
PyESG Documentation

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Feng Zhu

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INTRODUCTION

The Python library of Earth Spherical Geometry (PyESG) is aiming to perform spherical geometry on the earth and interpolate data from an unstructured mesh grid to another one, which is the so-called “regridding” or “remapping”.

SPHERICAL GEOMETRY

2.1 Point

2.2 Arc

2.3 Triangle

2.4 Quadrangle

2.5 Mesh

REGRIDDING

This section will introduce the algorithm for regridding in the PyESG.

3.1 Search

3.2 Interpolation

CLASSES

class pyesg.**Arc** (*p1, p2*)

An arc on the earth defined by two points p1 and p2. It also can be seen as the relationship between two points.

distance ()

Calculate the great-circle distance of the arc.

[reference: http://en.wikipedia.org/wiki/Great-circle_distance]

rad ()

Convert great-circle distance on the earth to radians.

waypoint (*k*)

Calculate the location of a selected point (lat, lon) according to: + the location of point 1 (lat1, lon1); + the location of point 2 (lat2, lon2); + the coefficient k decides the position between point 1 and point 2,

e.g.: + when k = 0.0, (lat, lon) is point 1; + when k = 0.5, (lat, lon) is the mid-point; + when k = 1.0, (lat, lon) is point 2. [reference: http://en.wikipedia.org/wiki/Great-circle_navigation]

class pyesg.**Interp**

Interpolation algorithms.

barycentric (*point, triangle*)

(point, triangle) -> weight1, weight2, weight3

Barycentric Interpolation: interpolation in a triangle.

[reference: <https://classes.soe.ucsc.edu/cmps160/Fall10/resources/barycentricInterpolation.pdf>]

regrid (*mesh_old, mesh_new, method='standard'*)

(mesh_old, mesh_new) -> matrix of weights and points indices.

Calculate the remapping coefficients (weights) from an old mesh to a new mesh. + When method == standard, the search algorithm can resolve any situation but slow; + When method == quick, the situation is that mesh_old and mesh_new are very similar to each other with some points nudged.

class pyesg.**Mesh** (*lat2d, lon2d*)

Unstructured mesh grids, which is defined by 2 dimensional arrays lat2d and lon2d.

class pyesg.**Point** (*lat, lon*)

A point on the earth defined by the latitude and longitude (unit: degree).

lat_deg ()

radians -> degree

lon_deg ()

radians -> degree

spherical_coord ()

p (lat, lon) -> x, y, z

Return the (x, y, z) in a UNIT spherical coordinate system.

[reference: http://en.wikipedia.org/wiki/Spherical_coordinate_system]

vector ()

Return the vector from the center of the Earth to the point.

class `pyesg.Quadrangle` (*p1, p2, p3, p4*)

An quadrangle on the earth defined by three points p1, p2, p3, and p4. It also can be seen as the relationship between four points.

Note: p1 -> p2 -> p3 -> p4 should be rotative.

angles ()

Treated as two triangles.

area ()

[reference: <http://mathworld.wolfram.com/SphericalPolygon.html>]

class `pyesg.Triangle` (*p1, p2, p3*)

An triangle on the earth defined by three points p1, p2, and p3. It also can be seen as the relationship between three points.

angles ()

Calculate the included angle between two sides on the earth. If we set a is the side p2-p3, b the side p3-p1, and c the side p1-p2. Then the return value A is the included angle between sides b and c.

area ()

Calculate the area of the triangle bounded by the sides made by the three points p1 (lat1, lon1), p2 (lat2, lon2), and p3 (lat3, lon3) according to the Girard's Theorem: $\text{area} = R^2 * E$, where R is the radius of the sphere, and E the angle excess: $E = A + B + C - \pi$. Cosine rules are used to calculate the angles A, B, and C.

[references: <http://www.princeton.edu/~rvdb/WebGL/GirardThmProof.html>
http://en.wikipedia.org/wiki/Spherical_trigonometry <http://mathforum.org/library/drmath/view/65316.html>
]

5.1 Author

5.2 License

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