

Pythagorean Theorem

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$$AC^2 = AD \cdot AB$$

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$$AC^2 + BC^2 = AD \cdot AB + BD \cdot AB = (AD + BD) \cdot AB = AB^2$$



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$$a^2 + b^2 = c^2$$

Corollary

- *If $a^2 + b^2 = c^2$, then the triangle is right.*

Proof.

$$AC^2 = AD \cdot AB$$

$$BC^2 = BD \cdot AB$$

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$$a^2 + b^2 = c^2$$

Corollary

- If $a^2 + b^2 = c^2$, then the triangle is right.
- If $a^2 + b^2 > c^2$, then the triangle is acute.

Proof.

$$AC^2 = AD \cdot AB$$

$$BC^2 = BD \cdot AB$$

$$AC^2 + BC^2 = AD \cdot AB + BD \cdot AB = (AD + BD) \cdot AB = AB^2$$



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$$a^2 + b^2 = c^2$$

Corollary

- If $a^2 + b^2 = c^2$, then the triangle is right.
- If $a^2 + b^2 > c^2$, then the triangle is acute.
- If $a^2 + b^2 < c^2$, then the triangle is obtuse.

Proof.

$$AC^2 = AD \cdot AB$$

$$BC^2 = BD \cdot AB$$

$$AC^2 + BC^2 = AD \cdot AB + BD \cdot AB = (AD + BD) \cdot AB = AB^2$$

