

Lecture 10 Problems: Problem 1

Expanding,

$$\det \begin{pmatrix} 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix} = 0(\text{junk}) - 0(\text{junk}) + 0(\text{junk}) - 1 \begin{vmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{vmatrix} = -1.$$

Expanding/calculating by cofactors is most efficient.

Problem 2

By expanding and noting that

$19(\text{known det}) + \text{other multiples of cofactors}$

must be 1 less than 11

$20(\text{known det}) + \text{same junk}$

Thus, since the latter is 1 then $1 - 1 = 0$.