

# Thinking & Coding Algorithms

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Recommended Reading

# Disclaimer #1

Lab, Not Lecture



# Disclaimer #2



Using JS





# TL;DW

1. Ask better clarifying questions
2. Balance CPU vs Memory
3. Shape data structure(s) to the problem, not the other way
4. “premature optimization” vs. “immature optimization”



# Quick DSA Primer



# Common Data Structures

Array, Stack, Queue

Set, Object, Map

Tree, Graph

# Common Algorithms

BubbleSort, QuickSort

Tree Traversal, Path Finding

Binary Search

# Common Techniques

Iteration

Recursion

Indexes, References



# Iteration



4



# Recursion



3



# Fuzzy?




2




# Warm-ups

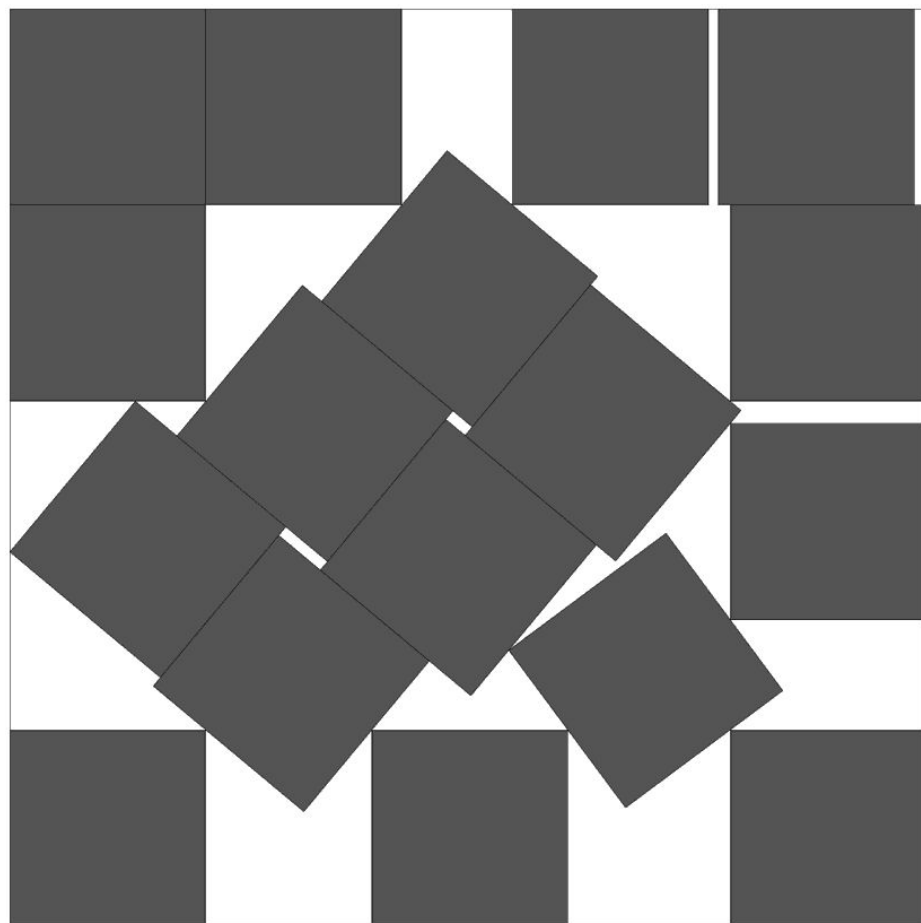


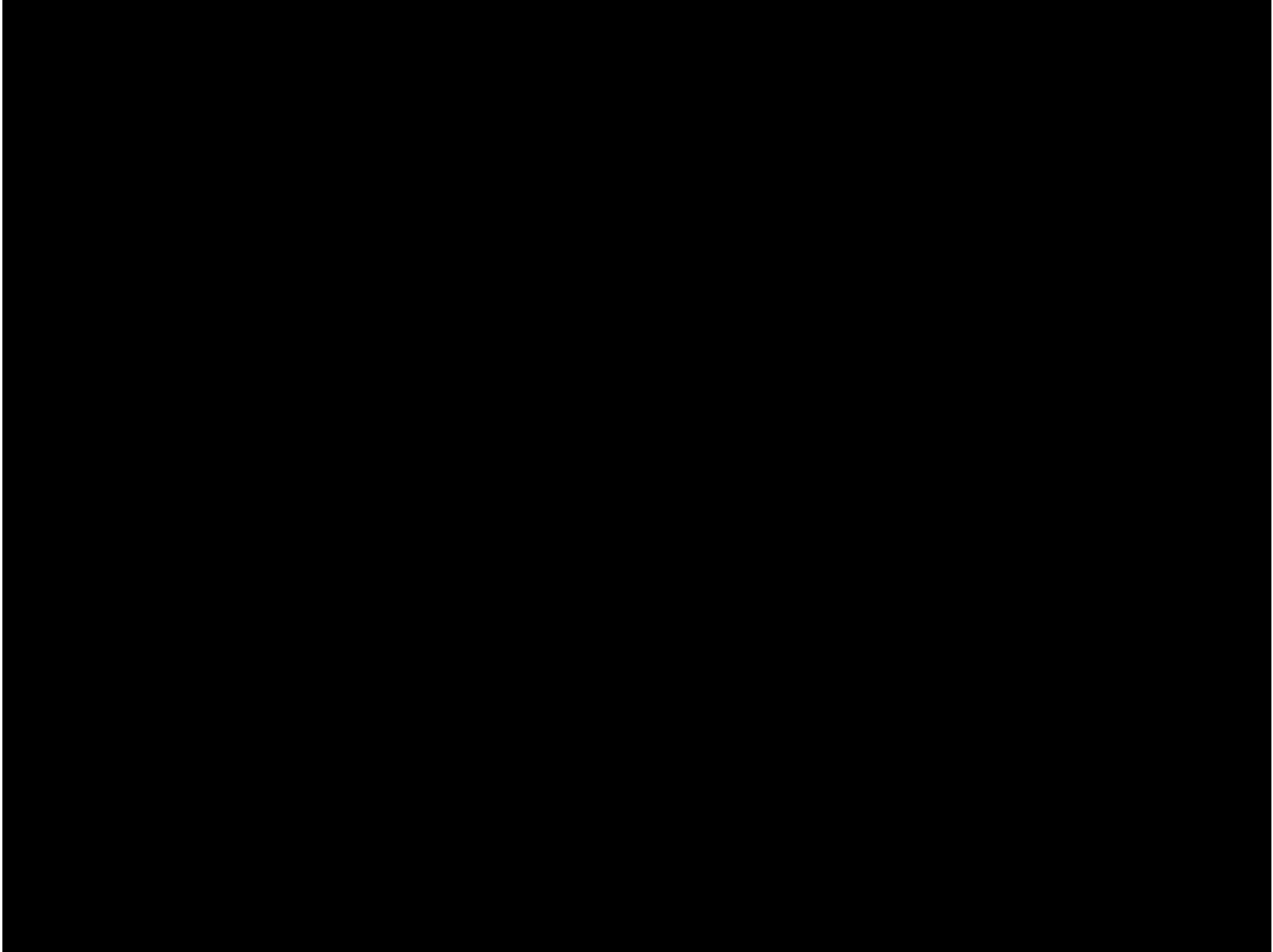
 `binary-to-decimal.js`

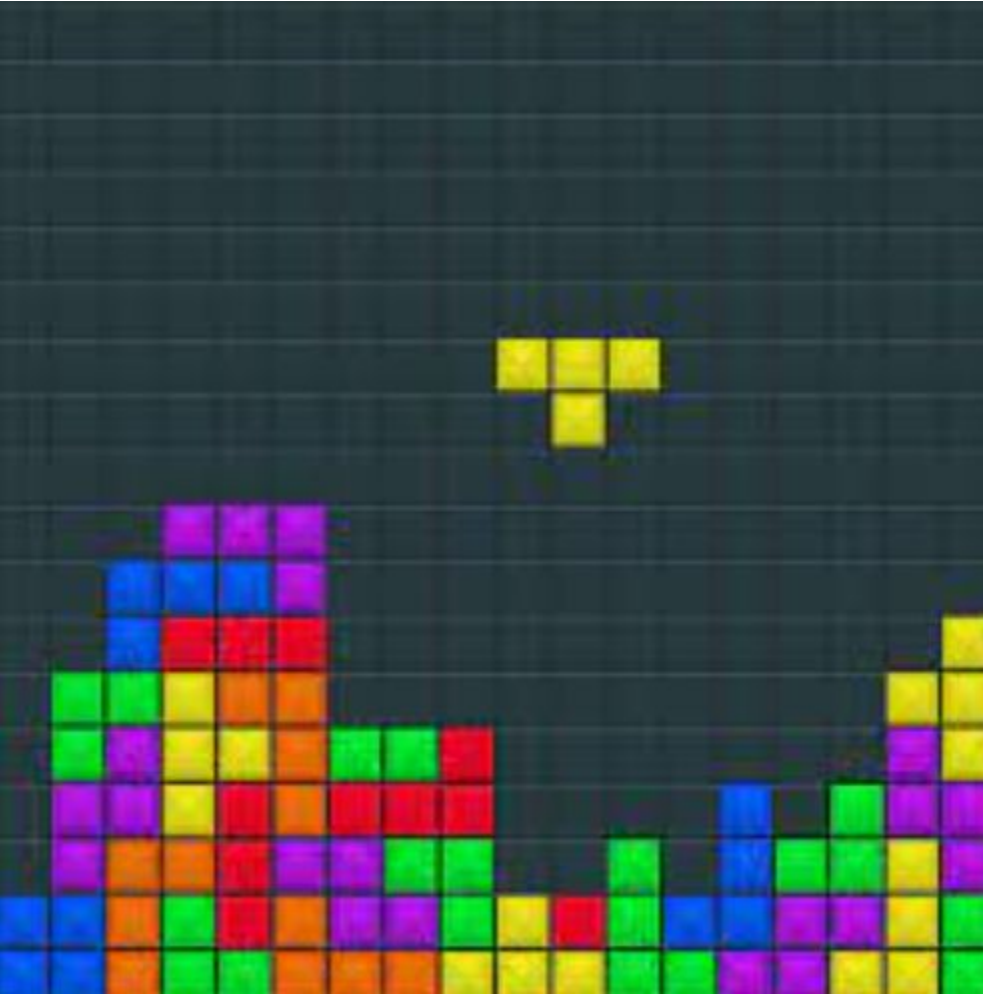
```
1  function binaryToDecimalConverter(binaryNumber) {
2    var decimal = 0n;
3    for (let [idx,digit] of Object.entries(binaryNumber)) {
4      let power = binaryNumber.length - idx - 1;
5      decimal += BigInt(digit) * (2n ** BigInt(power));
6    }
7    return decimal;
8  }
9
10 binaryToDecimalConverter("111110011101100"); // 31980n
```

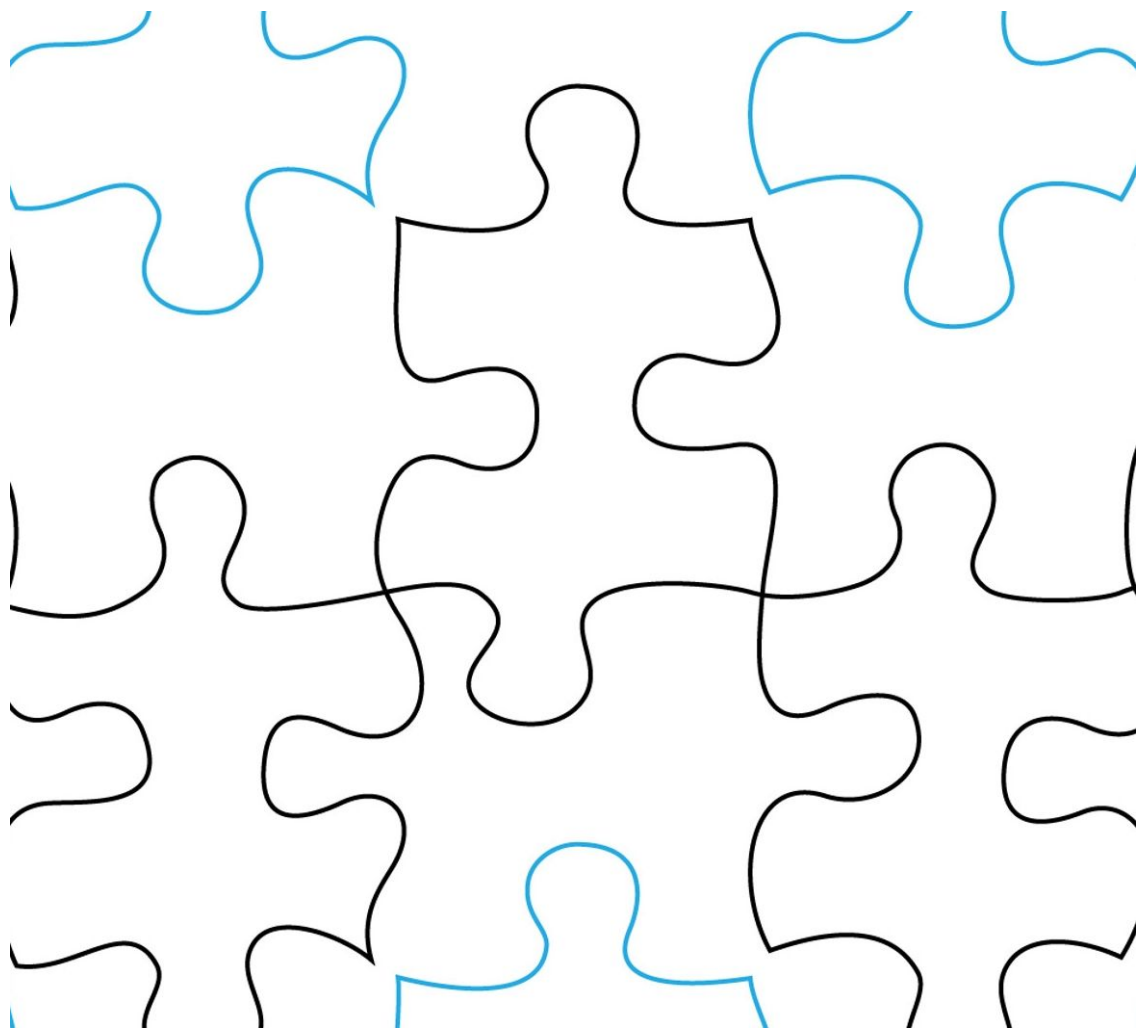
 `decimal-to-binary.js`

```
1  function decimalToBinaryConverter(base10number) {
2    var binary = "";
3    var next = base10number;
4    while (next > 0n) {
5      let remainder = next % 2n;
6      binary = remainder + binary;
7      next = next / 2n;
8    }
9    return binary;
10 }
11
12 decimalToBinaryConverter(31980n); // 111110011101100
```











2-BFS.js

```
1 // iterative breadth-first solution
2
3 function findMaxRegionArea(matr) {
4     const ROW_LEN = matr[0].length;
5     var area = 0;
6     var maxArea = 0;
7     var visited = new Set();
8
9     for (let [ rowIdx, row ] of matr.entries()) {
10         for (let [ colIdx, cell ] of row.entries()) {
11             if (
12                 !visited.has((rowIdx * ROW_LEN) + colIdx) &&
13                 cell == 1
14             ) {
15                 // initialize a breadth-first queue
16                 let toVisit = [ rowIdx, colIdx ];
17
18                 while (toVisit.length > 0) {
19                     // pull to-visit cell coordinates off the queue
20                     let [ visitedRowIdx, visitedColIdx ] = toVisit.shift();
21
22                     // compute the cell-index
23                     let visitedCellIdx = (visitedRowIdx * ROW_LEN) + visitedColIdx;
24
25                     // have we not visited this cell yet?
26                     if (!visited.has(visitedCellIdx)) {
27                         visited.add(visitedCellIdx);
28                         area++;
29
30                         // inspect current row and two (possibly) adjacent rows
31                         for (let rowDelta of [ -1, 0, 1 ]) {
32                             // inspect current column and two (possibly) adjacent columns
33                             for (let colDelta of [ -1, 0, 1 ]) {
34                                 // avoid re-considering the current cell
35                                 if (!(rowDelta == 0 && colDelta == 0)) {
36                                     let toVisitRowIdx = (visitedRowIdx + rowDelta);
37                                     let toVisitColIdx = (visitedColIdx + colDelta);
38
39                                     // is the cell actually in bounds of the matrix,
40                                     // and is has a '1' in it, and is not already
41                                     // a cell we've visited/counted?
```

<https://gist.github.com/getify/59ab7443723564eb40d20ab7c45d5f0a>

# Exercise: Periodic Table Speller

<https://github.com/getify/workshop-periodic-table>



# PERIODIC TABLE OF ELEMENTS

1 IA																	18 VIII A
1 H Hydrogen 1.00794	2 II A											13 III A	14 IV A	15 V A	16 VI A	17 VII A	2 He Helium 4.002602
3 Li Lithium 6.941	4 Be Beryllium 9.012182											5 B Boron 10.811	6 C Carbon 12.0107	7 N Nitrogen 14.0067	8 O Oxygen 15.9994	9 F Fluorine 18.9984032	10 Ne Neon 20.1797
11 Na Sodium 22.98976928	12 Mg Magnesium 24.305	3 III B	4 IV B	5 V B	6 VI B	7 VII B	8 VIII B	9 VIII B	10 VIII B	11 I B	12 II B	13 Al Aluminum 26.9815386	14 Si Silicon 28.0855	15 P Phosphorus 30.973762	16 S Sulfur 32.065	17 Cl Chlorine 35.453	18 Ar Argon 39.948
19 K Potassium 39.0983	20 Ca Calcium 40.078	21 Sc Scandium 44.9559	22 Ti Titanium 47.867	23 V Vanadium 50.9415	24 Cr Chromium 51.9961	25 Mn Manganese 54.938045	26 Fe Iron 55.845	27 Co Cobalt 58.933195	28 Ni Nickel 58.6934	29 Cu Copper 63.546	30 Zn Zinc 65.38	31 Ga Gallium 69.723	32 Ge Germanium 72.64	33 As Arsenic 74.9216	34 Se Selenium 78.96	35 Br Bromine 79.904	36 Kr Krypton 83.798
37 Rb Rubidium 85.4678	38 Sr Strontium 87.62	39 Y Yttrium 88.9055	40 Zr Zirconium 91.224	41 Nb Niobium 92.9063	42 Mo Molybdenum 95.96	43 Tc Technetium [98]	44 Ru Ruthenium 101.07	45 Rh Rhodium 102.9055	46 Pd Palladium 106.42	47 Ag Silver 107.8682	48 Cd Cadmium 112.411	49 In Indium 114.818	50 Sn Tin 118.71	51 Sb Antimony 121.76	52 Te Tellurium 127.6	53 I Iodine 126.90447	54 Xe Xenon 131.293
55 Cs Cesium 132.9054519	56 Ba Barium 137.327	57-71 Lanthanoids	72 Hf Hafnium 178.49	73 Ta Tantalum 180.94788	74 W Tungsten 183.84	75 Re Rhenium 186.207	76 Os Osmium 190.23	77 Ir Iridium 192.217	78 Pt Platinum 195.084	79 Au Gold 196.966569	80 Hg Mercury 200.59	81 Tl Thallium 204.3833	82 Pb Lead 207.2	83 Bi Bismuth 208.9804	84 Po Polonium [209]	85 At Astatine [210]	86 Rn Radon [222]
87 Fr Francium [223]	88 Ra Radium [226]	89-103 Actinoids	104 Rf Rutherfordium [261]	105 Db Dubnium [268]	106 Sg Seaborgium [271]	107 Bh Bohrium [272]	108 Hs Hassium [270]	109 Mt Meitnerium [276]	110 Ds Darmstadtium [281]	111 Rg Roentgenium [280]	112 Cn Copernicium [285]	113 Nh Nihonium [286]	114 Fl Flerovium [289]	115 Mc Moscovium [288]	116 Lv Livermorium [293]	117 Ts Tennessine [294]	118 Og Oganesson [294]
<div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div>																	
57 La Lanthanum 138.90547	58 Ce Cerium 140.116	59 Pr Praseodymium 140.90765	60 Nd Neodymium 144.242	61 Pm Promethium [145]	62 Sm Samarium 150.36	63 Eu Europium 151.964	64 Gd Gadolinium 157.25	65 Tb Terbium 158.9253	66 Dy Dysprosium 162.5	67 Ho Holmium 164.93032	68 Er Erbium 167.259	69 Tm Thulium 168.93421	70 Yb Ytterbium 173.054	71 Lu Lutetium 174.9668			
89 Ac Actinium [227]	90 Th Thorium 232.03806	91 Pa Protactinium 231.03688	92 U Uranium 238.02891	93 Np Neptunium [237]	94 Pu Plutonium [244]	95 Am Americium [243]	96 Cm Curium [247]	97 Bk Berkelium [247]	98 Cf Californium [251]	99 Es Einsteinium [252]	100 Fm Fermium [257]	101 Md Mendelevium [258]	102 No Nobelium [262]	103 Lr Lawrencium [262]			

