

18. Median of Two sorted arrays

Hard Accuracy: 46.21% Submissions: 11054 Points: 8

Given two sorted arrays of sizes **N** and **M** respectively. The task is to find the median of the two arrays when they get merged.

Example 1:

Input:

N = 5, M = 6

arr[] = {1,2,3,4,5}

brr[] = {3,4,5,6,7,8}

Output: 4

Explanation: After merging two arrays,
elements will be as 1 2 3 3 4 4 5 5 6 7 8
So, median is 4.

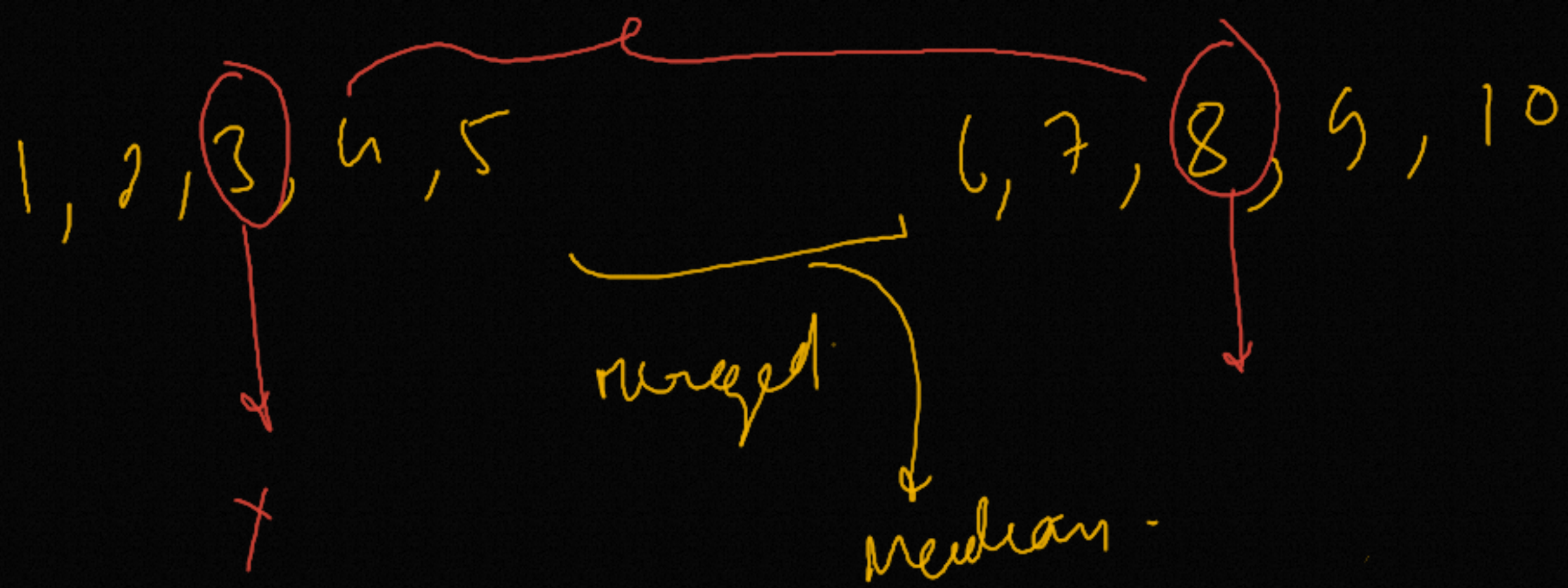
→ In $O(\log(\max(m,n)))$ & $O(1)$ S.

