirGuitar(yolanda):- listens2music(yolanda).
```

?-

KNOWLEDGE BASE 2

```
happy(yolanda).  
listens2music(mia).  
listens2music(yolanda):- happy(yolanda).  
playsAirGuitar(mia):- listens2music(mia).  
playsAirGuitar(yolanda):- listens2music(yolanda).
```

```
?- playsAirGuitar(mia).  
yes  
?-
```


KNOWLEDGE BASE 2

```
happy(yolanda).  
listens2music(mia).  
listens2music(yolanda):- happy(yolanda).  
playsAirGuitar(mia):- listens2music(mia).  
playsAirGuitar(yolanda):- listens2music(yolanda).
```

```
?- playsAirGuitar(mia).  
yes  
?- playsAirGuitar(yolanda).  
yes
```

CLAUSES

```
happy(yolanda).  
listens2music(mia).  
listens2music(yolanda):- happy(yolanda).  
playsAirGuitar(mia):- listens2music(mia).  
playsAirGuitar(yolanda):- listens2music(yolanda).
```

*There are five clauses in this knowledge base:
two facts, and three rules.*

The end of a clause is marked with a full stop.

PREDICATES

```
happy(yolanda).  
listens2music(mia).  
listens2music(yolanda):- happy(yolanda).  
playsAirGuitar(mia):- listens2music(mia).  
playsAirGuitar(yolanda):- listens2music(yolanda).
```

*There are three **predicates**
in this knowledge base:
happy, listens2music, and playsAirGuitar*

KNOWLEDGE BASE 3

happy(vincent).

listens2music(butch).

playsAirGuitar(vincent):- listens2music(vincent),
happy(vincent).

playsAirGuitar(butch):- happy(butch).

playsAirGuitar(butch):- listens2music(butch).

EXPRESSING CONJUNCTION

```
happy(vincent).  
listens2music(butch).  
playsAirGuitar(vincent):- listens2music(vincent), happy(vincent).  
playsAirGuitar(butch):- happy(butch).  
playsAirGuitar(butch):- listens2music(butch).
```

The comma "," expresses conjunction in Prolog

KNOWLEDGE BASE 3

```
happy(vincent).  
listens2music(butch).  
playsAirGuitar(vincent):- listens2music(vincent), happy(vincent).  
playsAirGuitar(butch):- happy(butch).  
playsAirGuitar(butch):- listens2music(butch).
```

```
?- playsAirGuitar(vincent).  
no  
?-
```

KNOWLEDGE BASE 3

```
happy(vincent).  
listens2music(butch).  
playsAirGuitar(vincent):- listens2music(vincent), happy(vincent).  
playsAirGuitar(butch):- happy(butch).  
playsAirGuitar(butch):- listens2music(butch).
```

```
?- playsAirGuitar(butch).  
yes  
?-
```

EXPRESSING DISJUNCTION

```
happy(vincent).  
listens2music(butch).  
playsAirGuitar(vincent):- listens2music(vincent), happy(vincent).  
playsAirGuitar(butch):- happy(butch).  
playsAirGuitar(butch):- listens2music(butch).
```

```
happy(vincent).  
listens2music(butch).  
playsAirGuitar(vincent):- listens2music(vincent), happy(vincent).  
playsAirGuitar(butch):- happy(butch); listens2music(butch).
```


KNOWLEDGE BASE 4

```
woman(mia).  
woman(jody).  
woman(yolanda).
```

```
loves(vincent, mia).  
loves(marsellus, mia).  
loves(pumpkin, honey_bunny).  
loves(honey_bunny, pumpkin).
```

PROLOG VARIABLES

```
woman(mia).  
woman(jody).  
woman(yolanda).
```

```
loves(vincent, mia).  
loves(marsellus, mia).  
loves(pumpkin, honey_bunny).  
loves(honey_bunny, pumpkin).
```

```
?- woman(X).
```

VARIABLE INSTANTIATION

```
woman(mia).  
woman(jody).  
woman(yolanda).
```

```
loves(vincent, mia).  
loves(marsellus, mia).  
loves(pumpkin, honey_bunny).  
loves(honey_bunny, pumpkin).
```

```
?- woman(X).  
X=mia
```

ASKING ALTERNATIVES

```
woman(mia).  
woman(jody).  
woman(yolanda).
```

```
loves(vincent, mia).  
loves(marsellus, mia).  
loves(pumpkin, honey_bunny).  
loves(honey_bunny, pumpkin).
```