Word:

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4 <b>Be</b> Beryllium	20 <b>Ca</b> Calcium	92 <b>U</b> Uranium	34 <b>Se</b> Selenium
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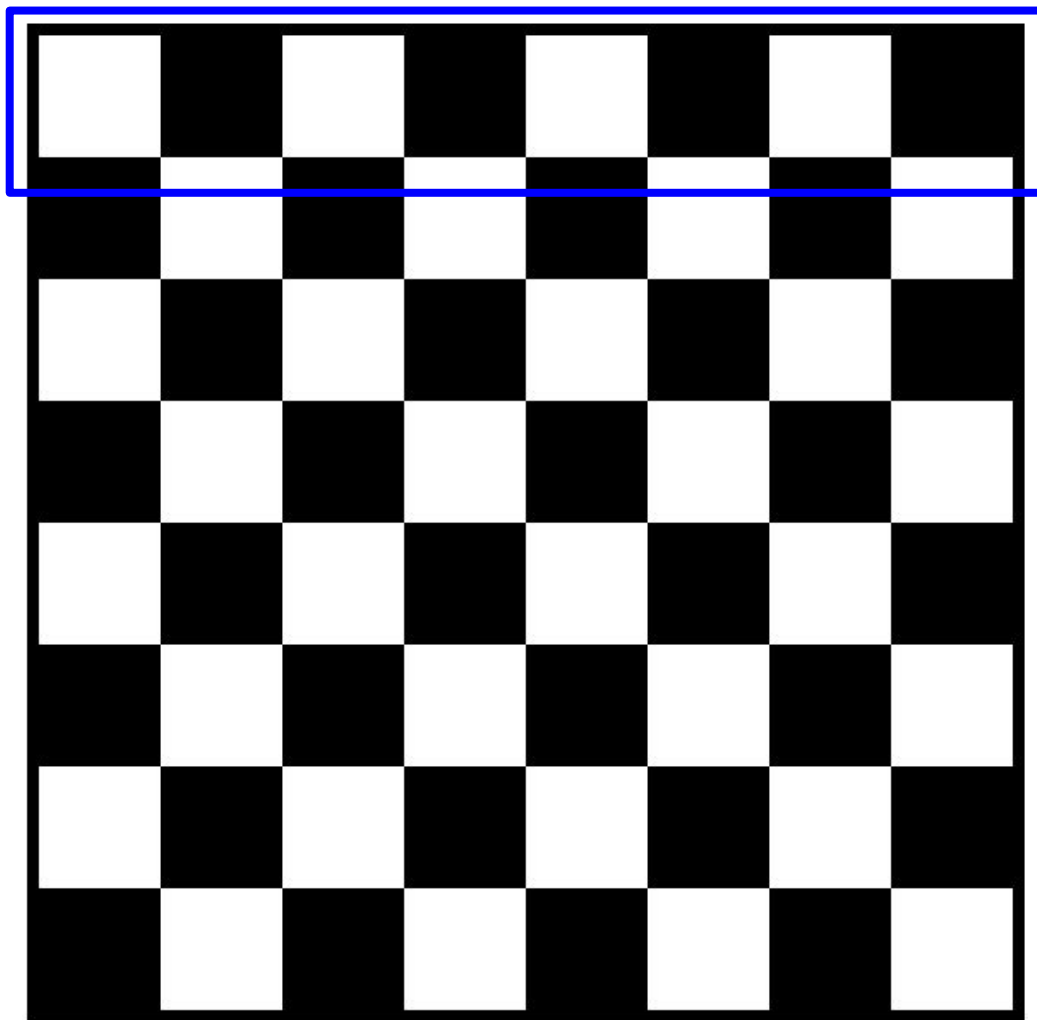
Periodic Table Speller

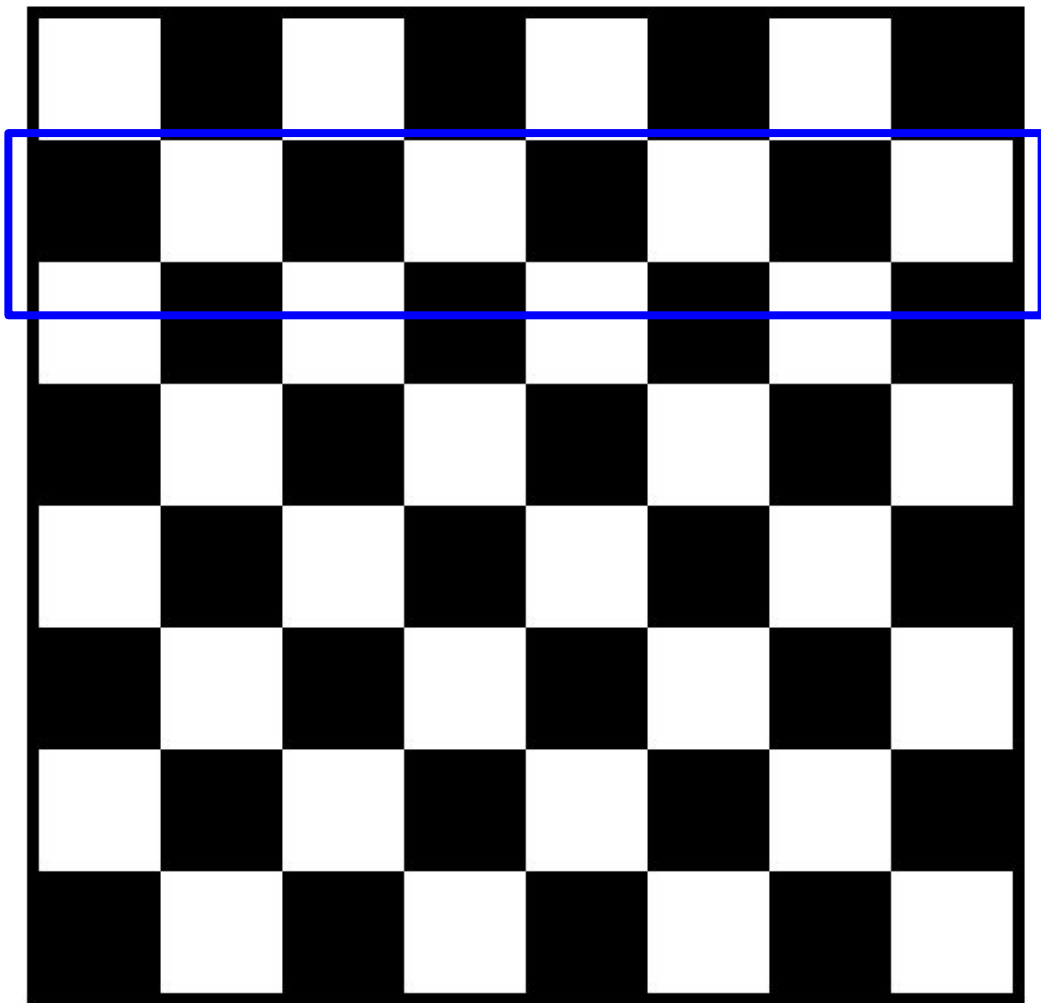


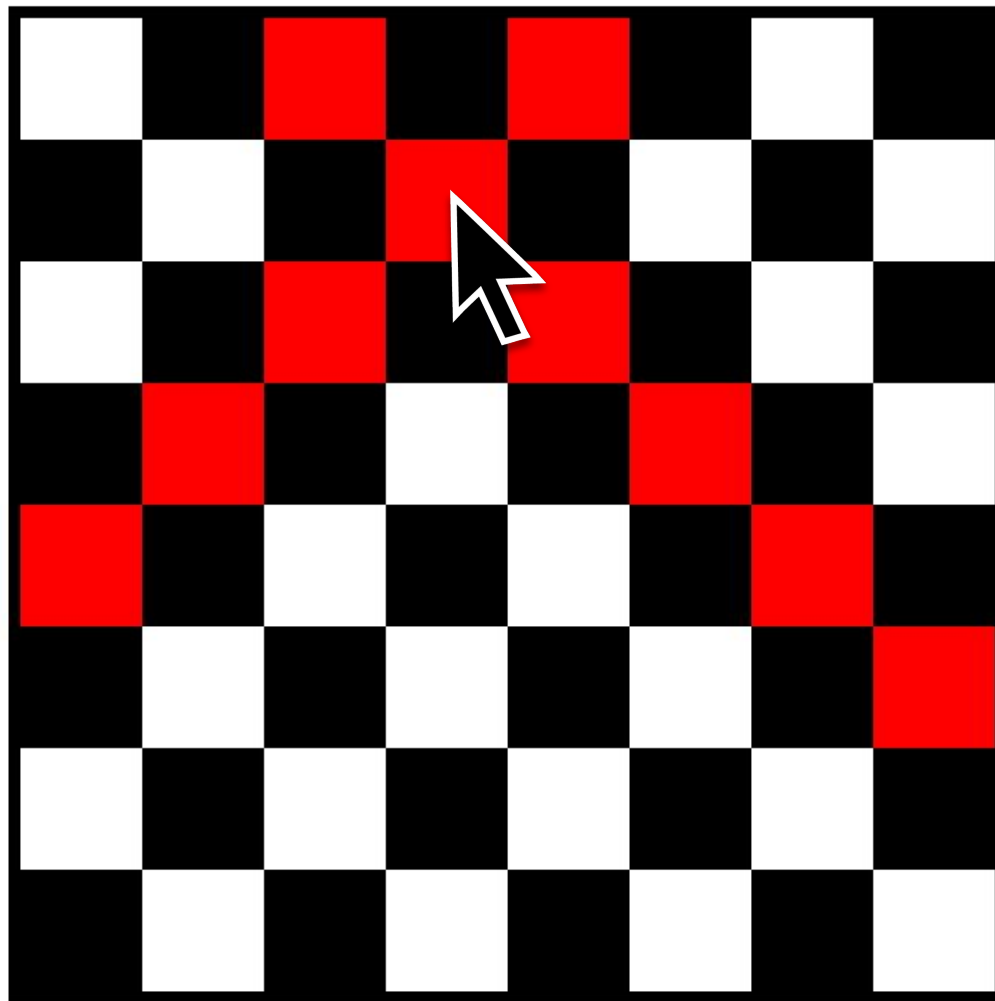
# Exercise:

