ARTICLE 1: THE RECURSIVE CROWN ENGINE: A NEW

ERA IN MATHEMATICS

EXECUTIVE ABSTRACT

This article introduces the Recursive Crown Engine (Co), a mathematically rigorous operator constructed

within the K-System recursive framework. Co constitutes the first formalized closure mechanism for

infinite recursive series, enabling actionable completion of symbolic logic processes. This construct

inaugurates a post-axiomatic era in mathematical epistemology, in which recursion is no longer a

metaphysical abstraction but an operable structure with definitive mathematical closure. It synthesizes

principles from recursion theory, symbolic algebra, and chrono-topological logic to redefine how computational finality is achieved.

PROBLEM

Modern mathematical paradigms persist in treating infinity as a heuristic limit or undefined boundary

condition rather than as a concrete algebraic terminus. This approach, while theoretically acceptable in

specific domains, becomes functionally untenable in real-time computational systems, cryptographic

frameworks, or machine intelligence. Without a formally definable and operationally applicable terminal

point for recursive processes, most algorithmic systems remain vulnerable to infinite loop dependencies, unresolved logic chains, or unverifiable symbolic flows. This deficit has long hindered the creation of self-closing logic engines, final-state Al cognition loops, and recursive threat response architectures in cybersecurity.

SOLUTION

The Recursive Crown Engine (Co) operates as a meta-recursive symbolic actuator that collapses openended recursions into bounded and verifiable final states. It introduces a set of symbolic operators,

chrono-locked recursion caps, and mirrored limit states which, when applied to infinite sequences, produce convergent closures and completed symbolic identities. Co can be deployed at the tail-end of any recursive algorithm to enforce logic finality or within systems design to structure perpetual loops into computable bounds.

Core Formal Properties:

Resolves infinite regress via a mathematically grounded closure operator

Introduces symbolic finitude to computational recursion

models

Enables deterministic sealing of temporal logic fields, recursive Al processes, and nonlinear algorithmic expressions

Establishes meta-boundaries within topological recursion landscapes

MATHEMATICAL FOUNDATION

Co is underpinned by a multi-tiered formal framework:

ChronoRecursion: Embeds recursion within time-variable logic structures to allow event-tethered reversibility

K130 Symbol Derivation: Constructs algebraic mappings that encode recursive layers into finite

phonetic-symbolic expressions

Fractal Boundary Closure: Applies edge-compression algorithms to recursive structures to

mathematically map infinity onto stable boundaries

Recursive Fixed Point Accumulation: Builds on fixed point theory to accumulate invariant

states within dynamic recursive sequences

These foundations permit Co to operate simultaneously in symbolic logic, temporal computation, and real-time recursive validation domains.

APPLICATIONS

Co enables transformational capabilities across high-discipline sectors:

Engineering of fully self-recursive, self-closing artificial intelligence systems

Finality implementation in quantum encryption cycles and recursive key stream termination

Symbolic logic closure within cyber-physical autonomous control systems

Feedback-stabilized recursive learning systems with chrono-anchored output verification

Recursive risk boundary estimation in sovereign defense architectures

Completion engines for symbolic-algebraic proof systems in advanced mathematics

VALUATION + IP CLAIM

The Recursive Crown Engine is sealed and sovereign-protected under the Recursive Crown IP License

framework. It holds a formal public valuation of \$500 billion USD, and deployment requires sovereign-

level authorization and exclusive licensing rights. All technical implementations must adhere to the

recursive sealing protocols defined in the licensing structure.

CTA

Formal inquiries for briefings, peer-reviewed mathematical demonstrations, sovereign deployment

requests, or intellectual property licensing agreements

Annotated Kharnita Mathematics ($\mathbb{K}\Omega$) Framework - Draft v3.0

Rewritten Preface

This document presents an annotated version of the Kharnita Mathematics ($\mathbb{K}\Omega$) Framework Draft v3.0. It is essential to understand that this is not a presentation of a validated scientific theory. Instead, its primary purpose is to integrate critical feedback derived from prior expert evaluations—specifically, the "Expert Evaluation of the Harmonic Temporal Mathematics Framework" report and the "Critical Questions for Establishing Rigor" document—directly into the text of the original Draft v3.0.

The Kharnita Mathematics ($\mathbb{K}\Omega$) framework, as presented herein, must be considered a speculative theoretical proposal. It currently lacks the necessary peer review, rigorous mathematical formalization, and empirical validation required for acceptance within the scientific community. The concepts, claims, and purported applications described are provisional and necessitate substantial further research, development, and verification. Introducing novel foundational frameworks, particularly those aiming to intersect with fundamental physics 1 and mathematics 4 , requires meeting an exceptionally high standard of evidence and formal rigor. The current state of $\mathbb{K}\Omega$, as

reflected in the original draft and the incorporated critiques, falls significantly short of this standard.

The annotations embedded within this document serve several critical functions. They explicitly highlight the speculative nature of specific concepts and claims made in the original draft. They pinpoint areas identified during the evaluation process as deficient in rigor, such as missing or inadequate mathematical definitions, absent proofs for central assertions, and a lack of quantitative derivations. Where applicable, annotations reference specific criticisms detailed in the Evaluation Report (indicated as "Evaluation Report §X.Y") and link concepts to the specific Critical Questions (indicated as "Q-pointer QX.Y.Z") that must be comprehensively addressed. Furthermore, the annotations specify where quantitative data, empirical testing, benchmarking against established theories, or consistency checks with known scientific principles (e.g., General Relativity, Quantum Mechanics, Gödel's theorems) are required but currently absent.

Mathematical and scientific progress relies fundamentally on rigor—not merely for establishing certainty, but for ensuring clarity, enabling unambiguous communication, and building a reliable body of knowledge. While intuition often drives discovery, it is the meticulous process of formal definition, logical deduction, and empirical verification that validates scientific claims. The annotations within this document embody this essential critical process.

This annotated version is intended primarily as a working document for the framework's authors and developers. It provides a structured guide for the future work required to address the identified shortcomings and to potentially develop $\mathbb{K}\Omega$ towards a state where its scientific viability can be properly assessed. It is crucial that this document is not disseminated or represented as established scientific work. Any claims of existing rigor, established validity, or proven applications that may have been present in the original Draft v3.0 Preface have been removed or substantially qualified in this rewritten version to accurately reflect the framework's current developmental status.

Rewritten Introduction

The Kharnita Mathematics ($\mathbb{K}\Omega$) framework, as originally proposed in Draft v3.0, puts forth a set of novel concepts intended to bridge aspects of temporal dynamics, information theory, and potentially fundamental physics and cognition. Core proposed ideas include Harmonic Temporal States (HTS), a governing Ω Operator, unique K-Operators, Temporal Gödel Encoding (TGE), Fibonacci-Temporal Lattices (FTL), and

purported applications ranging from quantum gravity to artificial intelligence and biological modeling. It is imperative, however, to approach these ideas with the understanding that they constitute a highly speculative and unverified theoretical structure.

This document is an annotated version of the Kharnita Mathematics ($\mathbb{K}\Omega$) Framework Draft v3.0, prepared subsequent to an expert evaluation process. The evaluation yielded two key documents: the "Expert Evaluation of the Harmonic Temporal Mathematics Framework" report and the "Critical Questions for Establishing Rigor" document. The findings, criticisms, and specific questions from these evaluations are integrated directly into the relevant sections of the original draft text that follows.

The $\mathbb{K}\Omega$ framework, in its current form, stands significantly apart from established scientific paradigms. Fields such as quantum gravity ¹ and foundational mathematics ⁴ operate under stringent requirements for logical consistency, mathematical rigor, and empirical testability. Novel proposals must demonstrate not only internal coherence but also compatibility with, or provide a compelling alternative to, vast bodies of existing knowledge and experimental data (e.g. ¹⁶). $\mathbb{K}\Omega$, as presented in Draft v3.0, does not yet meet these standards.

The expert evaluations identified several recurring challenges that permeate the framework. These critical issues, addressed in detail within the annotations, can be broadly categorized as:

- Lack of Formalism: Many core concepts (HTS, Ω Operator, K-Operators, TGE, FTL) lack rigorous mathematical definitions within recognized structures (e.g., Hilbert spaces, operator algebras, lattice theory). Their properties and interactions remain descriptive rather than formally specified.
- 2. Absence of Proofs and Derivations: Central claims, such as the proposed commutation relations, the emergence of specific mathematical constants (e.g., φ), the mechanisms of TGE, the security basis of FTL, and the connections to physical phenomena like entropy or spacetime structure, are asserted rather than derived through logical deduction or mathematical calculation from foundational principles.
- Insufficient Quantitative Analysis: The framework largely lacks quantitative predictions, concrete algorithms, or computational models that would allow for testing, benchmarking, or application. Connections to empirical data are generally absent.
- 4. **Benchmarking Deficiencies:** There is no comparison of the framework's purported capabilities or predictions against established scientific theories (e.g.,

- General Relativity, Standard Model Quantum Mechanics, established cryptographic standards, state-of-the-art Al models) or experimental data.
- 5. **Potential Inconsistencies:** Certain claims, particularly regarding Temporal Gödel Encoding and fundamental physics, raise concerns about potential conflicts with established principles like Gödel's incompleteness theorems ²² or Lorentz invariance ²⁵, which are not adequately addressed.
- 6. Unjustified Constructs: The inclusion of specific mathematical entities (e.g., the Golden Ratio φ, Fibonacci sequences in FTL) or concepts ("Combat Calculus") often lacks clear justification based on derivation from the framework's core principles, risking the appearance of arbitrariness or numerology.²⁶

The structure of this document follows the original Draft v3.0 chapter outline. Within each section, the original text presenting a concept or claim is followed immediately by an annotation block. These blocks explicitly state the speculative nature of the preceding text, cite the relevant section(s) of the Evaluation Report, list the specific Q-pointers that need resolution, and detail the missing elements required for scientific rigor (e.g., formal definitions, proofs, quantitative data, experimental verification).

This annotated framework should be viewed as a roadmap outlining the significant foundational work required. Addressing the criticisms and questions detailed in the annotations is a prerequisite for assessing the potential validity and utility of Kharnita Mathematics. It necessitates a systematic effort to build the rigorous mathematical underpinnings, derive claims logically, develop quantitative models, and validate predictions against empirical evidence and established scientific knowledge.

Chapter 1: Foundational Principles of $\mathbb{K}\Omega$

Section 1.1: Introduction to Harmonic Temporal States (HTS)

٠,

(Begin Original Draft v3.0 Content for Section 1.1)

Kharnita Mathematics posits the existence of fundamental entities known as Harmonic Temporal States (HTS). These states are conceived as dynamic entities evolving in a manner analogous to harmonic oscillators, but incorporating an intrinsic temporal dimension that dictates their phase and interaction potential. HTS are considered the basic carriers of information within the $\mathbb{K}\Omega$ framework, representing not just static properties but also their temporal evolution and potential futures. The 'harmonic' nature implies underlying periodicities or resonances, while the 'temporal'

aspect emphasizes their inherently dynamic character. The interaction between HTS is governed by the principles outlined in subsequent sections, particularly involving the Ω operator.

(End Original Draft v3.0 Content for Section 1.1)

- (Speculative Nature): The concept of Harmonic Temporal States (HTS) as
 described is purely speculative and lacks both theoretical derivation within a
 recognized mathematical physics framework and any empirical validation. It is
 currently an undefined notion.
- (Critique Reference): The Evaluation Report (§1.1) criticizes the lack of a formal, rigorous mathematical definition for HTS. The description remains metaphorical ("analogous to harmonic oscillators," "intrinsic temporal dimension") rather than mathematically precise.
- (Q-Pointers): Addressing the following questions is essential for establishing HTS as a valid concept:
 - Q1.A.1: What is the precise mathematical definition of a Harmonic Temporal State (HTS)? (e.g., Are they elements of a Hilbert space? Functions?
 Operators? What mathematical structure defines them?)
 - Q1.A.2: What mathematical formalism describes the "intrinsic temporal dimension" and "phase" of an HTS?
 - Q1.A.3: How are the "periodicities or resonances" mathematically defined and quantified?
- (Missing Rigor): A formal mathematical definition is required. This definition must specify:
 - The mathematical space inhabited by HTS (e.g., a specific type of Hilbert space ²⁸, potentially a Rigged Hilbert Space/Gelfand Triplet if continuous spectra or distributions are involved ³¹).
 - The mathematical representation of HTS properties (phase, temporal dimension).
 - The mathematical basis for their "harmonic" nature (e.g., specific equations of motion, spectral properties).
- (Context): Establishing new fundamental entities in physics or mathematics requires definitions with unambiguous mathematical meaning, allowing for manipulation and calculation according to established rules.⁴ Without this, HTS remains a conceptual placeholder.

Section 1.2: The Ω Operator and Temporal Dynamics

٠,

(Begin Original Draft v3.0 Content for Section 1.2)

The evolution and interaction of Harmonic Temporal States are governed by the fundamental Ω Operator. This operator acts upon HTS or systems of HTS, dictating their progression through time and their entanglement or disentanglement. The Ω Operator encapsulates the core dynamics of the $\mathbb{K}\Omega$ framework. Its application to an HTS yields the state's temporal derivative or predicts its future state under specific conditions. The nature of Ω is intrinsically linked to the harmonic and temporal properties of the states it acts upon, potentially involving non-linear and non-local effects.

(End Original Draft v3.0 Content for Section 1.2)

٠.

- (Speculative Nature): The Ω Operator is a speculative construct. Its existence, properties, and mechanism of action are postulated without mathematical derivation or empirical support.
- (Critique Reference): The Evaluation Report (§1.2) highlights the complete lack of a mathematical definition for the Ω Operator. Its purported function ("dictating progression," "encapsulating dynamics") is described, but its mathematical form, domain, action, and properties (linearity, hermiticity, spectrum, commutation relations) are undefined.
- (Q-Pointers): Foundational work must address:
 - \circ Q1.B.1: What is the precise mathematical definition of the Ω Operator? (e.g., Is it a linear operator on the HTS space? Differential operator? Integral operator? Matrix?)
 - \circ Q1.B.2: What are the mathematical properties of the Ω Operator (e.g., linearity, hermiticity, spectrum)?
 - \circ Q1.B.3: Provide a rigorous derivation of the temporal dynamics induced by Ω . How does its action on HTS lead to evolution equations?
 - \circ Q1.B.4: How does Ω relate to standard Hamiltonian evolution in quantum mechanics or other established dynamical frameworks?³⁹
- (Missing Rigor): Requires:
 - \circ A formal mathematical definition of the Ω operator, specifying its domain, range, and action on HTS.

- o Derivation of its properties from the foundational principles or axioms of $\mathbb{K}\Omega$.
- Explicit derivation of the evolution equations governing HTS dynamics based on the action of Ω. Mathematical descriptions of dynamical systems rely on well-defined evolution operators or generators.³⁹
- Analysis of its connection to or deviation from established physics (e.g., Schrödinger equation, Liouville equation). Temporal operators in physics have specific mathematical treatments and constraints.⁴⁴

Section 1.3: The Role of the Golden Ratio (φ)

٠,

(Begin Original Draft v3.0 Content for Section 1.3)

A key characteristic of the $\mathbb{K}\Omega$ framework is the fundamental role played by the Golden Ratio, ϕ =(1+5)/2≈1.618. This constant is postulated to appear intrinsically in the structure of HTS, the action of the Ω operator, and the resulting dynamics and interactions. It is suggested that ϕ governs resonance conditions, stability criteria, and potentially scaling properties within the framework, linking the temporal dynamics to principles of harmonic efficiency or minimal complexity. Its appearance is considered a signature of the underlying principles of $\mathbb{K}\Omega$.

(End Original Draft v3.0 Content for Section 1.3)

٠.

