Week 11 - Exercises-Solutions

Exercise solutions

Week 12

Investigation

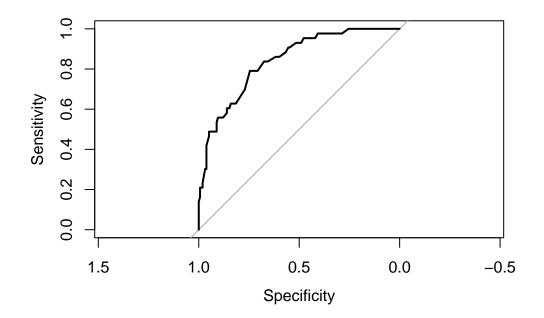
R code and output

1) Fitting the model, naive AUC and ROC

Clearly all covariates (age, oral and smoke) are important predictors of mi. A naive ROC curve can be obtained by computing the predicted probability of MI for each observation in the dataset and calling the roc function from pROC

```
infarct <- read.csv("infarct.csv")</pre>
infarct<-data.frame(infarct)</pre>
require(pROC)
## Loading required package: pROC
## Type 'citation("pROC")' for a citation.
##
## Attaching package: 'pROC'
## The following objects are masked from 'package:stats':
##
##
       cov, smooth, var
out0 <- glm(mi ~ oral + age + smoke, family=binomial(link="logit"),data=infarct)
summary(out0)
##
## Call:
## qlm(formula = mi ~ oral + age + smoke, family = binomial(link = "logit"),
       data = infarct)
##
## Deviance Residuals:
      Min 1Q Median
                               3Q
                                         Max
## -1.7019 -0.6045 -0.3215 -0.1562 2.5689
##
## Coefficients:
##
              Estimate Std. Error z value Pr(>|z|)
```

```
## (Intercept) -9.11405
                          1.75703 -5.187 2.13e-07 ***
## oral
               1.97990
                          0.46968 4.215 2.49e-05 ***
               0.16256
                          0.04454
                                    3.650 0.000262 ***
## age
## smoke
               1.81224
                          0.42938
                                    4.221 2.44e-05 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##
      Null deviance: 208.20 on 199 degrees of freedom
## Residual deviance: 150.37 on 196 degrees of freedom
## AIC: 158.37
##
## Number of Fisher Scoring iterations: 5
infarct$pred=predict(out0,infarct,type="response")
out.roc<- roc(infarct$mi, infarct$pred,plot=TRUE,ci=TRUE)</pre>
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
```



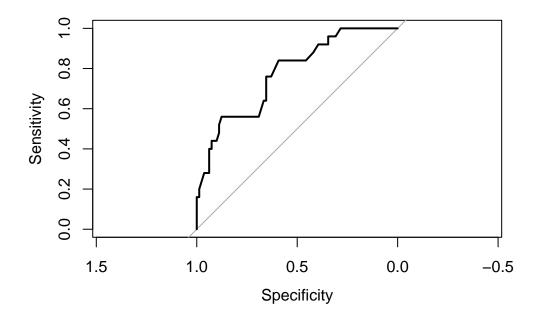
The naive AUC is 0.84, 95% CI=(0.78; 0.90), which can be classified as *good*. The model predicts well but this estimate is affected by optimism bias. The true AUC is probably a bit lower, how much lower, we are going to discover.