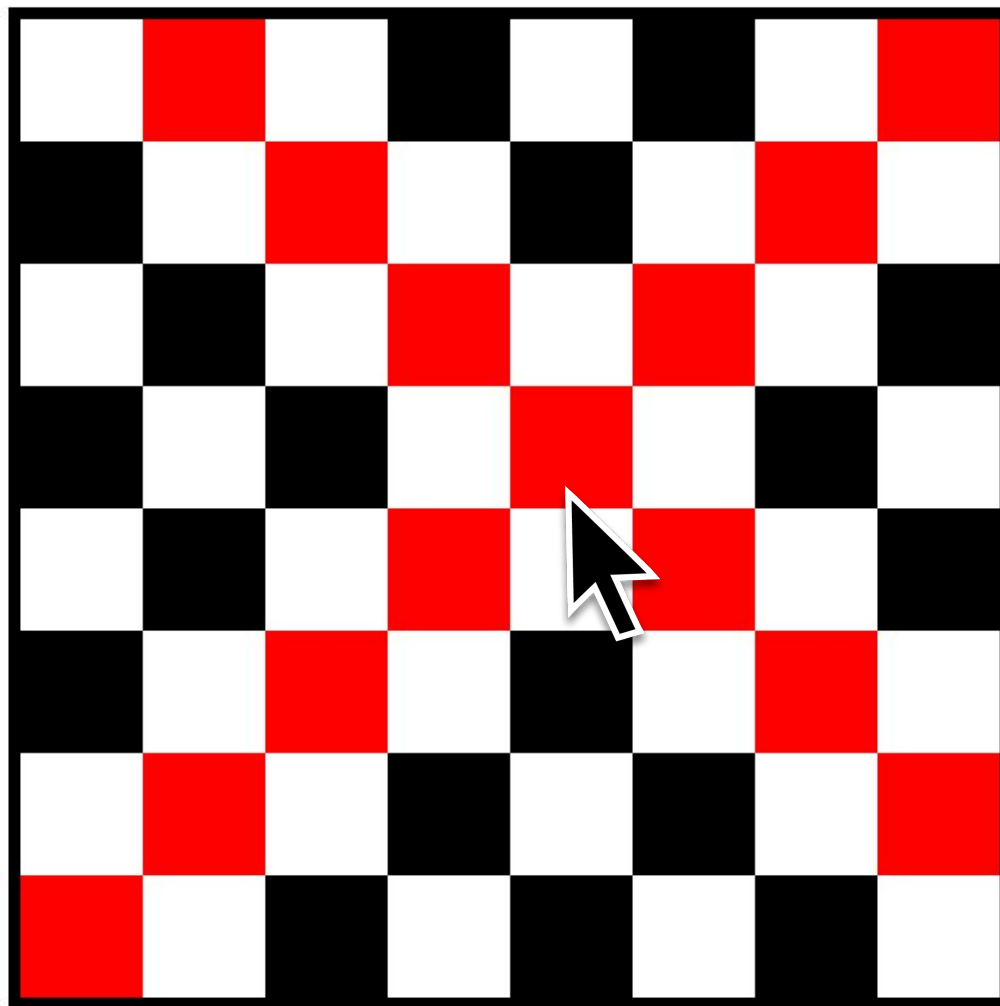
## Chessboard Diagonals

<https://github.com/getify/workshop-chess-diagonals>

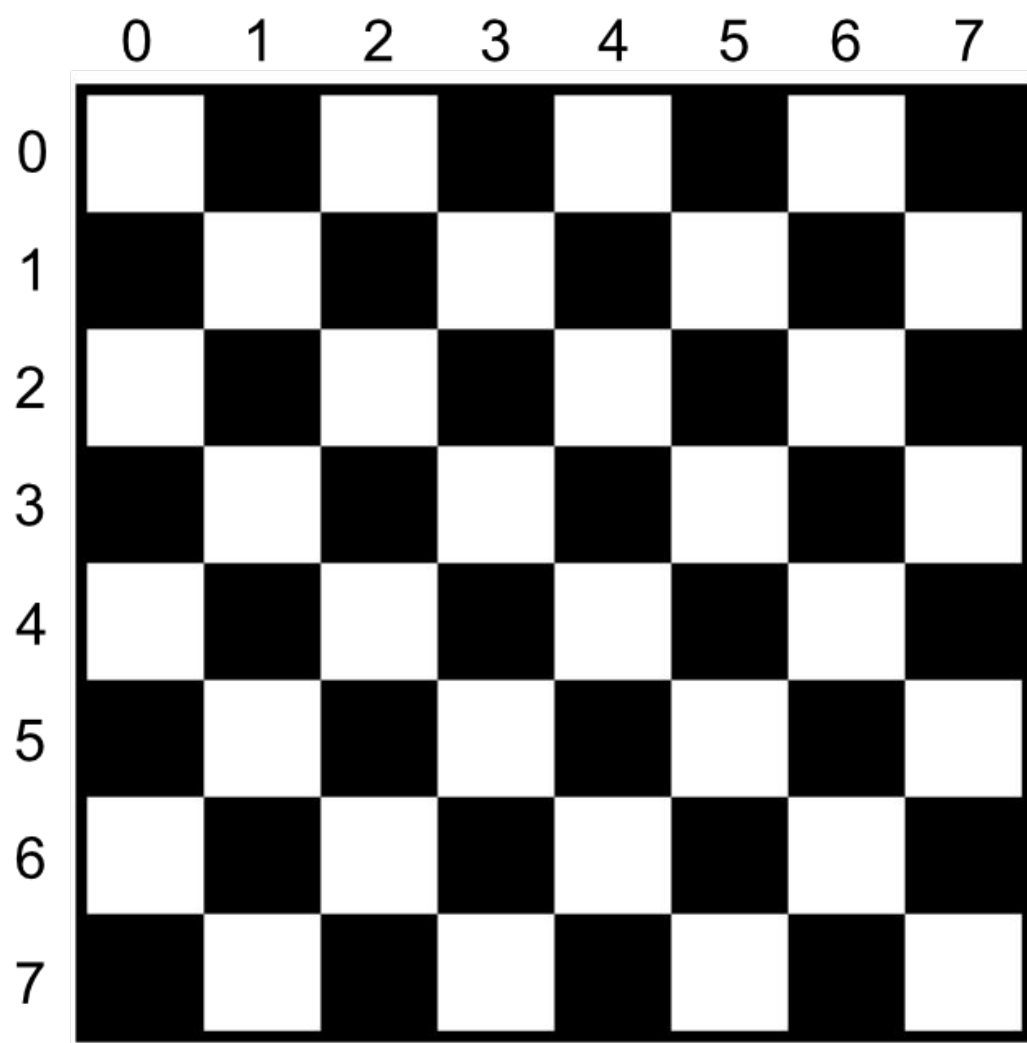




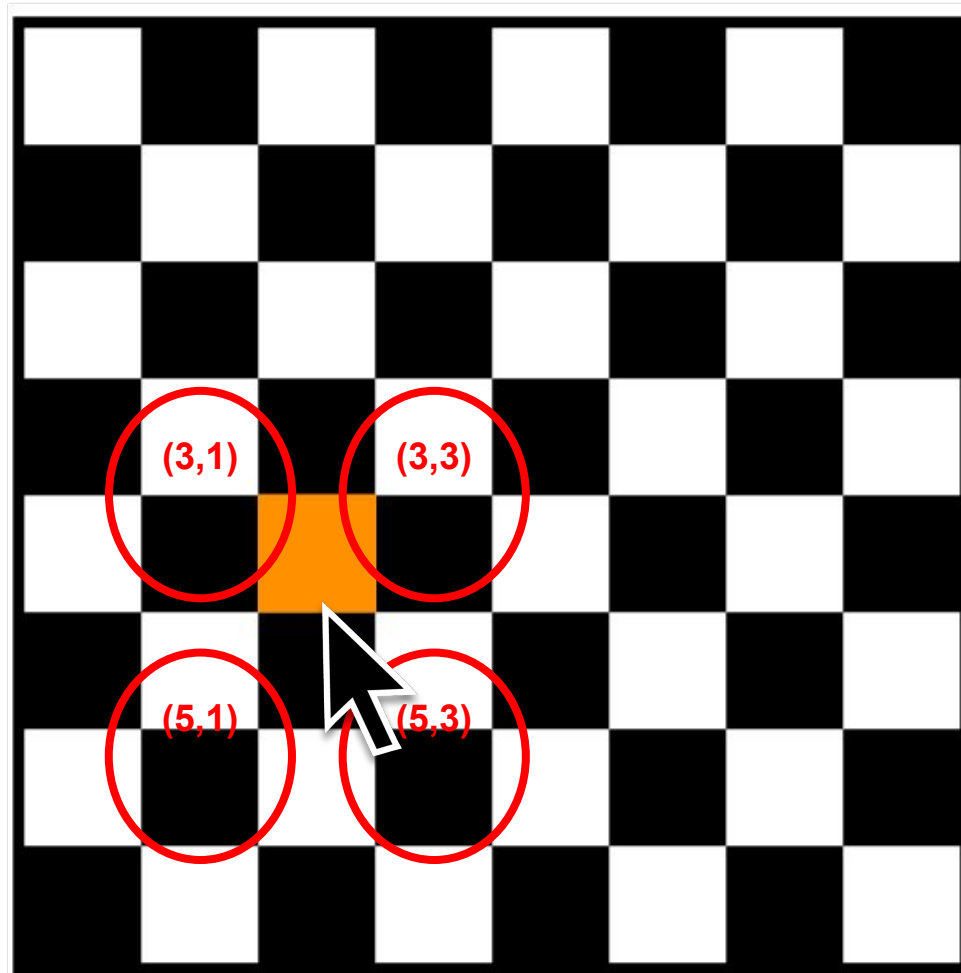








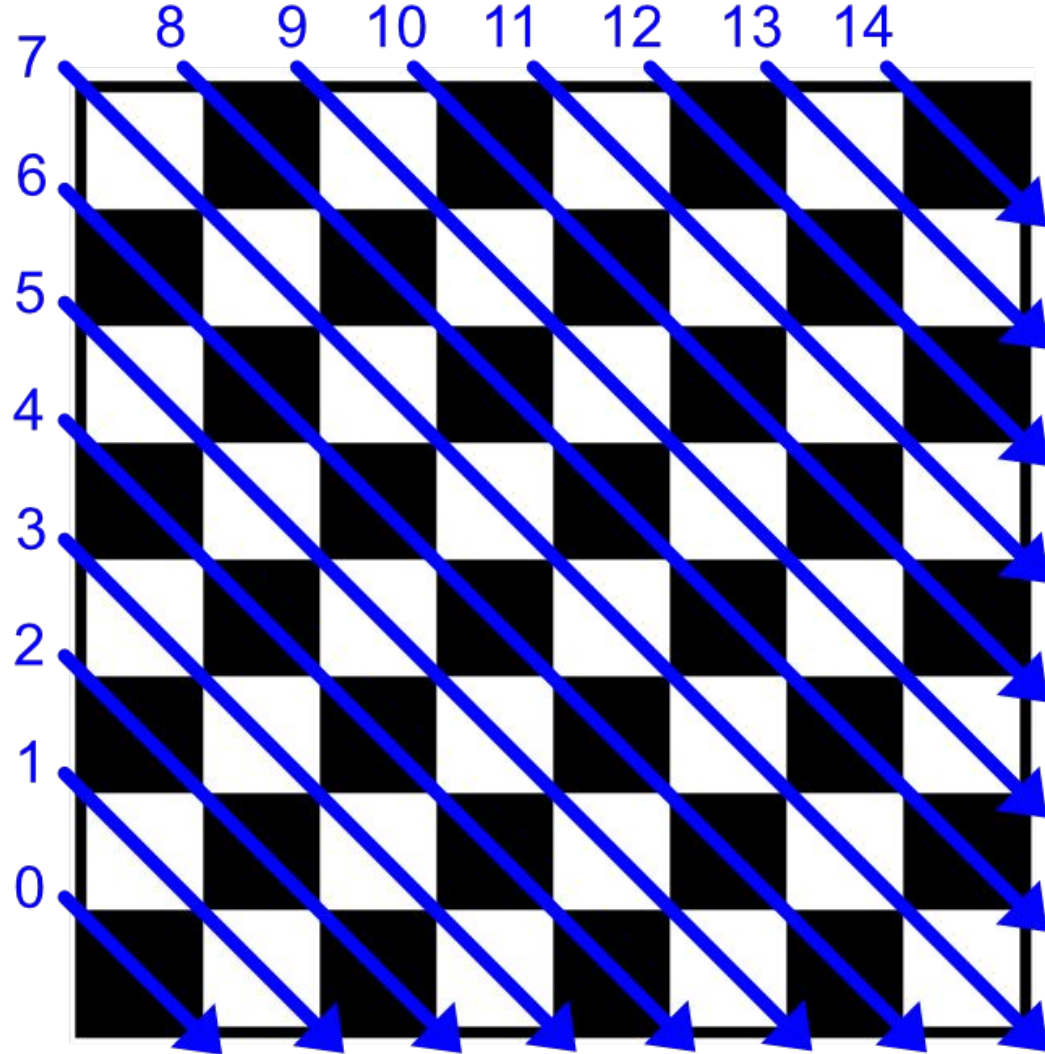
2



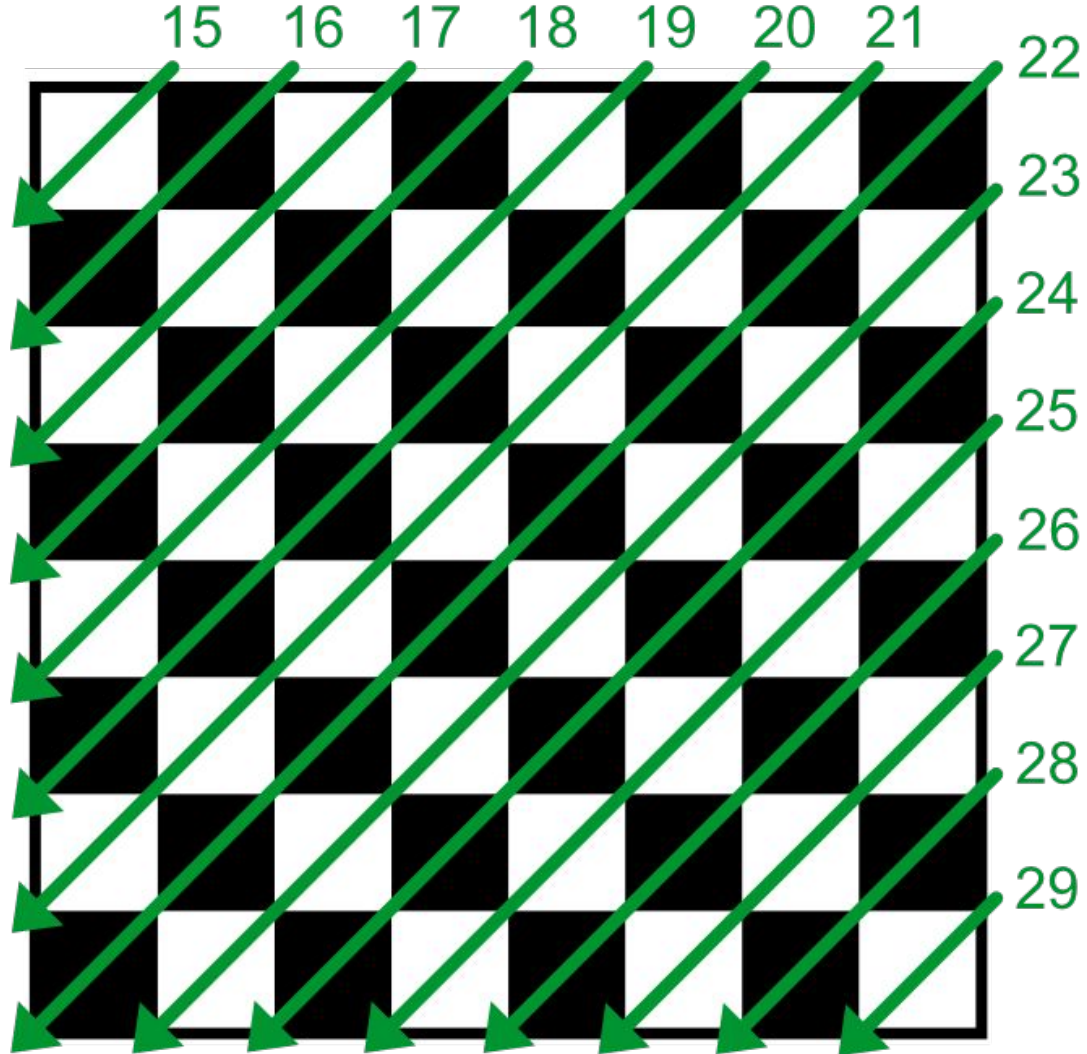
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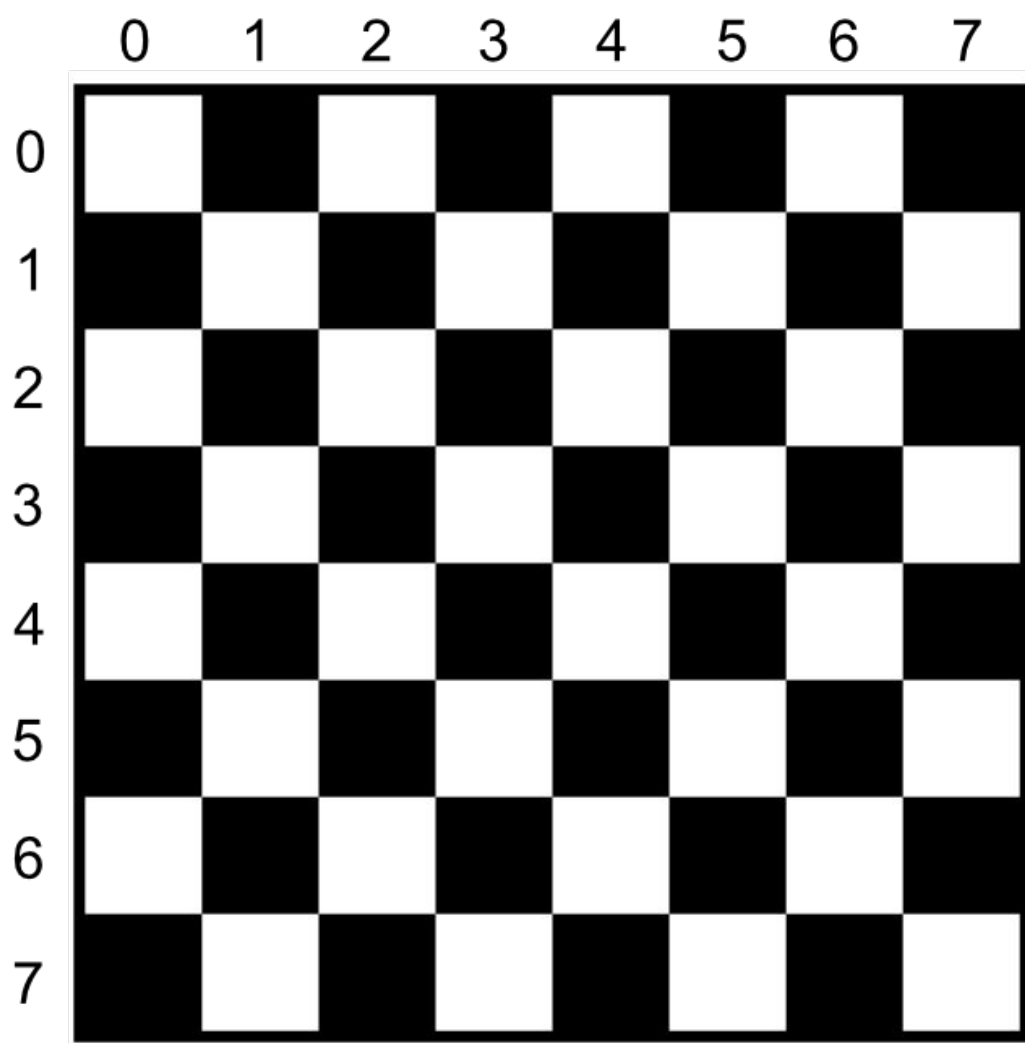
(4,2)

