TikZ 几何作图

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第1章 基本作图命令

这里的命令都是通过 /tikz/insert path[1] 在当前路径上插入新的路径.

1.1 仿射组合 Affine Combination

调用方式

```
affine={A,B,k}
```

参数说明

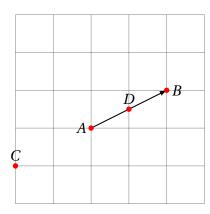
A,B 两点坐标

k 系数

返回点 A, B 的仿射组合: $A + k \cdot (B - A)$.

```
\draw[help lines] (0,0) grid (5,5);
\coordinate (A) at (2,2);
\coordinate (B) at (4,3);
\coordinate [affine={A,B,-1}] (C);
\coordinate [affine={A,B,.5}] (D);
\draw[thick, -latex] (A) -- (B);
\foreach \p/\placement in {A/left,B/right,
```

```
C/above,D/above}{
    \fill[red] (\p) circle (2pt);
    \draw (\p) node[\placement] {$\p$};
}
\end{tikzpicture}
```



1.2 中点 Midpoint

调用方式

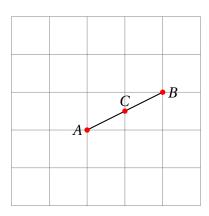
```
midpoint={A,B}
```

参数说明

A,B 两点坐标

返回点 A,B 的中点坐标.

```
\begin{tikzpicture}
\draw[help lines] (0,0) grid (5,5);
\coordinate (A) at (2,2);
```



1.3 平移 Translate

调用方式

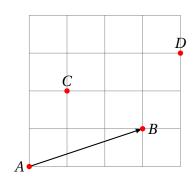
```
translate={A,B,C}
```

参数说明

A,B,C 三点坐标

返回 C 按向量 AB 移动所得的坐标: C + (B - A). 示例

```
\begin{tikzpicture}
  \draw[help lines] (0,0) grid (4,4);
  \coordinate (A) at (0,0);
  \coordinate (B) at (3,1);
  \coordinate (C) at (1,2);
  \coordinate [translate={A,B,C}] (D);
  \draw[thick, -latex] (A) -- (B);
  \foreach \p/\placement in
  - {A/left,B/right,C/above,D/above}{
    \fill[red] (\p) circle (2pt);
    \draw (\p) node[\placement] {$\p$};
}
\end{tikzpicture}
```



1.4 对称点 Reflect

调用方式

```
reflect={A,B,C}
```

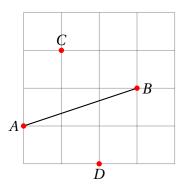
参数说明

A,B,C 三点坐标

1.5 投影 PROJECT 5

返回 C 关于直线 AB 的对称点的坐标 (设 D 为 C 在 AB 的投影): C+2(D-C). 示例

```
\begin{tikzpicture}
  \draw[help lines] (0,0) grid (4,4);
  \coordinate (A) at (0,1);
  \coordinate (B) at (3,2);
  \coordinate (C) at (1,3);
  \coordinate [reflect={A,B,C}] (D);
  \draw[thick] (A) -- (B);
  \draw[thick] (A) -- (B);
  \foreach \p/\placement in
  - {A/left,B/right,C/above,D/below}{
    \fill[red] (\p) circle (2pt);
    \draw (\p) node[\placement] {$\p$};
}
\end{tikzpicture}
```



1.5 投影 Project

调用方式

```
project={A,B,C}
```

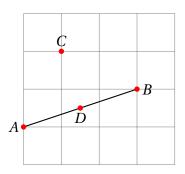
参数说明

A,B,C 三点坐标

返回 C 在直线 AB 的投影的坐标.

示例

```
\begin{tikzpicture}
  \draw[help lines] (0,0) grid (4,4);
  \coordinate (A) at (0,1);
  \coordinate (B) at (3,2);
  \coordinate (C) at (1,3);
  \coordinate [project={A,B,C}] (D);
  \draw[thick] (A) -- (B);
  \draw[thick] (A) -- (B);
  \foreach \p/\placement in
  - {A/left,B/right,C/above,D/below}{
    \fill[red] (\p) circle (2pt);
    \draw (\p) node[\placement] {$\p$};
}
\end{tikzpicture}
```



1.6 反演 Inverse

调用方式

1.6 反演 INVERSE

7

```
inverse={0,A,P}
```

参数说明

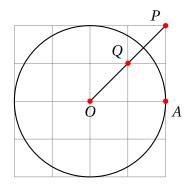
- 0 圆心
- A 圆上一点
- P 平面上任一点

返回 P 关于圆 (O, A) 的反演点.

```
\begin{tikzpicture}
\draw[help lines] (-2,-2) grid (2,2);
\coordinate (0) at (0,0);
\coordinate (A) at +(0:2); % 圆上一点,相对坐标
\coordinate (P) at (2,2);
\coordinate[inverse={0,A,P}] (Q);

\draw[thick,circle={0,A}];
\draw[thick] (0) -- (P);

\foreach \p/\placement in {0/below,A/below right,
P/above left,Q/above left}{
\fill[red] (\p) circle (2pt);
\draw (\p) node[\placement] {$\p$};
}
\end{tikzpicture}
```



1.7 旋转 Revolve

调用方式

revolve={A,B}

参数说明

A,B 两点坐标

注 为了避免覆盖 tikz 的 rotate, 这里将旋转命令为 revolve.

返回 B 绕 A 旋转的点.

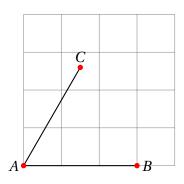
还需要指定 revolve/angle (default: 0) 和 revolve/angle scale(default: 1) 两个选项,可以通过下面的方式来指定 /revolve/angle:

- 1. 直接指定角度: revolve/angle=60
- 2. 位置向量与 x 轴夹角: revolve/angle={P1}
- 3. 两位置向量的夹角: revolve/angle={P1,P2}
- 4. 由三点定义的角 (P_1 为顶点, P_2 为起点, P_3 为终点): revolve/angle={P1,P2,P3}
- 5. 两向量的夹角 (逆时针方向): revolve/angle={P1,P2,P3,P4}

```
\begin{tikzpicture}
  \draw[help lines] (0,0) grid (4,4);
```

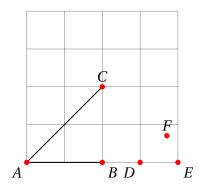
1.7 旋转 REVOLVE 9

```
\coordinate (A) at (0,0);
\coordinate (B) at (3,0);
\coordinate [revolve/angle=60, revolve={A,B}] (C);
\draw[thick] (A) -- (B) (A) -- (C);
\foreach \p/\placement in {A/left,B/right,C/above}{
  \fill[red] (\p) circle (2pt);
  \draw (\p) node[\placement] {$\p$};
}
\end{tikzpicture}
```



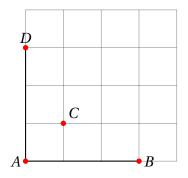
```
\begin{tikzpicture}
  \draw[help lines] (0,0) grid (4,4);
  \coordinate (A) at (0,0);
  \coordinate (B) at (2,0);
  \coordinate (C) at (2,2);
  \coordinate (D) at (3,0);
  \coordinate (E) at (4,0);
  \coordinate [revolve/angle={A,B,C},revolve={D,E}] (F);
  \draw[thick] (A) -- (B) (A) -- (C);
  \foreach \p/\placement in {
  A/below left,B/below right,C/above,
  D/below left,E/below right,F/above}{
```

```
\fill[red] (\p) circle (2pt);
\draw (\p) node[\placement] {$\p$};
}
\end{tikzpicture}
```



```
\begin{tikzpicture}
  \draw[help lines] (0,0) grid (4,4);
  \coordinate (A) at (0,0);
  \coordinate (B) at (3,0);
  \coordinate (C) at (1,1);
  \coordinate [revolve/angle={C},
    revolve/scale=2,
    revolve={A,B}] (D);
  \draw[thick] (A) -- (B) (A) -- (D);
  \foreach \p/\placement in {A/left,B/right,
    C/above right,D/above}{
    \fill[red] (\p) circle (2pt);
    \draw (\p) node[\placement] {$\p$};
  }
  \end{tikzpicture}
```

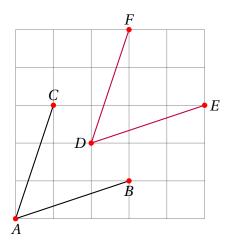
1.8 构造角 ANGLE 11



1.8 构造角 Angle

可以由 resovle 来构造一个角. 示例

```
\begin{tikzpicture}[scale=1]
 \draw[help lines] (0,0) grid (5,5);
 \coordinate (A) at (0,0);
 \coordinate (B) at (3,1);
  \coordinate (C) at (1,3);
  \coordinate (D) at (2,2);
  \coordinate (E) at (5,3);
  \coordinate [revolve/angle={A,B,C},
   revolve/scale=1,
   revolve={D,E}] (F);
  \draw[thick] (A) -- (B) (A) -- (C);
 \draw[thick, purple] (D) -- (E) (D) -- (F);
  \foreach \p/\placement in {A/below,B/below,C/above,
 D/left,E/right,F/above}{
    \fill[red] (\p) circle (2pt);
    \node[\placement] at (\p) {$\p$};
 }
\end{tikzpicture}
```



1.9 角平分线 Angle Bisector

调用方式

```
angle bisector={A,B,C}
```

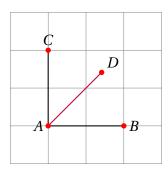
参数说明

A,B,C 三点坐标, A 为顶点 (apex), B 为起点, C 为终点返回 $\angle BAC$ 角平分线上的一点. 实际上, 该操作等价于:

```
revolve/angle={A,B,C}, revolve/scale=.5, revolve={A,B}
```

```
\begin{tikzpicture}
  \draw[help lines] (0,0) grid (4,4);
  \coordinate (A) at (1,1);
  \coordinate (B) at (3,1);
  \coordinate (C) at (1,3);
```

```
\coordinate [angle bisector={A,B,C}] (D);
\draw[thick] (A) -- (B) (A) -- (C);
\draw[thick, purple] (A) -- (D);
\foreach \p/\placement in {A/left,B/right,C/above,
D/above right}{
  \fill[red] (\p) circle (2pt);
  \draw (\p) node[\placement] {$\p$};
}
\end{tikzpicture}
```