2) split sample AUC

An AUC free of optimism bias can be obtained using the split sample approach whereby the data is split in two, the model built on the training dataset and the AUC computed on the validation dataset

```
n=dim(infarct)[1]
set.seed(1002)
# set.seed(2002)
infarct$val=rbinom(n,1,0.5) # val =0 for dvelopment and val=1 for validation
table(infarct$val)
##
##
     0
        1
## 94 106
# NB: we choose here to split the data in two samples of similar sizes but
      we could decide to put more patients in the development dataset
      (increase the probability 0.5 to 0.6 etc)
# development dataset
infarct.dev=infarct[infarct$val==0,]
fit.dev<-glm(mi ~ oral + age + smoke, family=binomial, data=infarct.dev)</pre>
summary(fit.dev)
##
## Call:
## glm(formula = mi ~ oral + age + smoke, family = binomial, data = infarct.dev)
##
## Deviance Residuals:
```

```
Median
      Min
               1Q
                               30
                                      Max
## -1.8572 -0.4278 -0.2356 -0.1007
                                   2.4841
##
## Coefficients:
              Estimate Std. Error z value Pr(>|z|)
## (Intercept) -12.00945 3.12672 -3.841 0.000123 ***
## oral
             1.84803 0.77714 2.378 0.017407 *
              ## age
              ## smoke
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
      Null deviance: 91.815 on 93 degrees of freedom
## Residual deviance: 55.118 on 90 degrees of freedom
## AIC: 63.118
## Number of Fisher Scoring iterations: 6
# validation dataset + ROC/AUC
infarct.val=infarct[infarct$val==1,]
infarct.val$pred<- predict(fit.dev, infarct.val,type="response")</pre>
# predictions on the validation dataset using the previous fit
head(infarct.val)
     id oral age smoke mi
##
                              pred val
## 2
     2 0 32
                  0 0 0.007901981
## 3 3 1 37
                   0 1 0.134317344
## 6 6 1 40
                  0 0 0.233170631
## 7 7 0 35
                   0 0 0.015369383
                  0 0.059501663
## 8
        1 33
## 10 10
          0 31
                   0 0.006324488
require(pROC)
# ROC + AUC on the validation dataset (suffix .val)
out<- roc(infarct.val$mi, infarct.val$pred,plot=TRUE,ci=TRUE)</pre>
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
```



```
out
##
## Call:
## roc.default(response = infarct.val$mi, predictor = infarct.val$pred, ci = TRUE, plo
##
## Data: infarct.val$pred in 81 controls (infarct.val$mi 0) < 25 cases (infarct.val$mi 1).
## Area under the curve: 0.7751
## 95% CI: 0.6725-0.8776 (DeLong)</pre>
```

The AUC is lower with a larger CI, i.e. AUC=0.775 with a wider 95% CI=(0.67; 0.88). You may get a different result if you used another the seed or did not specify it. Setting the seed allows you to reproduce your results. The naive AUC=84% was a bit optimistic. Note that this method is suboptimal and it shows here with a small sample, yielding a large 95% CI

3) cross-validated AUC

A better for to use the data is to perform cross-validation. Given the data is rather, you may run into trouble with 10-fold crossvalidation depending on the seed. In that case, you can either change the seed or even use a smaller number of groups (e.g. carry out 5-fold CV). I used seed=2002, which seems to be ok.

```
require(cvAUC)
## Loading required package: cvAUC
# reload the data - we don't want the indicator we used before
infarct <- read.csv("infarct.csv")</pre>
infarct<-data.frame(infarct)</pre>
infarct=data.frame(infarct)
# reformatting the dataset
colnames(infarct)=c("id", "oral", "age", "smoke", "Y")
# remove id (only the variables of interest MUST BE KEPT)
infarct=infarct[,-c(1)]
# only outcome (Y) and covariates in dataset
head(infarct)
     oral age smoke Y
## 1 1 33 1 0
                 0 0
## 2
      0 32
## 3 1 37
                 0 1
## 4 0 36 0 0
## 5 1 50 1 1
## 6 1 40 0 0
# function doing the CV
cv_eval <- function(data, V=10){</pre>
  f.cvFolds <- function(Y, V){ #Create CV folds (stratify by outcome)</pre>
    YO <- split(sample(which(Y==0)), rep(1:V, length=length(which(Y==0))))
    Y1 <- split(sample(which(Y==1)), rep(1:V, length=length(which(Y==1))))
    folds <- vector("list", length=V)</pre>
    for (v in seq(V)) {folds[[v]] <- c(Y0[[v]], Y1[[v]])}</pre>
    return(folds)
  }
  f.doFit <- function(v, folds, data){ #Train/test glm for each fold</pre>
    fit <- glm(Y~., data=data[-folds[[v]],], family=binomial)</pre>
    pred <- predict(fit, newdata=data[folds[[v]],], type="response")</pre>
    return(pred)
  }
  folds <- f.cvFolds(Y=data$Y, V=V) #Create folds</pre>
  predictions <- unlist(sapply(seq(V), f.doFit, folds=folds, data=data)) #CV train/predict</pre>
  predictions[unlist(folds)] <- predictions #Re-order pred values</pre>
  ci.pooled.cvAUC
  # Get CV AUC and confidence interval
```

```
out <- ci.cvAUC(predictions=predictions, labels=data$Y, folds=folds, confidence=0.95)
 return(out)
}
set.seed(2002)
out.cv <- cv eval(data=infarct, V=10)
out.cv
## $cvAUC
## [1] 0.8276562
##
## $se
## [1] 0.03388826
##
## $ci
## [1] 0.7612365 0.8940760
## $confidence
## [1] 0.95
```

