

BUS 220

Finansiering og investering

- høst 2024

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Oppgavesett 0 - Fasit

### Renteregning

#### Oppgave 1

$$15000 \cdot 1,05^6 + 5000 \cdot 1,05^5 = 26482,84$$

#### Oppgave 2

På konto etter 3 år:  $100.000 \cdot 1,055^3 = \text{kr } 117.424,14$

Opprinnelig sparekapital: kr 100,000,00

Renter kr 17,424,14

#### Oppgave 3

a)

4 %	År1	År2	År3	År4
30000	31200	32448	33745,92	35095,76

b)

		Rente	Rentes rente	Sluttbeløp	Andel
Opprinnelig beløp	30000				
Etter år 1	30000	1200	0	31200	
Etter år 2	30000	1200	48	32448	0,001479
Etter år 3	30000	1200	98	33746	0,004324
Etter år 4	30000	1200	150	35096	0,008427

c) 30 000 pluss rentene det siste året (1200) dvs. 31200

d) Se ovenfor

e) Sluttbeløp etter 20 år =  $30\,000 \cdot (1,04)^{20} = 65\,734$

Herav enkel rente  $1200 \cdot 20 = 24000$

Gir rentes rente  $65734 - 30000 - 24000 = 11734$

Andel =  $11734 / 65734 = 0,1785$

#### Oppgave 4

$$92.000 \cdot 1,05^x = 150.000$$

$$1,05^x = 1,63043$$

$$X \approx 10 \text{ år}$$

## Oppgave 5

$$X \cdot 1,05^6 = 200.000$$
$$X = 149.243$$

Kan sløse bort:  $200.000 - 149.243 = 50.757$

## Oppgave 6

The decision involves comparing the present value, PV, of each option. Choose the option with the highest PV. Since the first cash flow occurs 0 years in the future, or today, it does not need to be adjusted.

$$PV(C_0) = \$1,000$$

Since the second cash flow occurs 10 years in the future, it must be discounted back 10 years at eight percent.

$$\begin{aligned} PV(C_{10}) &= C_{10} / (1+r)^{10} \\ &= \$2,000 / (1.08)^{10} \\ &= \$926.39 \end{aligned}$$

**Since the present value of the cash flow occurring today is higher than the present value of the cash flow occurring in year 10, you should take the \$1,000 now.**

## Oppgave 7

The decision involves comparing the present value, PV, of each option. Choose the option with the highest PV.

- a. At a discount rate of zero, the future value and present value of a cash flow are always the same. There is no need to discount the two choices to calculate the PV.

$$PV(\text{Alternative 1}) = \$10,000,000$$

$$PV(\text{Alternative 2}) = \$20,000,000$$

**Choose Alternative 2 since its PV, \$20,000,000, is greater than that of Alternative 1, \$10,000,000.**

- b. Discount the cash flows at 10 percent. Discount Alternative 1 back one year and Alternative 2, five years.

$$\begin{aligned} PV(\text{Alternative 1}) &= C / (1+r) \\ &= \$10,000,000 / (1.10)^1 \\ &= \$9,090,909.10 \end{aligned}$$

$$\begin{aligned} PV(\text{Alternative 2}) &= \$20,000,000 / (1.10)^5 \\ &= \$12,418,426.46 \end{aligned}$$

**Choose Alternative 2 since its PV, \$12,418,426.46, is greater than that of Alternative 1, \$9,090,909.10.**

- c. Discount the cash flows at 20 percent. Discount Alternative 1 back one year and Alternative 2, five years.

$$\begin{aligned}
 \text{PV(Alternative 1)} &= C / (1+r) \\
 &= \$10,000,000 / (1.20)^1 \\
 &= \mathbf{\$8,333,333.33}
 \end{aligned}$$

$$\begin{aligned}
 \text{PV(Alternative 2)} &= \$20,000,000 / (1.20)^5 \\
 &= \mathbf{\$8,037,551.44}
 \end{aligned}$$

**Choose Alternative 1 since its PV, \$8,333,333.33, is greater than that of Alternative 2, \$8,037,551.44.**

d. You are indifferent when the PVs of the two alternatives are equal.

$$\begin{aligned}
 \text{Alternative 1, discounted at } r &= \text{Alternative 2, discounted at } r \\
 \$10,000,000 / (1+r)^1 &= \$20,000,000 / (1+r)^5
 \end{aligned}$$

Solve for the discount rate,  $r$ , at which the two alternatives are equally attractive.

$$\begin{aligned}
 [1 / (1+r)^1] (1+r)^5 &= \$20,000,000 / \$10,000,000 \\
 (1+r)^4 &= 2 \\
 1+r &= 1.18921 \\
 r &= 0.18921 = \mathbf{18.921\%}
 \end{aligned}$$

