

SLR: Single Ind. feature  
MLR: Multiple Ind. features  
AOE: Quadratic Prop.

Polynomial Regression

SLR:  $\hat{y} = \beta_0 + \beta_1 x_1$   
MLR:  $\hat{y} = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \beta_3 x_3 + \beta_4 x_4$   
 $\beta_0, \beta_1, \beta_2, \beta_3, \beta_4$

Gradient Descent:

$$\beta_1 = \beta_1 - \alpha \frac{\partial J}{\partial \beta_1}$$

$$\beta_2 = \beta_2 - \alpha \frac{\partial J}{\partial \beta_2}$$

$$\beta_3 = \beta_3 - \alpha \frac{\partial J}{\partial \beta_3}$$

$$\vdots$$

$$\beta_0 = \beta_0 - \alpha \frac{\partial J}{\partial \beta_0}$$

Polynomial Regression

$$\hat{y} = \beta_0 + \beta_1 x_1 + \beta_2 x_1^2 + \beta_3 x_1^3 + \beta_4 x_1^4$$

$$x_1^2 = x_2$$

$$x_1^3 = x_3$$

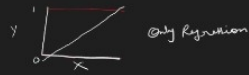
$$x_1^4 = x_4$$

$$= \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \beta_3 x_3 + \beta_4 x_4$$

Multiple Prediction (C, O)

$$\hat{y} = \beta_0 + \beta_1 P_1 P_2 P^2 + \beta_3 O + \beta_5 O^2$$

## LOGISTIC REGRESSION

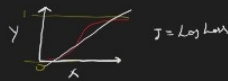


$$\text{Sigmoid}(x) = \frac{1}{1 + e^{-x}}$$

$$= \frac{1}{1 + e^{-x}}$$

$$\hat{y} = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \beta_3 x_3 + \beta_4 x_4$$

$$= \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \beta_3 x_3 + \beta_4 x_4$$



Threshold: 0.5  $CF > 0.5 = 1$   
 $CF < 0.5 = 0$

Case I - form 0.25  $CF > 0.25 = 1$   
 $CF < 0.25 = 0$

Effectiveness of V. using:

0.8  $CF > 0.8 = 1$   
 $CF < 0.8 = 0$

Multiclass Classification:

0.3 = I class  
0.3 = 0.4 = II class  
0.6 = 0.5 = III class

0.2  
0.7  
0.1

1/3  
2/3  
3/3

2  
0.3  
0.3  
0.4

1  
2  
3