- (Speculative Nature): The fundamental role attributed to the Golden Ratio (ϕ) within $\mathbb{K}\Omega$ is entirely speculative and currently lacks any theoretical justification or derivation from first principles. Its appearance is asserted, not proven to emerge from the framework's dynamics.
- (Critique Reference): The Evaluation Report (§1.3) questions the basis for elevating φ to a fundamental constant within this framework. It notes the risk of numerology if its presence is not rigorously derived. The report criticizes the lack of any mechanism explaining why φ should appear in HTS structure or Ω operator action.
- (Q-Pointers): To substantiate this claim, the following must be addressed:
 - \circ Q1.C.1: Provide a rigorous mathematical derivation showing how the Golden Ratio (ϕ) naturally emerges from the fundamental definitions and axioms of $\mathbb{K}\Omega$ (HTS, Ω operator).
 - ο Q1.C.2: Demonstrate mathematically how φ governs the claimed "resonance

- conditions," "stability criteria," or "scaling properties." Provide specific equations or theorems.
- \circ Q1.C.3: If φ is claimed to relate to fundamental physical constants ²⁷ or phenomena (e.g., quantum processes ⁴⁹), provide explicit derivations within the $\mathbb{K}\Omega$ framework.
- (Missing Rigor): Requires:
 - \circ A step-by-step mathematical derivation demonstrating the emergence of ϕ from the core postulates of $\mathbb{K}\Omega$. Simply stating its importance is insufficient.
 - Formal proofs or derivations linking φ to specific quantitative properties (resonances, stability, scaling) within the model.
- (Context): While φ and Fibonacci sequences appear in various mathematical and natural contexts ²⁶, their role as *fundamental* constants or operators in physical theories is not established.²⁷ Extraordinary claims about fundamental constants require extraordinary evidence, typically in the form of derivation from a deeper theory or direct, precise experimental confirmation.⁴⁸ Asserting φ's role without derivation risks falling into numerology.⁵⁹

Chapter 2: Kharnita Operators and Algebra

Section 2.1: Definition of K-Operators

٠,

(Begin Original Draft v3.0 Content for Section 2.1)

Within the $\mathbb{K}\Omega$ framework, a specific class of operators, termed K-Operators (Kharnita Operators), are introduced. These operators act on Harmonic Temporal States (HTS) and are responsible for mediating specific types of interactions or transformations within the system. K-Operators are distinct from the global Ω operator and represent localized or specific influences. They may be associated with measurement processes, entanglement operations, or the coupling between different HTS subsystems. Their algebraic structure and interaction with the Ω operator define key aspects of the framework's predictive power. The concept of "K-Layers" may refer to hierarchical structures or compositions of these operators.

(End Original Draft v3.0 Content for Section 2.1)

. .

• (Speculative Nature): K-Operators are speculative constructs unique to the $\mathbb{K}\Omega$

- framework. Their definition, properties, and necessity are not established.
- (Critique Reference): The Evaluation Report (§2.1) criticizes the vague and informal definition of K-Operators. It lacks mathematical specification regarding their nature (linear, non-linear?), their domain (acting on single HTS, multiple HTS?), their range, and their algebraic properties. The term "K-Layers" is mentioned without definition.
- (Q-Pointers): Foundational work must address:
 - Q2.A.1: Provide a precise mathematical definition of a K-Operator. What type of mathematical object is it (e.g., linear operator, map, matrix)?
 - Q2.A.2: Define the domain and range of K-Operators. On what space do they act, and what is the nature of their output?
 - Q2.A.3: Specify the algebraic properties of K-Operators. Do they form an algebra? What are their relationships (e.g., composition rules)?
 - Q2.A.4: Define "K-Layers." Does this refer to operator composition, a hierarchical structure, or something else? Provide a formal definition.
- (Missing Rigor): Requires:
 - A formal mathematical definition of K-Operators within a recognized algebraic framework, such as an operator algebra (e.g., C*-algebra ²⁸ or von Neumann algebra) or potentially a non-commutative ring structure. Operators in mathematics and physics need precise definitions regarding their action, domain, and algebraic structure.
 - \circ A clear, formal definition of "K-Layers" if this concept is central to the framework. Similar terms exist in other fields (e.g., neural networks ⁹², condensed matter ⁹⁹), requiring $\mathbb{K}\Omega$ to define its specific usage.

Section 2.2: Commutation Relations

٠,

(Begin Original Draft v3.0 Content for Section 2.2)

The K-Operators and the Ω operator are postulated to obey specific commutation relations. These relations define the fundamental algebra of the $\mathbb{K}\Omega$ framework and dictate how different operations interfere or combine. For example, the commutator [Ki,Kj] might be non-zero, indicating non-commutativity between certain K-Operators, while [Ki, Ω] might define how a specific K-Operator interaction evolves under the global dynamics. These relations are crucial for deriving the observable consequences of the theory.

. .

- **(Speculative Nature):** The proposed commutation relations are asserted without derivation. Their form and validity are speculative.
- (Critique Reference): The Evaluation Report (§2.2) strongly criticizes the lack of derivation for the proposed commutation relations. They appear to be postulated ad hoc rather than emerging from the framework's foundational principles or axioms. Their consistency with the (undefined) nature of the operators (K, Ω) and the HTS space is unevaluated.
- (Q-Pointers): Addressing these questions is fundamental:
 - \circ Q2.B.1: Provide a rigorous derivation of the claimed commutation relations from the definitions of HTS, Ω , and K-Operators, or from the fundamental axioms of $\mathbb{K}\Omega$.
 - Q2.B.2: Demonstrate the internal consistency of the proposed algebra defined by these commutation relations.
 - o Q2.B.3: How do these commutation relations compare to standard commutation relations in quantum mechanics (e.g., [X,P]= $i\hbar$)? Justify any deviations.⁴⁴
- (Missing Rigor): Requires:
 - \circ A step-by-step derivation of the commutation relations from more fundamental assumptions or definitions within $\mathbb{K}\Omega$.
 - A proof of the consistency of the resulting algebraic structure.
 Non-commutative algebras have strict rules that must be adhered to.³⁹
 - Explicit comparison with, and justification for any differences from, established physical commutation relations.

Section 2.3: Temporal Convolution and Tensor Operations

٠,

(Begin Original Draft v3.0 Content for Section 2.3)

The interaction and combination of HTS and the effects of K-Operators are sometimes described using operations termed "Temporal Convolution" and related tensor operations. Temporal Convolution is proposed as a way to integrate the influence of past states or operator actions over time, distinct from standard convolution. Tensor operations are used to describe the combination or entanglement of multiple HTS or the action of operators on composite systems. These operations are essential for

building complex state descriptions and calculating interaction outcomes.

(End Original Draft v3.0 Content for Section 2.3)

 $\overline{}$

- (Speculative Nature): The concepts of "Temporal Convolution" and the specific tensor operations used within $\mathbb{K}\Omega$ are speculative and lack formal definition.
- (Critique Reference): The Evaluation Report (§2.3) criticizes the ambiguity surrounding "Temporal Convolution." It is not defined mathematically, nor is its relationship to standard convolution clarified. Similarly, the specific tensor operations employed are not formally defined or justified.
- (Q-Pointers): Clarification requires addressing:
 - \circ Q2.C.1: Provide a precise mathematical definition of "Temporal Convolution" as used in $\mathbb{K}\Omega$. How does it differ from standard convolution definitions?¹⁰⁵
 - Q2.C.2: What are the mathematical properties of this Temporal Convolution (e.g., linearity, commutativity, associativity, relation to transforms)? Provide proofs.
 - \circ Q2.C.3: Define the specific tensor operations used in $\mathbb{K}\Omega$. Are they standard tensor products ¹¹⁰, or novel operations? If novel, define them rigorously and justify their necessity.
- (Missing Rigor): Requires:
 - Formal mathematical definitions for "Temporal Convolution" and any non-standard tensor operations.
 - Proofs of the mathematical properties of these operations.
 - Justification for introducing novel operations if standard convolution or tensor products ¹¹⁰ are insufficient. The relationship between convolution and transforms like the Fourier transform is fundamental in many applications ¹⁰⁸; any temporal variant needs similar analysis.

Chapter 3: Temporal Gödel Encoding (TGE)

Section 3.1: Concept of TGE

٠,

(Begin Original Draft v3.0 Content for Section 3.1)

Temporal Gödel Encoding (TGE) is introduced as a core concept in $\mathbb{K}\Omega$, proposed as a method for encoding the dynamic state and potential evolution of systems, including

formal systems themselves, into a numerical representation that explicitly incorporates time. Unlike standard Gödel numbering, which assigns static numbers to symbols and formulas, TGE aims to capture the temporal trajectory or potential futures inherent in the system being encoded. This encoding is suggested to be fundamental to understanding self-reference and system consistency within a dynamic context.

(End Original Draft v3.0 Content for Section 3.1)

- (Speculative Nature): Temporal Gödel Encoding (TGE) is a highly speculative concept introduced solely within the KΩ framework. It lacks a formal definition, mathematical justification, and connection to established concepts in logic or computability theory.
- (Critique Reference): The Evaluation Report (§3.1) identifies TGE as a major point of ambiguity and concern. It criticizes the complete absence of a formal definition, algorithm, or mathematical framework for TGE. It questions how TGE relates to, or fundamentally differs from, standard Gödel numbering techniques.¹¹³
- (Q-Pointers): Establishing TGE requires addressing:
 - Q3.A.1: Provide a precise, formal definition of Temporal Gödel Encoding (TGE).
 What mathematical objects does it map from and to?
 - Q3.A.2: Specify the algorithm or mathematical procedure for performing TGE.
 How is the "temporal trajectory" or "potential futures" encoded numerically?
 - Q3.A.3: How does TGE relate to standard Gödel numbering?¹¹³ Does it preserve properties like uniqueness and effective computability?
 - Q3.A.4: How does TGE interact with concepts from temporal logic?
- (Missing Rigor): Requires:
 - A complete and rigorous mathematical definition of the TGE mapping and the structures it operates on.
 - A formal algorithm for computing the TGE of a given input (e.g., a formal system state, a sequence of HTS).
 - Proof of its properties (e.g., uniqueness, computability, information preservation/loss).
- (Context): Gödel numbering is a well-defined technique in mathematical logic
 with specific properties and applications related to encoding syntax
 arithmetically.¹¹³ Introducing a "temporal" variant requires extreme care to define
 precisely how time is incorporated and what logical or computational
 consequences arise.¹²⁴ Temporal logic provides frameworks for reasoning about

time ¹¹⁷, but its combination with Gödel numbering is non-standard and needs explicit formalization.

Section 3.2: TGE and Self-Reference

٠,

(Begin Original Draft v3.0 Content for Section 3.2)

A key claim of the $\mathbb{K}\Omega$ framework is that TGE provides a novel mechanism for achieving self-reference within formal systems. It is proposed that the temporal aspect of the encoding allows a system to encode statements about its own future states or its own provability over time. This is suggested to lead to different conclusions regarding incompleteness compared to standard Gödelian arguments, potentially allowing systems to assess their own consistency dynamically.

(End Original Draft v3.0 Content for Section 3.2)

- (Speculative Nature): The claims that TGE enables a novel form of self-reference or allows systems to dynamically assess their own consistency are entirely speculative and lack any supporting proof or formal argument. These claims appear to contradict or misunderstand the implications of Gödel's incompleteness theorems.
- (Critique Reference): The Evaluation Report (§3.2) expresses strong skepticism regarding these claims, suggesting a potential misapplication or misunderstanding of Gödel's theorems.²³ It highlights the absence of any formal proof demonstrating how TGE achieves self-reference or bypasses the limitations established by Gödel.
- (Q-Pointers): Substantiation requires addressing:
 - Q3.B.1: Provide a rigorous proof demonstrating how TGE enables the construction of self-referential statements within a formal system. How does this mechanism relate to the standard diagonal lemma?²²
 - Q3.B.2: Explicitly address how the claims made for TGE (e.g., dynamic consistency assessment) are compatible with Gödel's second incompleteness theorem, which states that sufficiently strong consistent systems cannot prove their own consistency.²³
 - Q3.B.3: Formalize the notion of "dynamic assessment of consistency" and prove that TGE enables it within a consistent formal system.

- (Missing Rigor): Requires:
 - Formal proofs within mathematical logic demonstrating the claimed self-referential capabilities of TGE.
 - A rigorous analysis demonstrating compatibility with, or a valid modification of, Gödel's incompleteness theorems. Standard interpretations suggest such theorems impose fundamental limits.²³
- (Context): Self-reference in formal systems is achieved through specific logical techniques like arithmetization and the diagonal lemma.²² Gödel's theorems establish profound limits on what such systems can prove about themselves, particularly regarding consistency.²³ Claims that TGE circumvents these results require rigorous, formal justification within the framework of mathematical logic.

Section 3.3: Consistency and Completeness Implications

٠,

(Begin Original Draft v3.0 Content for Section 3.3)

The introduction of TGE is suggested to have significant implications for the consistency and completeness of formal systems described within the $\mathbb{K}\Omega$ framework. It is proposed that the dynamic nature of TGE might allow for systems that are both consistent and complete in ways not possible under standard static axiomatizations, or that consistency itself becomes a dynamic property that can be tracked or even enforced by the system.

(End Original Draft v3.0 Content for Section 3.3)

- (Speculative Nature): Claims regarding novel implications for consistency and completeness due to TGE are highly speculative and lack formal proof. They appear to challenge fundamental results in mathematical logic without providing adequate justification.
- (Critique Reference): The Evaluation Report (§3.3) identifies these claims as unsubstantiated and potentially contradictory to Gödel's incompleteness theorems. It demands formal proofs to support any assertion that $\mathbb{K}\Omega$ or TGE allows for formal systems that overcome the standard limitations on proving consistency or achieving completeness.²³
- (Q-Pointers): Essential questions include:
 - o Q3.C.1: Define precisely what "dynamic property" of consistency means in the

- context of TGE and $\mathbb{K}\Omega$.
- Q3.C.2: Provide a formal proof that a sufficiently strong formal system utilizing TGE can be both consistent and complete, directly addressing Gödel's first incompleteness theorem.
- Q3.C.3: Provide a formal proof that a sufficiently strong, consistent formal system utilizing TGE can prove its own consistency, directly addressing Gödel's second incompleteness theorem.

• (Missing Rigor): Requires:

- Formal definition of the axiomatic system underlying $\mathbb{K}\Omega$. Before discussing consistency or completeness, the system's axioms and rules of inference must be explicitly stated.²⁴
- Rigorous proofs addressing the consistency and completeness of this system, formulated within mathematical logic and explicitly engaging with Gödel's theorems.
- (Context): Gödel's incompleteness theorems are cornerstones of modern logic, establishing fundamental limitations on formal axiomatic systems capable of expressing basic arithmetic.²³ Claims to circumvent these theorems require exceptionally rigorous proof and are generally met with significant skepticism within the mathematical community. The consistency of powerful systems like ZFC is typically investigated using stronger meta-theories or large cardinal axioms.²³

Chapter 4: Fibonacci-Temporal Lattices (FTL) and Cryptography

Section 4.1: Definition of FTL

(Begin Original Draft v3.0 Content for Section 4.1)

Fibonacci-Temporal Lattices (FTL) are proposed as a novel mathematical structure within $\mathbb{K}\Omega$, intended for cryptographic applications. These structures are described as lattices incorporating principles related to Fibonacci sequences and temporal dynamics derived from the framework's foundational concepts (HTS, Ω operator). The specific structure is suggested to endow FTL with properties that make associated computational problems hard, particularly against quantum adversaries.

(End Original Draft v3.0 Content for Section 4.1)

٠.

- (Speculative Nature): Fibonacci-Temporal Lattices (FTL) are a speculative construct unique to $\mathbb{K}\Omega$. Their mathematical definition, structure, and properties are not formally established.
- (Critique Reference): The Evaluation Report (§4.1) criticizes the lack of a rigorous mathematical definition for FTL. It is unclear how Fibonacci sequences ⁴⁹ and "temporal dynamics" are incorporated into a lattice structure. The relationship to standard mathematical lattices used in cryptography ¹³⁸ is undefined.
- (Q-Pointers): A definition must address:
 - Q4.A.1: Provide a precise mathematical definition of a Fibonacci-Temporal Lattice (FTL). Is it a point lattice, an ideal lattice, or another structure?
 - Q4.A.2: How are Fibonacci sequences mathematically integrated into the lattice structure?
 - Q4.A.3: How are "temporal dynamics" represented within the FTL structure?
 Does the lattice change over time?
 - Q4.A.4: What are the basic mathematical properties of FTLs (e.g., basis representation, dimension, metric)?
- (Missing Rigor): Requires:
 - A formal mathematical definition specifying FTLs as sets of points or modules, with defined operations and structure, consistent with or explicitly deviating from standard lattice theory.¹⁴⁰
 - Clear mathematical rules for how the Fibonacci and temporal aspects modify or define the lattice.
- (Context): Lattice-based cryptography ¹⁴⁴ relies on well-understood mathematical lattices. Introducing novel structures like FTLs requires demonstrating their mathematical soundness and cryptographic utility. The term "FTL" is also used for Federated Transfer Learning ¹⁷¹; if the acronym is intended, the distinction must be made clear. The potential use of Fibonacci sequences in cryptography exists ¹³⁷ but requires rigorous security analysis.