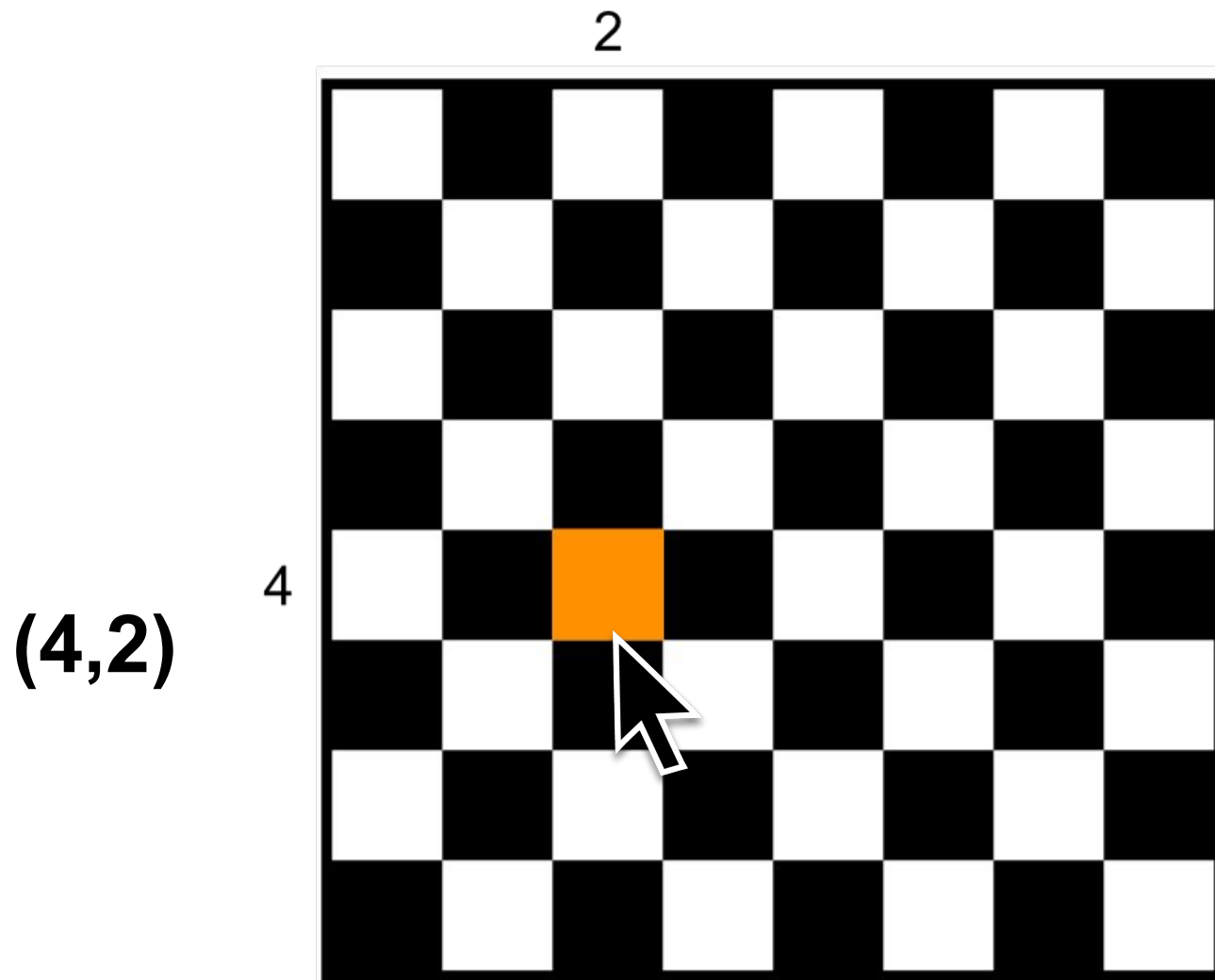
**Major  
Diagonals**



**Minor  
Diagonals**







2

21

$$5 = 7 - (4 - 2)$$

5

$$21 = 15 + (4 + 2)$$

$$5 = 7 - (2 - 0)$$

$$5 = 7 - (3 - 1)$$

$$5 = 7 - (4 - 2)$$

$$5 = 7 - (5 - 3)$$

$$5 = 7 - (6 - 4)$$

$$5 = 7 - (7 - 5)$$

4

$$21 = 15 + (6 + 0)$$

$$21 = 15 + (5 + 1)$$

$$21 = 15 + (4 + 2)$$

$$21 = 15 + (3 + 3)$$

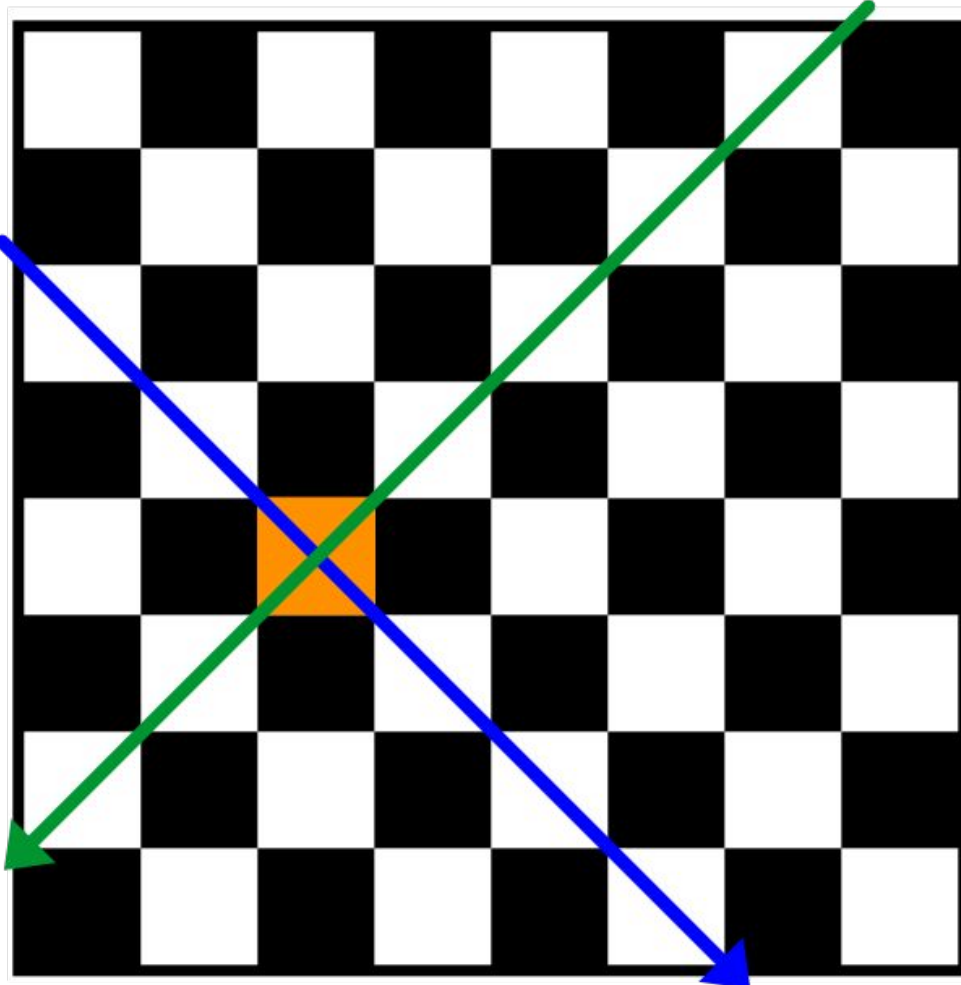
$$21 = 15 + (2 + 4)$$

$$21 = 15 + (1 + 5)$$

$$21 = 15 + (0 + 6)$$

$$7 - (\text{row} - \text{col})$$

$$15 + (\text{row} + \text{col})$$







# Exercise: Knight's Dialer

<https://github.com/getify/workshop-knights-dialer>

1

2

3

4

5

6

7

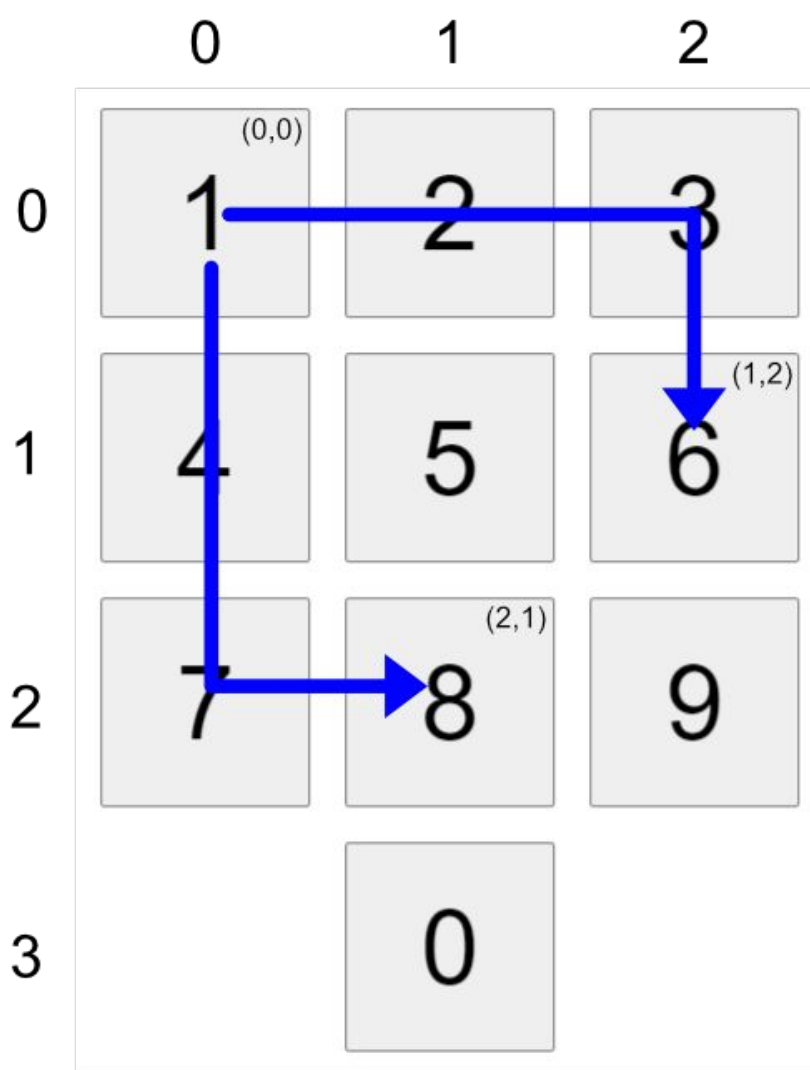
8

9

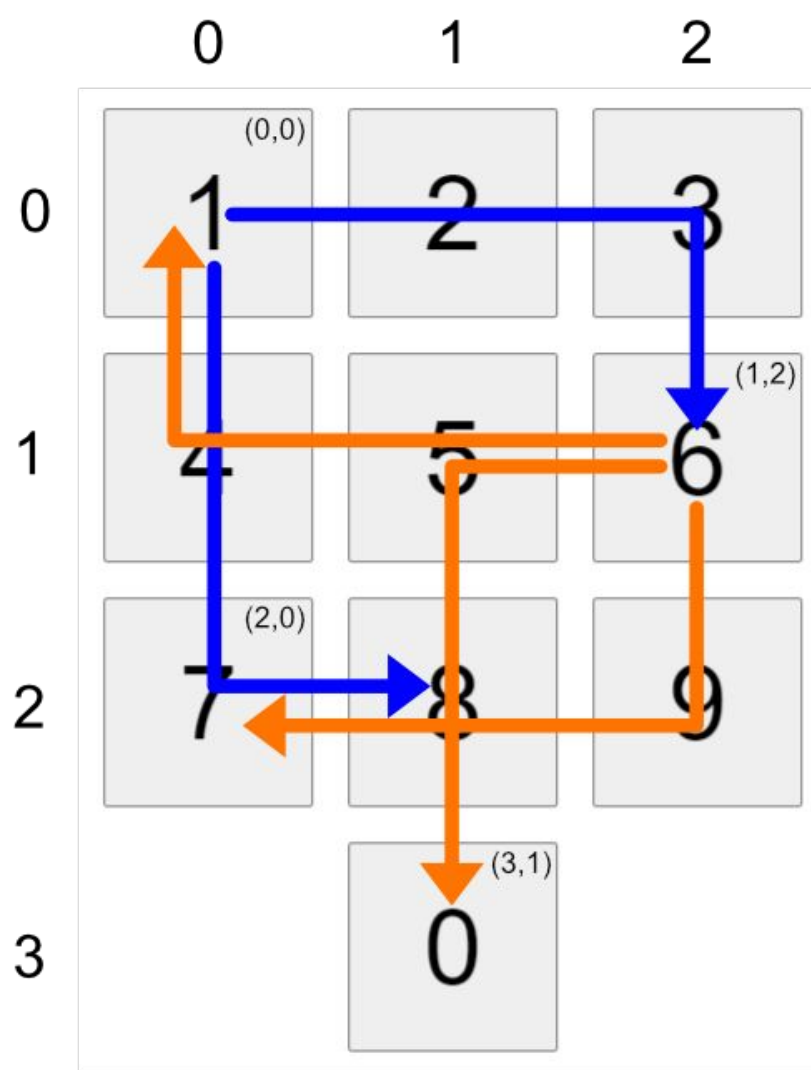
0

	0	1	2
0	1	2	3
1	4	5	6
2	7	8	9
3		0	

row +/- 2  
col +/- 1



row +/- 1  
col +/- 2



$$\begin{aligned} \text{countPaths}(4,6) &= & 168 \\ &\text{countPaths}(3,5) + & 52 \\ &\text{countPaths}(9,5) + & 52 \\ &\text{countPaths}(0,5) & 64 \end{aligned}$$

Recursion

countPaths(3,5) = 52

countPaths(4,4) + 32

countPaths(8,4) 20

Recursion

Breadth-First

Depth-First

Traversal



$$f(4,6)$$

Breadth-First Traversal      Iterative+Queue

$$f(4,6)$$

Depth-First Traversal

Recursion

$$O(n): \sim 2.222^n$$

$O(6)$ : ~120 ops     $O(7)$ : ~268 ops     $O(8)$ : ~595 ops

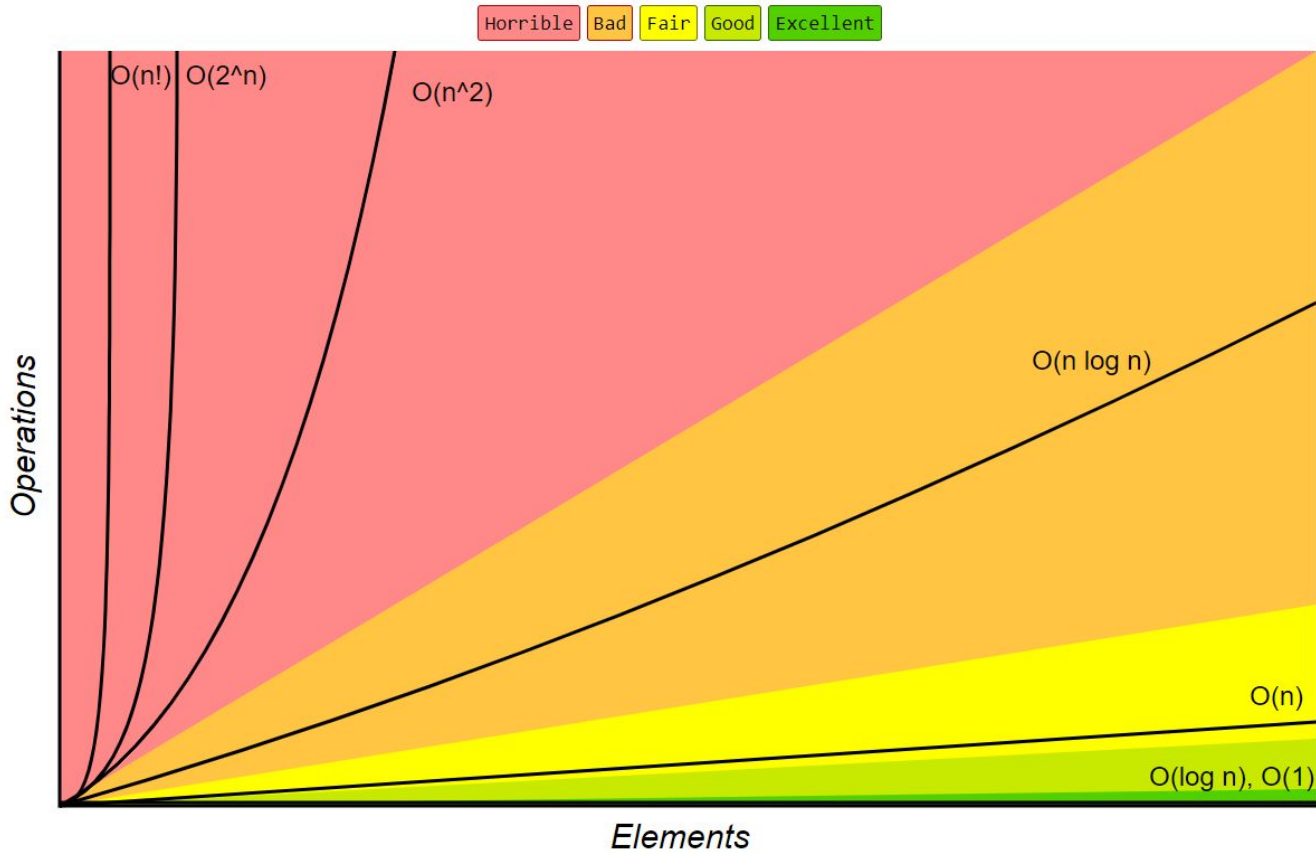
**Exponential**

Recursion

Factorial  
Exponential  
Polynomic  
Linear \* Logarithmic  
Linear  
Logarithmic  
Constant

# Big-O Complexity Chart

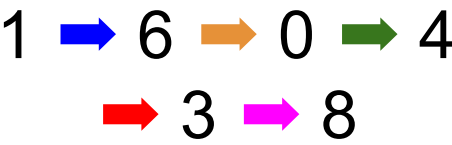
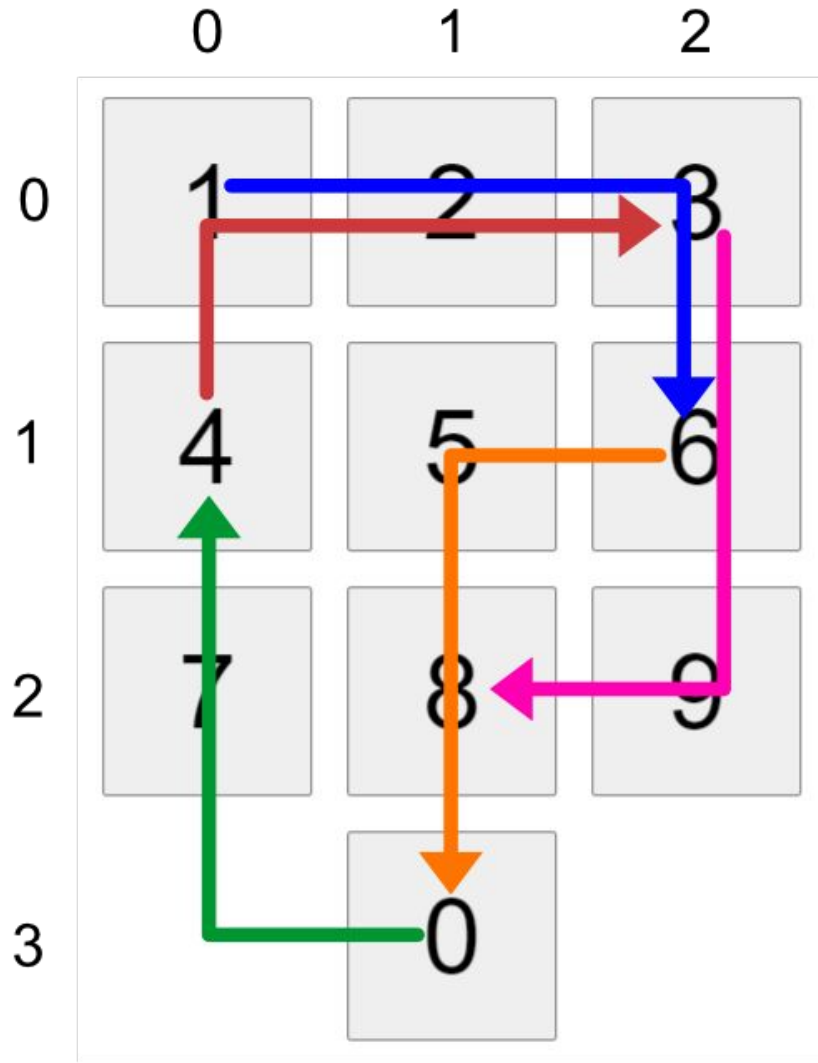
[bigocheatsheet.com](http://bigocheatsheet.com)

