



$$P(x) = C_0 + C_1(x - x_0) + C_2(x - x_0)(x - x_1) + C_3(x - x_0)(x - x_1)(x - x_2)$$

$$P(x) = 8 - 2(x + 2)$$

$$= 4 - 2x$$

$$f(x) = 3x^3 + x^2 - x - 5 \quad f'(x) = 9x^2 + 2x - 1$$

$$x(n+1) = x(n) - \frac{f(x(n))}{f'(x(n))}$$

$$x(0) = -1$$

$$x(1) = -1 - \frac{f(-1)}{f'(-1)} = 0$$

$$x(2) = -5$$

$$x(3) = -5.564$$

$$x(4) = -2.25$$

$$x(5) = -1.45$$

$$x(6) = -0.753$$

$$x(7) = -1.15$$

$$x(8) = -1.169$$

$$x(9) = -1.169 \Rightarrow f(x(9)) \approx 0$$



$$2.36 \quad 0.85866$$

$$2.37 \quad 0.86289$$

$$2.38 \quad 0.8671$$

$$2.39 \quad 0.87129$$

$$f'(x) \approx \frac{f(x) - f(x-h)}{h} \leftarrow \text{Backwards diff}$$

$$f'(x) \approx \frac{f(x+h) - f(x)}{h} \leftarrow \text{Forwards diff}$$

$$f'(x) \approx \frac{f(x+h) - f(x-h)}{2h} \leftarrow \text{Central diff}$$

$$\text{BD} \rightarrow f'(2.38) = \frac{0.8671 - 0.86289}{0.1} = 0.419$$

$$\text{FD} \rightarrow f'(2.38) = \frac{0.87129 - 0.8671}{0.1} = 0.4209$$

$$\text{CD} \rightarrow f'(2.38) = \frac{0.87129 - 0.86289}{0.2} = 0.422$$

$$\text{BD} f''(x) = \frac{f(x) - f(x-h) - f(x-h) - f(x-2h)}{h}$$

$$\text{BD} f''(2.38) = -0.0019$$

$$\int_a^b f(x) dx = \frac{b-a}{6} \left( f(a) + 4f\left(\frac{a+b}{2}\right) + f(b) \right)$$

$$\int_0^1 x^2 dx = \int_0^{0.5} x^2 dx + \int_{0.5}^1 x^2 dx = 0.333$$

$$= \sum_{i=0}^{n-1} \int_{i/n}^{(i+1)/n} x^2 dx$$

$$\sum_{i=0}^n \int_{i/n}^{(i+1)/n} x^2 dx = \sum_{i=0}^n \frac{(i+1)/n - i/n}{6} \left( f\left(\frac{i}{n}\right) + 4f\left(\frac{i}{n} + \frac{1}{2n}\right) + f\left(\frac{i+1}{n}\right) \right)$$