```
?- woman(X).  
X=mia;
```

ASKING ALTERNATIVES

```
woman(mia).  
woman(jody).  
woman(yolanda).
```

```
loves(vincent, mia).  
loves(marsellus, mia).  
loves(pumpkin, honey_bunny).  
loves(honey_bunny, pumpkin).
```

```
?- woman(X).  
X=mia;  
X=jody
```

ASKING ALTERNATIVES

```
woman(mia).  
woman(jody).  
woman(yolanda).
```

```
loves(vincent, mia).  
loves(marsellus, mia).  
loves(pumpkin, honey_bunny).  
loves(honey_bunny, pumpkin).
```

```
?- woman(X).  
X=mia;  
X=jody;  
X=yolanda
```

ASKING ALTERNATIVES

```
woman(mia).  
woman(jody).  
woman(yolanda).
```

```
loves(vincent, mia).  
loves(marsellus, mia).  
loves(pumpkin, honey_bunny).  
loves(honey_bunny, pumpkin).
```

```
?- woman(X).  
X=mia;  
X=jody;  
X=yolanda;  
no
```

KNOWLEDGE BASE 4

woman(mia).
woman(jody).
woman(yolanda).

loves(vincent, mia).
loves(marsellus, mia).
loves(pumpkin, honey_bunny).
loves(honey_bunny, pumpkin).

?- loves(marsellus,X), woman(X).

KNOWLEDGE BASE 4

woman(mia).
woman(jody).
woman(yolanda).

loves(vincent, mia).
loves(marsellus, mia).
loves(pumpkin, honey_bunny).
loves(honey_bunny, pumpkin).

?- loves(marsellus,X), woman(X).
X=mia
yes
?-

KNOWLEDGE BASE 4

woman(mia).
woman(jody).
woman(yolanda).

loves(vincent, mia).
loves(marsellus, mia).
loves(pumpkin, honey_bunny).
loves(honey_bunny, pumpkin).

?- loves(pumpkin,X), woman(X).

KNOWLEDGE BASE 4

woman(mia).
woman(jody).
woman(yolanda).

loves(vincent, mia).
loves(marsellus, mia).
loves(pumpkin, honey_bunny).
loves(honey_bunny, pumpkin).

?- loves(pumpkin,X), woman(X).
no
?-

KNOWLEDGE BASE 5

```
loves(vincent,mia).  
loves(marsellus,mia).  
loves(pumpkin, honey_bunny).  
loves(honey_bunny, pumpkin).  
  
jealous(X,Y):- loves(X,Z), loves(Y,Z).
```

KNOWLEDGE BASE 5

```
loves(vincent,mia).  
loves(marsellus,mia).  
loves(pumpkin, honey_bunny).  
loves(honey_bunny, pumpkin).  
  