1.10 等边三角形 Equilateral Triangle

调用方式

```
equilateral={A,B}
```

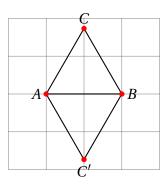
参数说明

A,B 两点坐标

返回以 AB 为边长的等边三角形的第 3 点 (位于向量 AB 的左侧). 实际上, 该操作等价于:

```
revolve/angle=60, revolve={A,B}
```

示例



1.11 旋转 90° Erect

调用方式

```
erect={A,B}
```

15

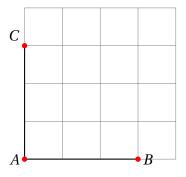
参数说明

A,B 两点坐标

返回 B 绕 A 旋转 90° 的坐标. 实际上, 该操作等价于:

```
revolve/angle=90, revolve={A,B}
```

```
\begin{tikzpicture}
  \draw[help lines] (0,0) grid (4,4);
  \coordinate (A) at (0,0);
  \coordinate (B) at (3,0);
  \coordinate [erect={A,B}] (C);
  \draw[thick] (A) -- (B) (A) -- (C);
  \foreach \p/\placement in {A/left,B/right,C/above
  - left}{
    \fill[red] (\p) circle (2pt);
    \draw (\p) node[\placement] {$\p$};
  }
  \end{tikzpicture}
```



1.12 截取 Intercept

调用方式

```
intercept={A,B}
```

参数说明

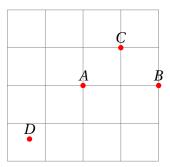
A,B 两点坐标

在直线 AB 截取指定长度线段, A 为新线段的起点, AB 是方向.

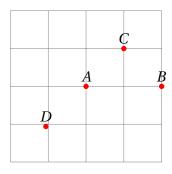
需要指定 intercept/length (default: 1cm) 和 intercept/scale(default: 1) 两个选项. 其中 intercept/length 有两种形式:

- 1. 直接指定长度: intercept/length=2cm
- 2. 指定线段长度: intercept/length={P1,P2}

```
\begin{tikzpicture}
  \draw[help lines] (-2,-2) grid (2,2);
  \coordinate (A) at (0,0);
  \coordinate (B) at (2,0);
  \coordinate (C) at (1,1);
  \coordinate[intercept/length={A,B},
    intercept/scale=-1, intercept={A,C}] (D);
  \foreach \p/\placement in
  - {A/above,B/above,C/above,D/above}{
    \fill[red] (\p) circle (2pt);
    \draw (\p) node[\placement] {$\p$};
}
\end{tikzpicture}
```



```
\draw[help lines] (-2,-2) grid (2,2);
\coordinate (A) at (0,0);
\coordinate (B) at (2,0);
\coordinate (C) at (1,1);
\coordinate[intercept/length=1.5cm,
    intercept/scale=-1,
    intercept={A,C}] (D);
\foreach \p/\placement in
    - {A/above,B/above,C/above,D/above}{
    \fill[red] (\p) circle (2pt);
    \draw (\p) node[\placement] {$\p$};
}
\end{tikzpicture}
```



1.13 直线与直线的交点 Line-Line Intersection

调用方式

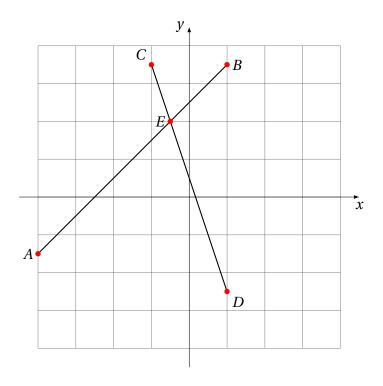
```
intersect={A,B,C,D}
```

参数说明

A,B,C,D 四点坐标

返回 AB 与 CD 的交点 (可以是延长线相交点).

```
\begin{tikzpicture}
 \draw[help lines] (-4,-4) grid[step=1] (4,4);
 \frac{-1atex}{-4.5,0} -- (4.5,0) node[below] {$x$};
  \frac{-\text{latex}}{0,-4.5} -- (0,4.5) node [left] \{\$y\$\};
 \coordinate (A) at (-4,-1.5);
  \coordinate (B) at (1,3.5);
 \coordinate (C) at (-1,3.5);
  \coordinate (D) at (1,-2.5);
  \coordinate [intersect={A,B,C,D}] (E);
  \draw[thick] (A) -- (B) (C) -- (D);
  \foreach \p/\placement in {A/left,B/right,
 C/above left,D/below right,E/left}{
    \fill[red] (\p) circle (2pt);
    \draw (\p) node[\placement] {$\p$};
 }
\end{tikzpicture}
```



1.14 垂直平分线/中垂线 Perpendicular Bisector

调用方式

```
perpendicular bisector={A,B}
```

参数说明

A,B 两点坐标

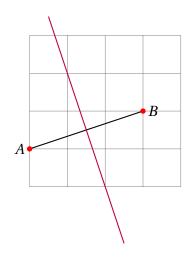
构造 AB 的中垂线, 默认起点为 $.5(A+B)+(B-A)\cdot \mathbf{i}$, 终点为 $.5(A+B)-(B-A)\cdot \mathbf{i}$. 可以对起始点进行调整, 见1.23.

示例

使用默认参数:

```
\begin{tikzpicture}
  \draw[help lines] (0,0) grid (4,4);
```

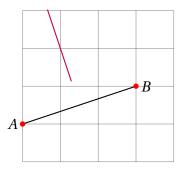
```
\coordinate (A) at (0,1);
\coordinate (B) at (3,2);
\draw[thick] (A) -- (B);
\draw[thick,purple,perpendicular bisector={A,B}];
\foreach \p/\placement in {A/left,B/right}{
  \fill[red] (\p) circle (2pt);
  \draw (\p) node[\placement] {$\p$};
}
\end{tikzpicture}
```



指定两端的长度:

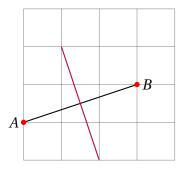
```
\begin{tikzpicture}
  \draw[help lines] (0,0) grid (4,4);
  \coordinate (A) at (0,1);
  \coordinate (B) at (3,2);
  \draw[thick] (A) -- (B);
  \draw[thick, purple,
    start modifier=.5cm, end modifier=2.5cm,
    perpendicular bisector={A,B}];
```

```
\foreach \p/\placement in {A/left,B/right}{
   \fill[red] (\p) circle (2pt);
   \draw (\p) node[\placement] {$\p$};
}
\end{tikzpicture}
```



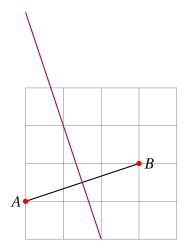
指定系数:

```
\begin{tikzpicture}
  \draw[help lines] (0,0) grid (4,4);
  \coordinate (A) at (0,1);
  \coordinate (B) at (3,2);
  \draw[thick] (A) -- (B);
  \draw[thick, purple,
    start modifier=.25, end modifier=.75,
    perpendicular bisector={A,B}];
  \foreach \p/\placement in {A/left,B/right}{
    \fill[red] (\p) circle (2pt);
    \draw (\p) node[\placement] {$\p$};
}
\end{tikzpicture}
```



可以是负数,这样就在相反方向:

```
\begin{tikzpicture}
  \draw[help lines] (0,0) grid (4,4);
  \coordinate (A) at (0,1);
  \coordinate (B) at (3,2);
  \draw[thick] (A) -- (B);
  \draw[thick, purple,
    start modifier=-.25,end modifier=0.75,
    perpendicular bisector={A,B}];
  \foreach \p/\placement in {A/left,B/right}{
    \fill[red] (\p) circle (2pt);
    \draw (\p) node[\placement] {$\p$};
}
\end{tikzpicture}
```



1.15 垂线 Perpendicular Line

调用方式

```
perpendicular={A,B,C}
```

参数说明

A,B,C 三点坐标

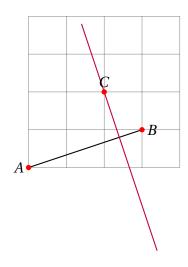
构造过 C 垂直于 AB 的直线 (设垂足为 D), 默认起点为 $D + (B - A) \cdot \mathbf{i}$, 终点为 $D - (B - A) \cdot \mathbf{i}$. 可以对起始点进行调整, 见1.23.

示例

过直线外一点的垂线:

```
\begin{tikzpicture}
  \draw[help lines] (0,0) grid (4,4);
  \coordinate (A) at (0,0);
  \coordinate (B) at (3,1);
  \coordinate (C) at (2,2);
  \draw[thick] (A) -- (B);
```

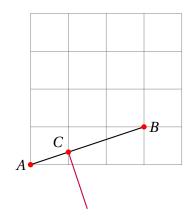
```
\path[draw, thick, purple, perpendicular={A,B,C}];
\foreach \p/\placement in {A/left,B/right,C/above}{
  \fill[red] (\p) circle (2pt);
  \draw (\p) node[\placement] {$\p$};
}
\end{tikzpicture}
```



过直线上一点的垂线:

```
\begin{tikzpicture}
  \draw[help lines] (0,0) grid (4,4);
  \coordinate (A) at (0,0);
  \coordinate (B) at (3,1);
  \coordinate (C) at ($(A)!1/3!(B)$);
  \draw[thick] (A) -- (B);
  \path[draw, thick, purple,
    start modifier=.5, end modifier=.75,
    perpendicular={A,B,C}];
  \foreach \p/\placement in {A/left,B/right,C/above}
    - left}{
```

```
\fill[red] (\p) circle (2pt);
   \draw (\p) node[\placement] {$\p$};
}
\end{tikzpicture}
```



1.16 平行线 Parallel Line

调用方式

```
parallel={A,B,C}
```

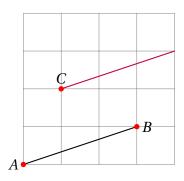
参数说明

过一点 C 作直线 AB 平行线, (如果 C 在 AB 上, 则重合). 首先将点 C 按向量 AB 平移至 D. 可以对起始点进行调整, 见1.23. 示例

指定起始点距离 C 的位置, 方向是 CD, 负值代表相反方向:

```
\begin{tikzpicture}
\draw[help lines] (0,0) grid (4,4);
\coordinate (A) at (0,0);
```