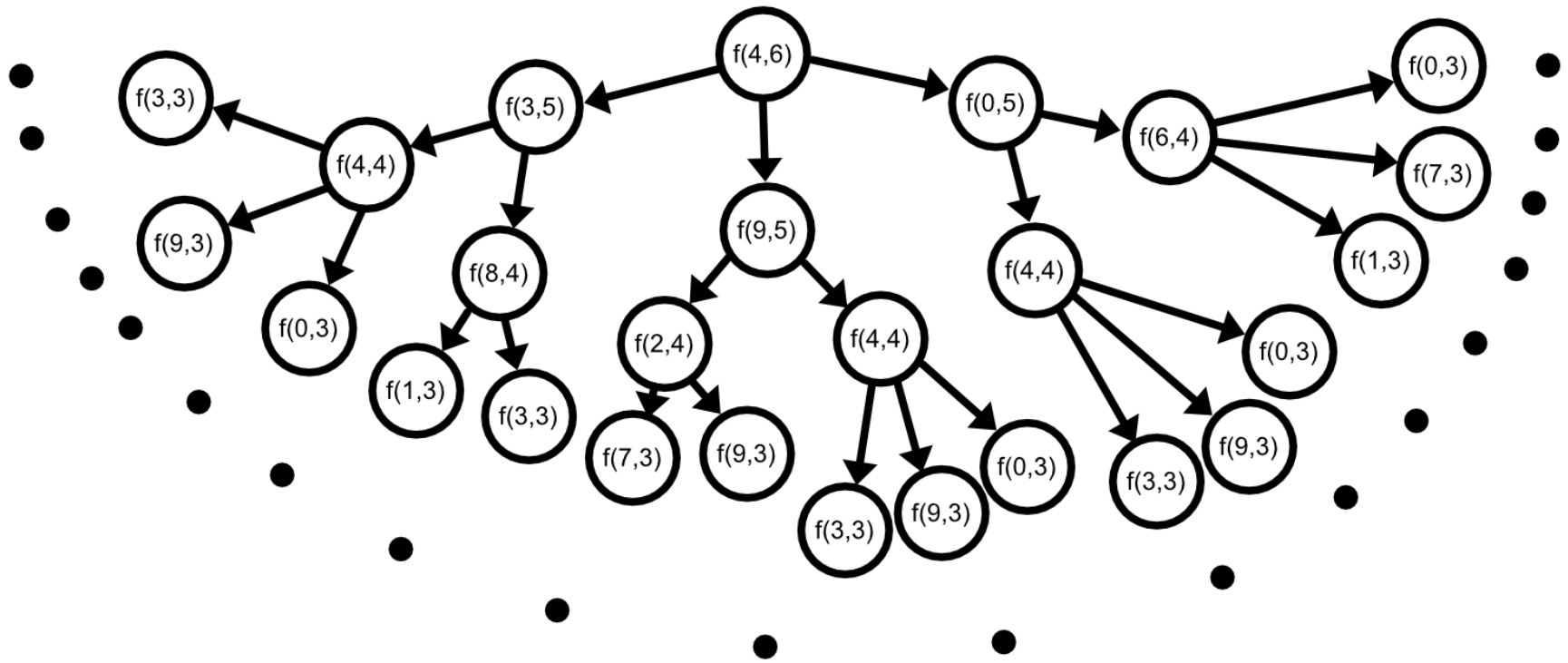


Acyclic  
Paths

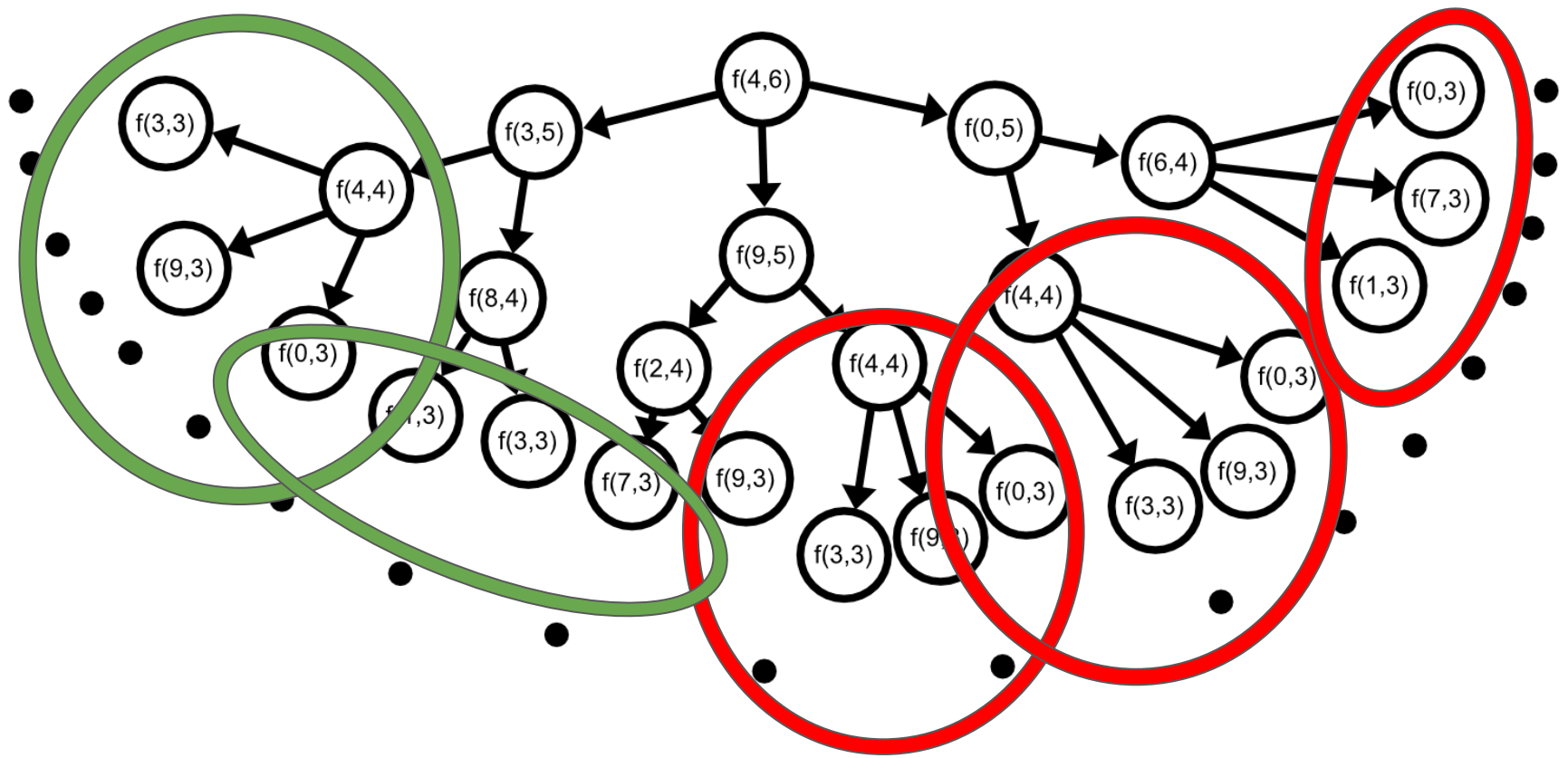
	0	1	2
0	1	2	3
1	4	5	6
2	7	8	9
3		0	

# Acyclic Paths



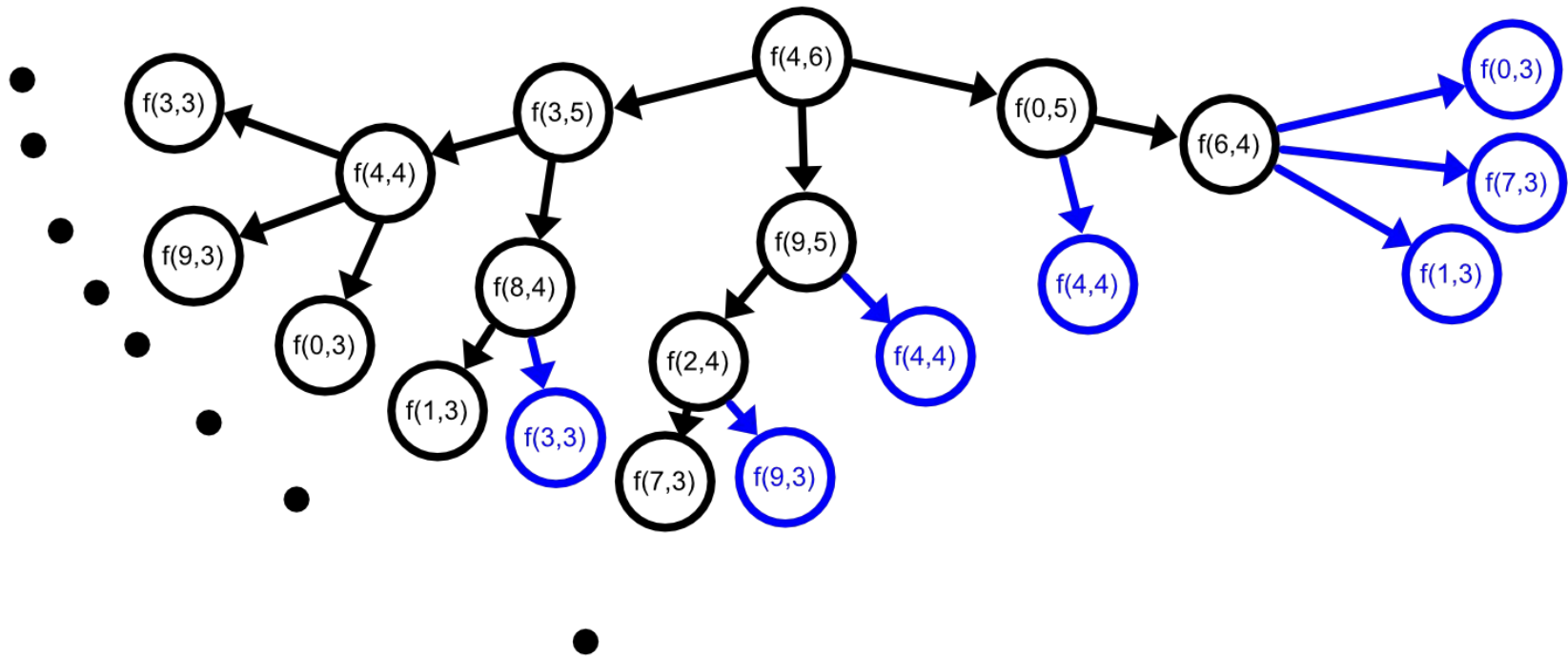


(Optimizing) Recursion



Recursion + Memoization





Recursion + Memoization

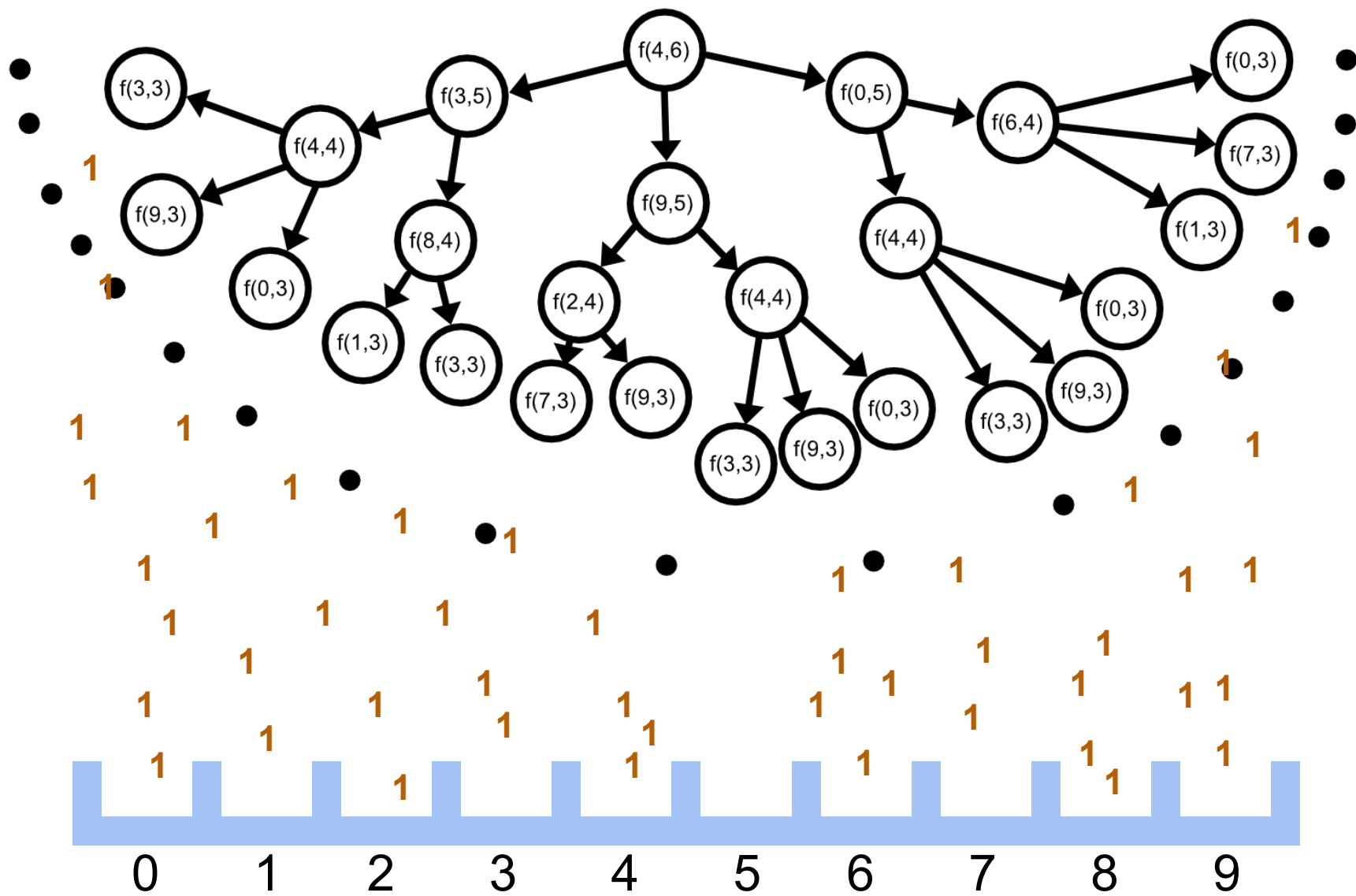
Top-Down

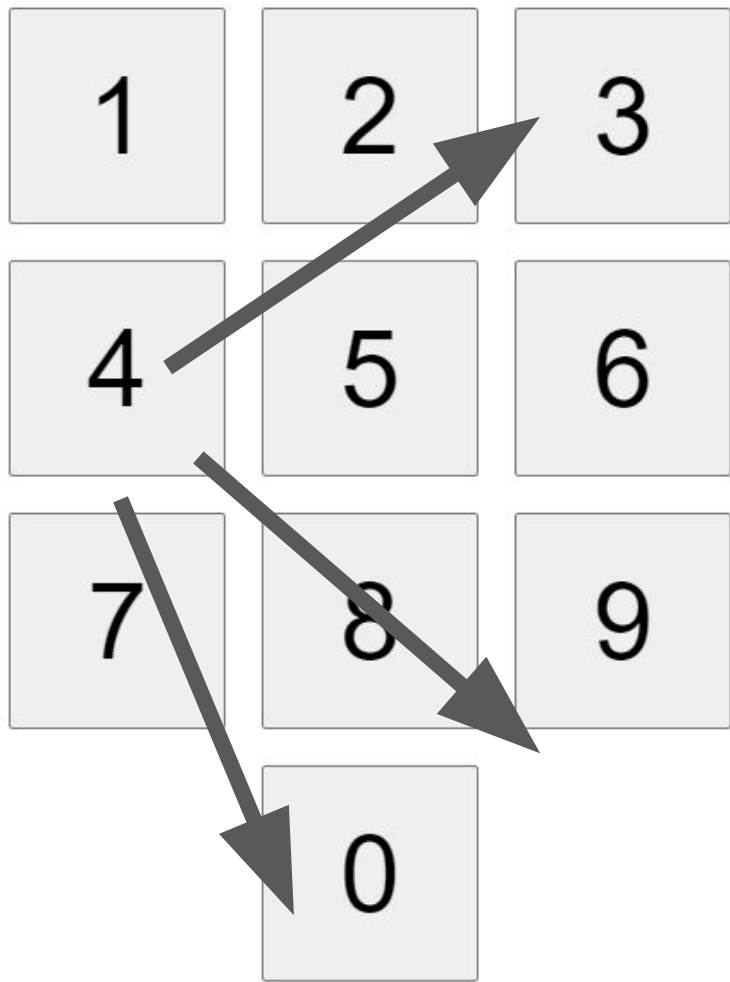
(memoization)

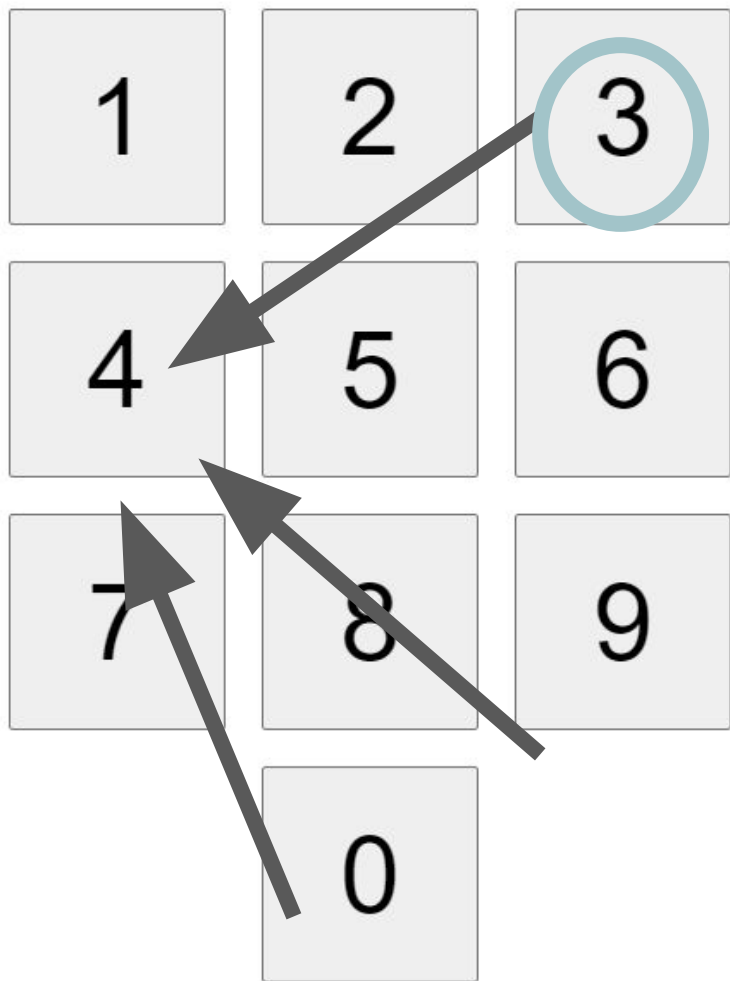
Bottom-Up

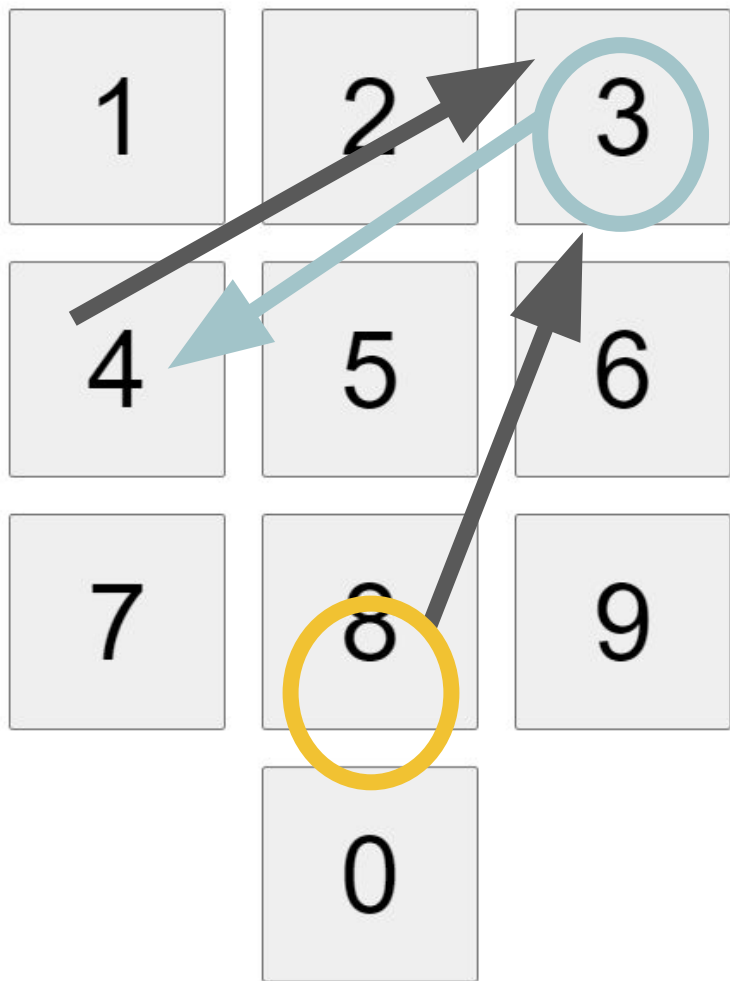
(tabulation)

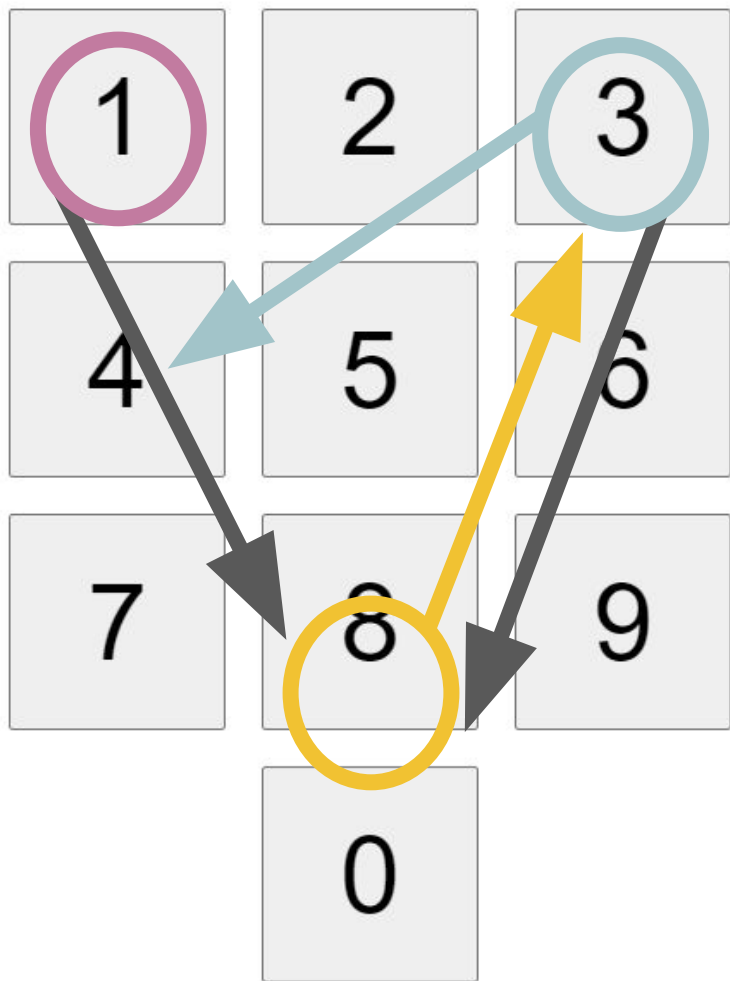
Dynamic Programming



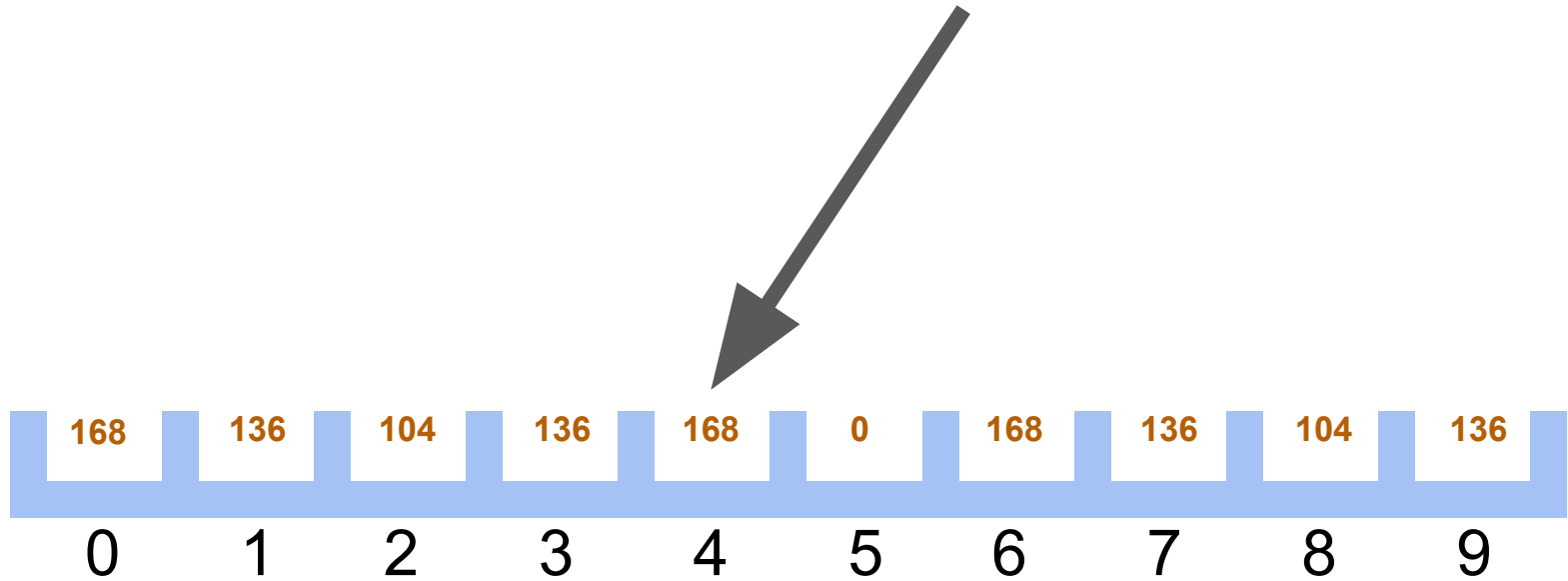






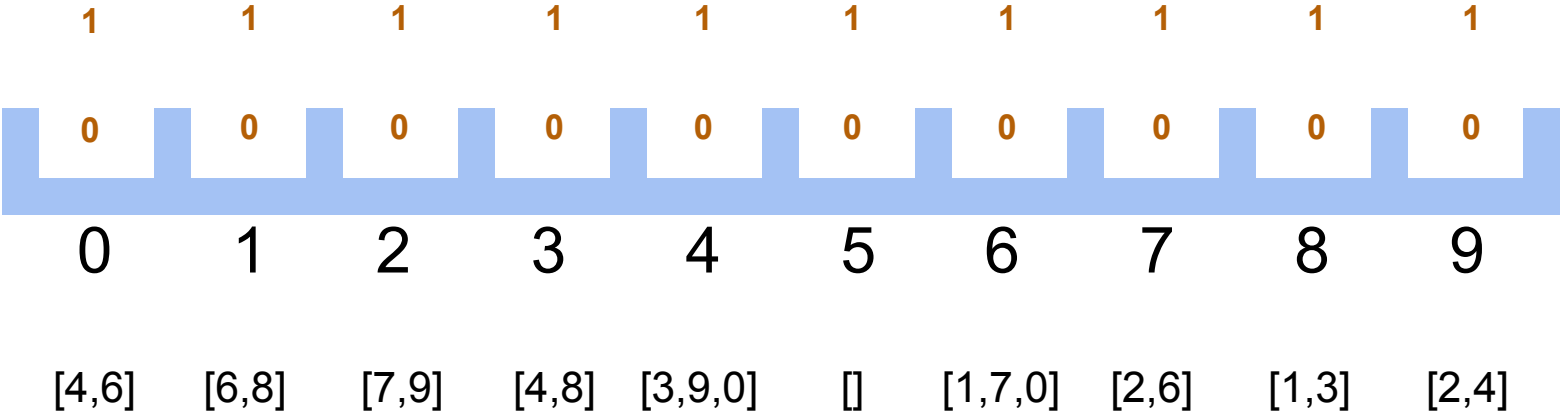


countPaths(4,6)

