

# Working Title: Improving Dark Matter Axion Searches with Active Resonators

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Axions are a well motivated candidate for dark matter. The most sensitive experiments searching for dark matter axions rely on the coupling of axions to the electromagnetic resonances of a microwave cavity immersed in a strong magnetic field. The sensitivity of the experiment is proportional to the  $Q$  of the resonance that is coupled to axions. To date, the resonators used in axion searches have all been passive, with  $Q$ s limited by power loss in the cavity walls. I propose the use of active feedback resonators to increase the  $Q$  of microwave cavity axion dark matter experiments by several orders of magnitude. This should allow experiments to significantly increase the rate at which they can test potential axion masses and couplings.

## INTRODUCTION

The axion is a hypothetical particle that is both a candidate for dark matter and a result of the Peccei-Quinn solution to the strong CP problem [1–7]. Axions with masses below  $10^{-3}$  eV are particularly interesting because they could be produced in sufficient quantities to account for dark matter [8]. For axions in this mass range the coupling between axions and photons, despite being exceptionally weak, provides the best chance of directly observing axion dark matter.

The most sensitive dark matter axion searches to date have been of the “microwave cavity” type. These experiments rely on the conversion of axions from the local dark matter halo into photons in a strong magnetic field. This conversion is resonantly enhanced when the resonant frequency of the microwave cavity is equal to the frequency of the photons produced from the axion conversion [9]. Operation of these experiments involves slowly tuning the resonant frequency of the microwave cavity to explore different potential axion masses and searching for an excess of power deposited from dark matter axion conversion. Microwave cavity experiments have been demonstrated to have the sensitivity required to detect optimistically coupled dark matter axions over a small mass range, but as of yet, axions have not been detected in a microwave cavity experiment [10].

The signal power in microwave cavity experiments is proportional to a number of factors, including the local density of dark matter, the strength of the magnetic field, the volume of the cavity, and the resonant quality factor  $Q$  of the resonance being used. The primary background is the thermal noise from the physical temperature of the cavity and the electronic noise from the first stage amplifier. The figure of merit for a microwave cavity experiment is the instantaneous axion signal to noise ratio (SNR). Experiments with a larger SNR can be sensitive to more pessimistic axion photon couplings for a given frequency tuning speed or tune more quickly for a given axion photon coupling sensitivity.

Increasing the cavity  $Q$  is one way to increase SNR in a microwave cavity experiment; the speed at which the cav-

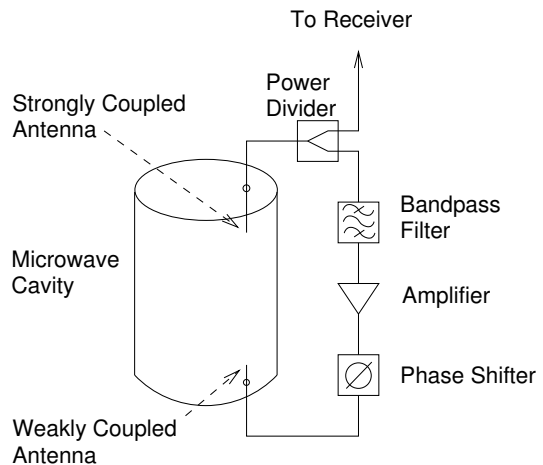


FIG. 1. Schematic of active feedback resonator for an axion experiment

ity frequency can be tuned while remaining sensitive to a given axion photon coupling is linearly proportional to  $Q$  [11]. The presence of a strong magnetic field precludes the use of high- $Q$  superconducting cavities in these experiments, so the cavities are usually made of or coated with copper. Loaded  $Q$ s of  $10^5$  at 1 GHz have been achieved with copper cavities in axion experiments [11]. Higher frequency cavities typically have smaller  $Q$ s.

I present here a means of artificially increasing the  $Q$  of the cavity resonance using active feedback in order to improve sensitivity to dark matter axions and increase the speed at which different axion masses can be tested.

