

Example: Melting Points of BeO through SrO

Which compound would you expect to have the highest melting point?

- |                                     |     |
|-------------------------------------|-----|
| <input checked="" type="checkbox"/> | BeO |
| <input type="checkbox"/>            | MgO |
| <input type="checkbox"/>            | CaO |
| <input type="checkbox"/>            | SrO |

BeO minimizes the sum of the ionic radii of the anion and cation.

Example: Relative melting points of compounds

~~Which of the following~~ Which compound would you expect to have the lowest melting point?

MgO —  
BeS  
NaCl  
X KCl

For this problem, we would like to maximize the sum of ionic radii. We see that BeS has a smaller atomic radius than MgO, thus we cross it out. Now compare it to the maximum of the chlorides; KCl. KCl's radius<sup>sum</sup> is clearly larger, thus it has the lowest melting point.

### Example: Atomic Radii of atoms and ions

Which atom or ion would you expect to have the smallest radius?

- |                |                 |
|----------------|-----------------|
|                | Ne              |
| <del>///</del> | F <sup>-</sup>  |
| X              | Na <sup>+</sup> |
|                | Ne <sup>-</sup> |

Ne<sup>-</sup> is right out; it is the only one with an electron occupying an orbital with  $n=3$ . Of the three remaining, all have their highest energy electrons in the 2p orbital, Na<sup>+</sup> has the highest proton:electron ratio and thus pulls the cloud of probability in closest.

Example: Ionization energy of Li, Na, K, and Mg  
Which atom would you expect to have the highest second ionization energy?

|   |    |
|---|----|
| X | Li |
|   | Na |
|   | K  |
|   | Mg |

Lithium; its second ionization is the ionization of Helium, the highest ionization on the periodic table.

### Example: Bond Energy of $KI$

What is the magnitude of the energy of a bond formed between a  $K^+$  and an  $I^-$ ? The ionic radii of  $K^+$  and  $I^-$  are 152 pm and 206 pm respectively. Assume the Born exponent  $n = 10$ .

Recall that 
$$E_{BE} = \frac{-Q_1 + Q_2 - e^2}{4\pi \epsilon_0 r_0} \left(1 - \frac{1}{n}\right)$$

Then insert

$$E_{BE} = \frac{e^2}{4\pi (8.854 \cdot 10^{-12}) (152 + 206 \text{ pm}) \cdot 10^{-12} \cdot 0.9}$$

~~$$= -1.144 \cdot 10^{-19} \text{ J}$$~~

$$= 3.62 \cdot 10^{-19} \text{ J}$$

### Example: Cohesive Energy

Calculate the magnitude of the cohesive energy of KI.  
~~What is the lattice energy?~~ The ionic radii of  $K^+$  and  $I^-$  are 152 pm and 206 pm respectively. Assume the Born exponent  $n$  is 10. Assume a Madelung constant of 1.7.

Recall the formula

$$E_{tot} = \frac{-N_A Q^+ Q^- e^2 M}{4\pi \epsilon_0 r_0} \left(1 - \frac{1}{n}\right)$$

Insert,

$$E_{tot} = \frac{N_A e^2 1.7}{4\pi \epsilon_0 (358 \cdot 10^{-12})} \cdot 0.9$$

$$= \cancel{321074} \text{ KJ/mol}$$

$$= \cancel{59392} 594 \text{ KJ/mol}$$

Example: Ionic radius of cesium

Estimate the radius of the cesium ion  $\text{Cs}^+$ . The lattice energy of cesium chloride,  $\text{CsCl}$ , is  $633 \text{ kJ/mol}$ . For  $\text{CsCl}$ , the Madelung constant  $M$  is  $1.763$ , and the Born exponent  $n$  is  $10.7$ . The radius of  $\text{Cl}^-$  is known to be  $1.81 \text{ \AA}$ . Express your answer in angstroms.

We must solve

$$-633,000 = \frac{-N_A \cdot 1.763 \cdot e^2}{4\pi \epsilon_0 (r_{\text{Cs}} + 1.81 \text{ \AA})} \left(1 - \frac{1}{10.7}\right)$$

$\Rightarrow$

$$r_{\text{Cs}} + 1.81 \text{ \AA} = 3.50 \text{ \AA}$$

$$r_{\text{Cs}} = 1.69 \text{ \AA}$$