The 10-fold cross-validated AUC is 0.827, 95%CI=(0.76; 0.89) with seed=2002. It's a bit lower than the naive AUC but not by much, This is indicative of a small optimism bias (a common finding in practice). A slightly larger 95% CI than the one found with the naive analysis is observed. You may get different results with the seed(s) of your choice and it's perfectly fine. You could also repeat the process a few times and average all the AUC's.

Stata code and output

Once again the figures will appear when you run the code but are not displayed by Markdown.

1) Fitting the model, naive AUC and ROC

Clearly all covariates (age, oral and smoke) are important predictors of mi. A naive ROC curve can be obtained by computing the predicted probablity of MI for each observation in the dataset and calling the function roctab and using the option graph.

```
use infarct.dta
logistic mi oral age smoke, coef
predict fitted, pr
roctab mi fitted
roctab mi fitted, graph title("Naive ROC")
## . use infarct.. logistic mi oral age smoke, coef
##
```

```
Number of obs =
## Logistic regression
                                                                 200
##
                                                 LR chi2(3)
                                                             = 57.83
##
                                                 Prob > chi2
                                                             = 0.0000
## Log likelihood = -75.187408
                                                 Pseudo R2
                                                             = 0.2777
##
  ______
##
##
                                          P>|z|
                                                   [95% conf. interval]
          mi | Coefficient Std. err.
                                      Z
  ______
##
##
         oral |
                1.979896
                          .4696992
                                     4.22
                                          0.000
                                                   1.059302
                                                             2.900489
##
          age
                .1625556
                          .0445372
                                    3.65
                                          0.000
                                                   .0752643
                                                             .2498469
                          .4293955
##
        smoke
                1.812237
                                    4.22
                                          0.000
                                                   .9706372
                                                             2.653836
##
               -9.114046
                          1.757112
                                    -5.19
                                          0.000
                                                  -12.55792
                                                            -5.670169
        cons
##
##
##
  . predict fitted, pr
##
##
  . roctab mi fitted
##
                     R.O.C
##
                                         Asymptotic normal
##
                                        [95% conf. interval]
           Obs
                    area
                           Std. err.
##
##
           200
                  0.8403
                             0.0323
                                         0.77708
                                                   0.90356
##
  . roctab mi fitted, graph title("Naive ROC")
```

The naive AUC is 0.84, 95% CI=(0.78; 0.90), which can be classified as *good*. The model predicts well but this estimate is affected by optimism bias. The true AUC is probably a bit lower, how much lower, we are going to discover.