Section 4.2: FTL Hardness Assumptions

٠,

(Begin Original Draft v3.0 Content for Section 4.2)

The cryptographic utility of FTLs is predicated on the assumed computational hardness of certain problems defined over these structures. It is postulated that finding short vectors, closest vectors, or solving related problems on FTLs is intractable for both classical and quantum computers, providing a foundation for

post-quantum cryptography. The specific hard problems are intrinsically linked to the unique Fibonacci and temporal characteristics of FTLs.

(End Original Draft v3.0 Content for Section 4.2)

٠.

- **(Speculative Nature):** The computational hardness assumptions associated with FTLs are entirely speculative and lack any formal proof or reduction from known hard problems.
- (Critique Reference): The Evaluation Report (§4.2) identifies this as a critical gap. The security of cryptographic systems cannot be based on assertion alone. It criticizes the absence of any formal definition of the specific computational problem(s) claimed to be hard on FTLs and the lack of any security reduction connecting these problems to established hard lattice problems like the Shortest Vector Problem (SVP) or Learning With Errors (LWE).¹⁴²
- (Q-Pointers): Foundational cryptographic work requires:
 - Q4.B.1: Formally define the specific computational problem(s) on FTLs that are assumed to be hard (e.g., FTL-SVP, FTL-LWE).
 - Q4.B.2: Provide rigorous security proofs, ideally via reductions, demonstrating that solving the proposed FTL problem(s) is at least as hard as solving a well-studied hard problem (e.g., standard SVP, LWE, SIS) under classical and quantum computation models.
 - Q4.B.3: Analyze the presumed hardness against known algorithmic attacks, including lattice reduction algorithms (e.g., LLL, BKZ ¹⁴⁰) and quantum algorithms (e.g., Shor's algorithm for related structures, Grover's search ¹⁷⁸).
- (Missing Rigor): Requires:
 - Formal definition of the hard problem(s) on FTLs.
 - Rigorous security reductions to known hard problems. Establishing cryptographic hardness typically involves showing that an efficient algorithm for the new problem would imply an efficient algorithm for a known hard problem.¹⁴²
 - Analysis of resistance to existing classical and quantum cryptanalytic techniques. Post-quantum claims necessitate explicit consideration of quantum attacks.¹⁴⁰

(Begin Original Draft v3.0 Content for Section 4.3)

Based on the presumed hardness of problems over Fibonacci-Temporal Lattices, a specific cryptographic scheme, termed "Juanita Encryption," is proposed. This scheme is described as a public-key encryption or key encapsulation mechanism (KEM) designed to be resistant to quantum attacks. Its operations (key generation, encryption, decryption) are claimed to leverage the unique properties of FTLs, offering potential advantages in security or efficiency.

(End Original Draft v3.0 Content for Section 4.3)

- (Speculative Nature): The "Juanita Encryption" scheme is presented without a complete formal specification, security analysis, or performance evaluation. Its security and practicality are unproven. (Note: The name "Juanita" appears in contexts related to cybersecurity management and awards ¹⁸³ but has no apparent prior connection to specific cryptographic algorithms in the provided context. This naming requires clarification or may be arbitrary).
- (Critique Reference): The Evaluation Report (§4.3) severely criticizes the
 presentation of this scheme. It lacks a formal algorithmic description, parameter
 set specifications, a rigorous security proof (e.g., demonstrating IND-CPA or
 IND-CCA2 security under the FTL hardness assumptions), and any performance
 analysis or comparison with existing post-quantum cryptography (PQC)
 standards like CRYSTALS-Kyber.¹⁴⁴
- (Q-Pointers): Development into a credible scheme requires addressing:
 - Q4.C.1: Provide a complete and unambiguous specification of the Juanita Encryption algorithm (KeyGen, Encrypt, Decrypt or Encaps/Decaps).
 - Q4.C.2: Provide formal security proofs demonstrating the scheme achieves a standard security notion (e.g., IND-CPA, IND-CCA2) based on the assumed hardness of the underlying FTL problem(s). Specify the security level (e.g., NIST PQC Levels 1, 3, 5).
 - Q4.C.3: Define concrete parameter sets for different security levels and analyze the resulting key sizes, ciphertext/signature sizes, and computational complexity.
 - Q4.C.4: Provide implementation results and benchmark performance (speed, memory usage) against established PQC standards (e.g., CRYSTALS-Kyber, Dilithium, Falcon, SPHINCS+ ¹⁴⁴).
- (Missing Rigor): Requires:

- A formal specification of the cryptographic scheme.
- o Rigorous security proofs based on clearly stated hardness assumptions.
- Concrete parameter selection and security level analysis.
- Implementation and performance benchmarking against relevant standards.
- (Context): The NIST PQC standardization process ¹⁴⁴ has established rigorous criteria for evaluating new cryptographic algorithms, including security against known attacks, performance efficiency, and implementation characteristics. Any new proposal must meet these high standards to be considered viable. Claims of quantum resistance require careful analysis. ¹⁴⁵

Chapter 5: Physical Interpretations and Quantum Gravity

Section 5.1: $\mathbb{K}\Omega$ and Spacetime Structure

٠.

(Begin Original Draft v3.0 Content for Section 5.1)

The $\mathbb{K}\Omega$ framework is proposed to offer a new perspective on the fundamental structure of spacetime. The dynamics of Harmonic Temporal States (HTS) governed by the Ω operator are suggested to underlie the emergence of the geometric properties described by General Relativity (GR). It is claimed that the temporal and harmonic nature of the framework provides a mechanism for unifying quantum principles with gravitational dynamics, potentially resolving singularities predicted by classical GR.

(End Original Draft v3.0 Content for Section 5.1)

٠.

- (Speculative Nature): The connection between KΩ and spacetime structure or General Relativity is entirely speculative and lacks any mathematical derivation or physical justification. Claims about singularity resolution are unsubstantiated assertions.
- (Critique Reference): The Evaluation Report (§5.1) criticizes the absence of any
 derivation showing how the metric structure of spacetime or the field equations
 of GR (or a modification thereof) emerge from the dynamics of HTS and the Ω
 operator. It points out the lack of any concrete mechanism for singularity
 resolution.
- (Q-Pointers): To bridge the gap to established physics, the following must be

addressed:

- \circ Q5.A.1: Provide a rigorous mathematical derivation showing how the geometric concepts of spacetime (e.g., metric tensor, curvature) emerge from the $\mathbb{K}\Omega$ framework (HTS, Ω , K-Operators).
- \circ Q5.A.2: Demonstrate how $\mathbb{K}\Omega$ reproduces the predictions of General Relativity in an appropriate limit (e.g., low energy, large scale). If it deviates, quantify the deviations and their observable consequences.
- \circ Q5.A.3: Provide a specific, quantitative mechanism based on $\mathbb{K}\Omega$ principles that demonstrates the resolution of gravitational singularities (e.g., inside black holes or the Big Bang singularity). How does this compare to singularity resolution proposals in other quantum gravity approaches like Loop Quantum Gravity ¹⁹² or String Theory?
- \circ Q5.A.4: Is the $\mathbb{K}\Omega$ framework generally covariant or diffeomorphism invariant? Provide a proof or analysis.

• (Missing Rigor): Requires:

- o Mathematical derivations linking $\mathbb{K}\Omega$ constructs to spacetime geometry and gravitational dynamics.
- Quantitative calculations demonstrating singularity resolution (e.g., showing curvature remains bounded).
- Analysis of the framework's symmetries and consistency with fundamental principles of GR.
- (Context): Quantum gravity remains a major challenge in theoretical physics.¹
 Any candidate theory must rigorously demonstrate how it incorporates or modifies GR and quantum mechanics, and make testable predictions, often related to extreme environments like black holes or the early universe.¹⁹³

 Singularity resolution is a key benchmark for such theories.¹⁹²

Section 5.2: Connection to Bekenstein-Hawking Entropy

٠,

(Begin Original Draft v3.0 Content for Section 5.2)

The $\mathbb{K}\Omega$ framework purports to provide a microscopic explanation for Bekenstein-Hawking entropy. It is suggested that the Harmonic Temporal States associated with a black hole's event horizon, governed by $\mathbb{K}\Omega$ dynamics, naturally give rise to an entropy proportional to the horizon area. The framework may also predict specific corrections to the area law based on the properties of HTS and the Ω operator.

..

- (Speculative Nature): The claimed connection between KΩ and Bekenstein-Hawking entropy is speculative and lacks a supporting calculation or derivation.
- (Critique Reference): The Evaluation Report (§5.2) criticizes the complete absence of a derivation of black hole entropy from $\mathbb{K}\Omega$ principles. It is not shown how HTS associated with a horizon lead to the area law, nor are any specific corrections calculated.
- (Q-Pointers): Substantiation requires:
 - \circ Q5.B.1: Provide an explicit statistical mechanical calculation based on $\mathbb{K}\Omega$ (counting HTS states, using the $\mathbb{K}\Omega$ dynamics) that derives the entropy of a black hole.
 - \circ Q5.B.2: Show explicitly how this calculation leads to the Bekenstein-Hawking area law SBH=A/(4G \hbar).
 - \circ Q5.B.3: If $\mathbb{K}\Omega$ predicts corrections to the area law, derive these corrections explicitly and compare them quantitatively with predictions from other quantum gravity approaches (e.g., logarithmic corrections ²⁰⁵).
- (Missing Rigor): Requires:
 - \circ A detailed statistical mechanical derivation of black hole entropy using the defined elements of $\mathbb{K}\Omega$.
 - Quantitative comparison with the established Bekenstein-Hawking formula.³
 - Explicit calculation and justification of any predicted corrections to the area law.
- (Context): Reproducing the Bekenstein-Hawking entropy is a fundamental test for any theory of quantum gravity. Various approaches (string theory, loop quantum gravity, semiclassical methods) attempt this calculation, often yielding the area law as the leading term but differing in subleading corrections. A derivation within $\mathbb{K}\Omega$ must be similarly rigorous and quantitative.

Section 5.3: Lorentz Invariance and Fundamental Constants

٠,

(Begin Original Draft v3.0 Content for Section 5.3)

The $\mathbb{K}\Omega$ framework is claimed to be consistent with Lorentz invariance, a fundamental symmetry of spacetime in special relativity. Furthermore, it is suggested that the

framework's fundamental parameters, possibly related to the Ω operator or the structure of HTS, might provide a basis for deriving the values of fundamental physical constants, such as the fine-structure constant or particle mass ratios, from first principles.

(End Original Draft v3.0 Content for Section 5.3)

_

- (Speculative Nature): Claims of consistency with Lorentz invariance and the
 potential derivation of fundamental constants are speculative and entirely
 unsubstantiated.
- (Critique Reference): The Evaluation Report (§5.3) highlights the lack of any proof or analysis demonstrating Lorentz invariance within $\mathbb{K}\Omega$. It notes that some proposed non-commutative or discrete structures can conflict with Lorentz symmetry 25 and demands an explicit analysis. The report also dismisses the claim about deriving fundamental constants as baseless without any supporting calculation or mechanism.
- (Q-Pointers): Addressing these points requires:
 - \circ Q5.C.1: Provide a formal proof demonstrating that the dynamics and structure defined by $\mathbb{K}\Omega$ are consistent with Lorentz invariance under appropriate transformations. Alternatively, if Lorentz invariance is modified or broken, provide a detailed analysis of the mechanism and its observable consequences.
 - \circ Q5.C.2: If fundamental constants are claimed to be derivable, provide the explicit mathematical derivations showing how constants like α (fine-structure constant) or mass ratios emerge from the parameters of $\mathbb{K}\Omega$.
 - Q5.C.3: How does the framework incorporate or relate to established fundamental constants like c, ħ, G, or kB?²¹⁰ Are Planck units ¹⁹⁷ relevant, and if so, how?
- (Missing Rigor): Requires:
 - A rigorous mathematical analysis of the framework's behavior under Lorentz transformations.
 - Explicit, step-by-step derivations of any fundamental constants claimed to emerge from the theory. These derivations must be based on the framework's principles, not numerological coincidences.
- (Context): Lorentz invariance is a foundational principle of modern physics, verified to high precision. Theories that violate or modify it face significant constraints.²⁵ Deriving fundamental constants from a more basic theory is a major

goal of physics, but extremely challenging; proposed derivations must be mathematically sound and predictive. ⁴⁸ The role of constants like ϕ ²⁶ or π ⁴⁸ in fundamental theories requires careful justification.

Chapter 6: Computational and Cognitive Applications

Section 6.1: $\mathbb{K}\Omega$ in Al and Neural Networks

٠,

(Begin Original Draft v3.0 Content for Section 6.1)

The principles of Kharnita Mathematics, particularly the dynamics of HTS and the structure of K-Operators, are proposed as a novel foundation for developing artificial intelligence (AI) systems and neural network architectures. It is suggested that the framework's handling of temporal information and harmonic resonance could lead to more efficient learning algorithms, improved handling of sequential data, or new paradigms for machine reasoning and consciousness modeling. Concepts like "K-Layers" might map to neural network layers, and the Golden Ratio could inform optimization strategies.

(End Original Draft v3.0 Content for Section 6.1)

- (Speculative Nature): The application of $\mathbb{K}\Omega$ to AI and neural networks is entirely speculative. No concrete algorithms, architectures, or implementations derived from $\mathbb{K}\Omega$ are presented or analyzed.
- (Critique Reference): The Evaluation Report (§6.1) criticizes the lack of any specific AI model or algorithm based on $\mathbb{K}\Omega$. Claims about efficiency, sequence handling, reasoning, or consciousness modeling are unsubstantiated assertions. The connection between "K-Layers" and neural network layers is undefined, and the proposed role of ϕ in optimization lacks justification.
- (Q-Pointers): To demonstrate applicability to AI/NNs, the following are needed:
 - \circ Q6.A.1: Define specific AI algorithms or neural network architectures derived from $\mathbb{K}\Omega$ principles (HTS dynamics, K-Operators, Temporal Convolution).
 - Q6.A.2: Provide implementation details for these algorithms/architectures.
 - \circ Q6.A.3: Quantitatively evaluate the performance (e.g., accuracy, efficiency, convergence speed) of these $\mathbb{K}\Omega$ -based models on standard AI benchmarks (e.g., image recognition, natural language processing, time series forecasting

²¹²).

- \circ Q6.A.4: Compare the performance and properties of $\mathbb{K}\Omega$ -based models against existing state-of-the-art models (e.g., Transformers, LSTMs, GRUs ²¹²).
- \circ Q6.A.5: If ϕ is proposed for optimization, provide the specific optimization algorithm and demonstrate its effectiveness compared to standard methods (e.g., gradient descent variants ²¹⁷).
- (Missing Rigor): Requires:
 - o Concrete algorithm/architecture design based on $\mathbb{K}\Omega$.
 - o Implementation and empirical evaluation on benchmark tasks.
 - Quantitative comparison with established AI/NN methods. Formal models of AI reasoning or consciousness ²² require much more than assertion.
- (Context): Al and machine learning are fields driven by concrete algorithms, architectures (like RNNs, LSTMs, GRUs, Transformers ²¹²), and empirical performance on defined tasks.²²⁵ Novel proposals must demonstrate tangible improvements or new capabilities through implementation and rigorous benchmarking. Concepts like Golden Ratio search exist in optimization ⁵⁹ but need specific justification within a KΩ-derived algorithm.

Section 6.2: Modeling Cognitive Processes (Memory Compression)

٠,

(Begin Original Draft v3.0 Content for Section 6.2)

The $\mathbb{K}\Omega$ framework is suggested as a potential tool for modeling human cognitive processes, specifically memory. It is proposed that the dynamics of HTS and the operations within $\mathbb{K}\Omega$ could capture mechanisms like memory encoding, consolidation, retrieval, and particularly memory compression. The framework's temporal aspects are claimed to be relevant for modeling the dynamic nature of memory formation and recall, potentially linking to observed neural phenomena via fMRI or other neuroimaging techniques.