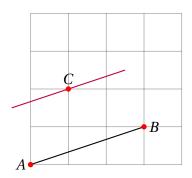
```
\coordinate (B) at (3,1);
\coordinate (C) at (1,2);
\draw[thick] (A) -- (B);
\path[draw, thick, purple, parallel={A,B,C}];
\foreach \p/\placement in {A/left,B/right,C/above}{
  \fill[red] (\p) circle (2pt);
  \draw (\p) node[\placement] {$\p$};
}
\end{tikzpicture}
```



指定系数:

```
\begin{tikzpicture}
  \draw[help lines] (0,0) grid (4,4);
  \coordinate (A) at (0,0);
  \coordinate (B) at (3,1);
  \coordinate (C) at (1,2);
  \draw[thick] (A) -- (B);
  \path[draw, thick, purple,
    start modifier=-.5, end modifier=.5,
    parallel={A,B,C}];
  \foreach \p/\placement in {A/left,B/right,C/above}{
    \fill[red] (\p) circle (2pt);
```

```
\draw (\p) node[\placement] {$\p$};
}
\end{tikzpicture}
```



1.17 延长线 Extend

调用方式

```
extend={A,B}
```

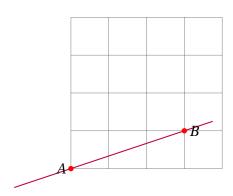
参数说明

作线段 AB 延长线, 可以对起始点进行调整, 见1.23. 实际上, 该操作等价于:

```
parallel={A,B,A}
```

```
\begin{tikzpicture}
  \draw[help lines] (0,0) grid (4,4);
  \coordinate (A) at (0,0);
  \coordinate (B) at (3,1);
```

```
\path[draw, thick, purple,
    start modifier=-.5, end modifier=1.25,
    extend={A,B}];
    \foreach \p/\placement in {A/left,B/right}{
        \fill[red] (\p) circle (2pt);
        \draw (\p) node[\placement] {$\p$};
    }
\end{tikzpicture}
```



1.18 圆 Circle

调用方式

```
circle={0,A}
```

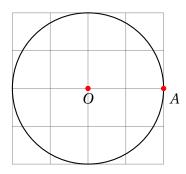
参数说明

0 圆心

A 圆上一点

构造圆心为 O, 经过 A 的圆.

```
\begin{tikzpicture}
  \draw[help lines] (-2,-2) grid (2,2);
  \coordinate (0) at (0,0);
  \coordinate (A) at +(0:2); % 圆上一点,相对坐标
  \draw[thick,circle={0,A}];
  \foreach \p in {0,A}
  \fill[red] (\p) circle (2pt);
  \draw (0) node[below] {$0$};
  \draw (A) node[below right] {$A$};
  \end{tikzpicture}
```



1.19 直线与圆的切点 Tangent Point

调用方式

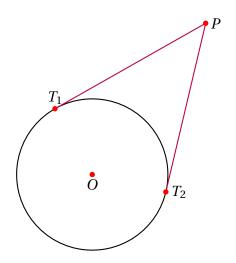
```
tangent point={0,A,P}
```

参数说明

O:圆心坐标

A:为圆上任意一点 **P**:圆外一点坐标 过圆 (O 为圆心, A 为圆上任意一点) 外一点 P 作切线, 求得一个切点 (在向量 OP 的左边), 另外一点可以通过对称 (reflect= $\{0,P,T\})$ 求得. 示例

```
\begin{tikzpicture}
  \coordinate (0) at (0,0);
  \coordinate (A) at +(0:2); % 圆上一点,相对坐标
  \coordinate (P) at (3,4);
  \coordinate [tangent point={0,A,P}] (T1);
  \coordinate [reflect={0,P,T1}] (T2);
  \draw[thick,circle={0,A}];
  \draw[thick,purple] (P) -- (T1) (P) -- (T2);
  \foreach \p in {0,P,T1,T2}
  \fill[red] (\p) circle (2pt);
  \draw (0) node[below] {$0$};
  \draw (P) node[right] {$P$};
  \draw (T1) node[above] {$T_1$};
  \draw (T2) node[right] {$T_2$};
  \end{tikzpicture}
```



1.20 外位似中心 External Homothetic Center

调用方式

```
external center={01,A1,02,A2}
```

参数说明

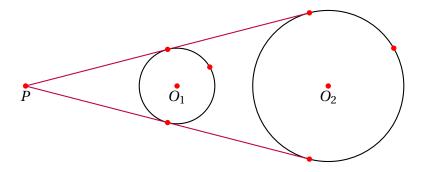
求圆 1 (O_1 为圆心, A_1 为圆上任意一点) 和圆 2 (O_2 为圆心, A_2 为圆上任意一点) 的外位似中心 (external homothetic center)[2].

示例

作外公切线: 先求位似中心, 可以求得两圆的外公切线.

```
\begin{tikzpicture}
 \tikzmath {
   a = 30;
   b = a;
   r1 = 1;
   r2 = 2;
 }
 \coordinate (01) at (0,0);
 \coordinate (A1) at (\$(01)+(\a:\r1)\$);
 \coordinate (02) at (4,0);
 \coordinate (A2) at (\$(02)+(\b:\r2)\$);
 \coordinate[external center={01,A1,02,A2}] (P);
 \coordinate[tangent point={01,A1,P}] (B);
 \coordinate[tangent point={02,A2,P}] (C);
 \coordinate[reflect={01,02,B}] (D);
 \coordinate[reflect={01,02,C}] (E);
 \draw[thick,circle={01,A1}];
 \draw[thick,circle={02,A2}];
 \draw[thick,purple] (P) -- (C) (P) -- (E);
```

```
\foreach \p in {A1,A2,B,C,D,E,O1,O2,P}
  \fill[red] (\p) circle (2pt);
  \draw (O1) node[below] {$0_1$};
  \draw (O2) node[below] {$0_2$};
  \draw (P) node[below] {$P$};
  \end{tikzpicture}
```



1.21 内位似中心 Internal Homothetic Center

调用方式

```
internal center={01,A1,02,A2}
```

参数说明

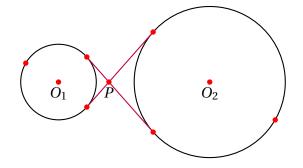
求圆 1 (O_1 为圆心, A_1 为圆上任意一点) 和圆 2 (O_2 为圆心, A_2 为圆上任意一点) 的内位似中心 (internal homothetic center)[2].

示例

作内公切线: 先求位似中心, 可以求得两圆的内公切线.

```
\begin{tikzpicture}
\tikzmath {
 \a = 150;
```

```
b = a - 180;
   r1 = 1;
   r2 = 2;
 }
 \coordinate (01) at (0,0);
 \coordinate (A1) at (\$(01)+(\lambda : r1)\$);
 \coordinate (02) at (4,0);
 \coordinate (A2) at (\$(02)+(\b:\r2)\$);
 \coordinate[internal center={01,A1,02,A2}] (P);
 \coordinate[tangent point={01,A1,P}] (B);
 \coordinate[tangent point={02,A2,P}] (C);
 \coordinate[reflect={01,02,B}] (D);
 \coordinate[reflect={01,02,C}] (E);
 \draw[thick,circle={01,A1}];
 \draw[thick,circle={02,A2}];
 \draw[thick,purple] (P) -- (B) (P) -- (C) (P) -- (D)
  \neg (P) -- (E);
 \foreach \p in {A1, A2, B, C, D, E, O1, O2, P}
   \fill[red] (\p) circle (2pt);
 \draw (01) node[below] {$0_1$};
 \draw (02) node[below] {$0_2$};
 \draw (P) node[below] {$P$};
\end{tikzpicture}
```



1.22 根轴 Radical Axis

调用方式

```
radical axis={01,A1,02,A2}
```

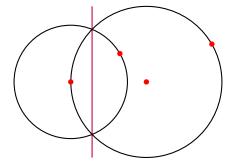
参数说明

构造两圆的根轴, 设与 O_1O_2 的交点为 P, 则默认起点为 $P + (O_2 - O_1) \cdot \mathbf{i}$, 终点为 $P - (O_2 - O_1) \cdot \mathbf{i}$. 可以对起始点进行调整, 见1.23.

示例

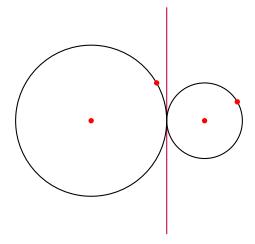
两圆相交:

```
\begin{tikzpicture}
 \tikzmath {
   a = 30;
   \b = \a;
   r1 = 1.5;
   r2 = 2;
 \coordinate (01) at (0,0);
 \coordinate (A1) at (\$(01)+(\a:\r1)\$);
 \coordinate (02) at (2,0);
 \coordinate (A2) at (\$(02)+(\b:\r2)\$);
 \draw[thick,purple,radical axis={01,A1,02,A2}];
 \draw[thick,circle={01,A1}];
 \draw[thick,circle={02,A2}];
 \foreach \p in {A1,A2,01,02}
    \fill[red] (\p) circle (2pt);
\end{tikzpicture}
```



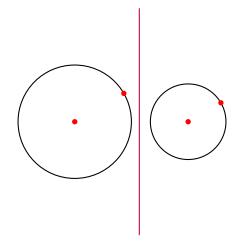
两圆外切:

```
\begin{tikzpicture}
  \tikzmath {
   a = 30;
   b = a;
    r1 = 2;
    r2 = 1;
 }
  \coordinate (01) at (0,0);
  \coordinate (A1) at (\$(01)+(\lambda : r1)\$);
  \coordinate (02) at (3,0);
 \coordinate (A2) at (\$(02)+(\b:\r2)\$);
  \draw[thick,purple,radical axis={01,A1,02,A2}];
  \draw[thick,circle={01,A1}];
  \draw[thick,circle={02,A2}];
 \foreach \p in {A1,A2,01,02}
    \fill[red] (\p) circle (2pt);
\end{tikzpicture}
```