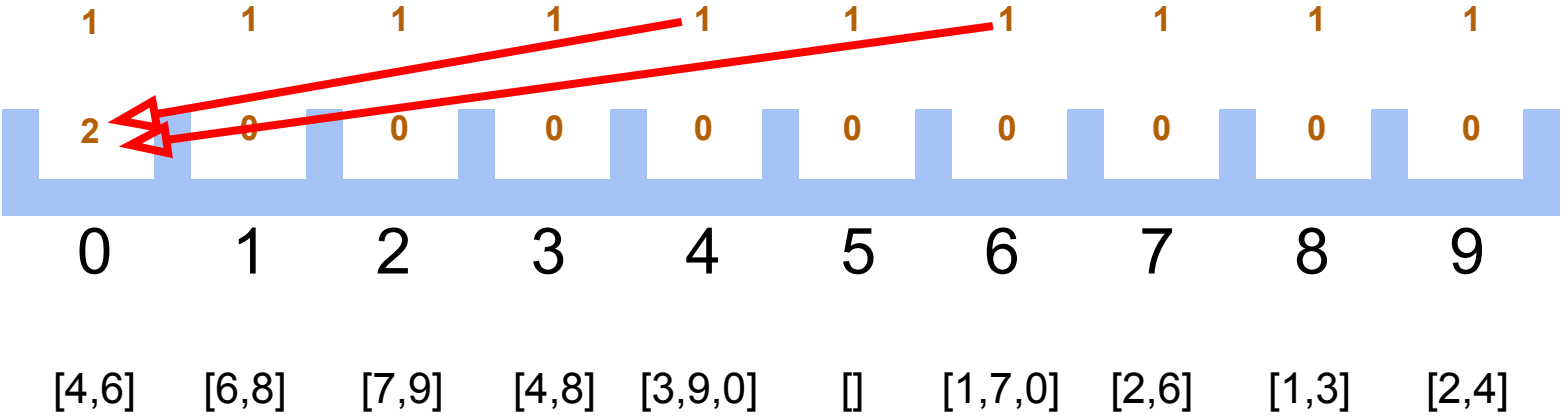




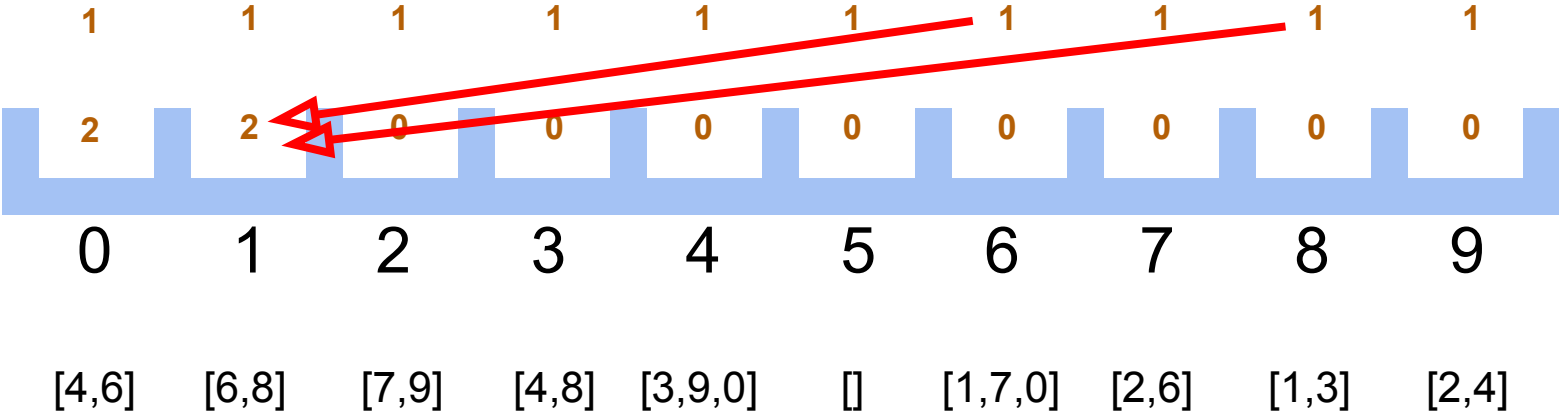
Iteration: 1  
hopCount: 6



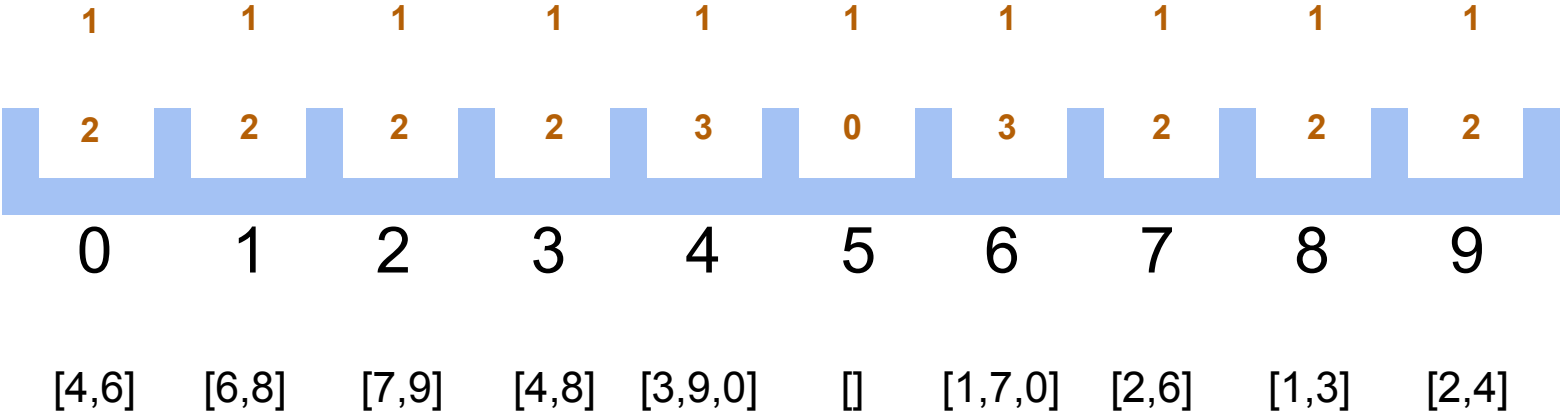
Iteration: 1  
hopCount: 6



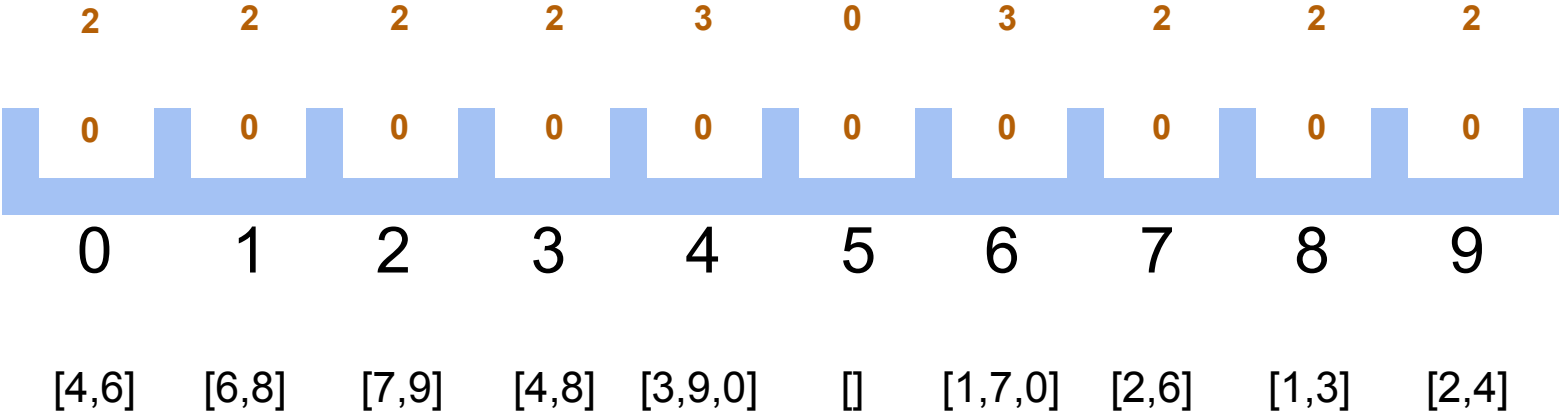
Iteration: 1  
hopCount: 6



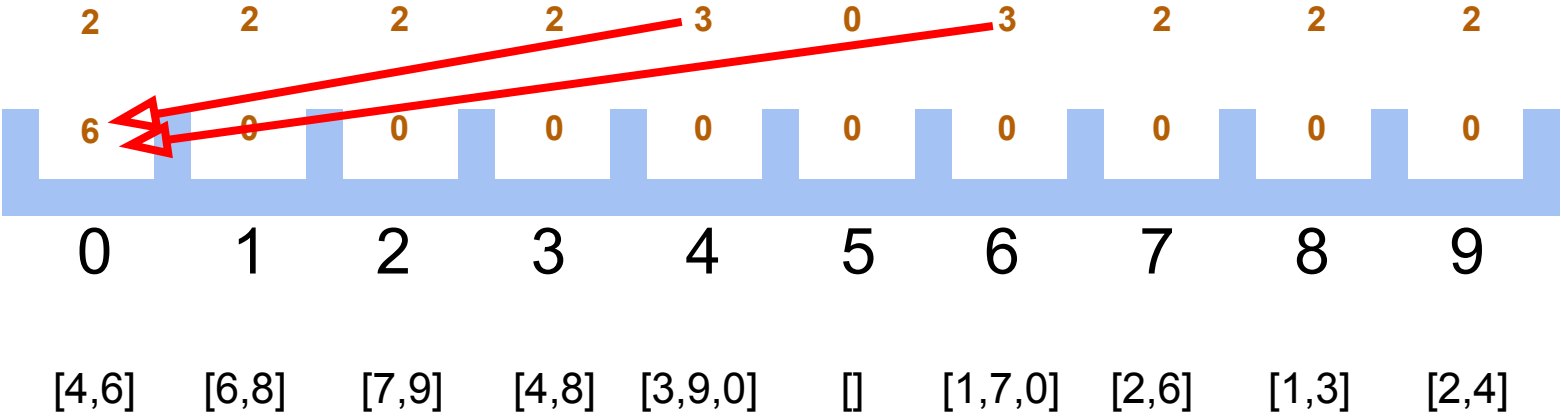
Iteration: 1  
hopCount: 6



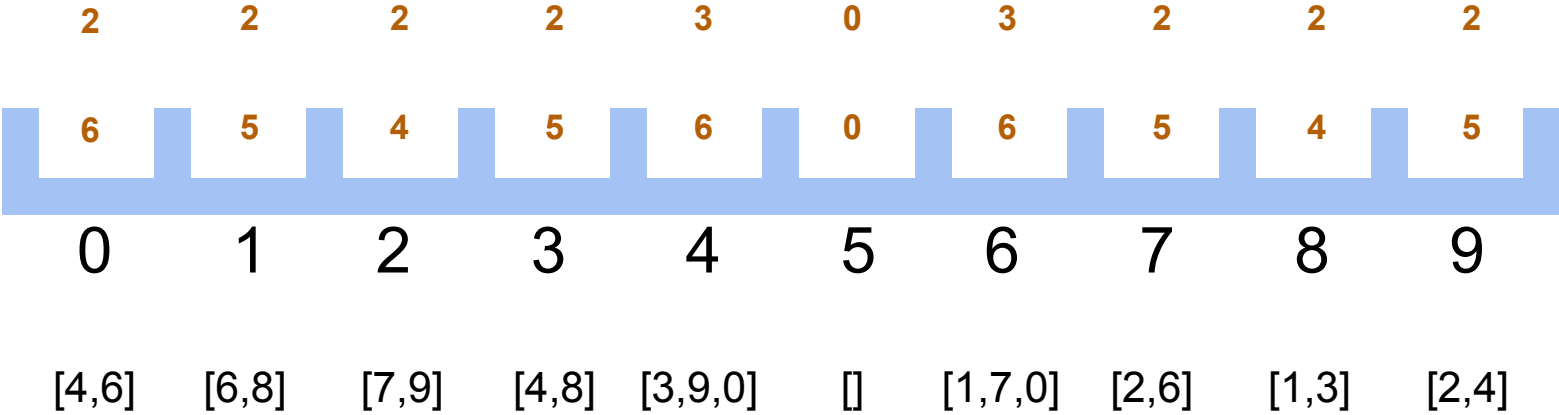
Iteration: 2  
hopCount: 5



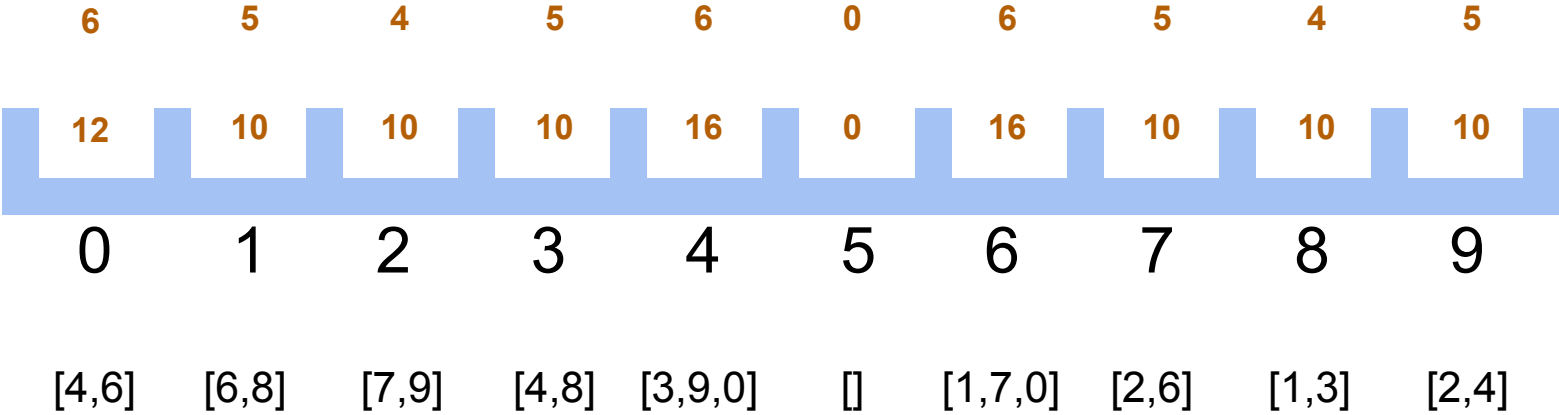
Iteration: 2  
hopCount: 5



Iteration: 2  
hopCount: 5

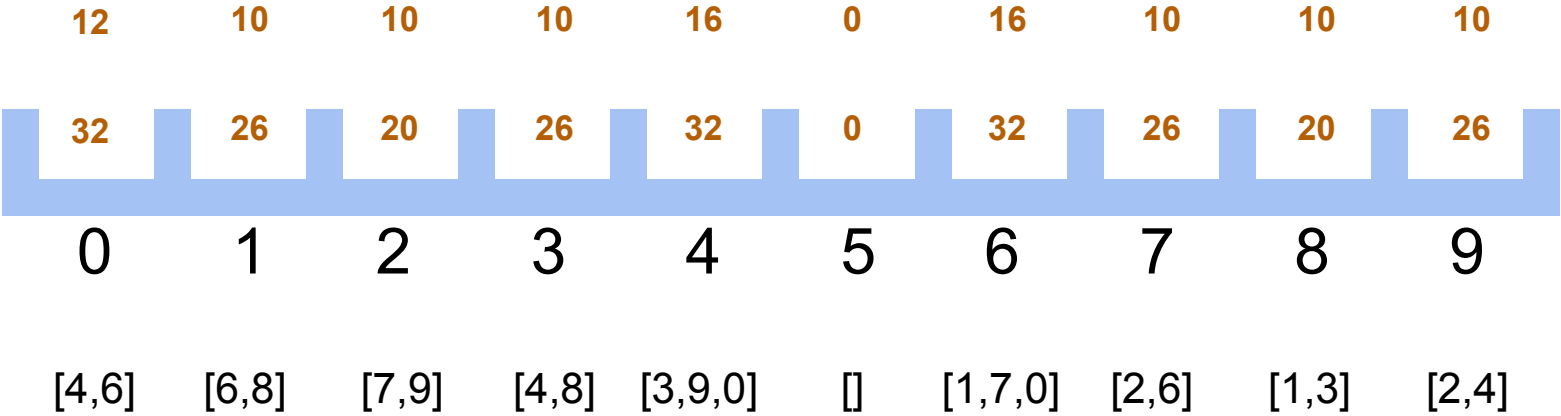


Iteration: 3  
hopCount: 4

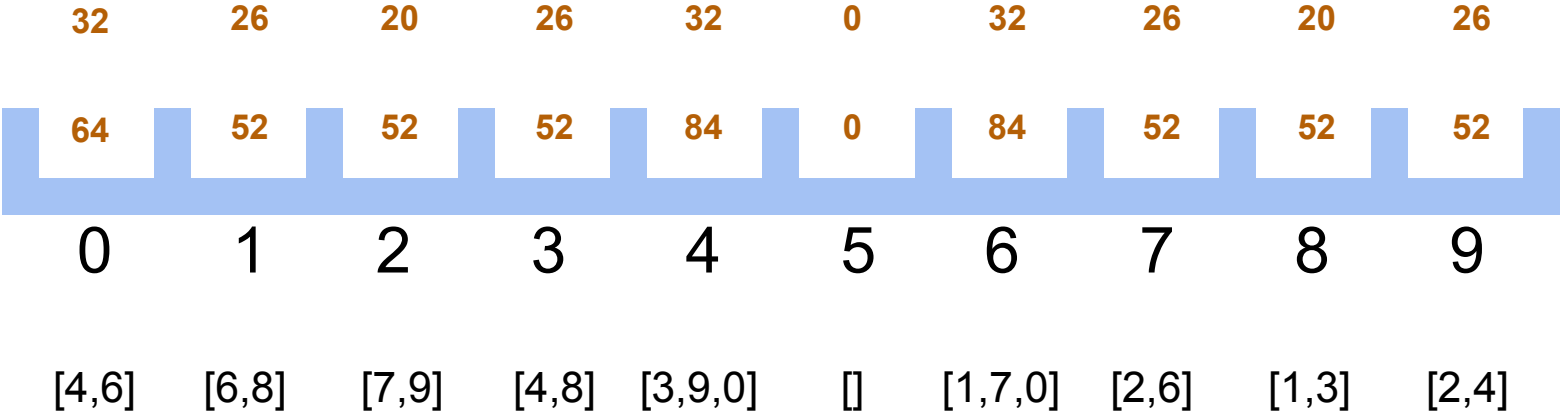




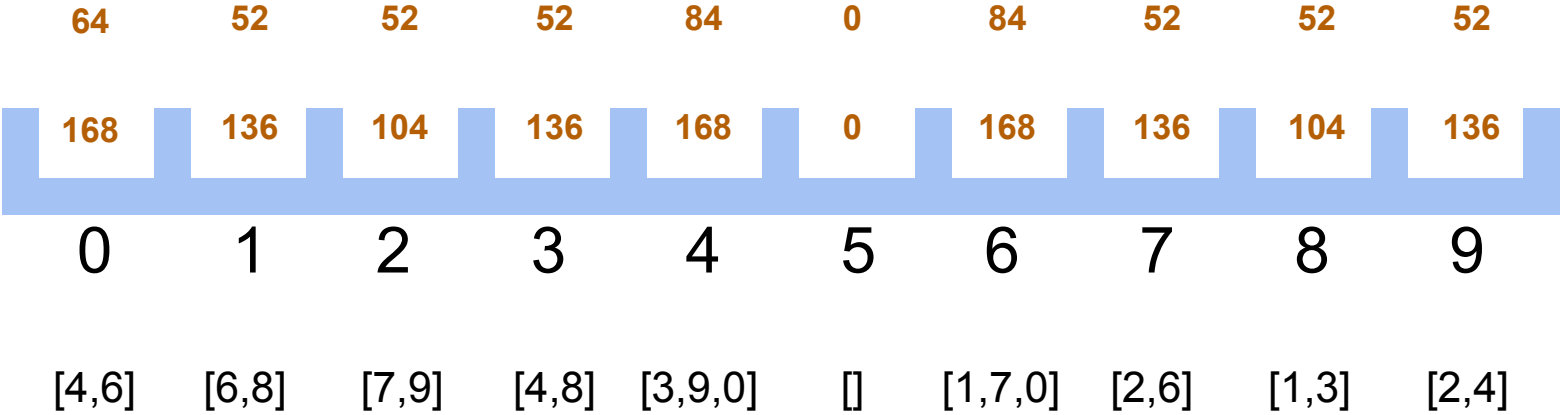
Iteration: 4  
hopCount: 3



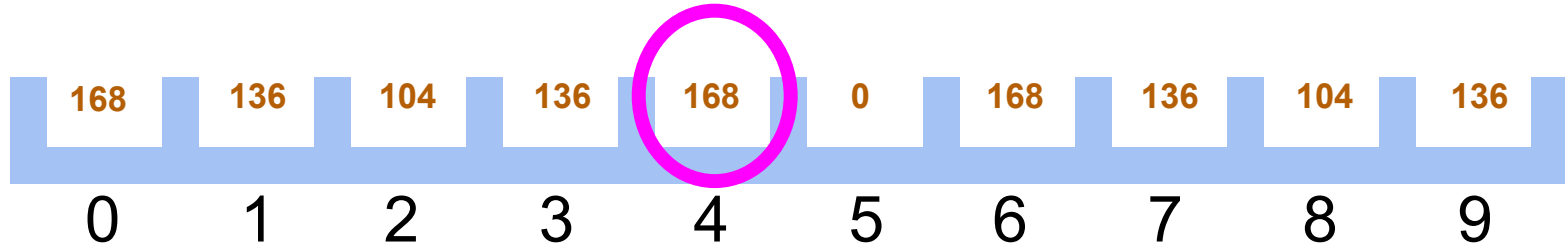
Iteration: 5  
hopCount: 2



Iteration: 6  
hopCount: 1



countPaths(4,6)