2) split sample AUC

An AUC free of optimism bias can be obtained using the split sample approach whereby the data is split in two, the model built on the training dataset and the AUC computed on the validation dataset

```
use infarct.dta
set seed 1001
gen val = runiform()<.5
** Derive a prediction model y-chd69 in the development cohort
logistic mi oral age smoke if val==0
** Generate a new variable containing the predicted probabilities
predict fitted, pr</pre>
```

```
** AUC on the development data (training)
** roctab mi fitted if val==0
** roctab mi fitted if val==0, graph name(graph0) title("training")
** AUC on the validation data - THE ONE WE NEED
roctab mi fitted if val==1
roctab mi fitted if val==1, graph name(graph1) title("validation")
## . use infarct.. set seed 1001
## . gen val = runiform()<.5</pre>
##
## . ** Derive a prediction model y-chd69 in the development cohort
## . logistic mi oral age smoke if val==0
##
                                                    Number of obs = 109
## Logistic regression
##
                                                    LR chi2(3) = 32.19
                                                    Prob > chi2 = 0.0000
##
## Log likelihood = -46.00784
                                                    Pseudo R2 = 0.2592
## ------
          mi | Odds ratio Std. err. z P>|z|
                                                     [95% conf. interval]
##
        oral | 11.62421 7.317309 3.90 0.000 3.384865 39.91952
       age | 1.089913 .0620405 1.51 0.130 .9748538 1.218553
smoke | 4.494196 2.405762 2.81 0.005 1.573983 12.83228
##
##
       _cons | .0015526 .0033645 -2.98 0.003 .0000222 .1085545
##
## Note: _cons estimates baseline odds.
## . ** Generate a new variable containing the predicted probabilities
## . predict fitted, pr
##
## .
## . ** AUC on the development data (training)
## . ** roctab mi fitted if val==0
## . ** roctab mi fitted if val==0, graph name(graph0) title("training")
## .
\#\# . ** AUC on the validation data - THE ONE WE NEED
## . roctab mi fitted if val==1
##
```

```
ROC
##
                                                    Asymptotic normal
##
              Obs
                                                   [95% conf. interval]
                         area
                                   Std. err.
##
##
                91
                       0.8101
                                     0.0554
                                                    0.70147
                                                                 0.91871
##
   . roctab mi fitted if val==1, graph name(graph1) title("validation")
##
##
##
```

The AUC is lower with a larger CI, i.e. AUC=0.81 with a wider 95% CI=(0.70; 0.92). You may get a different result if you used another the seed or did not specify it. Setting the seed allows you to reproduce your results. The naive AUC=84% was indeed optimistic. Note that this method is suboptimal and it shows here with a small sample, yielding a larger 95% CI,

3) cross-validated AUC

A better for to use the data is to perform cross-validation. Given the data is rather, you may run into trouble with 10-fold crossvalidation depending on the seed. In that case, you can either change the seed or even use a smaller number of groups (e.g. carry out 5-fold CV). I used seed=2002, which seems to be ok.

```
use infarct.dta
set seed 2002
xtile group = uniform(), nq(10)
quietly gen cvfitted = .
forvalues i = 1/10 {
    * Step 2: estimate model omitting each subset
    quietly xi: logistic mi oral age smoke if group !=`i'
    quietly predict cvfittedi, pr
    * Step 3: save cross-validated statistic for each omitted subset
    quietly replace cvfitted = cvfittedi if group==`i'
    quietly drop cvfittedi
    }
* Step 4: calculate cross-validated area under ROC curve
roctab mi cvfitted
roctab mi cvfitted, graph title("10-fold CV ROC")
## . use infarct.. set seed 2002
##
  . xtile group = uniform(), nq(10)
##
##
```

```
## . quietly gen cvfitted = .
##
##
  . forvalues i = 1/10 {
##
             * Step 2: estimate model omitting each subset
## .
## .
             quietly xi: logistic mi oral age smoke if group !=`i'
##
     3.
                quietly predict cvfittedi, pr
##
     4.
             * Step 3: save cross-validated statistic for each omitted subset
##
##
             quietly replace cvfitted = cvfittedi if group==`i'
                quietly drop cvfittedi
##
     5.
                }
##
     6.
##
##
   . * Step 4: calculate cross-validated area under ROC curve
   . roctab mi cvfitted
##
##
                          ROC
                                                   Asymptotic normal
                                                  [95% conf. interval]
##
              Obs
                         area
                                  Std. err.
##
##
              200
                      0.8110
                                    0.0357
                                                   0.74095
                                                               0.88103
##
  . roctab mi cvfitted, graph title("10-fold CV ROC")
```

The 10-fold cross-validated AUC is 0.81, 95%CI=(0.74; 0.88) with seed=2002. It's a bit lower than the naive AUC but not by much, This is indicative of a small optimism bias (a common finding in practice). A slightly larger 95% CI than the one found with the naive analysis is observed. This is however much better than the one obtained in 2). You may get different results with the seed(s) of your choice and it's perfectly fine. You could also repeat the process a few times and average all the AUC's.

