



Due Date: -----

HW 1

### Path loss, Shadowing, Link budget, and Coverage

1. In a wireless communication system working at  $f_c = 1\text{GHz}$ , the transmitted power is  $0\text{ dBm}$ . The path-loss follows the simplified model of  $P_L(\text{dB}) = 10 + 40 \log_{10}(d)$ , where  $d$  is the distance in meter. We also have a Log-Normal shadowing with a standard deviation of  $6\text{ dB}$ . The acceptable RX power is  $P_{r_{\min}} = -90\text{ dBm}$  (outage =  $P_r < P_{r_{\min}}$ ).
  - a. Determine the outage probability ( $P_{\text{out}}$ ) for users with a distance of  $d$  from the transmitter. Find the distance where  $P_{\text{out}}$  becomes 50% ?
  - b. Determine the total expected coverage area? Find the expected coverage radius.
  - c. Find the needed transmitted power such that the outage probability for a user located at a distance of  $100\text{m}$  becomes  $P_{\text{out}}$ . Sketch  $P_{\text{out}}$  (from 0% up to 100%) vs. needed TX power (in  $\text{dBm}$ ).
2. In Fig.1, the node RX receives signal form transmitter  $\text{TX}_1$  and also receives interference from  $\text{TX}_2$ . The path loss and shadowing between  $i^{\text{th}}$  transmitter and receiver are modeled as:

$$PL_i = K + 10n \log_{10}\left(\frac{d_i}{d_0}\right) + X_i (\text{dB}) , i = 1,2$$

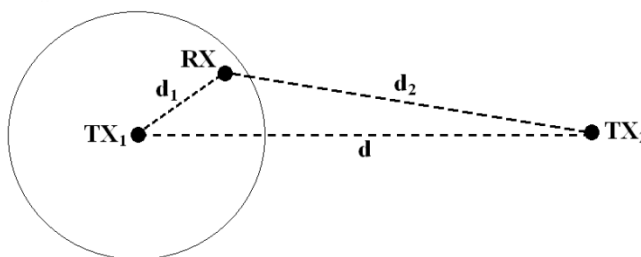


Fig.1

Where  $d_i$  is the distance between the receiver and transmitter  $i$  in meters, and  $n$  is the path loss exponent, the terms  $X_i$  are zero-mean Gaussian random variables with standard deviation  $\sigma$ , in  $\text{dB}$ , that model the variation of the received signals due to shadowing. Assume that the random variables  $X_i$  are independent of each other and also suppose that  $P_0$  is the received power at distance  $d_0$  from each of transmitters.  $\text{SINR}_{\min}$  is the minimum required SINR at receiver for non-outage.

- a. Using the parameters in Table.2, find the maximum radius  $R$  from  $\text{TX}_1$ , that if the receiver is in that circle, then the outage probability at each point be less than 0.05.
- b. Suppose that  $n$  is parameter, find the maximum radius  $R$  as a function of  $n$ , and plot  $R$  versus  $n$  and explain the behavior of  $R$ .

- c. Suppose that there is an additive white Gaussian noise at RX with  $N_0 = 10^{-12}$ , find the maximum radius R, for  $n=4$  and also plot R versus n and compare the results with part b.

Table 1

Parameter	Value
n	4
$\sigma$	5 dB
$P_0$	0 dBW
$d_0$	1 m
d	1000 m
$SINR_{min}$	10 dB

3. Consider a cellular system operating at 900 MHz where propagation follows free space path loss with variations from log normal shadowing with  $\sigma = 6$  dB. Suppose that for acceptable voice quality a signal-to-noise power ratio of 15 dB is required at the mobile. Assume the base station transmits at 1 W and its antenna has a 3 dB gain. There is no antenna gain at the mobile and the receiver noise in the bandwidth of interest is -10 dBm. Find the maximum cell size so that a mobile on the cell boundary will have acceptable voice quality 90% of the time.
4. Consider a random propagation environment. The received signal power  $P_r$  at a distance  $d(> d_0)$  is:

$$P_r^{(dBm)} = P_0^{(dBm)} - 10 \gamma \log_{10} \left( \frac{d}{d_0} \right) + X^{(dB)}$$

where  $P_0 = 0$  dBm is the received power, a reference distance  $d_0 = 1$  m,  $\gamma = 3$  is the path loss exponent,  $X(dB)$  is a discrete random variable distributed with

$$P_{X^{(dB)}}(x^{(dB)}) = \begin{cases} 0.2 & x^{(dB)} = 0 \text{ dB} \\ 0.2 & x^{(dB)} = -2 \text{ dB} \\ 0.2 & x^{(dB)} = -1 \text{ dB} \\ 0.2 & x^{(dB)} = 1 \text{ dB} \\ 0.2 & x^{(dB)} = 2 \text{ dB} \\ 0 & \text{otherwise} \end{cases}$$

Find the maximum radius of this basestation such that the power signal received (from basestation) is larger than -90dBm with a probability of 0.8.

5. Use MATLAB to plot each part of the following question:

Consider a base-station (BS) and a lot of mobile devices randomly are located around the BS with uniform distribution in a circular ring whose distance from BS starts from  $d_0 = 10 \text{ meter}$  and is limited to  $D = 1000 \text{ meter}$ .

The path-loss follows a simplified model with a path-loss exponent of  $n = 4$ . The transmitted power is such that the average received signal power at  $d = d_0$  is  $P_0 = 1 \mu W$ . The PSD of the AWGN at the receiver is  $N_0 = -174 \frac{\text{dBm}}{\text{Hz}}$  and the signal bandwidth is  $1 \text{ MHz}$ .

a. The average received signal power at distance  $d$  ( $d > d_0$ ) is obtained by the following equation:

$$P_r^{dBm} = P_0^{dBm} - 10n \log_{10} \left( \frac{d}{d_0} \right)$$

Simulate the  $P_r^{dBm}$  of the users and plot its CDF (cumulative distribution function). (you can use cdfplot in Matlab).

b. Plot expected  $SNR \text{ (dB)} = P_r^{dBm} - P_n^{dBm}$  as a function of distance ( $\log_{10} d$ ) for  $10 \leq d \leq 1000$ .

c. Now assume that we have Log-normal shadowing as well. The average received signal power at distance  $d$  ( $d > d_0$ ) is obtained by the following equation:

$$P_r^{dBm} = P_0^{dBm} - 10n \log_{10} \left( \frac{d}{d_0} \right) + X^{dB}$$

where  $X$  is a zero-mean Gaussian random variables with standard deviation  $\sigma = 5 \text{ dB}$  (independent of  $d$ ). Plot the CDF of  $P_r^{dBm}$  and  $SNR \text{ (dB)} = P_r^{dBm} - P_n^{dBm}$  for all users in the ring.

d. Plot  $P_{out} = \Pr(SNR < SNR_{min})$  as a function of distance ( $\log_{10} d$ ) for  $10 \leq d \leq 1000$ .

$SNR_{min} = 20 \text{ dB}$  is the minimum required SNR at receiver for non-outage.

e. How much area of the ring is covered if we need  $SNR_{min} = 20 \text{ dB}$  for coverage. Compare it with formula in Goldsmith.

Note: For uniformly distributed users in a ring, simulate some  $10^5$  users randomly located at (dx,dy), where dx and dy are independent random coordinates with uniform distribution in  $[-1000, 1000]$ . Then select the users that are located in the intended circular ring and remove the remaining users from your user set.