$O(n): n * 20 \Rightarrow n$

$O(6)$ : 120 ops

$O(60)$ : 1,200 ops

$O(600)$ : 12,000 ops

Linear



# Exercise: Wordy Unscrambler

<https://github.com/getify/workshop-wordy-unscrambler>

Short Dictionary (~2400 words) (entries: 2426) (0.0 ms)

Letters: PCERA

unscramble (28.1 ms)

Input: **PCERA**

ACRE

ARC

ARE

CAP

CAPE

CAR

CARE

EAR

PER

RACE

REAP

## Wordscapes



**CAN  
CAP  
CAPE  
CAR  
CARE  
CLAP  
EACH  
EAR**

**PCERA**



✓ CAN  
✓ CAP  
✓ CAPE  
✓ CAR  
✓ CARE  
✓ CLAP  
EACH  
EAR

PCERA

→ ✓ APPEAR

CAN

✓ CAP

✓ CAPE

✓ CAR

✓ CARE

✓ CLAP

EACH

EAR

✓

PCERA

**APPEAR**

**CAN**



**CAP**



**CAPE**



**CAR**



**CARE**

**CLAP**

**EACH**

**EAR**



**PCERA**

CAN  
CAP  
CAPE  
CAR  
CARE  
CLAP  
EACH  
EAR

**PCERA**

PCERA CPERA EPCRA PECRA... (5! = 120)

# PCERA

PCERA CPERA EPCRA PECRA CEPRA ECPRA RCPEA CRPEA PRCEA RPCEA  
CPREA PCREA PERCA EPRCA RPECA PRECA ERPCA REPCA RECPA ERCPA  
CREPA RCEPA ECRPA CERPA AERPC EARPC RAEPC AREPC ERAPC REAPC  
PEARC EPARC APERC PAERC EAPRC AEPRC ARPEC RAPEC PAREC APREC  
RPAEC PRAEC PREAC RPEAC EPRAC PERAC REPAC ERPAC CRPAE RCPAE  
PCRAE CPRAE RPCAE PRCAE ARCPE RACPE CARPE ACRPE RCAPE CRAPE  
CPARE PCARE ACPRE CAPRE PACRE APCRE APRCE PARCE RAPCE ARPCE  
PRACE RPACE EPACR PEACR AEPCR EAPCR PAECR APECR CPEAR PCEAR  
ECPAR CEPAR PECAR EPCAR EACPR AECPR CEAPR ECAPR ACEPR CAEPR  
CAPER ACPER PCAER CPAER APCER PACER RACEP ARCEP CRAEP RCAEP  
ACREP CAREP EARCP AERCP REACP ERACP ARECP RAECR RCEAP CREAP  
ERCAP RECAP CERAP ECRAP ECARP CEARP AECRP EACRP CAERP ACERP

## PCERA

PCERA CPERA EPCRA PECRA CEPRA ECPRA RCPEA CRPEA PRCEA RPCEA  
CPREA PCREA PERCA EPRCA RPECA PRECA ERPCA REPCA RECPA ERCPA  
CREPA RCEPA ECRPA CERPA AERPC EARPC RAEPC AREPC ERAPC REAPC  
PEARC EPARC APERC PAERC EAPRC AEPRC ARPEC RAPEC PAREC APREC  
RPAEC PRAEC PREAC RPEAC EPRAC PERAC REPAC ERPAC CRPAE RCPAE  
PCRAE CPRAE RPCAE PRCAE ARCPE RACPE CARPE ACRPE RCAPE CRAPE  
CPARE PCARE ACPRE CAPRE PACRE APCRE APRCE PARCE RAPCE ARPCE  
PRACE RPACE EPACR PEACR AEPCR EAPCR PAECR APECR CPEAR PCEAR  
ECPAR CEPAR PECAR EPCAR EACPR AECPR CEAPR ECAPR ACEPR CAEPR  
CAPER ACPER PCAER CPAER APCER PACER RACEP ARCEP CRAEP RCAEP  
ACREP CAREP EARCP AERCP REACP ERACP ARECP RAECR RCEAP CREAP  
ERCAP RECAP CERAP ECRAP ECARP CEARP AECRP EACRP CAERP ACERP

CAN

## PCERA

PCERA CPERA EPCRA PECRA CEPRA ECPRA RCPEA CRPEA PRCEA RPCEA  
CPREA PCREA PERCA EPRCA RPECA PRECA ERPCA REPCA RECPA ERCPA  
CREPA RCEPA ECRPA CERPA AERPC EARPC RAEPC AREPC ERAPC REAPC  
PEARC EPARC APERC PAERC EAPRC AEPRC ARPEC RAPEC PAREC APREC  
RPAEC PRAEC PREAC RPEAC EPRAC PERAC REPAC ERPAC CRPAE RCPAE  
PCRAE CPRAE RPCAE PRCAE ARCPE RACPE CARPE ACRPE RCAPE CRAPE  
CPARE PCARE ACPRE **CAP**RE PACRE APCRE APRCE PARCE RAPCE ARPCE  
PRACE RPACE EPACR PEACR AEPCR EAPCR PAECR APECR CPEAR PCEAR  
ECPAR CEPAR PECAR EPCAR EACPR AECPR CEAPR ECAPR ACEPR CAEPR  
CAPER ACPER PCAER CPAER APCER PACER RACEP ARCEP CRAEP RCAEP  
ACREP CAREP EARCP AERCP REACP ERACP ARECP RAECR RCEAP CREAP  
ERCAP RECAP CERAP ECRAP ECARP CEARP AECRP EACRP CAERP ACERP

CAN **CAP**

## PCERA

PCERA CPERA EPCRA PECRA CEPRA ECPRA RCPEA CRPEA PRCEA RPCEA  
CPREA PCREA PERCA EPRCA RPECA PRECA ERPCA REPCA RECPA ERCPA  
CREPA RCEPA ECRPA CERPA AERPC EARPC RAEP C AREPC ERAPC REAPC  
PEARC EPARC APERC PAERC EAPRC AEPRC ARPEC RAPEC PAREC APREC  
RPAEC PRAEC PREAC RPEAC EPRAC PERAC REPAC ERPAC CRPAE RCPAE  
PCRAE CPRAE RPCAE PRCAE ARCPE RACPE CARPE ACRPE RCAPE CRAPE  
CPARE PCARE ACPRE CAPRE PACRE APCRE APRCE PARCE RAPCE ARPCE  
PRACE RPACE EPACR PEACR AEPCR EAPCR PAECR APECR CPEAR PCEAR  
ECPAR CEPAR PECAR EPCAR EACPR AECPR CEAPR ECAPR ACEPR CAEPR  
CAPER ACPER PCAER CPAER APCER PACER RACEP ARCEP CRAEP RCAEP  
ACREP CAREP EARCP AERCP REACP ERACP ARECP RAEC RCEAP CREAP  
ERCAP RECAP CERAP ECRAP ECARP CEARP AECRP EACRP CAERP ACERP

CAN CAP CAPE



## PCERA

PCERA CPERA EPCRA PECRA CEPRA ECPRA RCPEA CRPEA PRCEA RPCEA  
CPREA PCREA PERCA EPRCA RPECA PRECA ERPCA REPCA RECPA ERCPA  
CREPA RCEPA ECRPA CERPA AERPC EARPC RAEPC AREPC ERAPC REAPC  
PEARC EPARC APERC PAERC EAPRC AEPRC ARPEC RAPEC PAREC APREC  
RPAEC PRAEC PREAC RPEAC EPRAC PERAC REPAC ERPAC CRPAE RCPAE  
PCRAE CPRAE RPCAE PRCAE ARCPE RACPE **CARPE** ACRPE RCAPE CRAPE  
CPARE PCARE ACPRE **CAPRE** PACRE APCRE APRCE PARCE RAPCE ARPCE  
PRACE RPACE EPACR PEACR AEPCR EAPCR PAECR APECR CPEAR PCEAR  
ECPAR CEPAR PECAR EPCAR EACPR AECPR CEAPR ECAPR ACEPR CAEPR  
**CAPER** ACPER PCAER CPAER APCER PACER RACEP ARCEP CRAEP RCAEP  
ACREP CAREP EARCP AERCP REACP ERACP ARECP RAECR RCEAP CREAP  
ERCAP RECAP CERAP ECRAP ECARP CEARP AECRP EACRP CAERP ACERP

CAN **CAP** CAPE CAR

## PCERA

PCERA CPERA EPCRA PECRA CEPRA ECPRA RCPEA CRPEA PRCEA RPCEA  
CPREA PCREA PERCA EPRCA RPECA PRECA ERPCA REPCA RECPA ERCPA  
CREPA RCEPA ECRPA CERPA AERPC EARPC RAEPC AREPC ERAPC REAPC  
PEARC EPARC APERC PAERC EAPRC AEPRC ARPEC RAPEC PAREC APREC  
RPAEC PRAEC PREAC RPEAC EPRAC PERAC REPAC ERPAC CRPAE RCPAE  
PCRAE CPRAE RPCAE PRCAE ARCPE RACPE **CARPE** ACRPE RCAPE CRAPE  
CPARE PCARE ACPRE **CAPRE** PACRE APCRE APRCE PARCE RAPCE ARPCE  
PRACE RPACE EPACR PEACR AEPCR EAPCR PAECR APECR CPEAR PCEAR  
ECPAR CEPAR PECAR EPCAR EACPR AECPR CEAPR ECAPR ACEPR CAEPR  
**CAPER** ACPER PCAER CPAER APCER PACER RACEP ARCEP CRAEP RCAEP  
ACREP **CAREP** EARCP AERCP REACP ERACP ARECP RAECR RCEAP CREAP  
ERCAP RECAP CERAP ECRAP ECARP CEARP AECRP EACRP CAERP ACERP

CAN **CAP** CAPE CAR CARE

## PCERA

PCERA CPERA EPCRA PECRA CEPRA ECPRA RCPEA CRPEA PRCEA RPCEA  
CPREA PCREA PERCA EPRCA RPECA PRECA ERPCA REPCA RECPA ERCPA  
CREPA RCEPA ECRPA CERPA AERPC EARPC RAEPC AREPC ERAPC REAPC  
PEARC EPARC APERC PAERC EAPRC AEPRC ARPEC RAPEC PAREC APREC  
RPAEC PRAEC PREAC RPEAC EPRAC PERAC REPAC ERPAC CRPAE RCPAE  
PCRAE CPRAE RPCAE PRCAE ARCPE RACPE **CARPE** ACRPE RCAPE CRAPE  
CPARE PCARE ACPRE **CAPRE** PACRE APCRE APRCE PARCE RAPCE ARPCE  
PRACE RPACE EPACR PEACR AEPCR EAPCR PAECR APECR CPEAR PCEAR  
ECPAR CEPAR PECAR EPCAR EACPR AECPR CEAPR ECAPR ACEPR CAEPR  
**CAPER** ACPER PCAER CPAER APCER PACER RACEP ARCEP CRAEP RCAEP  
ACREP **CAREP** EARCP AERCP REACP ERACP ARECP RAECR RCEAP CREAP  
ERCAP RECAP CERAP ECRAP ECARP CEARP AECRP EACRP CAERP ACERP

CAN **CAP** **CAPE** **CAR** **CARE** CLAP

## PCERA

PCERA CPERA EPCRA PECRA CEPRA ECPRA RCPEA CRPEA PRCEA RPCEA  
CPREA PCREA PERCA EPRCA RPECA PRECA ERPCA REPCA RECPA ERCPA  
CREPA RCEPA ECRPA CERPA AERPC EARPC RAEPC AREPC ERAPC REAPC  
PEARC EPARC APERC PAERC EAPRC AEPRC ARPEC RAPEC PAREC APREC  
RPAEC PRAEC PREAC RPEAC EPRAC PERAC REPAC ERPAC CRPAE RCPAE  
PCRAE CPRAE RPCAE PRCAE ARCPE RACPE **CARPE** ACRPE RCAPE CRAPE  
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ECPAR CEPAR PECAR EPCAR EACPR AECPR CEAPR ECAPR ACEPR CAEPR  
**CAPER** ACPER PCAER CPAER APCER PACER RACEP ARCEP CRAEP RCAEP  
ACREP **CAREP** EARCP AERCP REACP ERACP ARECP RAECR RCEAP CREAP  
ERCAP RECAP CERAP ECRAP ECARP CEARP AECRP EACRP CAERP ACERP

CAN **CAP CAPE CAR CARE** CLAP EACH

# PCERA

PCERA CPERA EPCRA PECRA CEPRA ECPRA RCPEA CRPEA PRCEA RPCEA  
CPREA PCREA PERCA EPRCA RPECA PRECA ERPCA REPCA RECPA ERCPA  
CREPA RCEPA ECRPA CERPA AERPC **EARPC** RAEP C AREPC ERAPC REAPC  
PEARC EPARC APERC PAERC EAPRC AEPRC ARPEC RAPEC PAREC APREC  
RPAEC PRAEC PREAC RPEAC EPRAC PERAC REPAC ERPAC CRPAE RCPAE  
PCRAE CPRAE RPCAE PRCAE ARCPE RACPE **CARPE** ACRPE RCAPE CRAPE  
CPARE PCARE ACPRE **CAPRE** PACRE APCRE APRCE PARCE RAPCE ARPCE  
PRACE RPACE EPACR PEACR AEPCR EAPCR PAECR APECR CPEAR PCEAR  
ECPAR CEPAR PECAR EPCAR EACPR AECPR CEAPR ECAPR ACEPR CAEPR  
**CAPER** ACPER PCAER CPAER APCER PACER RACEP ARCEP CRAEP RCAEP  
ACREP **CAREP** EARCP AERCP REACP ERACP ARECP RAEC P RCEAP CREAP  
ERCAP RECAP CERAP ECRAP ECARP CEARP AECRP EACRP CAERP ACERP

CAN **CAP** CAPE CAR CARE CLAP EACH **EAR**

## PCERA

PCERA CPERA EPCRA PECRA... ( $5! = 120$ )

## NPCERA

NPCERA PNCERA CNPERA NCPERA... ( $6! = 720$ )

## NPCERAH

NPCERAH PNCERAH CNPERAH NCPERAH... ( $7! = 5,040$ )

$O(k): k!$

## Factorial

$$4! = 24$$

$$5! = 120$$

$$6! = 720$$

$$7! = 5,040$$

$$8! = 40,320$$

$$9! = 362,880$$

$$10! = 3,628,800$$

$$11! = 39,916,800$$

$$12! = 479,001,600$$

$$13! = 6,227,020,800$$

$$14! = 87,178,291,200$$

$$15! = 1,307,674,368,000$$

**The worst part is, we can't just do this permutation once.**

**Above 11 or 12 characters, that'd be too many strings to hold in memory all at once.**

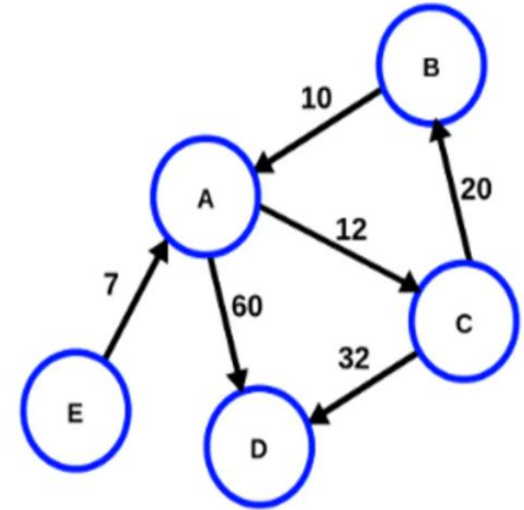
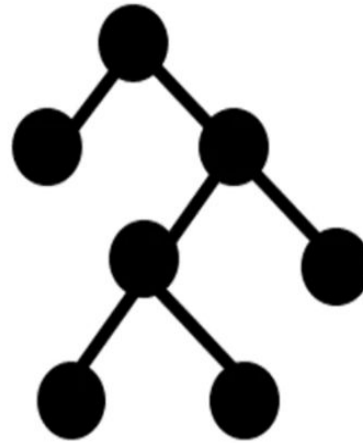
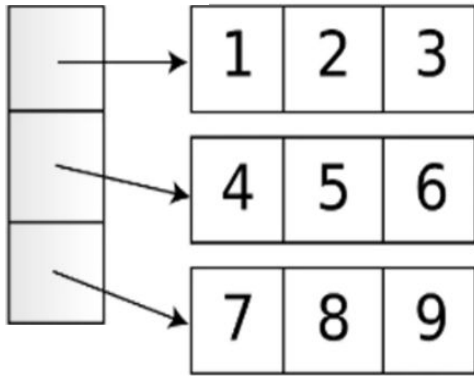
**So we're going to have to re-permute input for each word we check.  $O(n * k!)$**