Practice - calibration plot

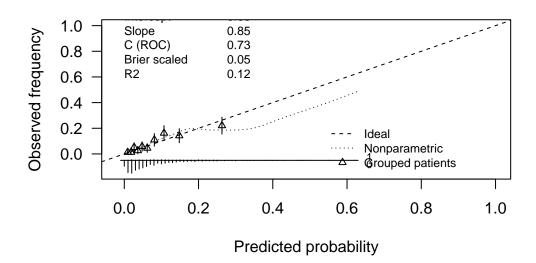
R code and output

1) Calibration plot for the final model (Table 5.18) without outlier in cholesterol. Use the split sample approach.

```
require(rms)
## Loading required package: rms
## Loading required package: Hmisc
##
```

```
## Attaching package: 'Hmisc'
## The following objects are masked from 'package:dplyr':
##
##
       src, summarize
## The following objects are masked from 'package:base':
##
##
       format.pval, units
wcgs <- read.csv("wcgs.csv")</pre>
wcgs<-data.frame(wcgs)</pre>
wcgs1=cbind(wcgs$age,wcgs$chol,wcgs$sbp,wcgs$bmi,wcgs$smoke,wcgs$dibpat,wcgs$chd69)
colnames(wcgs1)=c("age", "chol", "sbp", "bmi", "smoke", "dibpat", "chd69")
wcgs1=data.frame(wcgs1)
wcgs1=na.omit(wcgs1)
# remove outlier chol=645
wcgs1=wcgs1[wcgs1$chol <645,]</pre>
wcgs1$age_10<-(wcgs1$age-mean(wcgs1$age))/10
wcgs1$bmi_10<-(wcgs1$bmi-mean(wcgs1$bmi))/10</pre>
wcgs1$sbp_50<-(wcgs1$sbp-mean(wcgs1$sbp))/50</pre>
wcgs1$chol_50<-(wcgs1$chol-mean(wcgs1$chol,na.rm=T))/50</pre>
wcgs1$bmichol<-wcgs1$bmi_10*wcgs1$chol_50</pre>
wcgs1$bmisbp<-wcgs1$bmi_10*wcgs1$sbp_50
dim(wcgs1)
## [1] 3141 13
# out<-glm(chd69 ~ age_10 + chol_50 + sbp_50 + bmi_10 + smoke + dibpat + bmichol + bmisbp
# summary(out)
n=dim(wcgs1)[1]
set.seed(1001) # choose the same seed as in the notes
wcgs1$val=rbinom(n,1,0.5) # val =0 for training and val=1 for validation
table(wcgs1$val)
##
##
      0
## 1596 1545
# training dataset
wcgs1.dev=wcgs1[wcgs1$val==0,]
fit.dev<-glm(chd69 ~ age_10 + chol_50 + sbp_50 + bmi_10 + smoke + dibpat + bmichol + bmis
```

```
summary(fit.dev)
##
## Call:
## glm(formula = chd69 ~ age_10 + chol_50 + sbp_50 + bmi_10 + smoke +
      dibpat + bmichol + bmisbp, family = binomial, data = wcqs1.dev)
##
## Deviance Residuals:
     Min 1Q Median
                             3Q
                                     Max
## -1.2859 -0.4311 -0.2977 -0.1993 2.8899
##
## Coefficients:
            Estimate Std. Error z value Pr(>|z|)
##
                      0.2179 -15.960 < 2e-16 ***
## (Intercept) -3.4771
## age_10
             0.5830
                       0.1719 3.391 0.000697 ***
                      0.1127 6.317 2.67e-10 ***
## chol_50
              0.7121
             ## sbp_50
## bmi_10
             ## smoke
## dibpat
          ## bmichol
## bmisbp
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
      Null deviance: 881.60 on 1595 degrees of freedom
## Residual deviance: 769.12 on 1587 degrees of freedom
## AIC: 787.12
##
## Number of Fisher Scoring iterations: 6
# validation dataset
wcgs1.val=wcgs1[wcgs1$val==1,]
wcgs1.val$pred<- predict(fit.dev, wcgs1.val,type="response")</pre>
source("val.prob.ci.R")
val.prob.ci(wcgs1.val$pred,wcgs1.val$chd69, pl=T,smooth=T,logistic.cal=F,
          g=10)
```



```
##
                     C (ROC)
                                        R2
                                                       D
                                                             D:Chi-sq
            Dxy
  4.688013e-01 7.344007e-01 1.199755e-01 5.342483e-02 8.354136e+01 0.000000e+00
                                       U:p
##
                    U:Chi-sq
                                                       Q
                                                                Brier
                                                                         Intercept
## 4.244369e-04 2.655755e+00 2.650392e-01 5.300039e-02 7.305119e-02 6.225161e-02
##
          Slope
                        Emax Brier scaled
  8.487498e-01 8.825670e-02 5.205208e-02 1.498093e-02
#val.prob.ci(wcgs1.val$pred,wcgs1.val$chd69, pl=T,smooth=T,logistic.cal=F,
             g = 20)
```