## Axions, Dark Matter, and Microwave Cavities

### Technological Limitations, Overcoming them with Active Resonators

## SCHEMATIC

The use of active feedback resonators is a well established technique used in regenerative receivers [12]. It

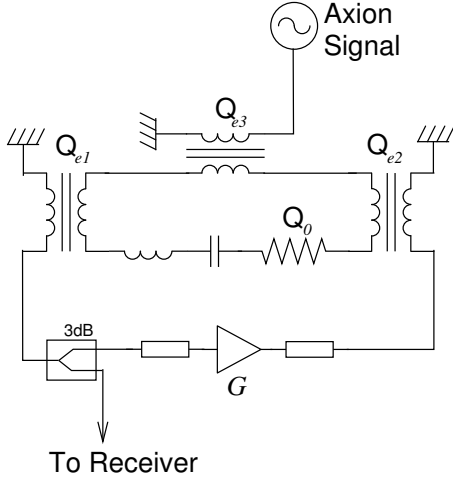


FIG. 2. Equivalent circuit to axion photon conversion in microwave cavity with active regeneration

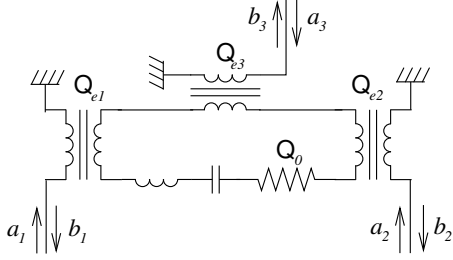


FIG. 3. Microwave cavity represented as three port device.

involves connecting positive feedback to a resonator at the appropriate phase and amplification such that the power lost each oscillation to the output and damping effects is nearly completely replaced. This has the effect of increasing the  $Q$  of the system.

A schematic of a microwave cavity axion experiment with active feedback is shown in Fig. 1. Power from axion to photon conversion exits the cavity via a strongly coupled antenna, some of which is sent to a detector. The remainder of the power is amplified, phase shifted, and then fed back into the cavity via a weakly coupled antenna. A filter may also be needed to select the desired mode.

## THEORY

### Derive multiplicative factor to gain

To calculate the effect of the active feedback, I will use the equivalent circuit to the cavity-amplifier system shown in Fig. 2. The cavity resonant mode is equivalent to an  $LRC$  circuit with an unloaded  $Q$  of  $Q_0$  and the coupled antennas are equivalent to transformers with couplings  $Q_{e1}$  and  $Q_{e2}$  [13].  $G$  is the com-

bined gain of the amplifier and power divider. There is also a phase shift between the two antennas around the loop, which will be denoted as  $\delta$ . The coupling between the electromagnetic resonance in the cavity and dark matter axions is equivalent to a third antenna with coupling  $Q_{e3}$ . The passive loaded  $Q$  of the resonator is  $Q_L = (Q_0^{-1} + Q_{e1}^{-1} + Q_{e2}^{-1} + Q_{e3}^{-1})^{-1}$ .

I can now treat the cavity as a three port device using amplitudes defined in Fig. 3 with an  $S$  matrix of

$$S_{\text{cavity}} = \begin{pmatrix} \frac{2Q_L}{Q_{e1}} - 1 & \frac{2Q_L}{\sqrt{Q_{e1}Q_{e2}}} & \frac{2Q_L}{\sqrt{Q_{e1}Q_{e3}}} \\ \frac{2Q_L}{\sqrt{Q_{e1}Q_{e2}}} & 1 - \frac{2Q_L}{Q_{e2}} & \frac{2Q_L}{\sqrt{Q_{e2}Q_{e3}}} \\ \frac{2Q_L}{\sqrt{Q_{e1}Q_{e3}}} & \frac{2Q_L}{\sqrt{Q_{e2}Q_{e3}}} & 1 - \frac{2Q_L}{Q_{e3}} \end{pmatrix} \quad (1)$$

assuming the resonant frequency of the cavity has been tuned to the axion frequency.

The output amplitude  $b_1$  can be determined with the cavity  $S$  matrix

$$\begin{pmatrix} b_1 \\ b_2 \\ b_3 \end{pmatrix} = S_{\text{cavity}} \begin{pmatrix} a_1 \\ a_2 \\ a_3 \end{pmatrix}, \quad (2)$$

the effect of the amplifier and phase shifter

$$a_2 = \sqrt{G}b_1e^{i\delta}, \quad (3)$$

and  $a_1 = 0$ . I will take  $\delta$  to have been chosen to be an integral multiple of  $2\pi$ . This gives

$$b_1 = \frac{2MQ_L}{\sqrt{Q_{e1}Q_{e3}}}a_3 \quad (4)$$

where I define  $M$  to be the apparent multiplier to the  $Q$  of the system

$$M = \left( 1 - 2Q_L \sqrt{\frac{G}{Q_{e1}Q_{e2}}} \right)^{-1}. \quad (5)$$

Note that for a passive resonator  $M = 1$  and that systems with  $M < 0$  will oscillate regardless of the presence of an axion signal.