jealous(X,Y):- loves(X,Z), loves(Y,Z).
```

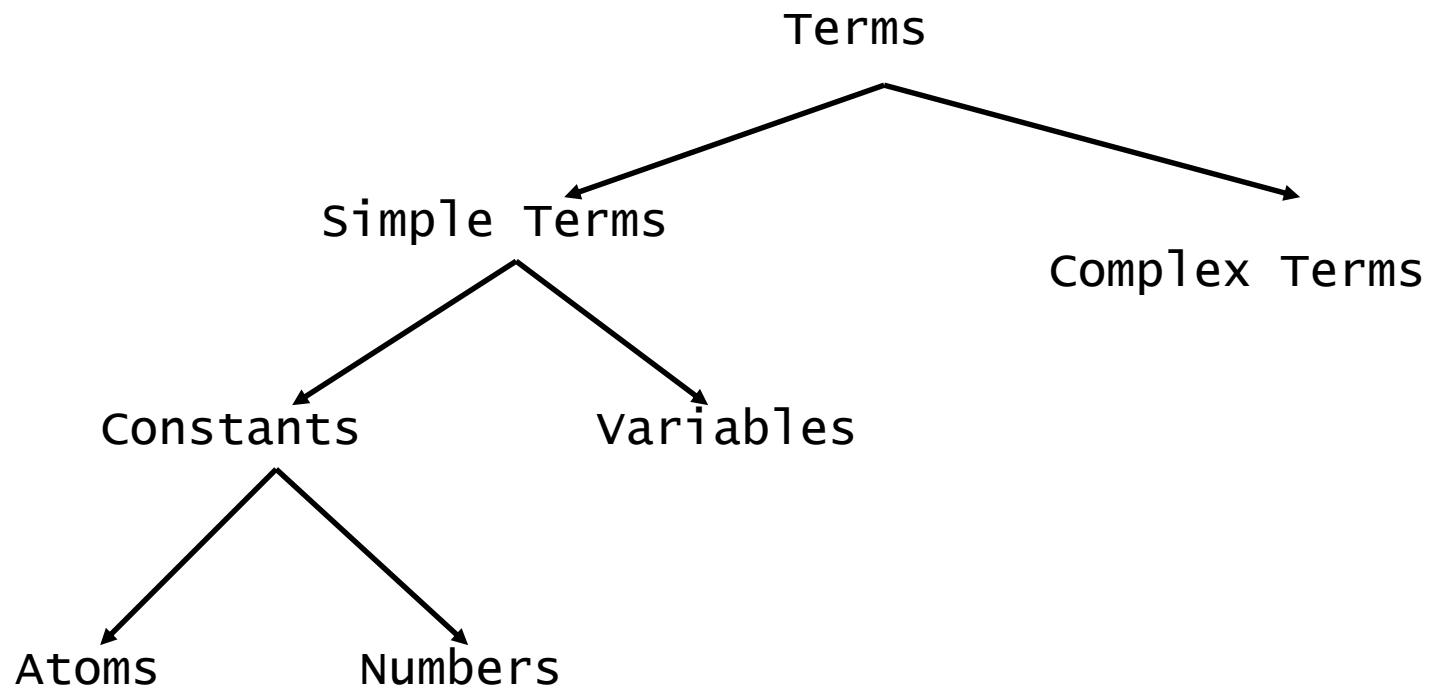
```
?- jealous(marsellus,W).
```

KNOWLEDGE BASE 5

```
loves(vincent,mia).  
loves(marsellus,mia).  
loves(pumpkin, honey_bunny).  
loves(honey_bunny, pumpkin).  
  
jealous(X,Y):- loves(X,Z), loves(Y,Z).
```

```
?- jealous(marsellus,W).  
W=vincent  
?-
```

PROLOG SYNTAX



ARITY

- The number of arguments a complex term has is called its arity
- Examples:

woman(mia) is a term with arity 1
loves(vincent,mia) has arity 2
father(father(butch)) arity 1

ARITY IS IMPORTANT

- In Prolog you can define two predicates with the same functor but with different arity
- Prolog would treat this as two different predicates
- In Prolog documentation arity of a predicate is usually indicated with the suffix "/" followed by a number to indicate the arity

EXAMPLE OF ARITY

happy(yolanda).

listens2music(mia).

listens2music(yolanda):- happy(yolanda).

playsAirGuitar(mia):- listens2music(mia).

playsAirGuitar(yolanda):- listens2music(yolanda).

○ This knowledge base defines

- happy/1
- listens2music/1
- playsAirGuitar/1

OPERATORS AND FUNCTIONS

- Normal Prolog operators are prefix:
 - `@>(Item1, Item2).`
 - `@=<(Item1, Item2).`
 - `==(Item1, Item2).`
 - `\==(Item1, Item2).`
- Some symbols can be used infix: arithmetic and comparison

COMPARISON OPERATORS

Operator	Meaning
\+	Not (negation by failure)
=, \=, =..	Unification, not unifiable, list unification
==, \==	Term identical, term not identical
@<, @=<, @>, @>=	Term less than, term less than or equal to, etc.
is	Unify left-hand side with result of evaluating right hand side.
:=, \=	Arithmetic equal, arithmetic not equal
<, =<, >, >=	Arithmetic less than, etc.
:	
+, -, ^, v	Add, subtract, bitwise AND, bitwise OR
*, /, //	Mult, div, integer division
rem, mod	Different versions of mod (see manual)
>>, <<	Shift right, shift left
**, ^, \	Exponentiation, bitwise XOR, bitwise NOT

ARITHMETIC FUNCTIONS

<code>sqrt(E)</code>	square root of <i>eval(E)</i>
<code>atan(E)</code>	arc tangent of <i>eval(E)</i>
<code>cos(E)</code>	cosine of <i>eval(E)</i>
<code>acos(E)</code>	arc cosine of <i>eval(E)</i>
<code>sin(E)</code>	sine of <i>eval(E)</i>
<code>asin(E)</code>	arc sine of <i>eval(E)</i>
<code>exp(E)</code>	<i>e</i> raised to the power of <i>eval(E)</i>
<code>log(E)</code>	natural logarithms of <i>eval(E)</i>
<code>float(E)</code>	the floating point number equal to <i>eval(E)</i>
<code>ceiling(E)</code>	rounds <i>eval(E)</i> upward to the nearest integer
<code>floor(E)</code>	rounds <i>eval(E)</i> downward to the nearest integer
<code>round(E)</code>	rounds <i>eval(E)</i> to the nearest integer
<code>truncate(E)</code>	the integer value of <i>eval(E)</i>

ARITHMETIC

○ Example.

