

Fair Assg 1

a) $\pi = \pi P$

$$\pi = [\pi(0) \pi(1) \dots \pi(j) \dots \pi(N)] = [\pi(0) \dots \pi(i) \pi(N)] \begin{bmatrix} \vdots \\ \vdots \\ \vdots \end{bmatrix}$$

\downarrow
 $\pi(j)$

$\leftarrow \begin{bmatrix} \pi(0) \rightarrow \boxed{\circ} \\ \pi(1) \rightarrow P_{1j} \\ \vdots \\ \pi(N) \rightarrow \boxed{\circ} \end{bmatrix} \sum_{i=0}^N \pi(i) P_{ij}$

$$\therefore \pi(j) = \sum_{i=0}^N \pi(i) P_{ij}$$

Just change vari. from i to j and j to i

$$\therefore \pi(i) = \sum_{j=0}^N \pi(j) P_{ji} = \sum_{j \neq i} \pi(j) P_{ji} + P_{ii} \pi(i)$$

$$\Rightarrow (1 - P_{ii}) \pi(i) = \sum_{j \neq i} \pi(j) P_{ji}$$

$$\Rightarrow \left(\sum_{j \neq i} P_{ij} \right) \pi(i) = \sum_{j \neq i} \pi(j) P_{ji}$$

flux out
(except one going out into itself i.e. self loop)

flux in
prob. of j (any other) to i (state considered) except one from itself (self loop).

b)

$$P_{x(x+1)} = 1 - \frac{x}{N}$$

$$P_{x(x-1)} = \frac{x}{N}$$