I note that from the signal power derived in Refs. [14, 15],

$$\frac{|a_3|^2}{Q_{e3}} = g_{a\gamma\gamma}^2 V B_0^2 \rho_a C \frac{1}{m_a} \quad (6)$$

where  $V$  is the volume of the microwave cavity,  $B_0$  is the magnetic field strength,  $\rho_a$  is the density of dark matter axions,  $C$  is a mode dependent form factor of order 1, and  $m_a$  is the axion mass.  $g_{a\gamma\gamma}$  is the axion-photon coupling strength, defined as  $g_{a\gamma\gamma} = \frac{\alpha g_\gamma}{\pi f_a}$  where  $\alpha$  is the fine structure constant,  $f_a$  is the axion decay constant and  $g_\gamma$  is an order unity model dependent factor.

The power measured at the output of the system is thus

$$P_{\text{signal}} = \frac{M^2 Q_L^2}{Q_{e1}} g_{a\gamma\gamma}^2 V B_0^2 \rho_a C \frac{1}{m_a} \quad (7)$$

It is important to note that for the isothermal halo model of dark matter axions, the characteristic width of the axion signal is expected to correspond of a  $Q$  of  $10^6$  [16]. Experiments with a bandwidth smaller than the axion signal width sample only a subset of axions. Thus the conservative estimate for signal power is

$$P_{\text{signal}} = \frac{M}{2} \min(MQ_L, 10^6) g_{a\gamma\gamma}^2 V B_0^2 \rho_a C \frac{1}{m_a}, \quad (8)$$

though it could be larger in models where the axion dark matter is unusually cold.

The thermal noise from the physical temperature of the cavity and electronic noise of the amplifier are also magnified by the active feedback.

## LITERATURE REVIEW

MENTION ARMSTRONG, MARK JONES SHOULD WE MENTION DISAGREEMENT BETWEEN ISAKAWA and ITALIAN?

## SNR AND BANDWIDTH

SNR expression (9)

FIGURE OF MERIT, ACCOUNTING FOR REDUCTION IN BW (10)

## MEASUREMENTS

### Results

### Comparison with Simulation

## DISCUSSION

Values of  $M$  have been reported as high as  $10^4$  yielding  $Q$ s of  $7 \times 10^7$  in active feedback resonators [17] used for other purposes, but that were operated at frequencies that could be relevant to dark matter axion searches. This would suggest existing experiments could increase their SNR by several orders of magnitude by implementing active feedback.

The ADMX experiment is within an order of magnitude of the sensitivity necessary to be sensitive to pessimistically coupled axion dark matter. The addition of active feedback, along with other planned upgrades,

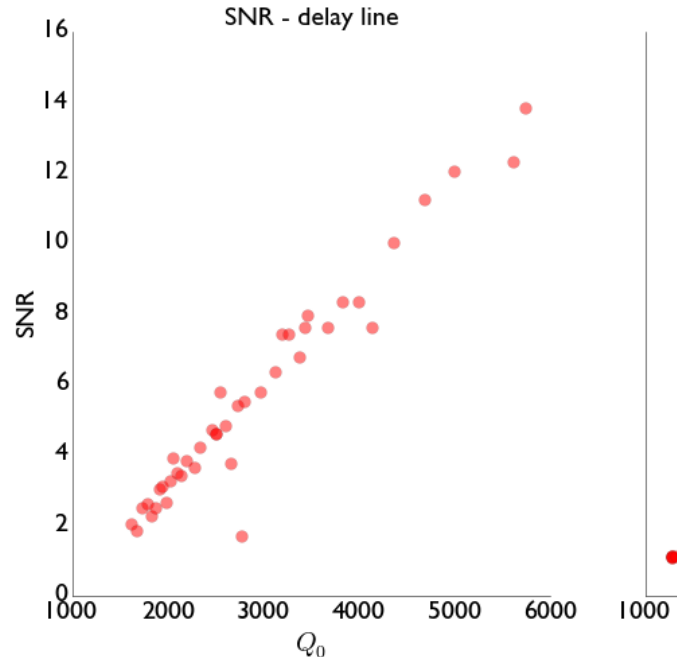


FIG. 4.

should allow it to be sensitive to pessimistically coupled axion dark matter even in models where axions constitute a very small fraction of the dark matter. The use of active feedback will also allow future experiments to operate at higher frequencies, where previous microwave cavity experiments have not had the sensitivity necessary to detect axion dark matter with a reasonable scan speed.

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## WILD SPECULATION

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