Algorithm: →

- ① We will calculate median of both the arrays and would discard one half of each array.
- ② Recursive fn. findMedianUtil → with 3 broad corner cases.

```
int idxA = ( N - 1 ) / 2;  
int idxB = ( M - 1 ) / 2;  
  
/* if A[idxA] <= B[idxB], then median must exist in  
   A[idxA....] and B[....idxB] */  
if (A[idxA] <= B[idxB] )  
    return findMedianUtil(A + idxA, N/2 + 1, B, M - idxA );  
  
/* if A[idxA] > B[idxB], then median must exist in  
   A[...idxA] and B[idxB....] */  
return findMedianUtil(A, N/2 + 1, B + idxA, M - idxA );  
}
```

→ can also take $idxA$.



Efficient: $O(\log n_1)$ where $n_1 \leq n_2$

$n_1 = 5$ $a_1[] = \{10, 20, 30, 40, 50\}$

$n_2 = 9$ $a_2[] = \{5, 15, 25, 35, 45, 55, 65, 75, 85\}$

$n_1 + n_2 = 14$

→ ① We know i_1 in this, and we can determine i_2 such that the whole array $(n_1 + n_2)$ is divided into 2 parts using this formula

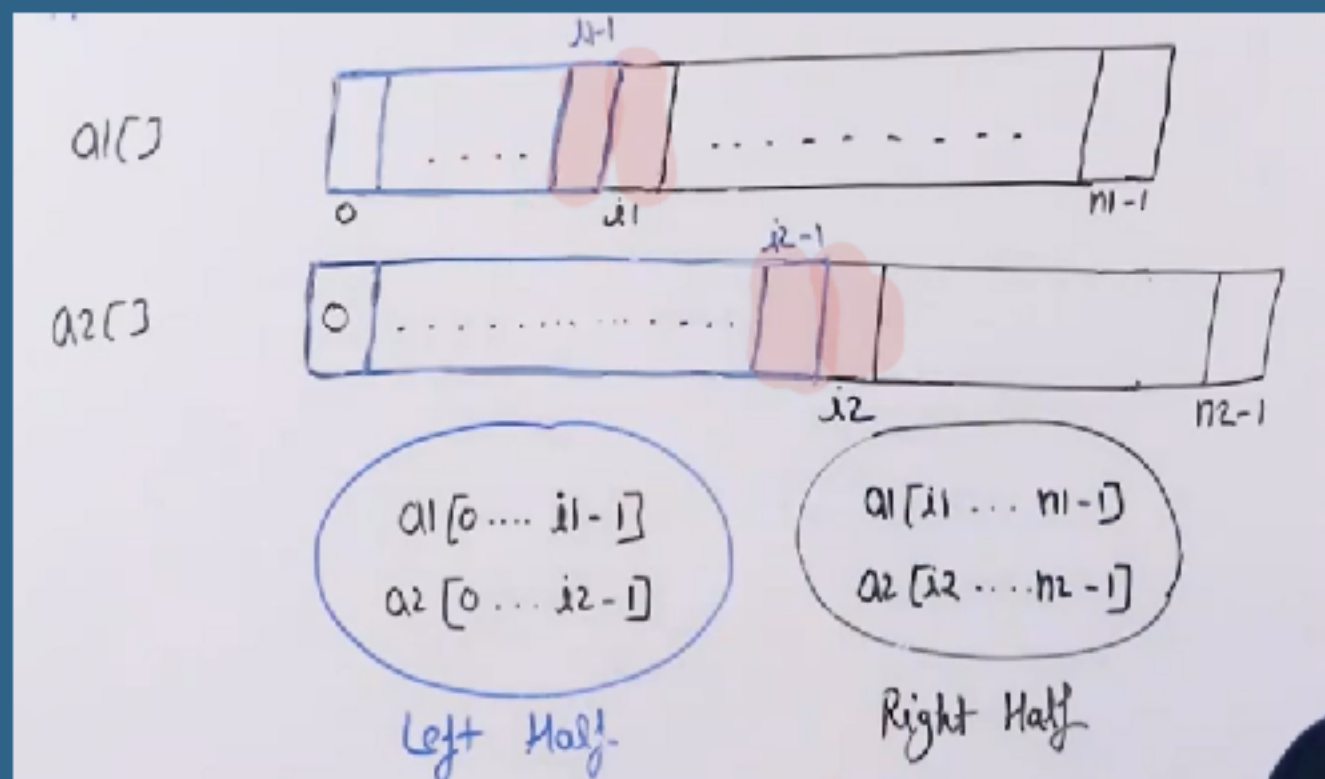
$$i_2 = \left\lceil \frac{n_1 + n_2 + 1}{2} \right\rceil - i_1$$