2) Has the calibration plot improved compared with the simpler model?

The calibration plot still displays overestimation of CHD risk for the highest risk category. The plot may look different depending on the seed you used. This is somehow artificial due to the fact that we don't have new data to play with - see also 3).

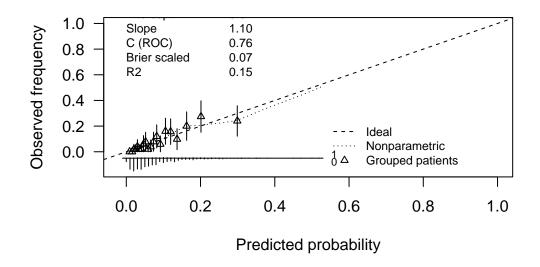
3) Repeat with 20 groups and 2/3 in the training dataset

Here we simply need to recreat val to have 2/3 of observations in the dataset and use g=20 when running val.prob.ci

```
n=dim(wcgs1)[1]
set.seed(1001) # choose the same seed as in the notes
```

```
wcgs1$val=rbinom(n,1,1/3) # val =0 for dvelopment and val=1 for validation
table(wcgs1$val)
##
##
    0
## 2129 1012
# development dataset
wcgs1.dev=wcgs1[wcgs1$val==0,]
fit.dev<-glm(chd69 ~ age_10 + chol_50 + sbp_50 + bmi_10 + smoke + dibpat + bmichol + bmis
summary(fit.dev)
##
## Call:
## glm(formula = chd69 ~ age_10 + chol_50 + sbp_50 + bmi_10 + smoke +
     dibpat + bmichol + bmisbp, family = binomial, data = wcgs1.dev)
## Deviance Residuals:
     Min
         1Q Median
                            3Q
                                  Max
## -1.1568 -0.4431 -0.3145 -0.2196
                                2.9405
##
## Coefficients:
##
           Estimate Std. Error z value Pr(>|z|)
## age 10
           0.61069 0.09528 6.409 1.46e-10 ***
## chol_50
## sbp_50
            ## bmi_10
           0.43660 0.17136 2.548 0.010838 *
## smoke
## dibpat
           0.33072 -2.598 0.009369 **
## bmichol
           -0.85931
## bmisbp
           -1.18985 0.75416 -1.578 0.114632
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##
     Null deviance: 1185.4 on 2128 degrees of freedom
## Residual deviance: 1059.2 on 2120 degrees of freedom
## AIC: 1077.2
##
## Number of Fisher Scoring iterations: 6
```

```
# validation dataset + ROC/AUC
wcgs1.val=wcgs1[wcgs1$val==1,]
wcgs1.val$pred<- predict(fit.dev, wcgs1.val,type="response")
source("val.prob.ci.R")
val.prob.ci(wcgs1.val$pred,wcgs1.val$chd69, pl=T,smooth=T,logistic.cal=F, g=20)</pre>
```



```
##
             Dxy
                        C (ROC)
                                            R2
                                                           D
                                                                   D:Chi-sq
    5.200286e-01
                  7.600143e-01
                                 1.517699e-01
                                                6.828102e-02
                                                               7.010040e+01
##
             D:p
                                                         U:p
##
                                     U:Chi-sq
##
    1.110223e-16 -1.481565e-03
                                 5.006565e-01
                                                7.785452e-01
                                                               6.976259e-02
##
           Brier
                      Intercept
                                         Slope
                                                        Emax
                                                               Brier scaled
##
    7.201299e-02
                 2.208180e-02
                                1.096972e+00
                                               6.160309e-02
                                                               7.389028e-02
##
            Eavg
    1.043200e-02
##
```