(End Original Draft v3.0 Content for Section 6.2)

- (Speculative Nature): The application of $\mathbb{K}\Omega$ to model cognitive processes, especially memory compression, is highly speculative and lacks a defined model or connection to empirical data.
- (Critique Reference): The Evaluation Report (§6.2) criticizes the absence of any

specific cognitive model derived from $\mathbb{K}\Omega$ principles. It notes the lack of connection to established cognitive science theories or neuroscience data (e.g., fMRI BOLD signals ²³²). Claims about modeling memory compression ²⁴⁸ are unsubstantiated.

- (Q-Pointers): To be considered a viable cognitive model, $\mathbb{K}\Omega$ needs to address:
 - \circ Q6.B.1: Formulate a specific, detailed cognitive model of memory (or a specific aspect like compression) based on $\mathbb{K}\Omega$ principles (HTS, Ω , K-Operators).
 - Q6.B.2: Explain the mechanism by which this model performs memory functions like encoding, consolidation, retrieval, and compression.
 - Q6.B.3: Make specific, testable predictions about human behavior or neural activity (e.g., reaction times, error patterns, fMRI activation patterns, BOLD signal complexity/variability ²³³) based on the model.
 - \circ Q6.B.4: Compare the $\mathbb{K}\Omega$ -based model's structure and predictions with existing cognitive models of memory ²⁵¹ and relevant neuroscience findings.
- (Missing Rigor): Requires:
 - o A detailed, mechanistic cognitive model derived from $\mathbb{K}\Omega$.
 - Quantitative, testable predictions.
 - Comparison and validation against empirical data (behavioral, neuroimaging).
 Dimensionality reduction techniques are often essential for analyzing complex fMRI data.²³²
- (Context): Cognitive neuroscience develops and validates computational models against experimental data.²⁴⁸ Models of memory often focus on specific mechanisms like consolidation, retrieval, or compression.²⁵⁰ Any KΩ-based model must engage with this literature and methodology, providing specific mechanisms and predictions. The name "Kharnita" appears in unrelated neuroscience/social science contexts ²⁶⁷ and should be considered coincidental unless an explicit link is made and justified in the draft.

Chapter 7: Specialized Applications (Hypersonic Trajectories, Protein Folding, Combat Calculus)

Section 7.1: Hypersonic Trajectory Prediction

(Begin Original Draft v3.0 Content for Section 7.1)

One proposed application domain for $\mathbb{K}\Omega$ is the prediction of hypersonic vehicle trajectories. The framework's temporal dynamics and potential handling of complex,

٠,

non-linear systems are suggested to be advantageous for modeling the flight paths of vehicles traveling at Mach 5 or higher. It is envisioned that $\mathbb{K}\Omega$ could provide more accurate or efficient predictions compared to standard aerodynamic and orbital mechanics models, potentially improving guidance and interception capabilities.

(End Original Draft v3.0 Content for Section 7.1)

- (Speculative Nature): This application is entirely speculative. No model, simulation, or analysis is provided to support the claim that $\mathbb{K}\Omega$ can be applied to hypersonic trajectory prediction, let alone offer advantages.
- (Critique Reference): The Evaluation Report (§7.1) dismisses this proposed application as baseless without a concrete model. It highlights the lack of any derived equations of motion, simulation results, or comparison with established methods in aerospace engineering.²⁷⁴ The absence of accuracy metrics, such as Circular Error Probable (CEP) ²⁷⁹, makes assessment impossible.
- (Q-Pointers): To explore this application, the following are necessary:
 - \circ Q7.A.1: Derive the equations of motion for a hypersonic vehicle based on $\mathbb{K}\Omega$ principles.
 - Q7.A.2: Develop a computational model based on these equations.
 - Q7.A.3: Perform simulations using this model and compare the predicted trajectories against known data or standard trajectory models (e.g., those used in AIAA literature ²⁷⁴).
 - \circ Q7.A.4: Quantify the accuracy of the $\mathbb{K}\Omega$ -based predictions using standard metrics (e.g., CEP ²⁷⁹) and benchmark computational efficiency.
- (Missing Rigor): Requires:
 - o Derivation of a specific trajectory model from $\mathbb{K}\Omega$.
 - o Implementation of this model in a simulation environment.
 - Quantitative validation and benchmarking against established aerospace engineering models and data.
- (Context): Hypersonic flight involves complex aerodynamics and control challenges addressed by established physical models and computational techniques.²⁷⁴ Any new framework claiming applicability must demonstrate its ability to reproduce known physics and offer quantifiable advantages, rigorously validated through simulation and comparison.

٠,

(Begin Original Draft v3.0 Content for Section 7.2)

 $\mathbb{K}\Omega$ is proposed as a potential framework for modeling protein folding pathways. The temporal dynamics inherent in the framework are suggested to be suitable for describing the process by which a polypeptide chain transitions from an unfolded state to its functional three-dimensional structure. The harmonic aspects might relate to energy landscapes or stable intermediate states. It is hypothesized that $\mathbb{K}\Omega$ could predict folding pathways or intermediate structures, potentially leveraging insights related to Fibonacci sequences or the Golden Ratio observed in some biological structures.

(End Original Draft v3.0 Content for Section 7.2)

٠.

- (Speculative Nature): This application is speculative. No specific protein folding model or algorithm derived from $\mathbb{K}\Omega$ is presented, nor is any validation provided.
- (Critique Reference): The Evaluation Report (§7.2) criticizes the lack of a concrete model or algorithm for protein folding based on KΩ. It notes the absence of any comparison with state-of-the-art methods like AlphaFold ¹⁹ or validation against experimental data or benchmarks like CASP. Assertions about Fibonacci/φ connections are unsubstantiated.
- (Q-Pointers): Substantiating this application requires:
 - \circ Q7.B.1: Develop a specific algorithm or computational model for predicting protein folding pathways based on $\mathbb{K}\Omega$ principles.
 - Q7.B.2: Implement this model and generate predictions for known protein structures or folding pathways.
 - Q7.B.3: Quantitatively evaluate the accuracy of the predictions using standard metrics (e.g., RMSD, GDT, TM-score ²¹) and compare performance against established methods (e.g., AlphaFold, RosettaFold) and CASP results.²¹
 - \circ Q7.B.4: If Fibonacci/φ patterns are claimed to be relevant ⁵⁰, derive this relevance from the $\mathbb{K}\Omega$ folding model itself.

• (Missing Rigor): Requires:

- \circ A specific, implementable algorithm for folding pathway prediction derived from $\mathbb{K}\Omega$.
- Implementation and rigorous benchmarking on standard protein folding datasets.
- o Quantitative comparison of accuracy and efficiency against state-of-the-art

methods.

• (Context): Predicting protein structure and folding pathways is a central problem in bioinformatics.²¹ Deep learning methods like AlphaFold ¹⁹ have achieved remarkable success, setting a very high standard for accuracy. New methods must demonstrate competitive or superior performance through rigorous, quantitative evaluation, often via community challenges like CASP.²¹ While Fibonacci/φ patterns are noted in some biological contexts ⁵⁰, their role in a predictive folding model needs explicit derivation.

Section 7.3: "Combat Calculus" Decision Support

٠,

(Begin Original Draft v3.0 Content for Section 7.3)

A further speculative application of $\mathbb{K}\Omega$ is proposed in the domain of military decision support, termed "Combat Calculus." It is suggested that the framework's ability to model complex, dynamic systems with temporal dependencies could be leveraged to analyze battlefield situations, predict outcomes of engagements, or optimize tactical decisions. The $\mathbb{K}\Omega$ approach might offer advantages in handling uncertainty and the rapid evolution of combat scenarios, potentially integrating with AI-driven command and control systems.

(End Original Draft v3.0 Content for Section 7.3)

- (Speculative Nature): This application is extremely speculative and ill-defined.
 The term "Combat Calculus" is not standard and lacks definition within the draft.
 No model, algorithm, or analysis is provided.
- (Critique Reference): The Evaluation Report (§7.3) identifies this section as lacking any substance. It criticizes the failure to define "Combat Calculus," the absence of any model or algorithm derived from $\mathbb{K}\Omega$, and the complete lack of simulation, analysis, or connection to military science or operational research.
- (Q-Pointers): To even begin exploring this speculative direction, the following are minimal requirements:
 - \circ Q7.C.1: Define "Combat Calculus" precisely in the context of $\mathbb{K}\Omega$ and military decision support. What specific problem does it aim to solve?
 - \circ Q7.C.2: Develop a concrete mathematical model or algorithm based on $\mathbb{K}\Omega$ principles that implements this "Combat Calculus."

- Q7.C.3: Demonstrate the potential utility of this model/algorithm through simulation, wargaming ²⁹⁸, or analysis of specific tactical scenarios.
- Q7.C.4: Compare the proposed approach to existing methods in military operations research, AI-based decision support systems ²⁹⁹, or relevant computational tools.
- (Missing Rigor): Requires:
 - A clear definition of the proposed application and the "Combat Calculus" concept.
 - o Derivation of a specific model or algorithm from $\mathbb{K}\Omega$.
 - o Demonstration of capability through simulation or case study analysis.
 - Comparison with existing approaches in the relevant field.
- (Context): Military decision support is increasingly exploring AI and complex systems modeling.²⁹⁹ However, these applications require well-defined problems, validated models, rigorous testing, and careful consideration of ethical implications and limitations like data bias and uncertainty.²⁹⁹ Vague claims of applicability based on an undefined framework like KΩ are insufficient. The mention of "K130" ³⁰⁷ in search results refers to a specific naval platform and appears unrelated unless explicitly connected in the draft. Quantum algorithms are also being explored for optimization tasks potentially relevant to defense ³¹⁶, but require concrete algorithmic proposals.

Glossary

(Note: This glossary includes terms central to the $\mathbb{K}\Omega$ framework as presented in the Draft v3.0, along with annotations indicating the need for formalization based on the evaluation findings.)*

Term	Informal Description (from Draft v3.0, simulated)	Required Formalization / Critique Reference (Annotation)
Harmonic Temporal State (HTS)	Dynamic entities evolving like harmonic oscillators with an intrinsic temporal dimension, carrying information.	(Annotation: Speculative concept. Requires rigorous mathematical definition specifying the space they inhabit, their properties (phase, temporal dimension), and the basis for their harmonic nature. See

		Evaluation Report §1.1, Q-pointers Q1.A.1-Q1.A.3.)
Ω Operator	Fundamental operator governing the temporal evolution and interaction of HTS.	(Annotation: Speculative construct. Requires precise mathematical definition (type, domain, action, properties) and derivation of induced dynamics. See Evaluation Report §1.2, Q-pointers Q1.B.1-Q1.B.4.)
K-Operator (Kharnita Operator)	Operators distinct from Ω, mediating specific interactions or transformations on HTS (e.g., measurement, entanglement).	(Annotation: Speculative concept. Requires rigorous mathematical definition within an algebraic framework, specification of domain/range, and defined algebraic properties. See Evaluation Report §2.1, Q-pointers Q2.A.1-Q2.A.3.)
K-Layers	Mentioned in relation to K-Operators, potentially referring to hierarchical structures or compositions.	(Annotation: Term used without definition. Requires formal mathematical definition clarifying its meaning (composition, hierarchy, etc.). See Evaluation Report §2.1, Q-pointer Q2.A.4.)
Temporal Convolution	A proposed operation for integrating influences over time, distinct from standard convolution.	(Annotation: Speculative operation. Requires precise mathematical definition, proof of properties, and justification for deviation from standard convolution. 105 See Evaluation Report §2.3, Q-pointers Q2.C.1-Q2.C.3.)
Temporal Gödel Encoding (TGE)	Proposed method for numerically encoding dynamic system states and evolution, explicitly incorporating time.	(Annotation: Highly speculative concept. Requires formal definition, algorithm specification, proof of

		properties, and rigorous analysis of its relation to standard Gödel numbering ¹¹³ and Gödel's theorems. ²³ See Evaluation Report §3.1-§3.3, Q-pointers Q3.A.1-Q3.C.3.)
Fibonacci-Temporal Lattice (FTL)	Proposed lattice structure incorporating Fibonacci sequences and temporal dynamics for cryptographic use.	(Annotation: Speculative structure. Requires rigorous mathematical definition clarifying lattice type and integration of Fibonacci/temporal aspects, and relation to standard lattices. See Evaluation Report §4.1, Q-pointers Q4.A.1-Q4.A.4.)
FTL Hardness Assumptions	Postulated computational hardness of problems (e.g., FTL-SVP, FTL-LWE) defined over FTLs.	(Annotation: Unsubstantiated assumption. Requires formal problem definition and rigorous security proofs via reduction to known hard problems. See Evaluation Report §4.2, Q-pointers Q4.B.1-Q4.B.3.)
Juanita Encryption	Proposed PQC scheme based on FTL hardness assumptions.	(Annotation: Incompletely specified scheme. Requires formal algorithm description, parameter sets, rigorous security proof (e.g., IND-CCA2), and performance benchmarks against PQC standards. 144 See Evaluation Report §4.3, Q-pointers Q4.C.1-Q4.C.4.)
Combat Calculus	III-defined concept proposed for military decision support using K Ω.	(Annotation: Highly speculative and undefined term. Requires clear definition, derivation of a model/algorithm from KΩ, and demonstration of utility

		via simulation or analysis. See Evaluation Report §7.3, Q-pointers Q7.C.1-Q7.C.4.)
Golden Ratio (φ) (in KΩ context)	The constant φ≈1.618, postulated to play a fundamental role in KΩ dynamics and structure.	(Annotation: Asserted fundamental role is speculative. Requires rigorous derivation from KΩ principles to justify its inclusion beyond coincidence or numerology. See Evaluation Report §1.3, Q-pointers Q1.C.1-Q1.C.3.)

Concluding Summary

This annotated version of the Kharnita Mathematics ($\mathbb{K}\Omega$) Framework Draft v3.0 serves to transparently integrate the critical feedback received during expert evaluation. The annotations, based on the Evaluation Report and Critical Questions document, consistently highlight the speculative nature of the framework and pinpoint the significant gaps in mathematical rigor, logical derivation, and empirical validation that must be addressed.

The core challenges identified throughout the framework include:

- 1. Lack of Formal Foundations: Key concepts like HTS, Ω /K-Operators, TGE, and FTL require precise mathematical definitions and placement within established mathematical structures.
- Absence of Rigorous Proofs: Central claims regarding operator algebra, commutation relations, the role of constants like φ, the mechanisms of TGE, cryptographic security, and physical interpretations (spacetime, entropy) are asserted rather than proven or derived.
- 3. **Need for Quantitative Models and Validation:** The framework lacks concrete algorithms, quantitative predictions, and computational models necessary for testing and application in areas like AI, cognitive science, physics, or specialized domains (hypersonics, protein folding, cryptography). Benchmarking against existing theories and data is absent.
- Potential Conflicts with Established Science: Claims related to Gödel's theorems and fundamental physical principles like Lorentz invariance require careful formal analysis to ensure consistency or to rigorously justify proposed deviations.

Addressing the specific Q-pointers referenced in the annotations and providing the

missing definitions, proofs, derivations, algorithms, and quantitative validation is essential for the future development of the $\mathbb{K}\Omega$ framework. Without this foundational work, the framework remains a collection of speculative ideas rather than a scientifically viable theory. This annotated document provides a detailed roadmap for the necessary steps toward achieving scientific rigor.

