

## 17. Rearrange an array with O(1) extra space

Medium Accuracy: 54.65% Submissions: 20753 Points: 4

Given an array `arr[]` of size `N` where every element is in the range from `0` to `n-1`. Rearrange the given array so that `arr[i]` becomes `arr[arr[i]]`.

### Example 1:

#### Input:

`N = 2`

`arr[] = {1,0}`

**Output:** `0 1`

#### Explanation:

`arr[arr[0]] = arr[1] = 0.`

`arr[arr[1]] = arr[0] = 1.`

Here, We will use the formula **Dividend = Divisor \* Quotient + Remainder**

where Divisor = size of array

Quotient = New number at index `i` after rearrangement

Remainder = Old Number at index `i` before rearrangement

Dividend = The number stored at index `i`

While Traversing the array, we will Look for the value at `arr[arr[i]]` (which is to be stored at index `i`), multiply it with Divisor (size of array), and add the old value present at `arr[i]` to it. Divisor is a value which is higher than values in array (in this case `n` - size of array, as array elements are between `0` to `n-1`)

Obviously, don't forget to remove the multiplier `n` from the values while accessing and outputting the new values.

Calculated

array size

old number =  $\text{Dividend} \% n$

$$\text{Dividend} = \text{Divisor} * \text{Quotient} + \text{Remainder}$$

Quotient =  $\frac{\text{Dividend} - \text{Remainder}}{\text{Divisor}}$

new no. at `i` after rearrangement

$$= \frac{\text{No. at arr[i]} - \text{old No.}}{\text{array size}}$$

### Algorithm:

1. Traverse the array from start to end.
2. For every index increment the element by  $array[array[index]] \% n$ . To get the  $i$ th element find the modulo with  $n$ , i.e.  $array[index] \% n$ .
3. Again Traverse the array from start to end
4. Store the  $i$ th element after dividing the  $i$ th element by  $n$ , i.e.  $array[i]/n$

$$\text{Divident} = \text{Divisor} \times \text{Quotient} + \text{Rem}$$

**Approach:** The array elements of the given array lies from 0 to  $n-1$ . Now an array element is needed that can store two different values at the same time. To achieve this increment every element at  $i$ th index is incremented by  $(arr[arr[i]] \% n) * n$ . After the increment operation of first step, every element holds both old values and new values. Old value can be obtained by  $arr[i] \% n$  and a new value can be obtained by  $arr[i]/n$ .

$$arr[i] = arr[i] + (arr[arr[i]] \% n) \times n$$

The diagram illustrates the decomposition of the expression  $arr[i] = arr[i] + (arr[arr[i]] \% n) \times n$ . Red arrows point from the terms in the equation to their respective parts in the decomposition below:

- An arrow from  $arr[i]$  points to old value i.e this.
- An arrow from  $(arr[arr[i]] \% n)$  points to Rem.
- An arrow from  $\times n$  points to Quotient.

The decomposition is shown as:

$$\frac{(arr[arr[i]] \% n)}{\text{Rem}} \quad \frac{(arr[arr[i]] / n)}{\text{Quotient}}$$

Algorithm:

1. Traverse the array from start to end.
2. For every index increment the element by  $\text{array}[\text{array}[\text{index}]] \% n$ . To get the  $i$ th element find the modulo with  $n$ , i.e.  $\text{array}[\text{index}] \% n$ .
3. Again Traversal the array from start to end
4. Print the  $i$ th element after dividing the  $i$ th element by  $n$ , i.e.  $\text{array}[i]/n$ .

$$\text{arr}[i] = \text{arr}[i] + \frac{\text{arr}[\text{arr}[i]]}{n}$$

0	1	2	3	4	5
1	2	3	4	0	4

$$1 + \{2 \times 1.5\} \times 5$$

$$11 / n \rightarrow 2$$

$$1 + \{11 \times 1.5\} \times 5$$

$$51 / 5 \rightarrow 10$$

$$\{a + b \% n\} \% n$$

↓  
i<sup>th</sup> element  
↓  
a



Algorithm:

$$y = a + \left\{ \overline{b \% n} \right\} \times n$$

$\downarrow$   $\searrow$

$arr[i]$   $arr[arr[i]]$

Given  $a \leq b \leq arr < n$

$\therefore b \% n \rightarrow b$  for unchanged  $arr[i]$  and would be  
diff for the one on which transformation

① has been applied

in our case

$y > n$ , and will give

$arr[i]$  original as answer.

$y \% n$

Basically the concept that we're using is

$$\text{Dividend} = \text{Divisor} \times \text{Quotient} + \text{Remainder}$$

↓  
 $n$

↓

↓

$arr[i]$

$arr[arr[i]]$

$\% n$

then  $arr[j] < n$

Simply  $arr[j]$   
if not transformed

else  $arr[j] \% n$

↓  
give Quotient

```
class Solution{
public:
    //Function to rearrange an array so that arr[i] becomes arr[arr[i]]
    //with O(1) extra space.
    void arrange(long long arr[], int n) {
        int i;

        //Increasing all values by (arr[arr[i]]%n)*n to store the new element.
        for(i=0;i<n;i++){
            arr[i]+=(arr[arr[i]]%n)*n;
        }

        //Since we had multiplied each element with n.
        //We will divide by n too to get the new element at that
        //position after rearranging.
        for(i=0;i<n;i++){
            arr[i]=arr[i]/n;
        }
    }
};
```