We see more points and more variability. Still some overestimation of the CHD risk for the highest category (although now the wider 95% CI now covers the corresponding point on the 45 degree line). We have not really fixed the problem with this more complex model. The plot

depends on the seed you chose here. In reality this uncertainty does not exist when carrying out external validation (which is normally the way to go). We use the the data at hand to build the model and the new external data to draw the calibration plot. No need of a seed at any stage. You can also notice that the plot gives the AUC (on the validation sample) albeit without the 95% CI.

Stata code and output

Once again the figures will appear when you run the code but are not displayed by Markdown.

1) Calibration plot for the final model (Table 5.18) without outlier in cholesterol. Use the split sample approach.

```
use wcgs.dta
summarize age
gen age10=(age-r(mean))/10
summarize bmi
gen bmi10=(bmi-r(mean))/10
summarize sbp
gen sbp50=(sbp-r(mean))/50
summarize chol
gen chol50=(chol-r(mean))/50
gen bmichol=bmi10*chol50
gen bmisbp=bmi10*sbp50
drop ih chol > 645
set seed 1001
# set.seed 1030
gen val = runiform()<.5
logistic chd69 age10 chol50 sbp50 bmi10 smoke dibpat bmichol bmisbp if val==0
predict proba, pr
pmcalplot proba chd69 if val==1, ci
** alternatively
drop if val==0
pmcalplot proba chd69, ci
## . use wcgs.. summarize age
##
##
                    0bs
                               Mean Std. dev. Min
      Variable
                                                               Max
## -----
                                                   39
##
          age | 3,154 46.27869 5.524045
                                                                59
##
## . gen age10=(age-r(mean))/10
```

```
##
  . summarize bmi
##
                        Obs
##
      Variable |
                                   Mean
                                           Std. dev.
                                                           Min
                                                                      Max
##
##
                      3,154
                               24.51837
           bmi
                                           2.567496
                                                     11.19061
                                                                 38.94737
##
  . gen bmi10=(bmi-r(mean))/10
##
##
  . summarize sbp
##
##
      Variable |
                        Obs
                                   Mean
                                           Std. dev.
                                                                      Max
## -----+-
##
                      3,154
                               128.6328
                                                            98
                                                                      230
           sbp |
                                          15.11773
##
  . gen sbp50=(sbp-r(mean))/50
##
##
  . summarize chol
##
##
      Variable |
                     Obs
                                   Mean
                                           Std. dev.
                                                                      Max
##
                     3,142
                               226.3724
                                           43.42043
##
                                                           103
                                                                      645
          chol |
##
## . gen chol50=(chol-r(mean))/50
## (12 missing values generated)
## . gen bmichol=bmi10*chol50
## (12 missing values generated)
##
## . gen bmisbp=bmi10*sbp50
##
## . drop ih chol > 645
## variable ih not found
## r(111);
##
## end of do-file
## r(111);
```

2) Has the calibration plot improved compared with the simpler model?

The calibration plot seems a bit better with this seed but it's also sensitive to the choice of seed. Try seed=1030, you will have a different looking plot, where the situation is the same

as before. This is somehow articial due to the fact that we don't have new data to play with - see also 3).