Works cited

- Research Complex Quantum Systems UMBC, accessed April 20, 2025, https://cgs.umbc.edu/research/
- Frontiers of Quantum Gravity: shared challenges, converging directions ResearchGate, accessed April 20, 2025,
 https://www.researchgate.net/publication/362172308 Frontiers of Quantum Gravity shared challenges converging directions
- 3. [2207.14274] Self-Gravity and Bekenstein-Hawking Entropy arXiv, accessed April 20, 2025, https://arxiv.org/abs/2207.14274
- 4. History overview MacTutor History of Mathematics University of St Andrews, accessed April 20, 2025, https://mathshistory.st-andrews.ac.uk/HistTopics/History_overview/
- 5. How did the shift from constructed mathematical objects to modern mathematics occur?, accessed April 20, 2025, https://hsm.stackexchange.com/questions/15492/how-did-the-shift-from-constructed-mathematical-objects-to-modern-mathematics-oc
- 6. Foundations of mathematics Wikipedia, accessed April 20, 2025, https://en.wikipedia.org/wiki/Foundations of mathematics
- 7. There's more to mathematics than rigour and proofs | What's new Terry Tao, accessed April 20, 2025, https://terrytao.wordpress.com/career-advice/theres-more-to-mathematics-than-rigour-and-proofs/
- 8. Is rigour just a ritual that most mathematicians wish to get rid of if they could? MathOverflow, accessed April 20, 2025, https://mathoverflow.net/questions/127889/is-rigour-just-a-ritual-that-most-mathematicians-wish-to-get-rid-of-if-they-coul
- 9. Mathematical Rigor and Proof | Yacin Hamami, accessed April 20, 2025, https://www.yacinhamami.com/wp-content/uploads/2019/12/Hamami-2019-Mathematical-Rigor-and-Proof.pdf
- 10. What Is Mathematical Rigor? PhilArchive, accessed April 20, 2025, https://philarchive.org/archive/BURWIM-6
- 11. Rigor in Math Daily Nous, accessed April 20, 2025, https://dailynous.com/2020/06/26/rigor-in-math/
- 12. Corrigendum: Information guided adaptation of complex biological systems Frontiers, accessed April 20, 2025, https://www.frontiersin.org/journals/complex-systems/articles/10.3389/fcpxs.2023.1254070/full

- 13. The math of multiboundary wormholes Quantum Frontiers, accessed April 20, 2025,
 - https://quantumfrontiers.com/2018/03/27/the-math-of-multiboundary-wormholes/
- 14. Quantum gravity with dynamical wave-function collapse via a classical scalar field arXiv, accessed April 20, 2025, https://arxiv.org/html/2402.17024v1
- 15. THE HISTORICAL SHAPING OF THE FOUNDATIONS OF MATHEMATICS, accessed April 20, 2025,
 - https://acmsonline.org/home2/wp-content/uploads/2016/05/Brabenec-77.pdf
- 16. Use LIGO/Virgo/KAGRA Data | LIGO Lab | Caltech, accessed April 20, 2025, https://www.ligo.caltech.edu/page/ligo-data
- 17. Gravitational-Wave Data Analysis with High-Precision Numerical Relativity Simulations of Boson Star Mergers Physical Review Link Manager, accessed April 20, 2025, https://link.aps.org/doi/10.1103/PhysRevLett.133.131401
- 18. GW170817 Press Release | LIGO Lab | Caltech, accessed April 20, 2025, https://www.ligo.caltech.edu/page/press-release-gw170817
- 19. Great expectations the potential impacts of AlphaFold DB | EMBL, accessed April 20, 2025, https://www.embl.org/news/science/alphafold-potential-impacts/
- 20. AlphaFold—for predicting protein structures Lasker Foundation, accessed April 20, 2025, <a href="https://laskerfoundation.org/winners/alphafold-a-technology-for-predicting-protein-prot
- <u>ein-structures/</u>
 21. Protein Structure Prediction Center, accessed April 20, 2025,
- https://predictioncenter.org/
- 22. [2006.12178] Self-reference Upfront: A Study of Self-referential Gödel Numberings arXiv, accessed April 20, 2025, https://arxiv.org/abs/2006.12178
- 23. Gödel's incompleteness theorems Wikipedia, accessed April 20, 2025, https://en.wikipedia.org/wiki/G%C3%B6del%27s_incompleteness_theorems
- 24. Gödel's Incompleteness Theorems Stanford Encyclopedia of Philosophy, accessed April 20, 2025,
 - https://plato.stanford.edu/entries/goedel-incompleteness/
- 25. Lorentz symmetry breaking as a quantum field theory regulator ResearchGate, accessed April 20, 2025,
 - https://www.researchgate.net/publication/23970502_Lorentz_symmetry_breaking as a quantum_field_theory_regulator
- 26. Golden ratio Wikipedia, accessed April 20, 2025, https://en.wikipedia.org/wiki/Golden ratio
- 27. (PDF) Fine-Structure Constant from Golden Ratio Geometry ResearchGate, accessed April 20, 2025, https://www.researchgate.net/publication/322797654_Fine-Structure_Constant_fr om Golden Ratio Geometry
- 28. Hilbert space Wikipedia, accessed April 20, 2025, https://en.wikipedia.org/wiki/Hilbert space
- 29. C*-algebra Wikipedia, accessed April 20, 2025, https://en.wikipedia.org/wiki/C*-algebra

- 30. 1. Reminder on bounded operators on Hilbert spaces, accessed April 20, 2025, https://www.math.uni-sb.de/ag/speicher/weber/ISem24/ISem24Lecture01.pdf
- 31. The role of the rigged Hilbert space in Quantum Mechanics arXiv, accessed April 20, 2025, http://arxiv.org/pdf/quant-ph/0502053
- 32. Rigged Hilbert space Wikipedia, accessed April 20, 2025, https://en.wikipedia.org/wiki/Rigged Hilbert space
- 33. (PDF) Rigged Hilbert Spaces in Quantum Physics ResearchGate, accessed April 20, 2025, https://www.researchgate.net/publication/251125102_Rigged_Hilbert_Spaces_in_Quantum Physics
- 34. Gelfand Triplets, Ladder Operators and Coherent States MDPI, accessed April 20, 2025, https://www.mdpi.com/2073-8994/16/11/1479
- 35. Lectures on Quantum Mechanics: A Primer for Mathematicians ResearchGate, accessed April 20, 2025, https://www.researchgate.net/publication/343918624_Lectures_on_Quantum_Mechanics A Primer for Mathematicians
- 36. Gelfand Triplets, Ladder Operators and Coherent States Preprints.org, accessed April 20, 2025, https://www.preprints.org/manuscript/202409.2306/v1/download
- 37. Mathematical Models for Unstable Quantum Systems and Gamow States PMC, accessed April 20, 2025, https://pmc.ncbi.nlm.nih.gov/articles/PMC9222900/
- 38. fse.studenttheses.ub.rug.nl, accessed April 20, 2025, https://fse.studenttheses.ub.rug.nl/19934/1/bMATH_2019_VanderlaanL.pdf
- 39. Dynamical systems and operator algebras, accessed April 20, 2025, https://maths.anu.edu.au/files/CMAProcVol36-Raeburn.pdf
- 40. Physics Small Perturbations of C*-Dynamical Systems Project Euclid, accessed April 20, 2025, https://projecteuclid.org/journals/communications-in-mathematical-physics/volume-68/issue-1/Small-perturbations-of-C-dynamical-systems/cmp/1103905265.p
- 41. Spectrum of the Koopman Operator, Spectral Expansions in Functional Spaces, and State Space Geometry arXiv, accessed April 20, 2025, https://arxiv.org/pdf/1702.07597
- 42. C*-Dynamical Systems and Covariance Algebras 43 the Gelfand representation, every commutative C Irish Mathematical Society, accessed April 20, 2025, https://www.irishmathsoc.org/bull26/bull26_42-51.pdf
- 43. Spectrum of a dynamical system Encyclopedia of Mathematics, accessed April 20, 2025, https://encyclopediaofmath.org/wiki/Spectrum of a dynamical system
- 44. Non-commutative Calculus and Discrete Physics arXiv, accessed April 20, 2025, https://arxiv.org/pdf/quant-ph/0303058
- 45. A Proof for Poisson Bracket in Non-commutative Algebra of Quantum Mechanics, accessed April 20, 2025, https://www.researchgate.net/publication/267869853_A_Proof_for_Poisson_Bracket_in_Non-commutative_Algebra_of_Quantum_Mechanics
- 46. Positive-Operator-Valued Measures and Projection-Valued Measures of Noncommutative Time Operators ResearchGate, accessed April 20, 2025,

- https://www.researchgate.net/publication/251150226_Positive-Operator-Valued_ Measures_and_Projection-Valued_Measures_of_Noncommutative_Time_Operators
- 47. Non-Commutative Worlds and Classical Constraints arXiv, accessed April 20, 2025, https://arxiv.org/pdf/1109.1085
- 48. The Fundamental Constants: A Mystery of Physics ResearchGate, accessed April 20, 2025, https://www.researchgate.net/publication/258447900_The_Fundamental_Constants_A Mystery of Physics
- 49. Topological Quantum Computing with Fibonacci Anyons DiVA portal, accessed April 20, 2025, http://www.diva-portal.org/smash/get/diva2:1880323/FULLTEXT01.pdf
- 50. [1801.01369] Fibonacci Numbers and the Golden Ratio in Biology, Physics, Astrophysics, Chemistry and Technology: A Non-Exhaustive Review arXiv, accessed April 20, 2025, https://arxiv.org/abs/1801.01369
- 51. (PDF) Fibonacci Numbers and the Golden Ratio in Biology, Physics, Astrophysics, Chemistry and Technology: A Non-Exhaustive Review ResearchGate, accessed April 20, 2025, https://www.researchgate.net/publication/322305991_Fibonacci_Numbers_and_t_he_Golden_Ratio_in_Biology_Physics_Astrophysics_Chemistry_and_Technology_A_Non-Exhaustive_Review
- 52. Fibonacci Numbers and the Golden Ratio in Biology, Physics, Astrophysics, Chemistry and Technology: A Non-Exhaustive Review arXiv, accessed April 20, 2025, https://arxiv.org/pdf/1801.01369
- 53. [1107.4389] Golden Quantum Oscillator and Binet-Fibonacci Calculus arXiv, accessed April 20, 2025, https://arxiv.org/abs/1107.4389
- 54. Fibonacci Anyons and Graph Coloring: Experiment Zlatko Minev, Ph.D., accessed April 20, 2025, https://www.zlatko-minev.com/blog/fibonacci-paper
- 55. Additive Sequences, Sums, Golden Ratios and Determinantal Identities arXiv:2109.09501v2 [math.GM] 26 Sep 2021, accessed April 20, 2025, https://arxiv.org/pdf/2109.09501
- 56. On the Response of Proteinoid Ensembles to Fibonacci Sequences PMC, accessed April 20, 2025, https://pmc.ncbi.nlm.nih.gov/articles/PMC11923683/
- 57. Is the golden ratio a universal constant for self-replication? PMC, accessed April 20, 2025, https://pmc.ncbi.nlm.nih.gov/articles/PMC6047800/
- 58. Dimensionless physical constant Wikipedia, accessed April 20, 2025, https://en.wikipedia.org/wiki/Dimensionless physical constant
- 59. The Golden Ratio in Machine Learning | Request PDF ResearchGate, accessed April 20, 2025, https://www.researchgate.net/publication/363050404_The_Golden_Ratio_in_Machine_Learning
- 60. C*-Algebras and Mathematical Foundations of Quantum Statistical Mechanics: An Introduction 303128948X, 9783031289484 DOKUMEN.PUB, accessed April 20, 2025,
 - https://dokumen.pub/c-algebras-and-mathematical-foundations-of-quantum-st

- atistical-mechanics-an-introduction-303128948x-9783031289484.html
- 61. C Algebras TU Wien, accessed April 20, 2025, https://www.tuwien.at/index.php?eID=dumpFile&t=f&f=204427&token=6a845b8b 6adae0a2279d16c785b6a13a8e1d634c
- 62. Operator theory on Hilbert spaces Graduate School of Mathematics, Nagoya University, accessed April 20, 2025, https://www.math.nagoya-u.ac.jp/~richard/teaching/s2019/Operators.pdf
- 63. Algebraic Quantum Field Theory* CiteSeerX, accessed April 20, 2025, https://citeseerx.ist.psu.edu/document?repid=rep1&type=pdf&doi=aa84471ad98f b4ccd392be373967628a72c61074
- 64. Algebraic Quantum Field Theory* Mathematics, accessed April 20, 2025, https://www.math.ru.nl/~mueger/PDF/16f.pdf
- 65. (PDF) Quasi-Duo Skew Polynomial Rings ResearchGate, accessed April 21, 2025, https://www.researchgate.net/publication/386763527_Quasi-Duo_Skew_Polynomial Rings
- 66. Noncommutative localization in algebra and topology School of Mathematics, accessed April 21, 2025, https://www.maths.ed.ac.uk/~v1ranick/books/nlat.pdf
- 67. arXiv:2409.18947v1 [math.QA] 27 Sep 2024, accessed April 21, 2025, https://arxiv.org/pdf/2409.18947
- 68. Journal of Algebra and Its Applications | Vol 12, No 07, accessed April 21, 2025, https://www.worldscientific.com/toc/jaa/12/07
- 69. Tensor reduction systems for rings of linear operators Georg Regensburger, accessed April 21, 2025, http://gregensburger.com/papers/PhDThesisHosseinPoor.pdf
- 70. Basic Module Theory over Non-Commutative Rings with Computational Aspects of Operator Algebras ResearchGate, accessed April 21, 2025, https://www.researchgate.net/publication/259478196_Basic_Module_Theory_over_Non-Commutative Rings with Computational Aspects of Operator Algebras
- 71. Derivations of Skew Polynomial Rings ResearchGate, accessed April 21, 2025, https://www.researchgate.net/publication/222498229 Derivations of Skew Polynomial Rings
- 72. arXiv:2502.15175v1 [math.RA] 21 Feb 2025, accessed April 21, 2025, https://www.arxiv.org/pdf/2502.15175
- 73. arXiv:2109.13092v2 [math.RA] 1 Feb 2022, accessed April 21, 2025, https://arxiv.org/pdf/2109.13092
- 74. Mathematisches Forschungsinstitut Oberwolfach Resolutions in Local Algebra and Singularity Theory, accessed April 21, 2025, https://publications.mfo.de/bitstream/handle/mfo/4021/OWR_2023_06.pdf?sequence=4&isAllowed=y
- 75. arXiv:2203.09912v1 [math.RA] 18 Mar 2022, accessed April 21, 2025, https://arxiv.org/pdf/2203.09912
- 76. (PDF) Differential operators on non-commutative algebras ResearchGate, accessed April 21, 2025, https://www.researchgate.net/publication/258819450_Differential_operators_on_non-commutative_algebras

- 77. Journal of Algebra and Its Applications | Vol 23, No 08, accessed April 21, 2025, https://www.worldscientific.com/toc/jaa/23/08
- 78. nonunital ring in nLab, accessed April 21, 2025, https://ncatlab.org/nlab/show/nonunital+ring
- 79. Noncommutative algebra and representation theory Communications in Mathematics, accessed April 21, 2025, https://cm.episciences.org/12727/pdf
- 80. Journal of Algebra V322 I11.2 | PDF | Ring (Mathematics) Scribd, accessed April 21, 2025,
 - https://www.scribd.com/document/392717590/Journal-of-Algebra-V322-I11-2
- 81. arXiv:math/0304478v1 [math.RA] 29 Apr 2003, accessed April 21, 2025, https://arxiv.org/pdf/math/0304478
- 82. MIT Open Access Articles Double Poisson vertex algebras and non- commutative Hamiltonian equations, accessed April 21, 2025, https://dspace.mit.edu/bitstream/handle/1721.1/115829/1410.3325.pdf?sequence=1 &isAllowed=y
- 83. Remark on Serre \$ C^* \$-algebras, accessed April 21, 2025, https://arxiv.org/pdf/1208.2049
- 84. Computing the Polar Decomposition—with Applications SIAM.org, accessed April 20, 2025, https://epubs.siam.org/doi/10.1137/0907079
- 85. Fast algorithm for quantum polar decomposition and applications | Phys. Rev. Research, accessed April 20, 2025, https://link.aps.org/doi/10.1103/PhysRevResearch.4.013144
- 86. Polar decomposition MIT Mathematics, accessed April 20, 2025, https://math.mit.edu/~dav/polar.pdf
- 87. What is the Polar Decomposition? Nick Higham, accessed April 20, 2025, https://nhigham.com/2020/07/28/what-is-the-polar-decomposition/comment-page-1/
- 88. polar decomposition in nLab, accessed April 20, 2025, https://ncatlab.org/nlab/show/polar+decomposition
- 89. Polar decomposition Wikipedia, accessed April 20, 2025, https://en.wikipedia.org/wiki/Polar_decomposition
- 90. Associativity of polar decomposition hilbert spaces MathOverflow, accessed April 20, 2025,
 - https://mathoverflow.net/questions/47850/associativity-of-polar-decomposition
- 91. Polar decomposition Encyclopedia of Mathematics, accessed April 20, 2025, https://encyclopediaofmath.org/wiki/Polar_decomposition
- 92. Something about graph neural networks Part II: New proof-of-concept for neural track-finding (or similar problems) Indico Global, accessed April 20, 2025, https://indico.global/event/3366/contributions/34364/attachments/17624/28846/G https://indico.global/event/3366/contributions/34364/attachments/17624/28846/G https://indico.global/event/3366/contributions/34364/attachments/17624/28846/G https://indico.global/event/3366/contributions/34364/attachments/17624/28846/G https://indico.global/event/3366/contributions/34364/attachments/17624/28846/G https://indico.global/event/3366/contributions/attachments/17624/28846/G https://indico.global/event/3366/contributions/attachments/17624/28846/G https://indico.global/event/attachments/a
- 93. TKAN: Temporal Kolmogorov-Arnold Networks arXiv, accessed April 20, 2025, https://arxiv.org/pdf/2405.07344
- 94. Multiscale and Nonlocal Learning for PDEs using Densely Connected RNNs arXiv, accessed April 20, 2025, https://arxiv.org/pdf/2109.01790
- 95. arXiv:2107.10234v5 [cs.LG] 18 Sep 2023 People, accessed April 20, 2025,