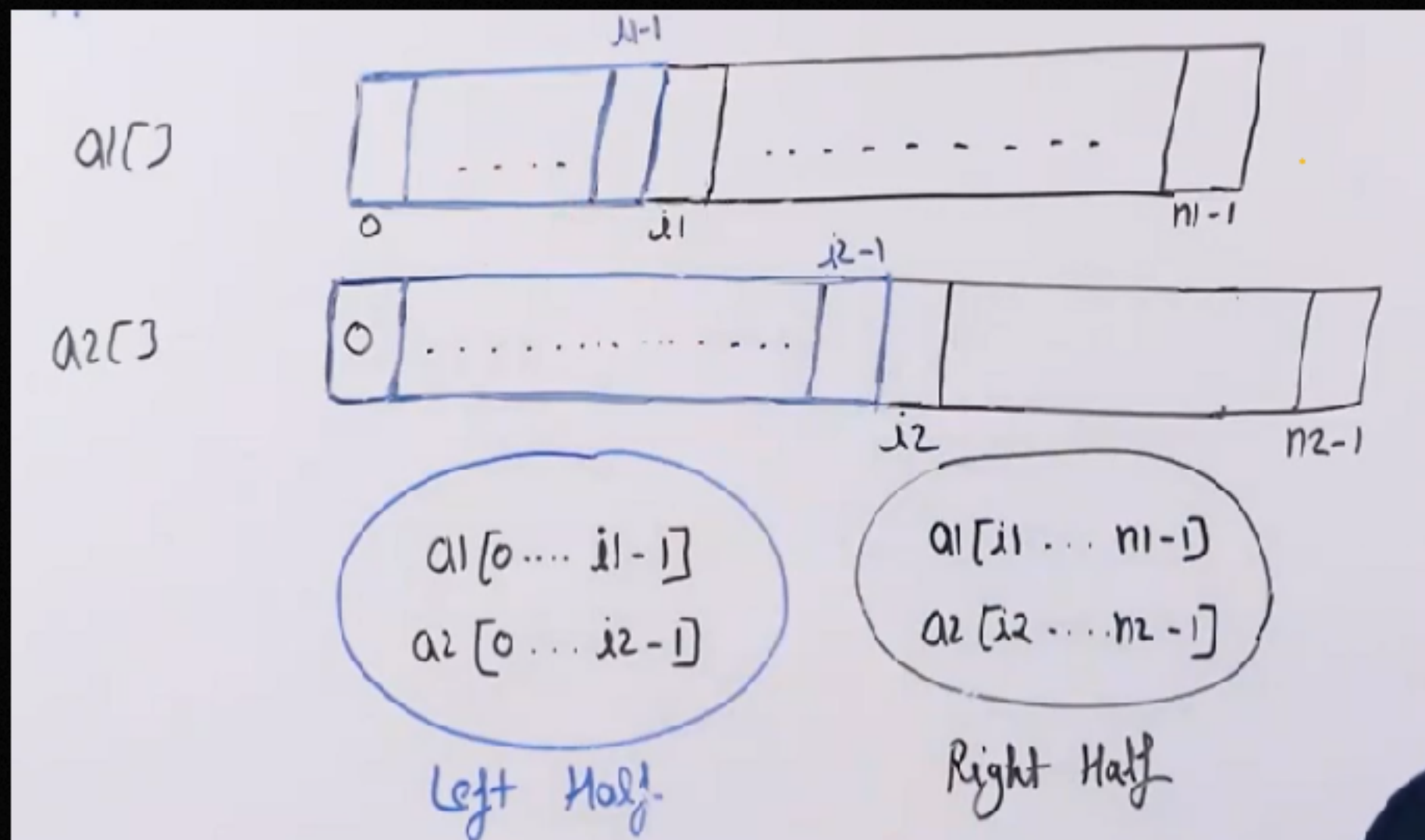
① We've to get to the condition when all the elements in blue set are smaller than the ones in right set.