两圆外离:

```
\begin{tikzpicture}
  \tikzmath {
   a = 30;
   b = a;
    r1 = 1.5;
   r2 = 1;
 }
  \coordinate (01) at (0,0);
  \coordinate (A1) at (\$(01)+(\lambda : r1)\$);
  \coordinate (02) at (3,0);
  \coordinate (A2) at (\$(02)+(\b:\r2)\$);
  \coordinate[radical axis={01,A1,02,A2}] (P);
  \draw[thick,purple,radical axis={01,A1,02,A2}];
  \draw[thick,circle={01,A1}];
  \draw[thick,circle={02,A2}];
  \foreach \p in {A1,A2,01,02}
    \fill[red] (\p) circle (2pt);
\end{tikzpicture}
```



1.23 Partway Modifiers and Distance Modifiers

perpendicular bisector, perpendicular, parallel, radical axis 等线段图形可以对起始点进行调整, 调整参数如下[3]:

start modifier (default: 0), 长度或系数, 如: 1cm 或.75 **end modifier** (default: 1), 长度或系数, 如: 1cm 或.75

1.24 坐标变换 Coordinates Transformations

调用方式

```
transform={angle:(xshift,yshift)}
```

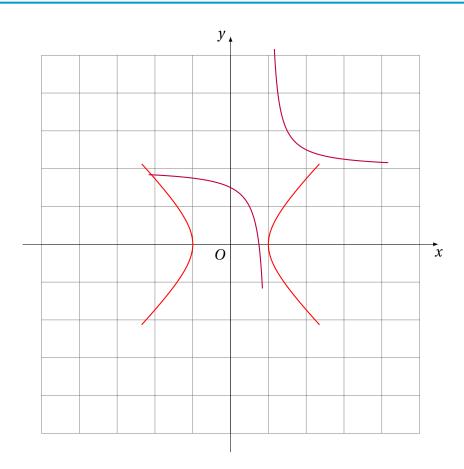
参数说明

绕原点旋转 angle, 然后水平方向和竖直方向分别平移 xshift 和 yshift 示例

```
\begin{tikzpicture}
\draw[help lines] (-5,-5) grid (5,5);
```

```
\draw[-latex] (-5.5,0) -- (5.5,0) node[below] {$x$};
\draw[-latex] (0,-5.5) -- (0,5.5) node[left] {$y$};
\draw (0,0) node[below left] {$0$};

\hyperbola[draw,thick,red] (1,1);
\hyperbola[draw,thick,purple,transform={45:(1,2)}]
- (1,1);
\end{tikzpicture}
```



第2章 三角形的中心

2.1 重心 Centroid

调用方式

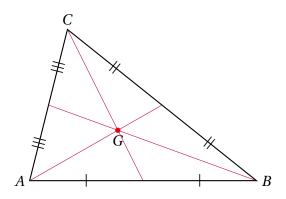
```
centroid={A,B,C}
```

参数说明

A,B,C 三角形的顶点 示例

```
\begin{tikzpicture}
  \coordinate (A) at (-2,0);
  \coordinate (B) at (4,0);
  \coordinate (C) at (-1,4);
  \coordinate (D) at ($(B)!0.5!(C)$);
  \coordinate (E) at ($(C)!0.5!(A)$);
  \coordinate (F) at ($(A)!0.5!(B)$);
  \path[centroid={A,B,C}] coordinate (G);
  \fill (G) [red] circle (2pt);
  \draw (G) node[below] {$G$};
  \draw[thick] (A) -- (B) -- (C) -- cycle;
  \draw[purple] (A) -- (D) (B) -- (E) (C) -- (F);
```

```
\draw (A) node[left] {$A$};
\draw (B) node[right] {$B$};
\draw (C) node[above] {$C$};
\draw (A) -- (B) node[near start,sloped] {$|$}
- node[near end,sloped] {$|$};
\draw (B) -- (C) node[near start,sloped] {$||$}
- node[near end,sloped] {$||$};
\draw (C) -- (A) node[near start,sloped] {$||$}
- node[near end,sloped] {$||$};
\end{tikzpicture}
```



2.2 垂心 Orthocenter

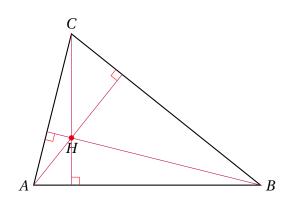
调用方式

```
orthocenter={A,B,C}
```

参数说明

A,B,C 三角形的顶点 示例

```
\begin{tikzpicture}
 \coordinate (A) at (-2,0);
 \coordinate (B) at (4,0);
 \coordinate (C) at (-1,4);
 \path[orthocenter={A,B,C}] coordinate (H);
 \fill (H) [red] circle (2pt);
 \draw (H) node[below] {$H$};
 \draw[thick] (A) -- (B) -- (C) -- cycle;
 \coordinate (D) at ($(B)!(A)!(C)$);
 \coordinate (E) at ($(A)!(B)!(C)$);
 \coordinate (F) at ($(B)!(C)!(A)$);
 \draw[purple] (A) -- (D) (B) -- (E) (C) -- (F);
 \draw (A) node[left] {$A$};
 \draw (B) node[right] {$B$};
 \draw (C) node[above] {$C$};
 \pic [draw,red,angle radius=6pt] {right angle=H--D--C};
 \pic [draw,red,angle radius=6pt] {right angle=H--E--A};
 \pic [draw,red,angle radius=6pt] {right angle=H--F--B};
\end{tikzpicture}
```



2.3 外心 Circumcenter

调用方式

```
circumcenter={A,B,C}
```

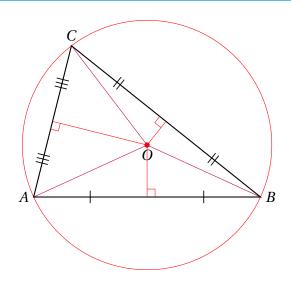
参数说明

A,B,C 三角形的顶点

```
\begin{tikzpicture}
 \coordinate (A) at (-2,0);
 \coordinate (B) at (4,0);
 \coordinate (C) at (-1,4);
 \path[circumcenter={A,B,C}] coordinate (0);
 \fill (0) [red] circle (2pt);
 \draw (0) node[below] {$0$};
 \node[draw,red] at (0) [circle through=(A)]{};
 \draw[thick] (A) -- (B) -- (C) -- cycle;
 \draw[purple] (A) -- (O) (B) -- (O) (C) -- (O);
 \draw (A) node[left] {$A$};
 \draw (B) node[right] {$B$};
 \draw (C) node[above] {$C$};
 \coordinate (D) at ($(B)!(O)!(C)$);
 \coordinate (E) at (\$(C)!(0)!(A)\$);
 \coordinate (F) at ($(A)!(0)!(B)$);
 \draw[red] (0) -- (D) (0) -- (E) (0) -- (F);
 \draw (A) -- (B) node[near start,sloped] {$|$}
  - node[near end,sloped] {$|$};
```

2.4 内心 INCENTER

```
\draw (B) -- (C) node[near start,sloped] {$||$}
- node[near end,sloped] {$||$};
\draw (C) -- (A) node[near start,sloped] {$|||$}
- node[near end,sloped] {$|||$};
\pic [draw,red,angle radius=6pt] {right angle=0--D--C};
\pic [draw,red,angle radius=6pt] {right angle=0--E--A};
\pic [draw,red,angle radius=6pt] {right angle=0--F--B};
\end{tikzpicture}
```



2.4 内心 Incenter

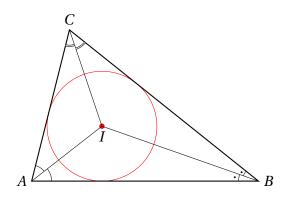
调用方式

```
incenter={A,B,C}
```

参数说明

A,B,C 三角形的顶点 示例

```
\begin{tikzpicture}
  \coordinate (A) at (-2,0);
  \coordinate (B) at (4,0);
  \coordinate (C) at (-1,4);
  \path[incenter={A,B,C}] coordinate (I);
 \fill (I) [red] circle (2pt);
  \draw (I) node[below] {$I$};
  \node[draw,red] at (I) [circle
  \rightarrow through=($(B)!(I)!(C)$)]{};
  \draw[thick] (A) -- (B) -- (C) -- cycle;
  \draw (A) node[left] {$A$};
 \draw (B) node[right] {$B$};
  \draw (C) node[above] {$C$};
  \draw (A) -- (I) (B) -- (I) (C) -- (I);
 \pic [draw,angle radius=12pt] {angle=I--A--C};
  \pic [draw,angle radius=15pt] {angle=B--A--I};
  \pic [draw,double,angle radius=12pt] {angle=A--C--I};
 \pic [draw,double,angle radius=15pt] {angle=I--C--B};
  \pic [draw,pic text=.,angle radius=12pt,
    angle eccentricity=1.2] {angle=C--B--I};
  \pic [draw,pic text=.,angle radius=15pt,
    angle eccentricity=1.2] {angle=I--B--A};
\end{tikzpicture}
```



2.5 旁心 Excenter

调用方式

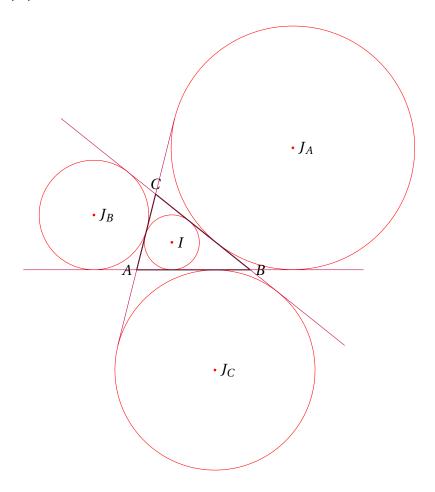
```
excenter={A,B,C}
```

参数说明

A,B,C 三角形的顶点,返回与 A 相对的旁心,调换顶点顺序就可以得到 3 个旁心.

```
\begin{tikzpicture}[scale=.5]
  \coordinate (A) at (-2,0);
  \coordinate (B) at (4,0);
  \coordinate (C) at (-1,4);
  \path[incenter={A,B,C}] coordinate (I);
  \path[excenter={A,B,C}] coordinate (JA);
  \path[excenter={B,A,C}] coordinate (JB);
  \path[excenter={C,A,B}] coordinate (JC);
  \foreach \point in {I,JA,JB,JC}
  \fill (\point) [red] circle (2pt);
```

```
\node[draw,red] at (I) [circle
  - through=($(B)!(I)!(C)$)]{};
 \node[draw,red] at (JA) [circle
  - through=($(B)!(JA)!(C)$)]{};
 \node[draw,red] at (JB) [circle
  through=($(B)!(JB)!(C)$)]{};
 \node[draw,red] at (JC) [circle
  - through=($(B)!(JC)!(C)$)]{};
 \draw[thick] (A) -- (B) -- (C) -- cycle;
 \draw (A) node[left] {$A$};
 \draw (B) node[right] {$B$};
 \draw (C) node[above] {$C$};
 \draw[purple] ($(A)!-1!(B)$) -- ($(A)!2!(B)$);
 \draw[purple] ($(B)!-1!(C)$) -- ($(B)!2!(C)$);
 \draw[purple] ($(C)!-1!(A)$) -- ($(C)!2!(A)$);
 \draw (I) node[right] {$I$};
 \draw (JA) node[right] {\$J_A\$};
 \draw (JB) node[right] {\$J_B\$};
 \draw (JC) node[right] {\$J_C\$};
\end{tikzpicture}
```