```
bonus(Number) :- Number is 2 + 3.
```

```
?- bonus(3) .
```

No

```
?- bonus(5) .
```

Yes

```
?- bonus(X) .
```

```
X = 5
```

ARITHMETIC

○ Example.

| ?- X **is** 5 + 2.

X = 7

yes

| ?- X **=** 5 + 2.

X = 5+2

yes

| ?- X **is** 5.3 + 7.

X = 12.3

yes

| ?-

= and **is** have different meanings

= means term assignment
is means arithmetic assignment

ARITHMETIC

○ Example: geography.pl

```
/*  
    north latitudes and west longitudes are positive.  
    south latitudes and east longitudes are negative.  
*/  
location(tokyo, 35, -139).  
location(rome, 41, -12).  
location(london, 51, 0).  
location(canberra, -31, -149).  
location(madrid, 48, 3).  
north_of(X, Y) :-  
    location(X, Lat1, _),  
    location(Y, Lat2, _),  
    Lat1 > Lat2.  
west_of(X, Y) :-  
    location(X, _, Long1),  
    location(Y, _, Long2),  
    Long1 > Long2.
```

Try:
 north_of(madrid, tokyo).

west_of(X, tokyo).
west_of(london, X).

TRACING

○ The prolog command is `trace`

```
|?-trace.
```

```
yes
```

```
[trace] 1 ?- north_of(madrid,tokyo).
```

```
    Call: (7) north_of(madrid, tokyo) ? creep
```

```
    Call: (8) location(madrid, _G2207, _G2208) ? creep
```

```
    Exit: (8) location(madrid, 48, 3) ? creep
```

```
    Call: (8) location(tokyo, _G2207, _G2208) ? creep
```

```
    Exit: (8) location(tokyo, 35, -139) ? creep
```

```
    Call: (8) 48>35 ? creep
```

```
    Exit: (8) 48>35 ? creep
```

```
    Exit: (7) north_of(madrid, tokyo) ? creep
```

```
true.
```

For more: visit:

<http://www.cse.unsw.edu.au/~billw/dictionaries/prolog/tracing.html>

TRACING

The command to turn off is `notrace`

```
|?-notrace.
```

The debugger is switched off

Yes

```
|?-
```

MAKING DECISIONS

- There are no *if* or *case* statements in prolog.
- How do we make decisions?
- Example: determine how hot it is:

```
// determine how hot it is
void howHot(string &HowHot, int Temp){
    if (Temp >= 100)
        HowHot = "very";
    else if (Temp >= 90)
        HowHot = "pretty";
    else if (Temp >= 70)
        HowHot = "perfect";
    else if (Temp < 70)
        HowHot = "cold";
}
```

MAKING DECISIONS

○ Making decisions (howHot.pl)

```
% determine how hot it is
```

```
Hot(HowHot, Temp) :-
```

```
    Temp >= 100,
```

```
    HowHot = 'very';
```

```
    Temp < 100,
```

```
    Temp >= 90,
```

```
    HowHot = 'pretty';
```

```
    Temp < 90,
```

```
    Temp >= 70,
```

```
    HowHot = 'perfect';
```

```
    Temp < 70,
```

```
    HowHot = 'cold'.
```

Can ask

`howHot(X, 80).`

But *not*

`howHot(very, X).`

Cannot use *is* must use =
is only works on arithmetic
expressions

Must have this test because prolog
will view each *or* clause
independently. If we left out `Temp < 100` then a temp of 110 would return both “very” and “pretty”

Thanks

?