② At this point we could calculate our median.

③ But when such sets are obtained we compute median using max of the largest element of blue set and smallest element of black set.

→ Based on these 2 values we make decision of our binary search's proceeding.





Coding the solution :-
 We maintain 4 variables

$\left\{ \begin{array}{ll} \text{min 1} & i_1 \\ \text{max 1} & i_1 - 1 \end{array} \right.$
 $\left\{ \begin{array}{ll} \text{min 2} & i_2 \\ \text{max 2} & i_2 - 1 \end{array} \right.$

⊛ Based on these 4 elements we do our binary search

max → blue set

min → Back set

```
double getMed(int a1[], int a2[], int n1,  
              int n2)
```

```
{  
    int begin1 = 0, end1 = n1;  
    while(begin1 <= end1)
```

```
{  
    int i1 = (begin1 + end1) / 2;  
    int i2 = (n1 + n2 + 1) / 2 - i1;  
    int mini = (i1 == n1) ? INT_MAX : a1[i1];  
    int maxi = (i1 == 0) ? INT_MIN : a1[i1 - 1];  
    int min2 = (i2 == n2) ? INT_MAX : a2[i2];  
    int max2 = (i2 == 0) ? INT_MIN : a2[i2 - 1];
```

```
    if (max1 <= min2 && max2 <= mini)  
    {  
        if ((n1 + n2) % 2 == 0)  
            return ((double) max(max1, max2) +  
                    min(min1, min2)) / 2;  
        else  
            return (double) max(max1, max2);  
    }
```

```
    else if (max1 > min2) end1 = i1 - 1;  
    else begin1 = i1 + 1;  
}
```