2.6 九点圆圆心 Nine-Point Center

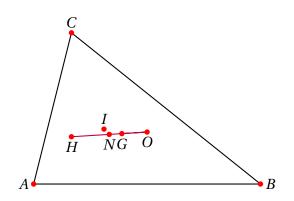
调用方式

nine-point center={A,B,C}

参数说明

A,B,C 三角形的顶点

```
\begin{tikzpicture}
 \coordinate (A) at (-2,0);
 \coordinate (B) at (4,0);
 \coordinate (C) at (-1,4);
 \path[orthocenter={A,B,C}] coordinate (H);
 \path[circumcenter={A,B,C}] coordinate (0);
 \path[centroid={A,B,C}] coordinate (G);
 \path[incenter={A,B,C}] coordinate (I);
 \path[nine-point center={A,B,C}] coordinate (N);
 \draw[thick] (A) -- (B) -- (C) -- cycle;
 \draw[thick,purple] (H) -- (O) -- (G);
 \foreach \p/\placement in {A/left,B/right,C/above,
 H/below,O/below,G/below,I/above,N/below}{
   \fill (\p) [red] circle (2pt);
   \draw (\p) node[\placement] {$\p$};
 }
\end{tikzpicture}
```



第3章 圆锥曲线 Conics

本章包含了一些自定义命令和 tikz 内置命令。

3.1 椭圆 Ellipse

调用方式

```
(center) ellipse ( a and b)
```

或

```
(center) ellipse [x radius = a, y radius = b]
```

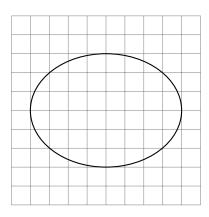
注 上面 ellipse 也可以替换为 circle.

参数说明

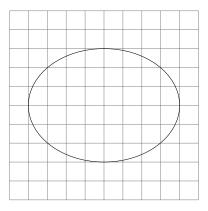
a, b 半长轴长和半短轴长, 需要指定单位, 如 4cm and 3cm 返回椭圆曲线.

```
\begin{tikzpicture}[scale=.5]
  \draw[help lines] (-5,-5) grid (5,5);
  \draw[thick] (0,0) ellipse (4cm and 3cm);
```

\end{tikzpicture}



```
\begin{tikzpicture}[scale=.5]
  \draw [help lines] (-5,-5) grid (5,5);
  \draw (0,0) ellipse [x radius=4cm,y radius=3cm];
  \end{tikzpicture}
```



3.2 双曲线 Hyperbola 与渐近线 Asymptote

调用方式

```
\hyperbola [options] (a,b);
```

或

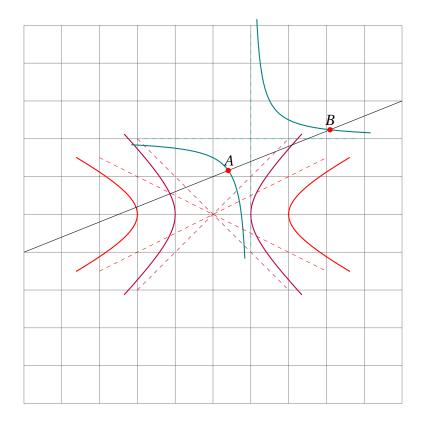
```
\asymptote [options] (a,b);
```

参数说明

a,b 半长轴长和半短轴长返回双曲线及其渐进线.示例

```
\begin{tikzpicture}
 \tikzmath{
    a = 1;
   b = 1;
 }
  \draw[help lines] (-5,-5) grid (5,5);
  \hyperbola [draw,thick,purple,name path=c1] (\a,\b);
  \asymptote [draw,dashed,purple] (\a,\b);
 \hyperbola [transform={45:(1,2)},draw,thick,teal,name
  → path=c2] (1,1);
  \asymptote [transform={45:(1,2)},draw,dashed,teal]
  - (1,1);
 \hyperbola [draw,thick,red,domain=-1.2:1.2,name

¬ path=c3] (2,1);
  \asymptote [draw,dashed,red,domain=-3:3] (2,1);
  \frac{1}{3} \draw[name path=1] (-5,-1) -- (5,3);
```



注 当指定绘制双曲线 (hyperbola) 的 domain (default: domain=-1.5:1.5) 时, domain 是下列双曲线参数方程中 t 的取值范围:

$$\begin{cases} x = \cosh t, \\ y = \sinh t \end{cases}$$

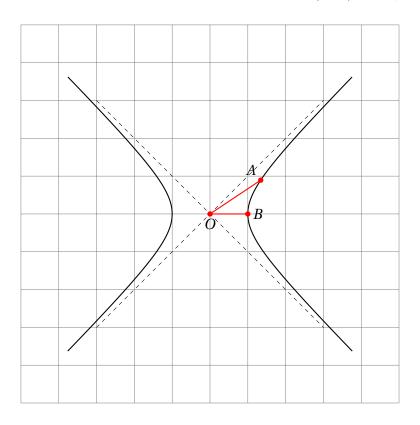
t的几何意义: 射线出原点交单位双曲线 $x^2-y^2=1$ 于 $(\cosh t,y=\sinh t),t$ 是射

线, 双曲线和 x 轴围成的面积的二倍. 对于双曲线上位于 x 轴下方的点, 这个面积被认为是负值.

当指定绘制渐进线 (asymptote) 的 domain (default: domain=-2:2) 时, domain 是下列直线方程中 x 的取值范围:

$$y = \pm \frac{b}{a}x$$

```
\begin{tikzpicture}
 \draw[help lines] (-5,-5) grid (5,5);
 \coordinate (0) at (0,0);
 \coordinate (A') at (3,2);
 \coordinate (B) at (1,0);
 \path[name path=ray] (0) -- (A');
 \hyperbola[draw,thick,domain=-2:2,name path=hyperbola]
  (1,1);
 \asymptote[draw,dashed,domain=-3:3] (1,1);
 \path[name intersections={of=ray and hyperbola, by=A}];
 \draw[thick,red] (A) -- (O) -- (B);
 \foreach \p/\placement in {0/below, A/above left,
  → B/right}{
   \fill[red] (\p) circle (2pt);
   \draw (\p) node[\placement] {$\p$};
 }
\end{tikzpicture}
```



附录A 两直线的交点

求解两直线交点的方程 [4]:

$$\begin{vmatrix} x & y & 1 \\ x_1 & y_1 & 1 \\ x_2 & y_2 & 1 \end{vmatrix} = 0$$

$$\begin{vmatrix} x & y & 1 \\ x_3 & y_3 & 1 \\ x_4 & y_4 & 1 \end{vmatrix} = 0$$

注意,两个方程的系数都是行列式,解得:

$$x = \frac{\begin{vmatrix} \begin{vmatrix} x_1 & y_1 \\ x_2 & y_2 \end{vmatrix} & \begin{vmatrix} x_1 & 1 \\ x_2 & y_2 \end{vmatrix} & \begin{vmatrix} x_1 & 1 \\ x_2 & 1 \end{vmatrix} \\ \begin{vmatrix} x_1 & y_1 \\ x_2 & y_2 \end{vmatrix} & \begin{vmatrix} x_1 - x_2 \\ x_2 & y_2 \end{vmatrix} & \begin{vmatrix} x_1 - x_2 \\ x_3 & y_3 \\ x_4 & y_4 \end{vmatrix} & \begin{vmatrix} x_3 - x_4 \\ x_3 - x_4 \end{vmatrix} \\ \begin{vmatrix} x_1 & 1 \\ x_2 & 1 \end{vmatrix} & \begin{vmatrix} y_1 & 1 \\ y_2 & 1 \end{vmatrix} \\ \begin{vmatrix} x_3 & 1 \\ x_4 & 1 \end{vmatrix} & \begin{vmatrix} y_3 & 1 \\ y_4 & 1 \end{vmatrix} \end{vmatrix}$$

$$y = \frac{\begin{vmatrix} \begin{vmatrix} x_1 & y_1 \\ x_2 & y_2 \end{vmatrix} & \begin{vmatrix} y_1 & 1 \\ y_2 & 1 \end{vmatrix}}{\begin{vmatrix} x_3 & y_3 \\ x_4 & y_4 \end{vmatrix} & \begin{vmatrix} y_3 & 1 \\ y_4 & 1 \end{vmatrix}} = \frac{\begin{vmatrix} \begin{vmatrix} x_1 & y_1 \\ x_2 & y_2 \end{vmatrix}}{\begin{vmatrix} x_3 & y_3 \\ x_4 & y_4 \end{vmatrix}} & y_3 - y_4$$
$$\frac{\begin{vmatrix} x_1 & 1 \\ x_2 & 1 \end{vmatrix} & \begin{vmatrix} y_1 & 1 \\ y_2 & 1 \end{vmatrix}}{\begin{vmatrix} x_3 & 1 \\ x_4 & 1 \end{vmatrix} & \begin{vmatrix} y_3 & 1 \\ y_4 & 1 \end{vmatrix}} = \frac{\begin{vmatrix} x_1 & y_1 \\ x_2 & y_2 \end{vmatrix}}{\begin{vmatrix} x_3 & y_3 \\ x_4 & y_4 \end{vmatrix}} = \frac{\begin{vmatrix} x_1 & y_1 \\ x_3 & y_3 \\ x_4 & y_4 \end{vmatrix}}{\begin{vmatrix} x_1 - x_2 & y_1 - y_2 \\ x_3 - x_4 & y_3 - y_4 \end{vmatrix}}$$

进一步化简得到1:

$$x = \frac{(x_1y_2 - y_1x_2)(x_3 - x_4) - (x_1 - x_2)(x_3y_4 - y_3x_4)}{(x_1 - x_2)(y_3 - y_4) - (y_1 - y_2)(x_3 - x_4)}$$
$$y = \frac{(x_1y_2 - y_1x_2)(y_3 - y_4) - (y_1 - y_2)(x_3y_4 - y_3x_4)}{(x_1 - x_2)(y_3 - y_4) - (y_1 - y_2)(x_3 - x_4)}$$

上述方法给出的交点坐标公式在 TikZ 环境中的计算稳定性不够好, 经常出现 Dimension too large 错误, 究其原因是分母可能有时会比较小. 下面给出一个计算更稳定的公式.