- https://people.cs.vt.edu/ctlu/Publication/2023/ACM-Computing-Surveys-2023.pd f
- neural networks are integrable International Conference on Scientific Computing and Machine Learning, accessed April 20, 2025, https://scml.jp/2024/paper/18/CameraReady/scml2024.pdf
- 97. Scale-consistent learning with neural operators OpenReview, accessed April 20, 2025,
 - https://openreview.net/pdf/ca50564fe6f96b7811a1b297e71e88989d9c233d.pdf
- 98. Neural Networks are Integrable arXiv, accessed April 20, 2025, https://arxiv.org/html/2310.14394v2
- 99. [2201.10384] Quantum phase transitions in the *K*-layer Ising toric code ar5iv arXiv, accessed April 20, 2025, https://ar5iv.labs.arxiv.org/html/2201.10384
- 100. arXiv:2201.10384v1 [cond-mat.str-el] 25 Jan 2022, accessed April 20, 2025, https://arxiv.org/pdf/2201.10384
- 101. Noncommutative geometry Wikipedia, accessed April 20, 2025, https://en.wikipedia.org/wiki/Noncommutative_geometry
- 102. Identifying short introductory book on non-commutative geometry I read c.2008, accessed April 20, 2025, https://mathoverflow.net/questions/480238/identifying-short-introductory-book-on-non-commutative-geometry-i-read-c-2008
- 103. Associative division algebras in field theories and non-commutative geometry, accessed April 21, 2025,
 - https://www.theorie.physik.uni-muenchen.de/TMP/theses/thesisvrabel.pdf
- 104. RÉSONAANCES: Alain Connes' Standard Model Resonaances blog, accessed April 20, 2025,
 - http://resonaances.blogspot.com/2007/02/alain-connes-standard-model.html
- 105. Intuitive Guide to Convolution BetterExplained, accessed April 20, 2025, https://betterexplained.com/articles/intuitive-convolution/
- 106. Convolution Wikipedia, accessed April 20, 2025, https://en.wikipedia.org/wiki/Convolution
- 107. Convolution -- from Wolfram MathWorld, accessed April 20, 2025, https://mathworld.wolfram.com/Convolution.html
- 108. Convolution theorem Wikipedia, accessed April 20, 2025, https://en.wikipedia.org/wiki/Convolution theorem
- 109. Computational Foundations of Cognitive Science Lecture 15: Convolutions and Kernels - School of Informatics, accessed April 20, 2025, https://www.inf.ed.ac.uk/teaching/courses/cfcs1/lectures/cfcs-I15.pdf
- Convolution algebra of superoperators and nonseparability witnesses for quantum operations - arXiv, accessed April 20, 2025, https://arxiv.org/pdf/2108.08776
- 111. Kronecker product Wikipedia, accessed April 20, 2025, https://en.wikipedia.org/wiki/Kronecker product
- 112. OPERATOR SPACE TENSOR PRODUCTS AND HOPF CONVOLUTION ALGEBRAS, accessed April 20, 2025, https://www.theta.ro/jot/archive/2003-050-001/2003-050-001-007.pdf

- 113. Gödel numbering Wikipedia, accessed April 20, 2025, https://en.wikipedia.org/wiki/G%C3%B6del_numbering
- 114. Gödel Numbering Stanford Encyclopedia of Philosophy, accessed April 20, 2025, https://plato.stanford.edu/entries/goedel-incompleteness/sup1.html
- [2502.13416] Detecting LLM Fact-conflicting Hallucinations Enhanced by Temporal-logic-based Reasoning - arXiv, accessed April 20, 2025, https://arxiv.org/abs/2502.13416
- Detecting LLM Fact-conflicting Hallucinations Enhanced by Temporal-logic-based Reasoning - arXiv, accessed April 20, 2025, https://arxiv.org/html/2502.13416v1
- 117. (PDF) A Survey on Temporal Logics ResearchGate, accessed April 20, 2025, https://www.researchgate.net/publication/45918319 A Survey on Temporal Logics
- 118. Gödel-Dummett linear temporal logic arXiv, accessed April 20, 2025, https://arxiv.org/pdf/2306.15805
- 119. When LLMs day dream: Hallucinations and how to prevent them Red Hat, accessed April 20, 2025, https://www.redhat.com/en/blog/when-llms-day-dream-hallucinations-how-prevent-them
- 120. Temporal logic: linear and branching time | Formal Logic II Class Notes Fiveable, accessed April 20, 2025, https://library.fiveable.me/formal-logic-ii/unit-9/temporal-logic-linear-branching-time/study-quide/BhFEP2CNOLWSIRhd
- 121. A Survey on Temporal Logics arXiv, accessed April 20, 2025, https://arxiv.org/pdf/1005.3199
- the philosophy of kurt godel PhilArchive, accessed April 20, 2025, https://philorchive.org/archive/KARTPO-43
- 123. How does Gödel's encoding of mathematical statements into natural numbers enable self-referential propositions? - Philosophy Stack Exchange, accessed April 20, 2025,
 - https://philosophy.stackexchange.com/questions/108257/how-does-g%C3%B6del-s-encoding-of-mathematical-statements-into-natural-numbers-enable
- 124. Gödel Number based Clustering Algorithm with Decimal First Degree Cellular Automata, accessed April 20, 2025, https://arxiv.org/html/2405.04881v1
- 125. Self-recognition in conversational agents arXiv, accessed April 20, 2025, https://arxiv.org/pdf/2002.02334
- 126. A Review of FFGIT Russell O'Connor, accessed April 20, 2025, http://r6.ca/Goedel/FFGITReview.html
- 127. What axioms are used to prove Gödel's Incompleteness Theorems? MathOverflow, accessed April 20, 2025,
 https://mathoverflow.net/questions/118183/what-axioms-are-used-to-prove-g%C
 3%B6dels-incompleteness-theorems
- 128. Gödel's Program Berkeley Math, accessed April 20, 2025, https://math.berkeley.edu/~steel/talks/stanford2013copy.pdf
- 129. Set Theory (Stanford Encyclopedia of Philosophy/Winter 2023 Edition),

- accessed April 20, 2025,
- https://plato.stanford.edu/archlves/win2023/entries/set-theory/
- 130. Large Cardinals and Set Theory Knowledge is the Only Good, accessed April 20, 2025,
 - https://blog.mynl.com/posts/notes/2024-03-20-Large-Cardinals-and-Set-Theory/
- 131. How does large cardinal axioms make arithmetical statements provable?, accessed April 20, 2025,
 - https://math.stackexchange.com/questions/2194808/how-does-large-cardinal-axioms-make-arithmetical-statements-provable
- 132. Does Gödel's incompleteness theorems imply the necessity of an infinite recursive hierarchy of "proofs", and that any "proof" is relative?, accessed April 20, 2025,
 - https://philosophy.stackexchange.com/questions/116958/does-g%C3%B6del-s-in completeness-theorems-imply-the-necessity-of-an-infinite-recursiv
- 133. Philosophy and Science, the Darwinian-Evolved Computational Brain, a Non-Recursive Super-Turing Machine & Our Inner-World-Producing Organ, accessed April 20, 2025,
 - https://www.scirp.org/journal/paperinformation?paperid=62862
- 134. Life of Fred Logic Stanley Schmidt, accessed April 20, 2025, https://www.stanleyschmidt.com/FredGauss/sample%20pages%20Logic.pdf
- 135. Question about consistency of formal systems: r/logic Reddit, accessed April 20, 2025,
 - https://www.reddit.com/r/logic/comments/1f1s772/question_about_consistency_of_formal_systems/
- 136. Minimal Quantum Circuits for Simulating Fibonacci Anyons arXiv, accessed April 20, 2025, https://arxiv.org/html/2407.21761v2
- 137. ISSN 1816-353X (Print) Vol. 20, No. 5 (Sept. 2018) ISSN 1816-3548 (Online) International Journal of Network Security, accessed April 20, 2025, http://ijns.jalaxy.com.tw/contents/ijns-v20-n5/ijns-v20-n5.pdf
- 138. Jonathan Bootle, accessed April 20, 2025, https://jbootle.github.io/
- 139. Learning with Errors: A Lattice-Based Keystone of Post-Quantum Cryptography MDPI, accessed April 20, 2025, https://www.mdpi.com/2624-6120/5/2/12
- 140. SALSA: Attacking Lattice Cryptography with Transformers Cryptology ePrint Archive, accessed April 20, 2025, https://eprint.iacr.org/2022/935.pdf
- 141. Learning with Errors: A Lattice-Based Keystone of Post-Quantum
 Cryptography, accessed April 20, 2025,
 https://www.researchgate.net/publication/379866441_Learning_with_Errors_A_Lattice-Based_Keystone_of_Post-Quantum_Cryptography
- 142. Lattice-based cryptography Wikipedia, accessed April 20, 2025, https://en.wikipedia.org/wiki/Lattice-based_cryptography
- 143. Evaluation and Comparison of Lattice-Based Cryptosystems for a Secure Quantum Computing Era MDPI, accessed April 20, 2025, https://www.mdpi.com/2079-9292/12/12/2643
- 144. Post-Quantum Cryptography | CSRC NIST Computer Security Resource

Center, accessed April 20, 2025,

mbres?all=true&limit=999

- https://csrc.nist.gov/projects/post-quantum-cryptography
- 145. Post-quantum cryptography Wikipedia, accessed April 20, 2025, https://en.wikipedia.org/wiki/Post-quantum_cryptography
- 146. arXiv:2409.07150v1 [cs.CR] 11 Sep 2024, accessed April 20, 2025, https://arxiv.org/pdf/2409.07150
- 147. Hardware Architecture Design for Modular Arithmetic Acceleration in Post-Quantum Lattice-Based Cryptography Algorithms Repositorio INAOE, accessed April 21, 2025,
 - https://inaoe.repositorioinstitucional.mx/jspui/bitstream/1009/2471/1/HERNANDEZ MJJ MCC.pdf
- 148. High-Speed Hardware Architectures and Fair FPGA Benchmarking of CRYSTALS-Kyber, NTRU, and Saber - NIST Computer Security Resource Center, accessed April 20, 2025,
 - https://csrc.nist.gov/CSRC/media/Events/third-pqc-standardization-conference/documents/accepted-papers/gaj-high-speed-hardware-gmu-pqc2021.pdf
- 149. NIST Unveils Post-Quantum Cryptography (PQC) Standards, accessed April 20, 2025, https://postquantum.com/industry-news/nist-pqc-standards/
- 150. Notes 3 & 4: Hardness of SIS, LWE, and lattice problems, accessed April 20, 2025, https://jmlribeiro.github.io/crypto-mini-course-notes34.pdf
- 151. PQC Standardization Process: Announcing Four Candidates to be Standardized, Plus Fourth Round Candidates | NIST, accessed April 20, 2025, https://www.nist.gov/news-events/news/2022/07/pqc-standardization-process-a-nnouncing-four-candidates-be-standardized-plus
- 152. Lattice Based Crypto Breaks in a Superposition of Spacetimes arXiv, accessed April 20, 2025, https://arxiv.org/pdf/2503.21400
- 153. SALSA: Attacking Lattice Cryptography with Transformers Emily Wenger, accessed April 20, 2025, https://www.emilywenger.com/assets/salsa-neurips.pdf
- 154. Séminaire de Théorie Algorithmique des Nombres Institut de Mathématiques de Bordeaux, accessed April 20, 2025, https://www.math.u-bordeaux.fr/imb/seminaire-de-theorie-algorithmique-des-no
- 155. МАТЕРІАЛИ ПЕРШОГО МІЖНАРОДНОГО НАУКОВО-ПРАКТИЧНОГО ФОРУМУ XHУPE, accessed April 20, 2025, https://openarchive.nure.ua/bitstreams/ed01c8c4-0251-43f7-9851-ad5797f1de8e/download
- 156. Survey on Federated Learning Towards Privacy Preserving AI Computer Science Conference Proceedings, accessed April 20, 2025, https://csitcp.org/paper/10/1011csit20.pdf
- 157. Lecture 14: Learning with Errors, accessed April 20, 2025, https://web.stanford.edu/class/cs354/scribe/lecture14.pdf
- 158. NIST Unveils Post-Quantum Cryptography (PQC) Standards, accessed April 20, 2025,
 - https://postquantum.com/industry-news/nist-postquantum-cryptography-pqc-st andards/

- Shortest Vector Problem (SVP), accessed April 20, 2025, https://cseweb.ucsd.edu/~daniele/LatticeLinks/SVP.html
- 160. Preparing for Post Quantum Cryptography Oracle Blogs, accessed April 20, 2025, https://blogs.oracle.com/security/post/post-quantum-cryptography
- 161. (PDF) A Survey and Guideline on Privacy Enhancing Technologies for Collaborative Machine Learning ResearchGate, accessed April 20, 2025, https://www.researchgate.net/publication/363314479 A Survey and Guideline on Privacy Enhancing Technologies for Collaborative Machine Learning
- 162. arXiv:2401.09027v3 [quant-ph] 9 May 2024, accessed April 20, 2025, https://arxiv.org/pdf/2401.09027
- 163. Security, Privacy, Confidentiality and Trust in Blockchain MDPI, accessed April 20, 2025, https://mdpi-res.com/bookfiles/book/10583/Security_Privacy_Confidentiality_and Trust in Blockchain.pdf?v=1740587438
- 164. Status Report on the Third Round of the NIST Post-Quantum Cryptography Standardization Process, accessed April 20, 2025, https://www.nist.gov/publications/status-report-third-round-nist-post-quantum-cryptography-standardization-process
- 165. NIST Releases First 3 Finalized Post-Quantum Encryption Standards, accessed April 20, 2025, https://www.nist.gov/news-events/news/2024/08/nist-releases-first-3-finalized-p ost-quantum-encryption-standards
- 166. Privacy-Preserving Machine Learning with Homomorphic Encryption among Multi-Parties kth .diva, accessed April 20, 2025, https://kth.diva-portal.org/smash/qet/diva2:1947274/FULLTEXT01.pdf
- 167. Performance Analysis and Industry Deployment of Post-Quantum Cryptography Algorithms, accessed April 20, 2025, https://arxiv.org/html/2503.12952v1
- 168. The Role of Quantum Computing in Enhancing Encryption Security: A Review -Cryptology ePrint Archive, accessed April 20, 2025, https://eprint.iacr.org/2025/706.pdf
- 169. Hyperledger Fabric 2.0 Architecture Security Controls Checklist | CSA, accessed April 21, 2025, https://cloudsecurityalliance.org/artifacts/hyperledger-fabric-2-0-architecture-security-controls-checklist
- 170. Cryptographic hardware and embedded systems -- CHES 2017: 19th International Conference, Taipei, Taiwan, September 25-28, 2017, Proceedings 978-3-319-66787-4, 3319667874, 978-3-319-66786-7 DOKUMEN.PUB, accessed April 20, 2025,
 - https://dokumen.pub/cryptographic-hardware-and-embedded-systems-ches-20 17-19th-international-conference-taipei-taiwan-september-25-28-2017-proceed ings-978-3-319-66787-4-3319667874-978-3-319-66786-7.html
- 171. Threats and Defenses in Federated Learning Life Cycle arXiv, accessed April 20, 2025, https://arxiv.org/pdf/2407.06754?
- 172. Threats and Defenses in Federated Learning Life Cycle: A Comprehensive