→ computing i_1 & i_2

→ values on the right side

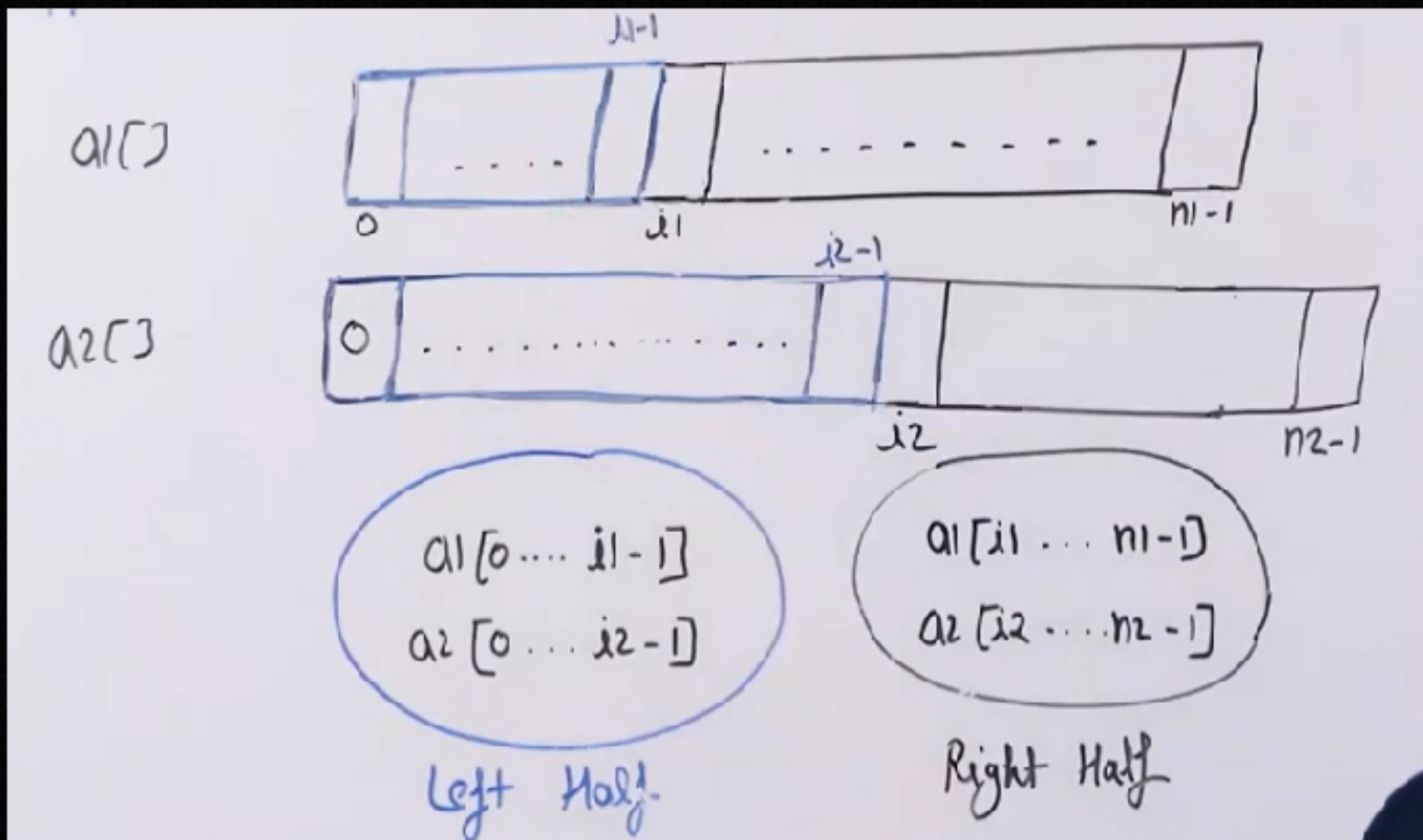
→ values on left side

other way $i_1, i_1 - 1, i_2, i_2 - 1$

Since the array is sorted:

① $max1 \leq min2$

$max2 \leq min1$



$max1 \rightarrow i1-1$ $min1 \rightarrow i2$
 $max2 \rightarrow i2-1$ $min2 \rightarrow i2$

check condition \rightarrow

$$\left\{ \begin{array}{l} max1 \leq min2 \\ max2 \leq min1 \end{array} \right\}$$

violated; min has check

violated
 \hookrightarrow end $\rightarrow i1-1$

\leftarrow all the elements till $max1$
 not smaller than
 therefore we call $min2$

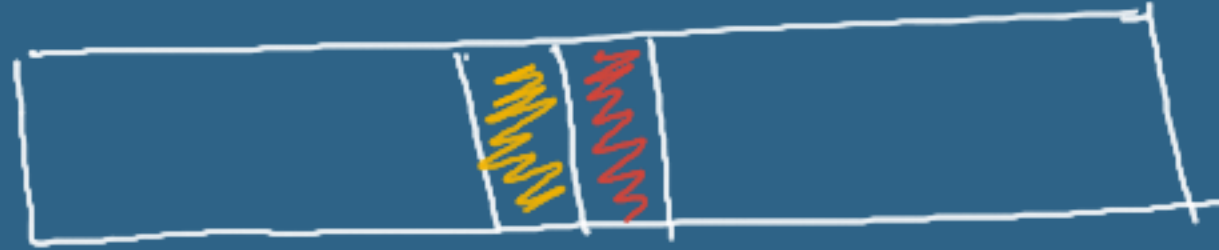
⊗ Beginning $\rightarrow i1+1$

① Given 2 arrays, we need to find their median, when merged, given both of their arrays are sorted.