**Actually, it's not that bad. (but it's still bad)**

**Permutation of the input can stop  
once the length of the word is  
reached.**

**Also, we can abandon any partial  
permutation result that doesn't  
match the beginning of each word.**



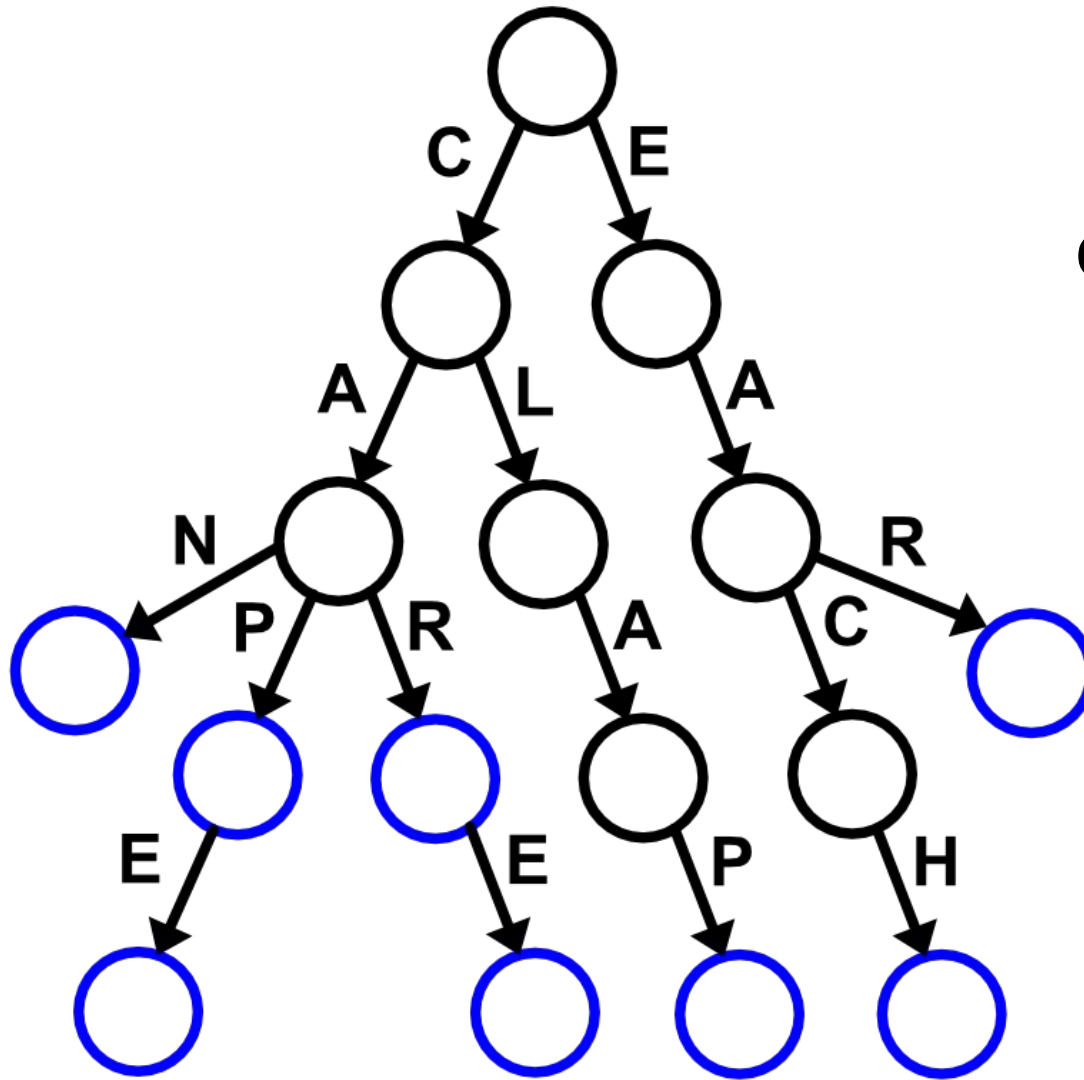
Data Structures

# Trie

CAN  
CAP  
CAPE  
CAR  
CARE  
CLAP  
EACH  
EAR

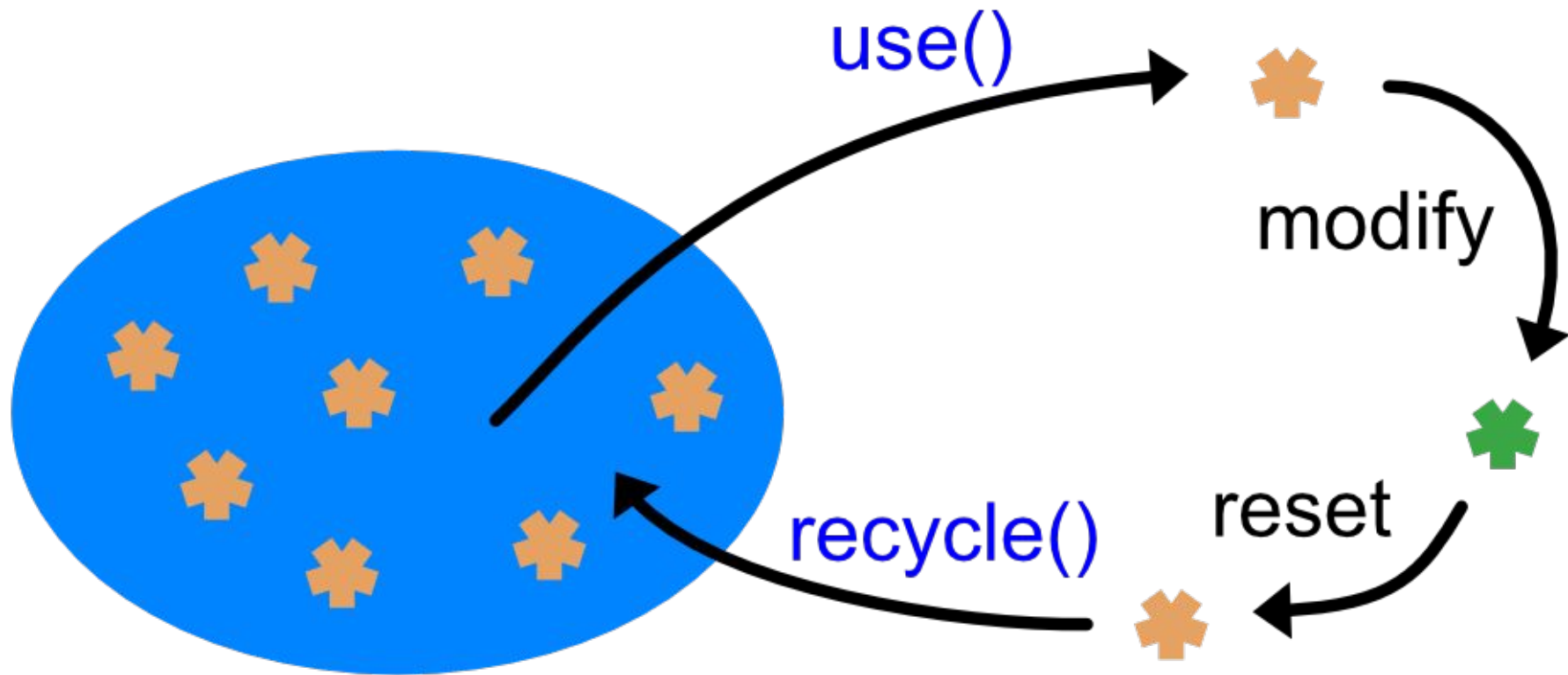
**$O(k): k * m$**

# Linear

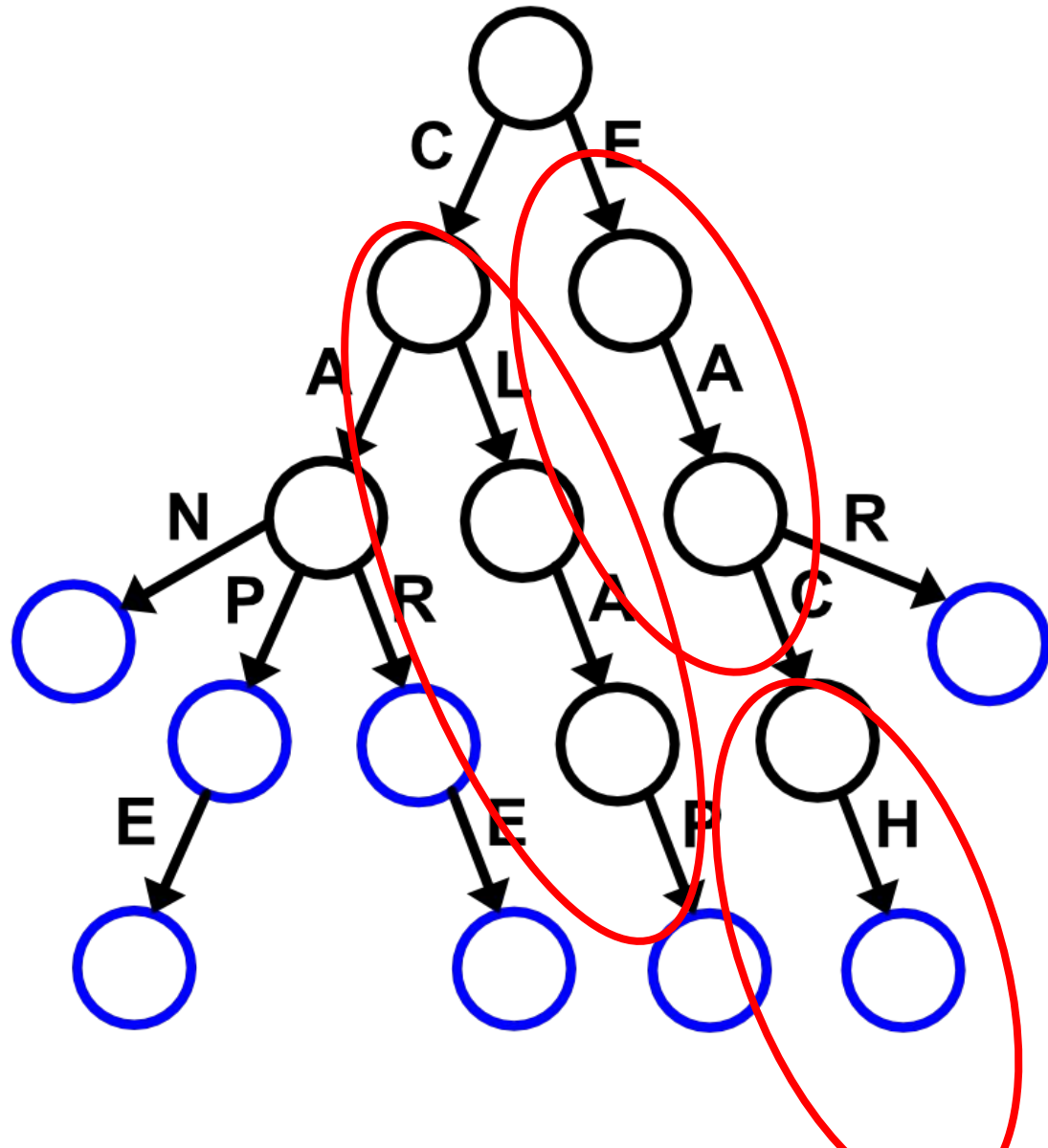




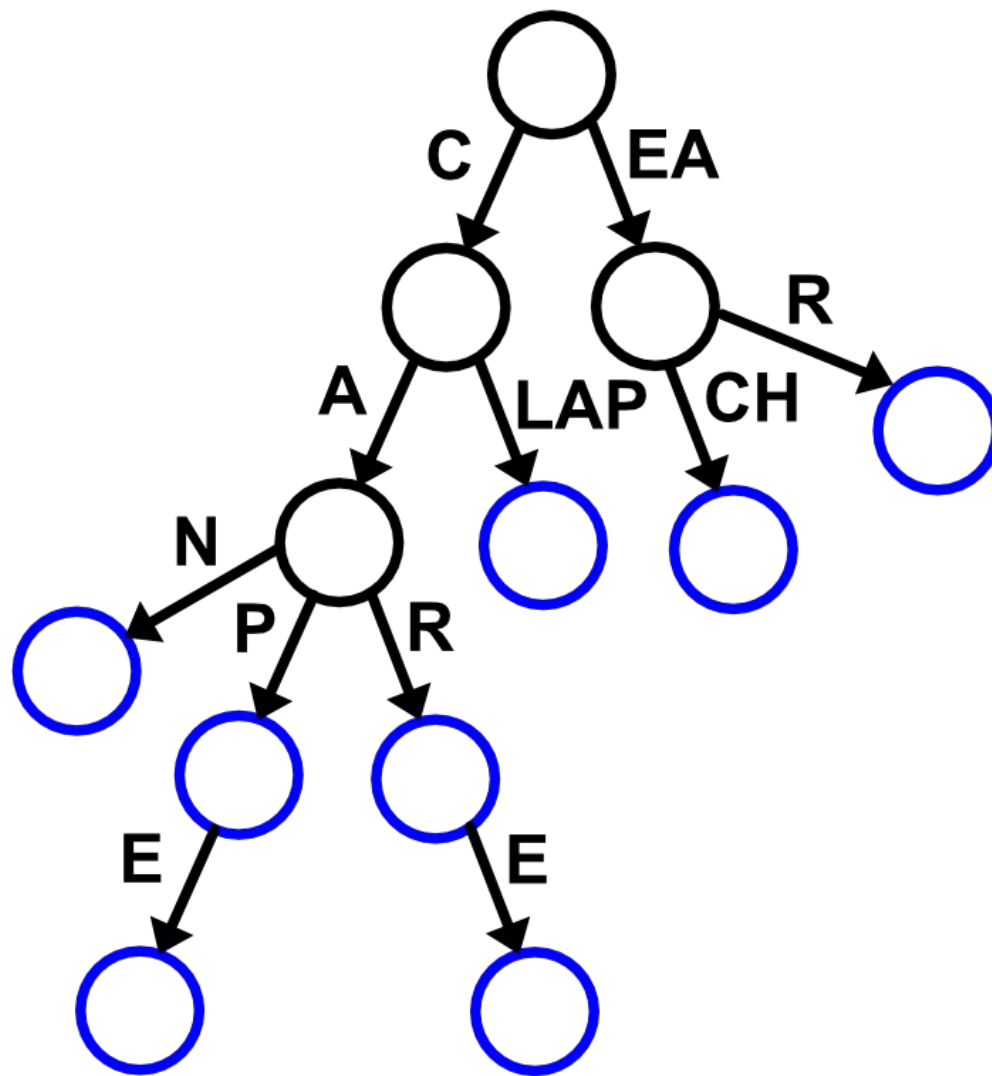
Minimizing Garbage Collection



Object Pool

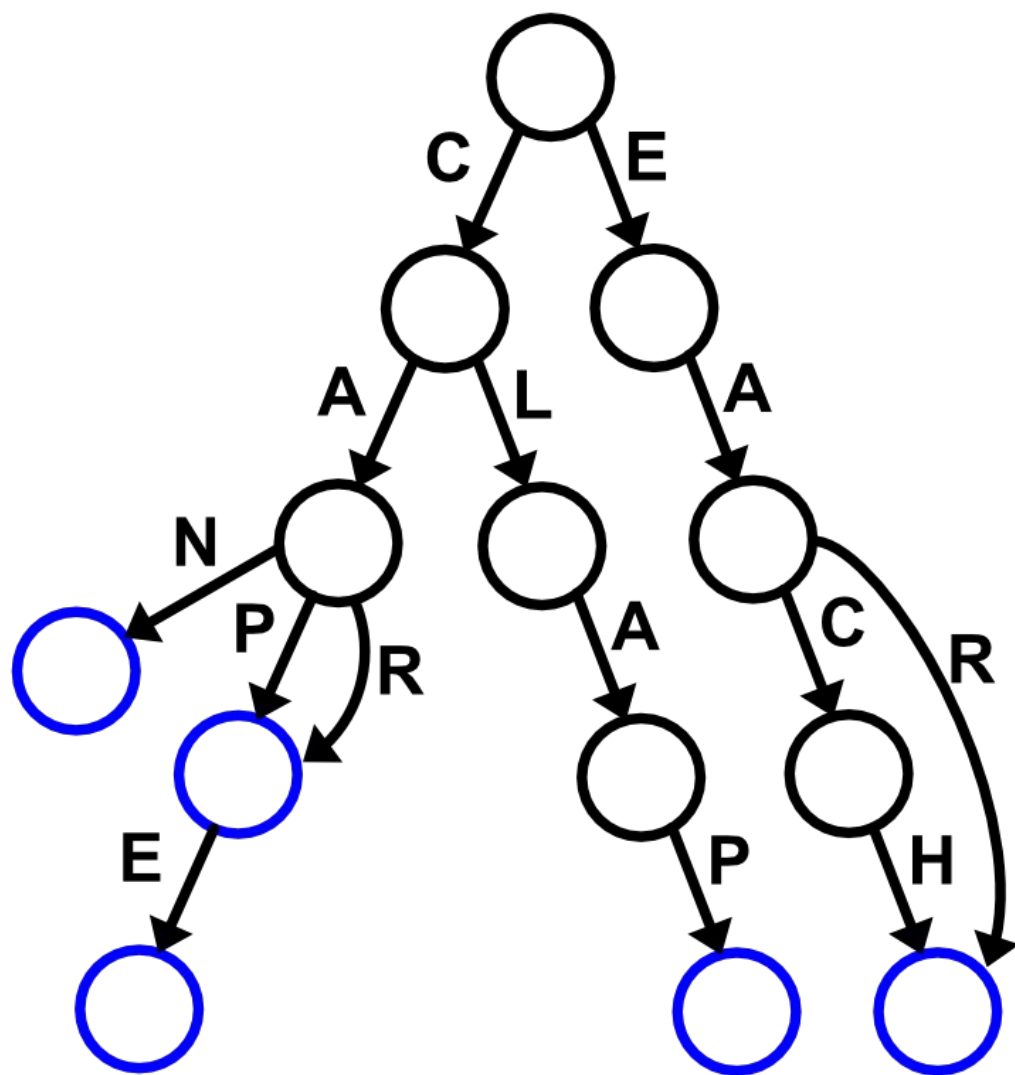


CAN  
CAP  
CAPE  
CAR  
CARE  
CLAP  
EACH  
EAR



Radix  
Tree

CAN  
CAP  
CAPE  
CAR  
CARE  
CLAP  
EACH  
EAR



DAFSA /  
DAWG



\_ H \_ \_ \_



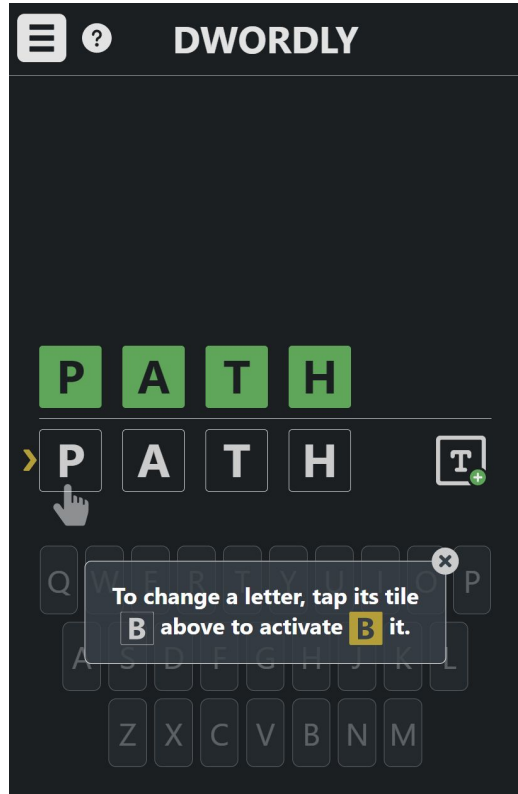
explain

e xplain  
xe plain  
pxe lain  
lpxe ain  
alpxe in  
ialpxe n  
nialpxe

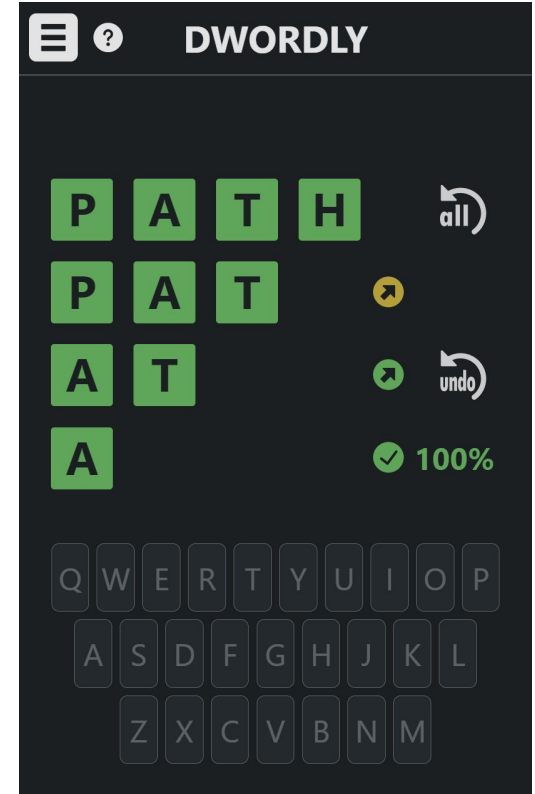
GADDAG

<https://en.wikipedia.org/wiki/GADDAG>





Bonus:  
Dwordly



<https://dwordly.fun>

The End