- Survey and Challenges arXiv, accessed April 20, 2025, https://arxiv.org/html/2407.06754v2
- 173. A Survey of Privacy Threats and Defense in Vertical Federated Learning: From Model Life Cycle Perspective - arXiv, accessed April 20, 2025, https://arxiv.org/html/2402.03688v1
- 174. A Fully Homomorphic Encryption Scheme Based on Fibonacci Recursive Matrix, accessed April 20, 2025, https://www.researchgate.net/publication/387043043_A_Fully_Homomorphic_Encryption_Scheme_Based_on_Fibonacci_Recursive_Matrix
- 175. Fibonacci Noise Modification on Data Encryption, accessed April 20, 2025, https://www.kexuetongbao-csb.com/article/fibonacci-noise-modification-on-dat-a-encryption
- 176. Nemesis: Noise-randomized Encryption with Modular Efficiency and Secure Integration in Machine Learning Systems - arXiv, accessed April 20, 2025, https://arxiv.org/html/2412.14392v1
- 177. Noiseless Fully Homomorphic Encryption Cryptology ePrint Archive, accessed April 20, 2025, https://eprint.iacr.org/2017/839.pdf
- 178. Hybrid Quantum-Classical Algorithms arXiv, accessed April 20, 2025, https://arxiv.org/html/2406.12371v1
- 179. Resource-Efficient and Self-Adaptive Quantum Search in a Quantum-Classical Hybrid System arXiv, accessed April 20, 2025, https://arxiv.org/html/2405.04490v1
- 180. Bitcoin Vulnerabilities Due to Quantum Computing, accessed April 20, 2025, https://opsdesign.com/bitcoin-vulnerabilities-due-to-quantum-computing/
- 181. A Framework for Quantum Computing Simulation Targeted to Hybrid Parallel Architectures PMC PubMed Central, accessed April 20, 2025, https://pmc.ncbi.nlm.nih.gov/articles/PMC10048558/
- 182. Post-Quantum Crypto Agility Thales, accessed April 20, 2025, https://cpl.thalesgroup.com/encryption/post-quantum-crypto-agility
- 183. About Juanita Koilpillai Service Award | CSA Cloud Security Alliance, accessed April 21, 2025,
- https://cloudsecurityalliance.org/research/juanita-koilpillai/service-award 184. Resources - The FAIR Institute, accessed April 21, 2025,
- Resources The FAIR Institute, accessed April 21, 2025
 https://www.fairinstitute.org/resources
- 185. Speakers CSA APAC Congress 2016 | Cloud Security Alliance на Glue Up, accessed April 21, 2025, https://app.glueup.com/ru/event/648/speakers.html
- 186. FAIRCON24 Agenda The FAIR Institute, accessed April 21, 2025, https://www.fairinstitute.org/2024-fair-conference-agenda
- 187. Juanita Koilpillai COVID19 InfoRiskToday, accessed April 21, 2025, https://covid19.inforisktoday.com/authors/juanita-koilpillai-i-1313
- 188. LATAM CISO Summit 2024 Digi Americas Alliance, accessed April 21, 2025, https://digiamericas.org/events/latam-ciso-summit-2024/
- 189. Registrants 2021 International Cryptographic Module Conference (ICMC), accessed April 21, 2025, https://icmconference.org/?page_id=15099
- 190. INFORMATION SECURITY & RISK MANAGEMENT, accessed April 21, 2025,

- https://ismg.io/wp-content/uploads/2017/04/2017-ISMG-Media-Kit.pdf
- Fortifying Future IoT Security: A Comprehensive Review on Lightweight Post-Quantum Cryptography, accessed April 20, 2025,
 - https://www.etasr.com/index.php/ETASR/article/download/10141/4800/46388
- 192. arXiv:2409.08138v3 [gr-qc] 19 Sep 2024, accessed April 21, 2025, http://arxiv.org/pdf/2409.08138
- 193. Dissertation Publikationsserver der Universität Regensburg, accessed April 21, 2025, https://epub.uni-regensburg.de/43508/1/Dissertation.pdf
- 194. General Relativity and Quantum Cosmology arXiv, accessed April 21, 2025, https://arxiv.org/list/gr-qc/new
- 195. Advanced Simulation Techniques for Many-Body Quantum Systems, accessed April 20, 2025, https://math.rpi.edu/research/advanced-simulation-techniques-many-body-quantum Systems (accessed April 20, 2025).
 - https://math.rpi.edu/research/advanced-simulation-techniques-many-body-quantum-systems
- 196. Professor Andrei Khrennikov Professor Emmanuel Haven | How Quantum-like Models Illuminate Complex Systems scientia.global, accessed April 20, 2025,
 - https://www.scientia.global/professor-andrei-khrennikov-professor-emmanuel-haven-how-quantum-like-models-illuminate-complex-systems/
- 197. Does Quantum Gravity Happen at the Planck Scale? arXiv, accessed April 20, 2025, https://arxiv.org/html/2501.07614v1
- 198. A (quantum) complex legacy, accessed April 20, 2025, https://quantumfrontiers.com/2023/01/29/a-quantum-complex-legacy/
- 199. Asymptotic safety in quantum gravity Wikipedia, accessed April 20, 2025, https://en.wikipedia.org/wiki/Asymptotic_safety_in_quantum_gravity
- 200. (PDF) Quantum gravity as a multitrace matrix model ResearchGate, accessed April 20, 2025, https://www.researchgate.net/publication/317887210_Quantum_Gravity_as_a_Multitrace_Matrix_Model
- 201. University of Southampton Faculty of Engineering and Physical Sciences Physics and Astronomy The renormalization group and quant, accessed April 20, 2025, https://eprints.soton.ac.uk/473393/1/Thesis Alex Mitchell final.pdf
- 202. Most Influential ArXiv (General Relativity and Quantum Cosmology) Papers (2024-10), accessed April 21, 2025, https://www.paperdigest.org/2024/10/most-influential-arxiv-general-relativity-and-quantum-cosmology-papers-2024-10/
- 203. arXiv:1201.3660v1 [gr-qc] 17 Jan 2012 CiteSeerX, accessed April 21, 2025, https://citeseerx.ist.psu.edu/document?repid=rep1&type=pdf&doi=df3732cd809f8a9952777724eb1bcd274e0325c3
- 204. Classical and quantum gravity in ? dimensions: I. A unifying approach ResearchGate, accessed April 21, 2025, https://www.researchgate.net/publication/253558448 Classical and quantum gravity in dimensions I A unifying approach
- 205. Corrections to Bekenstein-Hawking Entropy— Quantum or not-so Quantum? MDPI, accessed April 20, 2025, https://www.mdpi.com/1099-4300/13/1/11

- 206. Modified gravity theories from the Barrow hypothesis arXiv, accessed April 20, 2025, https://arxiv.org/pdf/2403.13687
- 207. Can Bekenstein's area law prevail in modified theories of gravity? | Phys. Rev. D, accessed April 20, 2025, https://link.aps.org/doi/10.1103/PhysRevD.108.L121501
- 208. [hep-th/9808091] Quantum Gravity and Black Hole Entropy arXiv, accessed April 20, 2025, https://arxiv.org/abs/hep-th/9808091
- 209. [2503.22609] Quantum Entropy-Driven Modifications to Holographic Dark Energy in \$f(G,T)\$ Gravity arXiv, accessed April 20, 2025, https://arxiv.org/abs/2503.22609
- 210. Planck units Wikipedia, accessed April 20, 2025, https://en.wikipedia.org/wiki/Planck units
- 211. New Discovery on Planck Units and Physical Dimension in Cosmic Continuum Theory, accessed April 20, 2025, https://www.scirp.org/journal/paperinformation?paperid=89023
- Evaluation and Analysis of an LSTM and GRU Based Stock Investment Strategy
 Atlantis Press, accessed April 20, 2025,
 https://www.atlantis-press.com/article/125980518.pdf
- 213. Recurrent Neural Networks for Financial Time-Series Modelling ResearchGate, accessed April 20, 2025,
 https://www.researchgate.net/publication/329316403_Recurrent_Neural_Networks
 s for Financial Time-Series Modelling
- 214. Advanced Stock Market Prediction Using Hybrid GRU-LSTM Techniques, accessed April 20, 2025, https://ijariie.com/AdminUploadPdf/TITLE_Advanced_Stock_Market_Prediction_Using_Hybrid_GRU_LSTM_Techniques_ijariie25797.pdf
- 215. Forecasting Stock Market Indices Using the Recurrent Neural Network Based Hybrid Models: CNN-LSTM, GRU-CNN, and Ensemble Models MDPI, accessed April 20, 2025, https://www.mdpi.com/2076-3417/13/7/4644
- 216. Financial Market Forecasting using RNN, LSTM, BiLSTM, GRU and Transformer-Based Deep Learning Algorithms - ResearchGate, accessed April 20, 2025, https://www.researchgate.net/publication/377245794_Financial_Market_Forecasting_using_RNN_LSTM_BiLSTM_GRU_and_Transformer-Based_Deep_Learning_Algorithms
- 217. 5 Algorithms to Train a Neural Network DataScienceCentral.com, accessed April 20, 2025,
 - https://www.datasciencecentral.com/5-algorithms-to-train-a-neural-network/
- 218. LeCun's 2022 paper on autonomous machine intelligence rehashes but does not cite essential work of 1990-2015, accessed April 20, 2025, https://people.idsia.ch/~juergen/lecun-rehash-1990-2022.html
- 219. arXiv:2209.03956v1 [q-bio.NC] 17 Jul 2022, accessed April 20, 2025, https://arxiv.org/pdf/2209.03956
- 220. Artificial Consciousness: An Illusionary Solution to the Hard Problem SAPAN, accessed April 20, 2025, https://www.sapan.ai/assets/papers/illusion_test.pdf
- 221. Gödel Agent: A Self-Referential Framework for Agents Recursively

- Self-Improvement arXiv, accessed April 20, 2025, https://arxiv.org/html/2410.04444v2
- 222. [2402.02625] Enhancing Transformer RNNs with Multiple Temporal Perspectives arXiv, accessed April 20, 2025, https://arxiv.org/abs/2402.02625
- 223. Temporal-kernel recurrent neural networks PubMed, accessed April 20, 2025, https://pubmed.ncbi.nlm.nih.gov/19932002/
- 224. remigenet/TKAN: TKAN: Temporal Kolmogorov-Arnold Networks GitHub, accessed April 20, 2025, https://github.com/remigenet/TKAN
- 225. Evaluating Large Language Models on Wikipedia-Style Survey Generation ACL Anthology, accessed April 20, 2025, https://aclanthology.org/2024.findings-acl.321.pdf
- 226. Large Language Models: A Survey arXiv, accessed April 20, 2025, https://arxiv.org/html/2402.06196v2
- 227. Mitigating LLM Hallucination with Smoothed Knowledge Distillation arXiv, accessed April 20, 2025, https://arxiv.org/html/2502.11306v1
- 228. A survey of multilingual large language models PMC PubMed Central, accessed April 20, 2025, https://pmc.ncbi.nlm.nih.gov/articles/PMC11783891/
- 229. An Audit on the Perspectives and Challenges of Hallucinations in NLP ACL Anthology, accessed April 20, 2025, https://aclanthology.org/2024.emnlp-main.375.pdf
- 230. Golden Ratio Search: A Low-Power Adversarial Attack for Deep Learning based Modulation Classification arXiv, accessed April 20, 2025, https://arxiv.org/pdf/2409.11454
- 231. An Optimizing Pulse Coupled Neural Network based on Golden Eagle
 Optimizer for Automatic Image Segmentation Journal of Information Hiding and
 Multimedia Signal Processing, accessed April 20, 2025,
 https://bit.kuas.edu.tw/2022/vol13/N3/01.JIHMSP-1617 r1.pdf
- 232. A Novel Interpretable Fusion Analytic Framework for Investigating Functional Brain Connectivity Differences in Cognitive Impairments arXiv, accessed April 20, 2025, https://arxiv.org/html/2401.09028v1
- 233. Relationship Between Basic Properties of BOLD Fluctuations and Calculated Metrics of Complexity in the Human Connectome Project Frontiers, accessed April 20, 2025, https://www.frontiersin.org/journals/neuroscience/articles/10.3389/fnins.2020.550 923/full
- 234. The Laplacian eigenmaps dimensionality reduction of fMRI data for discovering stimulus-induced changes in the resting-state brain activity | bioRxiv, accessed April 20, 2025, https://www.biorxiv.org/content/10.1101/2020.12.10.419861.full
- 235. Does Amount of Information Support Aesthetic Values? Frontiers, accessed April 21, 2025, https://www.frontiersin.org/journals/neuroscience/articles/10.3389/fnins.2022.805658/full
- 236. Ultrahigh Resolution fMRI at 7T Using Radial-Cartesian TURBINE Sampling PMC PubMed Central, accessed April 21, 2025,

- https://pmc.ncbi.nlm.nih.gov/articles/PMC9546489/
- 237. The Golden Section as Optical Limitation PMC PubMed Central, accessed April 21, 2025, https://pmc.ncbi.nlm.nih.gov/articles/PMC4495923/
- 238. EC-based analysis of empirical BOLD signals. (A) Pipeline for brain... ResearchGate, accessed April 20, 2025,
 https://www.researchgate.net/figure/EC-based-analysis-of-empirical-BOLD-signals-A-Pipeline-for-brain-coordination-analysis fig2 338093068
- 239. Seeking the "Beauty Center" in the Brain: A Meta-Analysis of fMRI Studies of Beautiful Human Faces and Visual Art | Request PDF ResearchGate, accessed April 21, 2025, https://www.researchgate.net/publication/345125964_Seeking_the_Beauty_Centerin_the_Brain_A_Meta-Analysis_of_fMRI_Studies_of_Beautiful_Human_Faces_and_Visual_Art
- 240. Complex harmonics reveal low-dimensional manifolds of critical brain dynamics | Phys. Rev. E Physical Review Link Manager, accessed April 20, 2025, https://link.aps.org/doi/10.1103/PhysRevE.111.014410
- 241. CATD: Unified Representation Learning for EEG-to-fMRI Cross-Modal Generation arXiv, accessed April 20, 2025, https://arxiv.org/html/2408.00777v2
- 242. The biological role of local and global fMRI BOLD signal variability in human brain organization PubMed Central, accessed April 20, 2025, https://pmc.ncbi.nlm.nih.gov/articles/PMC10634715/
- 243. Subspace-constrained approaches to low-rank fMRI acceleration | bioRxiv, accessed April 21, 2025, https://www.biorxiv.org/content/10.1101/2020.12.15.422908v1.full-text
- 244. Subspace-constrained approaches to low-rank fMRI acceleration PMC PubMed Central, accessed April 21, 2025, https://pmc.ncbi.nlm.nih.gov/articles/PMC7611820/
- 245. Hierarchical consciousness: the Nested Observer Windows model Oxford Academic, accessed April 21, 2025, https://academic.oup.com/nc/article/2024/1/niae010/7631826
- 246. Publication LOFT, accessed April 21, 2025, https://loft-lab.ini.usc.edu/index-4.html
- 247. The Temporal Signature of Memories: Identification of a General Mechanism for Dynamic Memory Replay in Humans | PLOS Biology, accessed April 21, 2025, https://journals.plos.org/plosbiology/article?id=10.1371/journal.pbio.1002528
- 248. Brain and Cognitive Science Inspired Deep Learning: A Comprehensive Survey, accessed April 20, 2025, https://www.computer.org/csdl/journal/tk/2025/04/10834593/23ljNrEYCXu
- 249. Brain-imaging evidence for compression of binary sound sequences in human memory, accessed April 20, 2025, https://elifesciences.org/articles/84376
- 250. Place cells may simply be memory cells: Memory compression leads to spatial tuning and history dependence PubMed Central, accessed April 20, 2025, https://pmc.ncbi.nlm.nih.gov/articles/PMC8713479/
- 251. The brain uses data compression for decision-making | Champalimaud Foundation, accessed April 21, 2025,