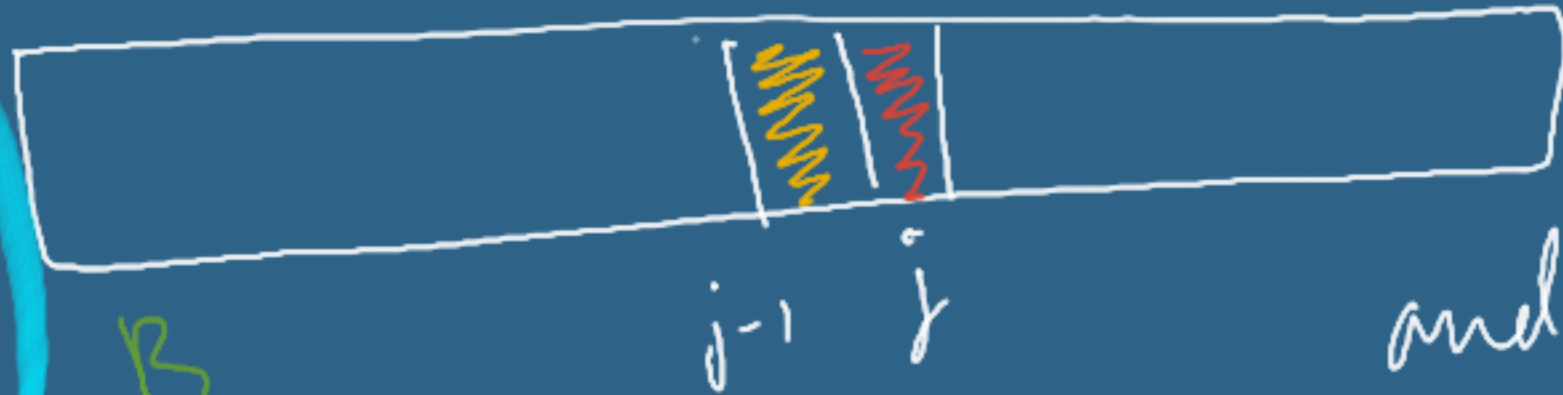
② Approach → To find 2 such points that, could divide combined array elements $(m+n)$ into 2 halves.

③

A



B



We're gonna be calculating position of i & j based on comparisons with the bigger array

and do keep in mind

with every iteration indices
would be recalculated for
both the arrays.

formula used to divide the arrays in half the element is

$$i_2 = \frac{(n_1 + n_2 + 1)}{2} - i_1$$

A \rightarrow smaller array \rightarrow

① begin = 0 end = n.

② while begin < end

$\hookrightarrow i_1 = \text{begin} + \text{end} / 2 \quad i_2 = \frac{n_1 + n_2 + 1}{2} \cdot j_1$

③ A \rightarrow min1 \rightarrow INT-MAX ($i_1 := n_1$) else a[i1]
max1 \rightarrow INT-MIN ($i_2 := 0$) else a[i1-1]

④ B \rightarrow min2 \rightarrow INT-MAX ($i_2 := n_2$) else B[i2]
max2 \rightarrow INT-MAX ($i_2 := 0$) INT-MIN else B[i2-1]

⑤ if $(\max_1 \leq \min_2 \text{ \& \& } \max_2 \leq \min_1) \rightarrow \text{perfect partition}$

{ if $(n_1 + n_2) \% 2 \neq 0 \rightarrow \text{false}$

return $(\text{double}(\frac{\max(\max_1, \max_2) + \min(\min_1, \min_2)}{2}))$

else
return $(\text{double}) \max(\max_1, \max_2)$

1) { else initialize the pointers of arrays

$\max_1 > \min_2$

$\max_2 > \min_1$

$\leftarrow \text{end} = i - 1$

$\rightarrow \text{min} \rightarrow \text{begin} = i + 1$