我们可以给出两条直线的参数方程:

直线 L1 的方程:

$$\begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} x_1 \\ y_1 \end{bmatrix} + s \begin{bmatrix} x_2 - x_1 \\ y_2 - y_1 \end{bmatrix}$$

直线 L2 的方程:

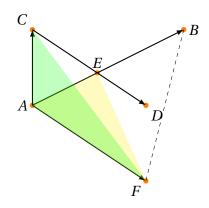
$$\begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} x_3 \\ y_3 \end{bmatrix} + t \begin{bmatrix} x_4 - x_3 \\ y_4 - y_3 \end{bmatrix}$$

lhttps://en.wikipedia.org/wiki/Lineline_intersection

可以解出 s, t:

$$s = \frac{\begin{vmatrix} x_1 - x_3 & x_3 - x_4 \\ y_1 - y_3 & y_3 - y_4 \end{vmatrix}}{\begin{vmatrix} x_1 - x_2 & x_3 - x_4 \\ y_1 - y_2 & y_3 - y_4 \end{vmatrix}}$$
$$t = \frac{\begin{vmatrix} x_1 - x_3 & x_1 - x_2 \\ y_1 - y_3 & y_1 - y_2 \end{vmatrix}}{\begin{vmatrix} x_1 - x_2 & x_3 - x_4 \\ y_1 - y_2 & y_3 - y_4 \end{vmatrix}}$$

我们也可从几何的角度来分析:



$$\overrightarrow{AE} = s\overrightarrow{AB}$$

$$s = \frac{S_{\triangle AEF}}{S_{\triangle ABF}}$$

$$= \frac{S_{\triangle ACF}}{S_{\triangle ABF}}$$

$$= \frac{\overrightarrow{AF} \times \overrightarrow{AC}}{\overrightarrow{AF} \times \overrightarrow{AB}}$$

$$= \frac{\overrightarrow{CD} \times \overrightarrow{AC}}{\overrightarrow{CD} \times \overrightarrow{AB}}$$

为了保证数值计算的稳定性,可以对下面的方程进行列主元消元法求解:

$$x_1 + s(x_2 - x_1) = x3 + t(x_4 - x3)$$

$$y_1 + s(y_2 - y_1) = y_3 + t(y_4 - y_3)$$

```
\ProvidesFile{tikzlibraryeuclidea.code.tex}[2024/01/09
 v1.3.0 A tikz library for plane geometry]
\usetikzlibrary{math,calc,quotes}
% https://tex.stackexchange.com/questions/455991/
→ pgfmath-function-for-strings-and-numbers
% Solving the error:
% Package PGF Math: Could not parse input 'A' as a

→ floating

% point number, sorry. The unreadable part was near
'A'..
\pgfkeys{
 /pgf/fpu/handlers/invalid number/.code = {%
    \pgfmathfloatparsenumber{3Y0.0e0]}%
 }
}
\makeatletter
% 注意: 计算过程是保留坐标单位 (pt) 的, 所以存在乘除法单位
   的问题, 首先数值始终携带单位,
```

```
% 在 calc 运算时有的需要转换为标量;将坐标转换为 pt 值,数
- 值可能超出限值,出现
% Dimension too large 错误,在计算长度时及时进行缩小
% https://tex.stackexchange.com/questions/475556/tikz-

→ why-is-dimension-too-large

% 具体方法是修改默认的 1cm, 如:
\Rightarrow [scale=1.0,x=0.5cm,y=0.5cm]
% 注意此处的变量不要和 tikzpicture 环境重名, 否则被替换掉
% triangle centers:
% https://mathworld.wolfram.com/BarycentricCoordinates. |
→ html
\tikzmath{
 % 采用列主元消元法求直线 P1P2 与直线 P3P4 的交点 P 位置
  → 参数 s: s = P1P/P1P2
 function intersectll(x1, y1, x2, y2, x3, y3, x4, y4)
{
   a1 = x2-x1; b1 = x3-x4; c1 = x3-x1;
   a2 = y2-y1; b2 = y3-y4; c2 = y3-y1;
   \forall x = max(max(abs(\a1), abs(\a2)),
    \rightarrow max(abs(\b1),abs(\b2)));
   a1 = a1/dmax; b1 = b1/dmax; c1=c1/dmax;
   a2 = a2/dmax; b2 = b2/dmax; c2=c2/dmax;
   if abs(a1) < abs(a2) then {
     \neq = a1; a1 = a2; a2 = \pm p;
     \neq b1; b1 = b2; b2 = \pm p;
     \neq \c1; \c1 = \c2; \c2 = \temp;
   };
   b1 = b1/a1; c1 = c1/a1; a1 = 1.0;
   b2 = b2-a2*b1; c2 = c2-a2*c1; a2 = 0.0;
   n2 = c2/b2; n1 = c1-b1*n2;
```

```
return \n1;
 };
\tikzset{
 % specifying start and end with modifiers(see tikz
  → manual 13.5)
 % commands supporting partway modifiers:
 % radical axis, perpendicular bisector, perpendicular,
  → parallel
 start modifier/.initial = 0,
 start modifier/.default = 0,
 end modifier/.initial = 1,
 end modifier/.default = 1,
 % ====== Coordinates Transformations =======
 % affine={A,B,k}: returns affine combination of two
  → points
 \% with affine ratio, i.e. A + k * ( B - A )
 affine/.style args = {#1,#2,#3}{
   insert path = {
      ($(#1)!{#3}!(#2)$)
   }
 },
 % midpoint={A,B}: returns midpoint of AB.
 midpoint/.style args = {#1,#2}{
   insert path = {
      ($(#1)!.5!(#2)$)
   }
 },
 % translate={A,B,C}: returns translation of C by
```

```
\% the vector AB, i.e. C + ( B - A )
translate/.style args = \{#1, #2, #3\}{
  insert path = {
    (\$(#3)+(#2)-(#1)\$)
  }
},
% reflect={A,B,C}: reflects point C across line AB.
reflect/.style args = {#1,#2,#3}{
  insert path = {
    let
      p{ft} = ($(#1)!(#3)!(#2)$),% perpendicular foot
    in (\$(#3)!2!(\p{ft})\$)
  }
},
% project={A,B,C}: projects point C onto line AB.
project/.style args = {#1,#2,#3}{
  insert path = {
    ($(#1)!(#3)!(#2)$)
  }
},
% inverse={0,A,P}: returns inverse point P with respect
 - to
% a reference circle(0,A).
inverse/.style args = {#1,#2,#3}{
  insert path = {
    let
      p{0A} = (\$(#2)-(#1)\$),
      p{OP} = (\$(#3)-(#1)\$),
      n\{r\} = \{veclen(p\{OA\})\},\
      \n{d} = {veclen(p{OP})},
```

```
n1 = \{scalar((n\{r\}/n\{d\}))\},\
    in (\$(\#1)! \ln 1* \ln 1! (\#3)\$)
  }
},
revolve/scale/.initial = 1,% angle scale
revolve/@angle/.initial = 90,
revolve/@argn/.initial = 0,% arguments count
% set revolve/@angle with certain degrees or angle of a

    vector

revolve/@set angle 1/.code args = {#1}{
  \pgfmathanglebetweenpoints
    {\pgfpoint{0cm}{0cm}}
    {\pgfpointanchor{#1}{center}}
  \pgfkeysalso{/tikz/revolve/@angle = \pgfmathresult}
  \typeout{========}
  \typeout{/tikz/revolve/@angle:\pgfkeysvalueof{/tikz/_
   → revolve/@angle}}
  \typeout{=========}
},
% set revolve/@angle with angle between two position

    vectors

revolve/@set angle 2/.code args = {#1,#2}{
  \pgfmathanglebetweenpoints
    {\pgfpointanchor{#1}{center}}
    {\pgfpointanchor{#2}{center}}
  \pgfkeysalso{/tikz/revolve/@angle = \pgfmathresult}
  \typeout{========}
  \typeout{/tikz/revolve/@angle:\pgfkeysvalueof{/tikz/_
   → revolve/@angle}}
  \typeout{=========}
```

```
},
% set revolve/@angle with angle {A,B,C}, angle between

→ two sides

% (A is apex, B is the start point, C is the end point)
revolve/@set angle 3/.code args = {#1,#2,#3}{
  \pgfmathanglebetweenlines
    {\pgfpointanchor{#1}{center}}
   {\pgfpointanchor{#2}{center}}
   {\pgfpointanchor{#1}{center}}
   {\pgfpointanchor{#3}{center}}
  \pgfkeysalso{/tikz/revolve/@angle = \pgfmathresult}
  \typeout{=========}
  \typeout{/tikz/revolve/@angle:\pgfkeysvalueof{/tikz/_

¬ revolve/@angle}}
  \typeout{=========}
},
% set revolve/@angle with angle between two

¬ vectors(ccw, AB and CD)

revolve/@set angle 4/.code args = {#1,#2,#3,#4}{
  \pgfmathanglebetweenlines
   {\pgfpointanchor{#1}{center}}
   {\pgfpointanchor{#2}{center}}
   {\pgfpointanchor{#3}{center}}
   {\pgfpointanchor{#4}{center}}
  \pgfkeysalso{/tikz/revolve/@angle = \pgfmathresult}
  \typeout{========}
  \typeout{/tikz/revolve/@angle:\pgfkeysvalueof{/tikz/_
   → revolve/@angle}}
  \typeout{=========}
```

```
},
revolve/angle/.code = {%
  \pgfmathfloatparsenumber{#1}
  \pgfmathfloattomacro{\pgfmathresult}{\F}{\M}{\E}
  \pgfmathparse{#1}
  \else
    % Compute the Number of Arguments
    \pgfutil@for\arg:=#1\do{
      \pgfmathparse{int(add(\pgfkeysvalueof{/tikz/_1

¬ revolve/@argn},1))}

      \pgfkeysalso{/tikz/revolve/@argn =
       → \pgfmathresult}
    }
    \ifnum \pgfkeysvalueof{/tikz/revolve/@argn} = 1
      \tikzset{revolve/@set angle 1 = {#1}}
    \else\ifnum \pgfkeysvalueof{/tikz/revolve/@argn} =
      \tikzset{revolve/@set angle 2 = {#1}}
    \else\ifnum \pgfkeysvalueof{/tikz/revolve/@argn} =

→ 3

      \tikzset{revolve/@set angle 3 = {#1}}
    \else\ifnum \pgfkeysvalueof{/tikz/revolve/@argn} =
      \tikzset{revolve/@set angle 4 = {#1}}
    \else
      \pgferror{"Incorrect number of arguments!"}
    \fi\fi\fi
    \fi
  \fi
```

```
\pgfkeysalso{/tikz/revolve/@angle = \pgfmathresult}
},
% revolve={A,B}: rotates point B by the angle around
 → point A.
revolve/.style args = {#1,#2}{
  insert path = {
    let
      \n1 = {\pgfkeysvalueof{/tikz/revolve/@angle}},
      \n2 = {\pgfkeysvalueof{/tikz/revolve/scale}}
    in (\$(\#1)!1!\n1*\n2:(\#2)\$)
  }
},
% angle bisector={A,B,C}: alias for [revolve/angle={_1}
 - A,B,C},revolve/scale=.5,revolve={A,B}]
angle bisector/.style args = {#1,#2,#3}{
  revolve/angle={#1,#2,#3},revolve/scale=.5,revolve={#1
   \rightarrow 1,#2}
},
% erect={A,B}: alias for
- [revolve/angle=90,revolve={A,B}]
erect/.style args = {#1,#2}{
  revolve/angle=90,revolve={#1,#2}
},
% equilateral={A,B}: alias for
 - [revolve/angle=60,revolve={A,B}]
equilateral/.style args = {#1,#2}{
  revolve/angle=60,revolve={#1,#2}
},
% cut a line segment of a certain length on a straight
 - line
```

```
intercept/@length/.initial = 1cm,
intercept/scale/.initial = 1,% length scale
intercept/length/.code = {% set length by distance of

    segment

  \pgfutil@in@{,}{#1}
  \ifpgfutil@in@%compute segment length
   \euclidea@ComputeLength#1\euclidea@stop
   \pgfkeysalso{/tikz/intercept/@length =
    → \pgfmathresult}
  \else
    \pgfkeysalso{/tikz/intercept/@length = #1}
  \typeout{=========}
  \typeout{/tikz/intercept/@length:\pgfkeysvalueof{/_1
  tikz/intercept/@length}}
  \typeout{=========}
},
% intercept={A,B}: intercepts a line segment(starting
% from point A) of a certain length on line AB.
intercept/.style args = {#1,#2}{
  insert path = {
   let
     \n1 = {\pgfkeysvalueof{/tikz/intercept/@length}},
     \n2 = {\pgfkeysvalueof{/tikz/intercept/scale}},
     p{AB} = (\$(#2)-(#1)\$),
     \n{d} = {veclen(p{AB})},
     n3 = \{scalar(n1*n2/n{d})\}
   in (\$(#1)! \n3!(#2)\$)
  }
},
```

```
% intersect={A,B,C,D}: returns the intersection
 % of line AB and line CD.
% https://en.wikipedia.org/wiki/Line%E2%80%_
 → 93line intersection
intersect/.style args = {#1,#2,#3,#4}{
  insert path = {
    let
      p1 = (#1), p2 = (#2), p3 = (#3), p4 = (#4),
      \n1 = \{intersectll(\x1,\y1,\x2,\y2,\x3,\y3,\x4,\)
       \rightarrow y4)},
    in (\$(\p1)!\n1!(\p2)\$)
 }
},
% ====== Triangle Centers ======
% calculated from barycentric coordinates
% incenter = {A,B,C}
incenter/.style args = \{#1, #2, #3\}{
  insert path = {
    let
      p1 = (#1), p2 = (#2), p3 = (#3),
      p{AB} = (\$(#2)-(#1)\$),
      p\{BC\} = (\$(#3)-(#2)\$),
      \p{CA} = (\$(\#1) - (\#3)\$),
      n{a} = {veclen(x{BC}, y{BC})},
      \n{b} = {veclen(\x{CA}, \y{CA})},
      \n{c} = {veclen(\x{AB}, \y{AB})},
      \n{s} = {\n{a}+\n{b}+\n{c}},
      n1 = {n{a}/n{s}},
      n2 = {n\{b\}/n\{s\}},
```

```
n3 = {n{c}/n{s}},
    in ({n1*}x1+n2*x2+n3*x3,n1*y1+n2*y2+n3*_1
     y3})
 }
},
% excenter = {A,B,C}, returns excenter opposite to the

→ vertex A

excenter/.style args = \{#1, #2, #3\}{
  insert path = {
    let
      p1 = (#1), p2 = (#2), p3 = (#3),
      p{AB} = ($(#2)-(#1)$),
      p\{BC\} = (\$(#3)-(#2)\$),
      p{CA} = (\$(#1)-(#3)\$),
      n{a} = {veclen(x{BC}, y{BC})},
      \n{b} = {veclen(\x{CA}, \y{CA})},
      \n{c} = {veclen(\x{AB}, \y{AB})},
      \n{s} = {-\n{a}+\n{b}+\n{c}},
      n1 = {n{a}/n{s}},
      n2 = {n\{b\}/n\{s\}},
      n3 = {n{c}/n{s}},
    in ({-\ln 1*}\x1+\ln 2*\x2+\ln 3*\x3,-\ln 1*\y1+\ln 2*\y2+\_
     \rightarrow n3*\y3})
 }
},
% circumcenter = {A,B,C}
circumcenter/.style args = {#1,#2,#3}{
  insert path = {
    let
      p1 = (#1), p2 = (#2), p3 = (#3),
```