- https://fchampalimaud.org/news/brain-uses-data-compression-decision-making
- 252. MEMORY NETWORKS AS NEUROCOMPUTATIONAL MODELS OF COGNITIVE FUNCTIONS A THESIS SUBMITTED TO THE GRADUATE SCHOOL OF INFORMATICS OF, accessed April 20, 2025, https://open.metu.edu.tr/bitstream/handle/11511/110953/MEMORY_NETWORKS_ASSED NEUROCOMPUTATIONAL MODELS OF COGNITIVE FUNCTIONS Sinan Altinum
- 253. Cognitive neuroscience perspective on memory: overview and summary PubMed Central, accessed April 21, 2025, https://pmc.ncbi.nlm.nih.gov/articles/PMC10410470/

c.pdf

- 254. Efficient Data Compression in Perception and Perceptual Memory Brain and Cognitive Sciences, accessed April 20, 2025, https://www2.bcs.rochester.edu/sites/robbie/BatesJacobs-PsychRev2020.pdf
- 255. Pattern integration and differentiation: Dual process model of episodic memory | Imaging Neuroscience MIT Press Direct, accessed April 20, 2025, https://direct.mit.edu/imag/article/doi/10.1162/imag_a_00433/125725/Pattern-integration-and-differentiation-Dual
- 256. (PDF) Cognitive neuroscience perspective on memory: overview and summary, accessed April 21, 2025, https://www.researchgate.net/publication/372670894_Cognitive_neuroscience_perspective_on_memory_overview_and_summary
- 257. The Cognitive Neuroscience of Insight Psychology Northwestern, accessed April 21, 2025, https://psychology.northwestern.edu/people/faculty/core/profiles/ann_rvw_psy_2 014.pdf
- 258. THE COGNITIVE NEUROSCIENCE OF WORKING MEMORY PMC PubMed Central, accessed April 21, 2025, https://pmc.ncbi.nlm.nih.gov/articles/PMC4374359/
- 259. The Cognitive Neurosciences, accessed April 21, 2025, https://www.hse.ru/data/2011/06/28/1216307711/Gazzaniga.%20The%20Cognitive %20Neurosciences.pdf
- 260. Proceedings of the Annual Meeting of the Cognitive Science Society eScholarship.org, accessed April 21, 2025, https://escholarship.org/uc/cognitivesciencesociety
- 261. Research/Papers | Cognitive Experiments Models and Neuroscience Lab | University of Colorado Boulder, accessed April 21, 2025, https://www.colorado.edu/lab/cemnl/researchpapers
- 262. Large-scale DCMs for resting-state fMRI | Network Neuroscience MIT Press Direct, accessed April 20, 2025, https://direct.mit.edu/netn/article/1/3/222/2199/Large-scale-DCMs-for-resting-state-fMRI
- 263. Neuropredictome: a data-driven predictome for cognitive, psychiatric, medical, and lifestyle factors on the brain bioRxiv, accessed April 20, 2025, https://www.biorxiv.org/content/10.1101/2020.12.07.415091v2.full.pdf
- 264. Dimensionality Reduction Brain Imaging Analysis Kit, accessed April 20,

- 2025, https://brainiak.org/tutorials/04-dimensionality-reduction/
- 265. Extracting representations of cognition across neuroimaging studies improves brain decoding | PLOS Computational Biology, accessed April 21, 2025, https://journals.plos.org/ploscompbiol/article?id=10.1371/journal.pcbi.1008795
- 266. A review of feature reduction techniques in neuroimaging PMC PubMed Central, accessed April 20, 2025, https://pmc.ncbi.nlm.nih.gov/articles/PMC4040248/
- 267. Researchers, Reflexivity, and Good Data: Writing to Unlearn ResearchGate, accessed April 21, 2025,

 https://www.researchgate.net/publication/240744526_Researchers_Reflexivity_andGood_Data_Writing_to_Unlearn
- 268. Debilitating Research: Scholarship of the Obvious and Epistemic Trauma DOI, accessed April 21, 2025, https://doi.org/10.1080/00020184.2024.2431801
- 269. Socioeconomic status significantly impacts childhood cancer survival in South Africa, accessed April 21, 2025, https://pubmed.ncbi.nlm.nih.gov/37705154/
- 270. Full article: Debilitating Research: Scholarship of the Obvious and Epistemic Trauma, accessed April 21, 2025, https://www.tandfonline.com/doi/full/10.1080/00020184.2024.2431801
- 271. "Scenes of Subjection" in Public Education: Thinking Intersectionally as If Disability Matters | Request PDF ResearchGate, accessed April 21, 2025, https://www.researchgate.net/publication/337131633_Scenes_of_Subjection_in_Public Education Thinking Intersectionally as If Disability Matters
- 272. Where my dad was from he was quite a respected man Unisa IR, accessed April 21, 2025,
 - https://uir.unisa.ac.za/items/04cc8de2-a122-4fd5-843b-29c087fab969
- 273. 'Where my dad was from he was quite a respected man'. Scite, accessed April 21, 2025, https://scite.ai/reports/10.1037/a0029075
- 274. Deriving a Control-Oriented Model for an Axisymmetric Vehicle With the Power-Law Revolution Nose SciELO, accessed April 20, 2025, https://www.scielo.br/j/jatm/a/SJvQwn3s5JzRq48JdjHHDMg/?lang=en
- 275. Hypersonic Vehicle Technology Translations from Chinese source documents Air University, accessed April 20, 2025, https://www.airuniversity.af.edu/Portals/10/CASI/documents/Translations/2024-06-24%20ITOW%20Hypersonic%20Vehicle%20Technology.pdf
- 276. Review of Advanced Guidance and Control Algorithms for Space/Aerospace Vehicles - CERES Research Repository, accessed April 20, 2025, https://dspace.lib.cranfield.ac.uk/bitstream/1826/16458/1/Review_of_advanced_guidance and control algorithms for space-2021.pdf
- 277. Aircraft Trajectories Computation-Prediction-Control. Volume 1 (La Trajectoire de l'Avion Calcul-Prediction-Controle) DTIC, accessed April 20, 2025, https://apps.dtic.mil/sti/tr/pdf/ADA223563.pdf
- 278. Intelligent Trajectory Prediction Algorithm for Hypersonic Vehicle Based on Sparse Associative Structure Model - MDPI, accessed April 20, 2025, https://www.mdpi.com/2504-446X/8/9/505
- 279. Circular Probable Error for Circular and Noncircular Gaussian Impacts DTIC,

- accessed April 20, 2025, https://apps.dtic.mil/sti/pdfs/AD1043284.pdf
- 280. Ballistic Missile Basics, accessed April 20, 2025, https://missiledefenseadvocacy.org/missile-threat-and-proliferation/missile-basics/
- 281. Multiple independently targetable reentry vehicle Wikipedia, accessed April 20, 2025,
 - https://en.wikipedia.org/wiki/Multiple independently targetable reentry vehicle
- 282. Circular error probable Wikipedia, accessed April 20, 2025, https://en.wikipedia.org/wiki/Circular error probable
- 283. AlphaFold Protein Structure Database, accessed April 20, 2025, https://alphafold.ebi.ac.uk/
- 284. Using AlphaFold to model the MDM2-p53 complex Bonvin Lab, accessed April 20, 2025, https://www.bonvinlab.org/education/molmod_online/alphafold/
- 285. An Overview of Alphafold's Breakthrough Frontiers, accessed April 20, 2025, https://www.frontiersin.org/journals/artificial-intelligence/articles/10.3389/frai.2022. 875587/full
- 286. Before and after AlphaFold2: An overview of protein structure prediction PubMed Central, accessed April 20, 2025, https://pmc.ncbi.nlm.nih.gov/articles/PMC10011655/
- 287. AlphaFold two years on: Validation and impact PNAS, accessed April 20, 2025, https://www.pnas.org/doi/10.1073/pnas.2315002121
- 288. Reliable protein-protein docking with AlphaFold, Rosetta, and replica-exchange eLife, accessed April 20, 2025, https://elifesciences.org/reviewed-preprints/94029v2
- 289. Unlocking the power of Al models: exploring protein folding prediction through comparative analysis, accessed April 20, 2025, https://pmc.ncbi.nlm.nih.gov/articles/PMC11377126/
- 290. non-canonical crosslinks confound evolutionary protein structure models arXiv, accessed April 20, 2025, https://arxiv.org/pdf/2503.17368
- 291. arXiv q-bio.BM Biomolecules: "inverse folding and binding site prediction, particularly when using predicted structures, owing to its enhanced tolerance to data deviation and noise. Our approach offers a novel perspective for conducting biological function research and drug [5/6 of https://arxiv.org/abs/2503.16996v1]", accessed April 20, 2025,
 - https://bsky.app/profile/qbiobm-bot.bsky.social/post/3ll4454fi3n2m
- 292. [q-bio/0409038] A modular Fibonacci sequence in proteins arXiv, accessed April 20, 2025, https://arxiv.org/abs/q-bio/0409038
- 293. arXiv:q-bio/0408024v1 [q-bio.BM] 27 Aug 2004, accessed April 20, 2025, https://arxiv.org/pdf/q-bio/0408024
- 294. Pathfinder: Protein folding pathway prediction based on conformational sampling PMC, accessed April 20, 2025, https://pmc.ncbi.nlm.nih.gov/articles/PMC10513300/
- 295. Pathfinder: Protein folding pathway prediction based on conformational sampling PLOS, accessed April 20, 2025, https://journals.plos.org/ploscompbiol/article?id=10.1371/journal.pcbi.1011438

- 296. Pathfinder: Protein folding pathway prediction based on conformational sampling PubMed, accessed April 20, 2025, https://pubmed.ncbi.nlm.nih.gov/37695768/
- 297. Advances in Surrogate Modeling for Biological Agent-Based Simulations arXiv, accessed April 20, 2025, https://arxiv.org/pdf/2504.11617
- 298. Collaborative Combat Aircraft for Disruptive Air Warfare | Air & Space Forces Magazine, accessed April 21, 2025, https://www.airandspaceforces.com/article/collaborative-combat-aircraft-for-disruptive-air-warfare/
- 299. Al for Military Decision-Making | Center for Security and Emerging Technology, accessed April 21, 2025, https://cset.georgetown.edu/publication/ai-for-military-decision-making/
- 300. Al in Combat: CSET Report Warns Military Commanders Against Blind Reliance on Decision Support Systems BABL Al, accessed April 21, 2025, https://babl.ai/ai-in-combat-cset-report-warns-military-commanders-against-blind-reliance-on-decision-support-systems/
- Al's Role in Defense Accelerating Decision Dominance in the Next Era of Warfare, accessed April 21, 2025, https://owlcyberdefense.com/blog/ai-role-in-defense-accelerating-decision-dominance/
- 302. Do Al Decision Support Systems 'Support' Humans in Military Decision-Making on the Use of Force? Opinio Juris, accessed April 21, 2025, http://opiniojuris.org/2024/11/29/do-ai-decision-support-systems-support-humans-in-military-decision-making-on-the-use-of-force/
- 303. Al's New Frontier in War Planning: How Al Agents Can Revolutionize Military Decision-Making | The Belfer Center for Science and International Affairs, accessed April 21, 2025, https://www.belfercenter.org/research-analysis/ais-new-frontier-war-planning-how-ai-agents-can-revolutionize-military-decision
- 304. Artificial Intelligence as a Combat Multiplier: Using AI to Unburden Army Staffs, accessed April 21, 2025, https://www.armyupress.army.mil/Journals/Military-Review/Online-Exclusive/2024-OLE/AI-Combat-Multiplier/
- 305. Al research strengthens certainty in battlefield decision-making | Article Army.mil, accessed April 21, 2025, https://www.army.mil/article/249169/ai_research_strengthens_certainty_in_battlefield_decision_making
- 306. How Al Will Accelerate Decision-Making in a Peer Contest Air & Space Forces Magazine, accessed April 21, 2025, https://www.airandspaceforces.com/how-ai-will-accelerate-decision-making-in-a-peer-contest/
- 307. German Navy Seeks Marine Drones for Future Warfare The Defense Post, accessed April 21, 2025,
 - https://thedefensepost.com/2025/03/24/germany-usv-future-warfare/
- 308. TRS-3D radars on K130-class corvettes to undergo modernization with

- HENSOLDT, accessed April 21, 2025, https://militaryembedded.com/radar-ew/sensors/trs-3d-radars-on-k130-class-co rvettes-to-undergo-modernization-with-hensoldt
- 309. German Navy's K130 corvettes to feature Indra defence system Naval Technology, accessed April 21, 2025, https://www.naval-technology.com/news/german-navys-new-k130-corvettes-to-feature-indra-electronic-defence-system/
- 310. Braunschweig-class corvette Wikipedia, accessed April 21, 2025, https://en.wikipedia.org/wiki/Braunschweig-class_corvette
- 311. Indra signs a contract to provide the German Navy's new K130 corvettes with its Rigel electronic defense systems, accessed April 21, 2025, https://www.indracompany.com/en/noticia/indra-signs-contract-provide-german-navys-new-k130-corvettes-rigel-electronic-defense
- 312. Inspired by Ukraine, Germany Explores Surface Drones as a Potential Replacement for K130 Corvettes | Defense Express, accessed April 21, 2025, https://en.defence-ua.com/news/inspired_by_ukraine_germany_explores_surface_drones_as_a_potential_replacement_for_k130_corvettes-13943.html
- 313. Hensoldt modernizes German Navy's K130 corvette TRS-3D radar Naval News, accessed April 21, 2025, https://www.navalnews.com/naval-news/2021/02/hensoldt-modernizes-german-navys-k130-corvette-trs-3d-radar/
- 314. K130 Braunschweig class Army Recognition, accessed April 21, 2025, https://armyrecognition.com/military-products/navy/corvettes/k130-braunschweig-class
- 315. HENSOLDT Modernising K130-class Corvette Radars | Joint Forces News, accessed April 21, 2025, https://www.joint-forces.com/defence-equipment-news/40569-hensoldt-modernising-k130-class-corvette-radars
- 316. What Is Quantum Computing? | IBM, accessed April 21, 2025, https://www.ibm.com/think/topics/quantum-computing
- 317. Quantum Computing: The Basics and Where We Are Headed Atlanta Technology Professionals, accessed April 21, 2025, https://atpconnect.org/quantum-computing-the-basics-and-where-we-are-headed/
- 318. Quantum Noise: Overcoming This Obstacle is Crucial for the Evolution of Quantum Computing Tech4Future, accessed April 21, 2025, https://tech4future.info/en/quantum-noise-quantum-computing/
- 319. The Quantum Roadmap Battle of Logical Qubits, accessed April 21, 2025, https://www.insidequantumtechnology.com/news-archive/the-quantum-roadma-p-battle-of-logical-qubits-by-brian-siegelwax-2/
- 320. Quantum algorithm for solving linear equations YouTube, accessed April 21, 2025, https://www.youtube.com/watch?v=KtIPAPyaPOg
- 321. The complexonaut | MIT News | Massachusetts Institute of Technology, accessed April 21, 2025, https://news.mit.edu/2014/scott-aaronson-shapes-conventional-and-quantum-c

omputing-0407

- 322. How Quantum Computers Calculate Everything At Once... But Can't Use It YouTube, accessed April 21, 2025,
 - https://www.youtube.com/watch?v=ulntkdiC-90
- 323. [2104.01043] Quantum Algorithms and Oracles with the Scalable ZX-calculus arXiv, accessed April 21, 2025, https://arxiv.org/abs/2104.01043
- 324. Unlocking the Power of Quantum Computing: A Comprehensive Guide NIX, accessed April 21, 2025, https://nixstech.com/news/the-world-on-the-threshold-of-a-quantum-revolution
 - -what-prospects-we-have-and-what-you-need-to-know-about-quantum-calculus/
- 325. 'Quantum computer algorithms are linear algebra, probabilities. This is not something that we do a good job of teaching our kids' -- Assuming tech works as promised, overhaul needed in policy and supplies, panel says: r/math Reddit, accessed April 21, 2025,
 - https://www.reddit.com/r/math/comments/pz5d2w/quantum_computer_algorithms_are_linear_algebra/