**The two alternatives are equally attractive when discounted at 18.921 percent.**

## Oppgave 8

Har i banken etter 19 år:

$$X \cdot (1,043)^{19} = 150000$$

$$X = \frac{150000}{(1,043)^{19}} = 67405$$

## Oppgave 9

$$10.000 \cdot \frac{(1 + 0,055)^{18} - 1}{0,055} = 294.812$$

## Oppgave 10

$$\text{NV for 1. alternativ: } \frac{150.000}{1,04} + \frac{204.000}{1,04^4} = 318.610,82$$

$$\text{NV for 2. alternativ: } 38.000 + \frac{38.000}{1,04} + \dots + \frac{38.000}{1,04^9} = 320.542,62$$

$$\text{NV for 3. alternativ: } 300.000$$

$$\text{NV for 4. alternativ: } \frac{420000}{1,04^5} = 345.209,39$$

#### 4. alternativ er best

### Oppgave 11

Du vinner en tv-konkurranse og kan velge mellom følgende premier

- 1) 120 000 som utbetales om ett år
- 2) 170 000 etter fem år og så ingen ting før etter femten da du får 20 000 til.
- 3) 10 300 hvert år til evig, utbetales første gang i dag.
- 4) 16 000 hvert år i ti år utbetales første gang om ett år.
- 5) 7 000 neste år som øker med 4% hvert år siden

- a) Dersom kapitalkostnaden er 12 prosent, hvilken premie velger du?
- b) Dersom kapitalkostnaden er 5 prosent, hvilken premie velger du

NB: Vis utregninger

#### **Løsningsforslag:**

Regner om alt til nåverdier:

a) 12 prosent

- 1)  $120\,000/(1+0,12)=107142$
- 2)  $170\,000/(1+0,12)^5+20\,000/(1+0,12)^{15}=100116$
- 3)  $(10\,300/0,12)+10300=96133$
- 4)  $16\,000 * A$  ( $A$ =annuitetsfaktoren for rente 12% og 10 år) = 90 403
- 5)  $7000/(0,12-0,04)=87500$

Du velger alternativ 1

b) 5 prosent

- 1)  $120\,000/(1+0,05)=114285$
- 2)  $170\,000/(1+0,05)^5+20\,000/(1+0,05)^{15}=142819$
- 3)  $10\,300/0,05=216300$
- 4)  $16\,000 * A$  ( $A$ =annuitetsfaktoren for rente 12% og 10 år) = 123 547
- 5)  $7000/(0,12-0,04)=700\,000$

Du velger alternativ 5

### Oppgave 12

The deposit at the end of the first year will earn interest for six years, from the end of year 1 to the end of year 7.

$$\begin{aligned} FV &= \$1,000 (1.12)^6 \\ &= \$1,973.82 \end{aligned}$$

The deposit at the end of the second year will earn interest for five years.

$$\begin{aligned} FV &= \$1,000 (1.12)^5 \\ &= \$1,762.34 \end{aligned}$$

The deposit at the end of the third year will earn interest for four years.

$$\begin{aligned}\text{FV} &= \$1,000 (1.12)^4 \\ &= \$1,573.52\end{aligned}$$

The deposit at the end of the fourth year will earn interest for three years.

$$\begin{aligned}\text{FV} &= \$1,000 (1.12)^3 \\ &= \$1,404.93\end{aligned}$$

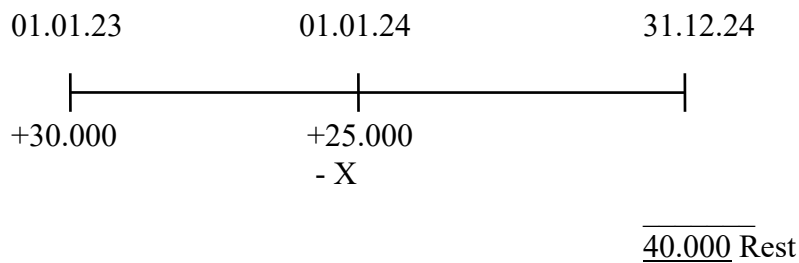
Combine the values found above to calculate the total value of the account at the end of the seventh year:

$$\begin{aligned}\text{FV} &= \$1,973.82 + \$1,762.34 + \$1,573.52 + \$1,404.93 \\ &= \mathbf{\$6,714.61}\end{aligned}$$

**The value of the account at the end of seven years will be \$6,714.61.**

### Oppgave 13

Kan maksimalt ta ut kr X



$$30000 \cdot 1,05 = 31.500$$

$$(31.500 + 25.000 - X) \cdot 1,05 = 40.000$$

$$59.325 - 1,05X = 40.000$$

$$1,05X = 19.325$$

$$X = \underline{18.404}$$

Han kan altså ta ut 18404 kroner 01.01.24.