70 附录 B 源代码

```
p{AB} = ($(#2)-(#1)$),
      p\{BC\} = (\$(#3)-(#2)\$),
      p{CA} = (\$(#1)-(#3)\$),
      n{a} = {veclen(x{BC}, y{BC})},
      \n{b} = {veclen(\x{CA}, \y{CA})},
      \n{c} = {veclen(\x{AB}, \y{AB})},
      n\{m\} = \{\max(\max(n\{a\}, n\{b\}), n\{c\})\},\
      n\{a\} = \{n\{a\}/n\{m\}\},\
      n{a} = {n{a}*n{a}},
      \n{b} = {\n{b}/\n{m}},
      \n{b} = {\n{b}*\n{b}},
      n\{c\} = \{n\{c\}/n\{m\}\},\
      n\{c\} = \{n\{c\}*n\{c\}\},\
      \ln 1 = {\ln\{a\}*(\ln\{b\}+\ln\{c\}-\ln\{a\})\}},
      n2 = {n{b}*(n{c}+n{a}-n{b})},
      n3 = {n{c}*(n{a}+n{b}-n{c})},
      n\{s\} = \{n1+n2+n3\},\
      n1 = \{ n1/n\{s\} \},
      n2 = {n2/n\{s\}},
      n3 = {n3/n\{s\}},
    in ({\frac{x1+\n2*\x2+\n3*\x3,\n1*\y1+\n2*\y2+\n3*\}_{1}}

    y3})
  }
},
% orthocenter = {A,B,C}
orthocenter/.style args = {#1,#2,#3}{
  insert path = {
    let
      p1 = (#1), p2 = (#2), p3 = (#3),
      p{AB} = ($(#2)-(#1)$),
```

```
p\{BC\} = (\$(#3)-(#2)\$),
      p{CA} = (\$(#1)-(#3)\$),
      \n{a} = {veclen(\x{BC}, \y{BC})},
      \n{b} = {veclen(\x{CA}, \y{CA})},
      \n{c} = {veclen(\x{AB}, \y{AB})},
      n\{m\} = \{\max(\max(n\{a\}, n\{b\}), n\{c\})\},\
      n\{a\} = \{n\{a\}/n\{m\}\},\
      \n{a} = {\n{a}*\n{a}},
      n\{b\} = \{n\{b\}/n\{m\}\},\
      \n{b} = {\n{b}*\n{b}},
      n\{c\} = \{n\{c\}/n\{m\}\},\
      n\{c\} = \{n\{c\}*n\{c\}\},\
      n{a2} = {n{b}+n{c}-n{a}},
      \n{b2} = {\n{c}+\n{a}-\n{b}},
      n\{c2\} = \{n\{a\}+n\{b\}-n\{c\}\},\
      n1 = {n{c2}*n{b2}},
      n2 = {n{a2}*n{c2}},
      n3 = {n{b2}*n{a2}},
      n\{s\} = \{n1+n2+n3\},\
      n1 = \{ n1/n\{s\} \},
      n2 = {n2/n\{s\}},
      n3 = {n3/n\{s\}},
    in ({n1*\x1+\n2*\x2+\n3*\x3,\n1*\y1+\n2*\y2+\n3*\y}
     y3})
 }
},
% centroid = {A,B,C}
centroid/.style args = \{#1, #2, #3\}{
  insert path = {
    let
```

