

Constant Optimizations

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What Are Constant

Optimizations?

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- For example, searching for palindromic numbers can be done by iterating through integers in ascending order.
- Noticing that all palindromic integers are divisible by 11 allows for a constant optimization, where the time complexity remains the same.

Sometimes the slowest part of your program is reading input and writing output. We can limit the impact I/O has on our program by:

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- (C++) using a custom built function to read integers: LINK
- (Python) using sys.stdin and sys.stdout, and only flushing when needed. Note that print and input may flush your output arbitrarily, possibly slowing your program unnecessarily.
- (Java): I do not know how to make it fast, if I/O is a bottleneck, use a different language maybe? Kattio.java exists but is not even comparable to C++ speed.

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- We will be examining a bit how data and instructions are processed by a CPU.
- Be aware that microbenchmarks such as the ones I made for the slides may not always mean the changes translate perfectly into efficiency for real world code.
- The intent is to teach you the ideas. Do not assume that doing things manually guarantees speed increases! Try it out!

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- Temporal locality: A recently accessed (memory) address is likely to be accessed in the near future.
- Spatial locality: An address nearby a recently accessed address likely to be accessed in the near future.

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   int result = 0;
   for (int i = 0; i < N; i++) {
      result += a[i];
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- Here the same instructions are used in each iteration of a short loop: temporal locality of instructions
- Here array elements are accessed in increasing order with no gaps: spatial locality of data
- Here instructions are processed sequentially: spatial locality of instructions

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int sum_by_col(int arr[N][M]){
   int result = 0;
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- That way the CPU cache will be utilized better.

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A Scheduling Problem - From Errichto on CF

Problem description

There are N workers, where $1 \leq N \leq 5\,000.$ Each worker is either available or unavailable each day. There is a 30 day window for a two man group project. The project can only be worked on if both group members are available. You may assume all workers are equally competent, so you only want to maximize the number of days they work together. What is the best pair of workers to select?

```
vector<vector<int>> workers:
int intersection(int a, int b) {
    int i = 0, j = 0;
    int result = 0;
    while (i < N && j < N) {
        if (workers[a][i] == workers[b][j]) {
            result++, i++, j++;
        else if (workers[a][i] < workers[b][j]) {</pre>
            i++:
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```
vector<int> workers:
int intersection(int a, int b) {
    int result = 0;
    int inter = workers[a] & workers[b];
    for (int i = 0; i < D; i++) {
        if (inter & 1) {
            result++;
        inter >>= 1;
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    return result;
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- It's time complexity is $\mathcal{O}(1)$ and most CPUs have it as a single instruction.
- Now our time complexity is $\mathcal{O}(N^2)$ and the code runs fast enough.
- But wait, there is more!

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- What if D > 64?

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The Infamous Bitset

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- We could make a size $\left\lceil \frac{D}{w} \right\rceil$ array using w-bit integers to store our set.
- Implementing this includes a lot of shifts and indexing and it is easy to make a mistake and get it wrong.

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- The array is therefore 1024^3 bytes or 1 Gibibyte.
- Bitsets use the method discussed previously, packing 8 booleans in each byte.
- A bitset<1 \ll 30> is therefore 1024^3 bits or 128 Mebibytes.

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constexpr int D{ 365 };
constexpr int max_n{ 5'000 };
bitset<D> workers[max_n];
int intersection(int i, int j) {
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- Practice problem: Chef and Queries

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- Loops are the same, either you repeat or break from the loop.
- A higher number of iterations on average with less branching is often faster.

```
constexpr int N{ 100'000'000 };
int arr[N];
int regular_loop(int arr[N]) {
    int sm = 0;
    for (int i = 0; i < N; i++) {
        if (arr[i] % 3 == 0) sm -= arr[i];
        else if (arr[i] \% 3 == 2) sm += arr[i];
    return sm;
}
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 This code adds up all the numbers in an array with a slight modification.

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constexpr int N{ 100'000'000 };
int arr[N];
int unroll_2_loop(int arr[N]) {
    int sm = 0;
    for (int i = 0; i < N; i+=2) {
        if (arr[i] \% 3 == 0) sm -= arr[i]:
        else if (arr[i] \% 3 == 2) sm += arr[i]:
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constexpr int N{ 100'000'000 };
int arr[N];
int branchless(int arr[N]) {
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   for (int i = 0; i < N; i++) {
      sm += (arr[i] % 3 - 1) * arr[i];
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   return sm;
}</pre>
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 Often we can use multiplication or bitmasks as a replacement for arithmetic within if blocks.

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int branchless_16(int arr[N]) {
    int sm = 0;
    for (int i = 0; i < N; i+=16) {
        sm += (arr[i] \% 3 - 1) * arr[i]:
        sm += (arr[i+1] \% 3 - 1) * arr[i+1];
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        sm += (arr[i+15] \% 3 - 1) * arr[i+15];
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Single Instruction, Multiple Data

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- See documentation for details on functions.

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#include <x86intrin.h> // includes all SIMD intrinsics
constexpr int N{ 100'000'000 };
int arr[N]:
int simd(int arr[N]) {
    __m128i sm = _mm_setzero_si128();
    _{m128i} one = _{mm_{set_{epi32}(1, 1, 1, 1)}};
    for (size_t i = 0; i < N; i+=4) {
        __m128i nums = _mm_loadu_si128((__m128i*) (arr+i));
        __m128i to_add = _mm_set_epi32(arr[i+3]%3, arr[i+2]%
        to_add = _mm_sub_epi32(to_add, one);
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        sm = _mm_add_epi32(sm, to_add);
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- When you do it yourself it is crucial to test whether it is actually faster.
- Constant time improvements are sometimes easier than algorithmic improvements, and may prove sufficient.