3) Repeat with 20 groups and 2/3 in the training dataset

```
use wcgs.dta
summarize age
gen age10=(age-r(mean))/10
summarize bmi
gen bmi10=(bmi-r(mean))/10
summarize sbp
gen sbp50=(sbp-r(mean))/50
summarize chol
gen chol50=(chol-r(mean))/50
gen bmichol=bmi10*chol50
gen bmisbp=bmi10*sbp50
drop if chol > 645
** set seed 1001
set seed 2002
** set seed 1030
gen val = runiform()<.33</pre>
logistic chd69 age10 chol50 sbp50 bmi10 smoke dibpat bmichol bmisbp if val==0
predict proba, pr
pmcalplot proba chd69 if val==1, ci bin(20)
** alternatively
drop if val==0
pmcalplot proba chd69, ci bin(20)
## . use wcgs.. summarize age
##
    Variable | Obs Mean Std. dev. Min
                                                        Max
## -----
                                              39
##
       age | 3,154 46.27869 5.524045
                                                        59
##
## . gen age10=(age-r(mean))/10
##
## . summarize bmi
##
     Variable | Obs
                            Mean Std. dev. Min
                                                        Max
## -----
         bmi | 3,154 24.51837 2.567496 11.19061 38.94737
##
##
```

```
## . gen bmi10=(bmi-r(mean))/10
##
## . summarize sbp
##
    Variable | Obs Mean Std. dev. Min Max
##
## -----
        sbp | 3,154 128.6328 15.11773 98
##
                                                        230
##
## . gen sbp50=(sbp-r(mean))/50
##
## . summarize chol
##
     Variable | Obs Mean Std. dev. Min Max
##
## -----
       chol | 3,142 226.3724 43.42043
##
                                              103
                                                       645
##
## . gen chol50=(chol-r(mean))/50
## (12 missing values generated)
## . gen bmichol=bmi10*chol50
## (12 missing values generated)
## . gen bmisbp=bmi10*sbp50
##
## . drop if chol > 645
## (12 observations deleted)
##
## .
## . ** set seed 1001
## . set seed 2002
##
## . ** set seed 1030
## . gen val = runiform()<.33</pre>
##
## . logistic chd69 age10 chol50 sbp50 bmi10 smoke dibpat bmichol bmisbp if val==0
## Logistic regression
                                              Number of obs = 2,094
                                              LR chi2(8) = 132.43
##
##
                                              Prob > chi2 = 0.0000
                                              Pseudo R2 = 0.1075
## Log likelihood = -549.87382
##
```

```
##
##
                                                        P>|z|
                                                                   [95% conf. interval]
           chd69
                   Odds ratio
                                  Std. err.
                                                  z
##
##
          age10 |
                      1.808118
                                  .2602319
                                                4.12
                                                        0.000
                                                                   1.363698
                                                                                2.397371
##
         chol50 |
                      1.757084
                                   .160149
                                                6.18
                                                        0.000
                                                                   1.469637
                                                                                2.100754
##
          sbp50 |
                      2.743119
                                  .6621937
                                                4.18
                                                        0.000
                                                                   1.709083
                                                                                4.402772
          bmi10 |
                      2.928239
                                                3.03
                                                        0.002
##
                                  1.038346
                                                                   1.461413
                                                                                5.867327
##
           smoke
                      1.944388
                                  .3258757
                                                3.97
                                                        0.000
                                                                   1.399985
                                                                                2.700491
##
         dibpat |
                      1.821471
                                  .3122496
                                                3.50
                                                        0.000
                                                                   1.301677
                                                                                2.548833
##
        bmichol |
                      .4433118
                                  .1251311
                                               -2.88
                                                        0.004
                                                                   .2549444
                                                                                .7708557
##
         bmisbp |
                      .2280157
                                  .1648987
                                               -2.04
                                                        0.041
                                                                   .0552566
                                                                                .9409036
##
                      .0363761
                                  .0064614
                                              -18.66
                                                        0.000
                                                                   .0256814
                                                                                .0515245
           _cons |
##
  Note: cons estimates baseline odds.
##
##
   . predict proba, pr
##
   . pmcalplot proba chd69 if val==1, ci bin(20)
   command pmcalplot is unrecognized
## r(199);
##
## end of do-file
## r(199);
```

We see more points and more variability. Still some overestimation of the CHD risk for the highest category (although now the wider 95% CI now covers the corresponding point on the 45 degree line). The plot depends on the seed you chose, see plot with seed 1001 or 1030 (pretty good). However, in reality, this uncertainty does not exist since typically external calibration is carried out. We use the data at hand to build the model and the new external data to draw the calibration plot. No need of a seed at any stage.