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```
p1 = (#1), p2 = (#2), p3 = (#3),
    in ({(x1+x2+x3)/3},{(y1+y2+y3)/3})
  }
},
% nine-pint center = {A,B,C}
nine-point center/.style args = {#1,#2,#3}{
  insert path = {
    let
      p1 = (#1), p2 = (#2), p3 = (#3),
      p{AB} = (\$(#2)-(#1)\$),
      p\{BC\} = (\$(#3)-(#2)\$),
      p{CA} = ($(#1)-(#3)$),
      n{a} = {veclen(x{BC}, y{BC})},
      \n{b} = {veclen(\x{CA}, \y{CA})},
      \n{c} = {veclen(\x{AB}, \y{AB})},
      n\{m\} = \{\max(\max(n\{a\}, n\{b\}), n\{c\})\},\
      n\{a\} = \{n\{a\}/n\{m\}\},\
      n\{a\} = \{n\{a\}*n\{a\}\},\
      \n{b} = {\n{b}/\n{m}},
      \n{b} = {\n{b}*\n{b}},
      n\{c\} = \{n\{c\}/n\{m\}\},\
      n\{c\} = \{n\{c\} * n\{c\}\},\
      n1 = {n{a}*(n{b}+n{c})-(n{b}-n{c})*(n{b}-1)}
       \neg \ \n\{c\})\},
      n2 = {n{b}*(n{c}+n{a})-(n{c}-n{a})*(n{c}-1)}
       \neg \n{a})
      n3 = {n{c}*(n{a}+n{b})-(n{a}-n{b})*(n{a}-1)}
       \neg \n{b})
      \n{s} = {\n1+\n2+\n3},
      n1 = \{ n1/n\{s\} \},
```

```
n2 = {n2/n\{s\}},
      n3 = {n3/n\{s\}},
    in ({n1*}x1+n2*x2+n3*x3,n1*y1+n2*y2+n3*_1
    y3})
 }
},
% ====== Circle Operations =======
% circle = {0,A}, creates circle with the center (0)
→ through A
circle/.style args = {#1,#2}{
  insert path = {
    let
      p{OA} = ($(#2)-(#1)$),
    in (#1) circle ({veclen(\p{OA})})
 }
},
% tagent point = {0,A,P}
% O,A: center of circle and an abitary point on the
% P: a point outside the circle
tangent point/.style args = {#1,#2,#3}{
  insert path = {
    let
      p{OA} = (\$(\#2) - (\#1)\$), \% 半径
      p{OP} = (\$(#3)-(#1)\$),
      n1 = \{veclen(p{OA})\},
      n2 = {veclen(p{OP})},
      n3 = {scalar(n1/n2)}
    in (\$(\#1)! \n3! \{acos(\n1/\n2)\}: (\#3)\$)
  }
```

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```
},
% external homothetic center
% 01,A1: center of circle 1 and an abitary point on the
% O2, A2: center of circle 2 and an abitary point on the
external center/.style args = {#1,#2,#3,#4}{
  insert path = {
    let
      \p{01A1} = ($(#2)-(#1)$),% 半径 01A1
      \p{02A2} = ($(#4)-(#3)$),% 半径 02A2
     n{r1} = {veclen(p{01A1})},
     n{r2} = {veclen(p{02A2})},
      n1 = {scalar(n{r1}/(n{r1}-n{r2}))}
    in (\$(#1)! \ln ! (#3)\$)
  }
},
% internal homothetic center
% O1, A1: center of circle 1 and an abitary point on the
% 02,A2: center of circle 2 and an abitary point on the

→ circle

internal center/.style args = {#1,#2,#3,#4}{
  insert path = {
    let
      \p{01A1} = ($(#2)-(#1)$),% 半径 01A1
      \p{02A2} = ($(#4)-(#3)$),% 半径 02A2
     n{r1} = {veclen(p{01A1})},
      n{r2} = {veclen(p{02A2})},
      n1 = {scalar(n{r1}/(n{r1}+n{r2}))}
```

```
in (\$(\#1)! \setminus n1! (\#3)\$)
  }
},
% creates the radical axis of two non-concentric
 % O1,A1: center of circle 1 and an abitary point on the
% 02,A2: center of circle 2 and an abitary point on the
 radical axis/.style args = \{\#1, \#2, \#3, \#4\}{
  insert path = {
    let
      \n{s} = {\pgfkeysvalueof{/tikz/start modifier}},
      \n{e} = {\pgfkeysvalueof{/tikz/end modifier}},
      \p{01A1} = ($(#2)-(#1)$),% 半径 01A1
      p{02A2} = ($(#4)-(#3)$),% 半径 02A2
      p{0102} = ($(#3)-(#1)$),
      n{r1} = {veclen(p{01A1})},
      n\{r2\} = \{veclen(p\{02A2\})\},\
      n{d} = {veclen(p{0102})},
      n1 = {scalar(n{r1}/n{d})},
      n2 = \{scalar(n\{r2\}/n\{d\})\},\
      n3 = \{.5*(1+n1*n1-n2*n2)\},
      p{ft} = ($(#1)!\n3!(#3)$),% perpendicular foot
      p{s0} = ($(p{ft})+(-y{0102}, x{0102})$),
      p\{e0\} = (\$(p\{ft\})+(y\{0102\},-x\{0102\})\$),
      p\{s\} = (\$(p\{s0\})! n\{s\}! (p\{e0\})\$), \%  start
      p\{e\} = (\$(p\{s0\})! n\{e\}! (p\{e0\})\$)\% end
    in (\p{s}) -- (\p{e})
  }
```

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```
},
% ====== Path Definitions =======
% perpendicular bisector of the line segment (#1 -- #2)
perpendicular bisector/.style args = {#1,#2}{
  insert path = {
    let
      \n{s} = {\pgfkeysvalueof{/tikz/start modifier}},
      \n{e} = {\pgfkeysvalueof{/tikz/end modifier}},
      p{AB} = ($(#2)-(#1)$),
      p\{m\} = (\$(\#1)!0.5!(\#2)\$),\% midpoint
      p\{s0\} = (\$(p\{m\})+(-y\{AB\}, x\{AB\})\$), \% rotate
       → ccw, default start
      p\{e0\} = (\$(p\{m\})+(y\{AB\},-x\{AB\})\$),\% rotate
       p\{s\} = (\$(p\{s0\})! n\{s\}! (p\{e0\})\$), \%  start
      p\{e\} = (\$(p\{s0\})! n\{e\}! (p\{e0\})\$)\%  end
    in (\p{s}) -- (\p{e})
  }
},
% perpendicular line of the line (#1 -- #2) through #3
% specifying start and end with modifiers(see tikz
 → manual 13.5)
perpendicular/.style args = {#1,#2,#3}{
  insert path = {
    let
      \n{s} = {\pgfkeysvalueof{/tikz/start modifier}},
      \n{e} = {\pgfkeysvalueof{/tikz/end modifier}},
      p{AB} = ($(#2)-(#1)$),
      p{ft} = ($(#1)!(#3)!(#2)$),% perpedicular foot
      \p{s0} = (\$(\p{ft}) + (-\y{AB}, \x{AB})\$),
```

```
p\{e0\} = (\$(p\{ft\})+(y\{AB\},-x\{AB\})\$),
      p\{s\} = (\$(p\{s0\})! n\{s\}! (p\{e0\})\$), \%  start
      p\{e\} = (\$(p\{s0\})! n\{e\}! (p\{e0\})\$)\%  end
    in (\p{s}) -- (\p{e})
  }
},
% parallel line of the line (#1 -- #2) through #3
% specifying start and end with modifiers(see tikz
 → manual 13.5)
parallel/.style args = \{\#1, \#2, \#3\}{
  insert path = {
    let
      \n{s} = {\pgfkeysvalueof{/tikz/start modifier}},
      \n{e} = {\pgfkeysvalueof{/tikz/end modifier}},
      p{s0} = (#3),
      p\{e0\} = (\$(#3)+(#2)-(#1)\$),
      p\{s\} = (\$(p\{s0\})! n\{s\}! (p\{e0\})\$), \%  start
      p\{e\} = (\$(p\{s0\})! n\{e\}! (p\{e0\})\$)\%  end
    in (\p{s}) -- (\p{e})
  }
},
% alias for parallel={A,B,A}
extend/.style args = {#1,#2} {
  parallel={#1,#2,#1}
},
% rotate around the origin by `angle` and then shift by
- (`xshift`,`yshift`)
% tansform = {angle:(xshift,yshift)}
transform/.style args = {#1:(#2,#3)} {
  cm = {cos(#1), sin(#1), -sin(#1), cos(#1), (#2,#3)}
```

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```
},
}
% Utilities for implementation of 'intercept'
\def\euclidea@ComputeLength#1,#2\euclidea@stop{
  \newdimen\euclidea@ax
  \newdimen\euclidea@ay
  \newdimen\euclidea@bx
  \newdimen\euclidea@by
  \pgfextractx{\euclidea@ax}{\pgfpointanchor{#1}{_|
center}}
  \pgfextracty{\euclidea@ay}{\pgfpointanchor{#1}{_|
center}}
  \pgfextractx{\euclidea@bx}{\pgfpointanchor{#2}{_|
center}}
  \pgfextracty{\euclidea@by}{\pgfpointanchor{#2}{_|
center}}
 % 以下 showthe 指令 overleaf.com 编译通过, 而在
  → macOS+texlive 2021 报错
  % \showthe\euclidea@ax
 % \showthe\euclidea@ay
  % \showthe\euclidea@bx
  % \showthe\euclidea@by
  \pgfmathveclen{\euclidea@ax-\euclidea@bx}{\_
   - euclidea@ay-\euclidea@by}
}
% Syntax of hyperbola:
  \hyperbola [options] (a,b);
% wherein, a,b are major/minor semi axis.
```

```
\newcommand\hyperbola{} % just for safety
\def\hyperbola[#1]#2(#3,#4){
  \path[smooth,domain=-1.5:1.5,#1,variable=\]
   → euclidea@temp]
    plot({-(#3)*cosh(\wedge euclidea@temp)}, {(#4)*sinh(\wedge_{\perp})})
     - euclidea@temp)}) % right arm
    plot({ (#3)*cosh(\euclidea@temp)},{(#4)*sinh(\_
     - euclidea@temp)}); % left arm
}
% Syntax of asymptote:
  \asymptote [options] (a,b);
% wherein, a,b are major/minor semi axis.
\newcommand\asymptote{} % just for safety
\def\asymptote[#1]#2(#3,#4){
  \path[domain=-2:2,#1,variable=\euclidea@temp,]
    plot({\euclidea@temp},{ (#4)/(#3)*(\euclidea@temp)})
    plot({\euclidea@temp}, {-(#4)/(#3)*(\euclidea@temp)});
}
\makeatother
```

参考文献

- [1] Syntax for path specifications. https://tikz.dev/tikz-paths.
- [2] Homothetic center. https://en.wikipedia.org/wiki/Homothetic_center.
- [3] Coordinate calculations. https://tikz.dev/tikz-coordinates#sec-13.5.
- [4] Line-line intersection. https://mathworld.wolfram.com/Line-LineIntersection.html.