

Power and Sample Size for Longitudinal Models in R – The longpower Package and Shiny App

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Abstract Longitudinal studies are ubiquitous in medical and clinical research. Sample size computations are critical to ensure that these studies are sufficiently powered to provide reliable and valid inference. There are several methodologies for calculating sample sizes for longitudinal studies that depend on many considerations including the study design features, outcome type and distribution, and proposed analytical methods. We briefly review the literature and describe sample size formulas for continuous longitudinal data. We then apply the methods using example studies comparing treatment versus control groups in randomized trials assessing treatment effect on clinical outcomes. We also introduce a Shiny app that we developed to assist researchers with obtaining required sample sizes for longitudinal studies by allowing users enter required pilot estimates. For Alzheimer's studies, the app can estimate required pilot parameters using data from the Alzheimer's Disease Neuroimaging Initiative (ADNI). Illustrative examples are used to demonstrate how the package and app can be used to generate sample size and power curves. The ease and flexibility in the use of the package and app can significantly aid researcher to optimally perform power analysis for Alzheimer's clinical trials and other research studies.

Introduction

Longitudinal designs are generally preferred over cross-sectional research designs as they provide richer data and greater statistical power. As such, many biomedical and medical studies employ longitudinal designs to study changes over time in outcomes at the individual, group, or population level. Early in the design of a longitudinal experimental or natural history study, it is imperative to ensure that the study is adequately powered for its aims. Inadequate sample sizes leads to invalid or inconclusive inference and squandered resources (??). On the other hand, oversampling squanders resources and exposes participants to unnecessary risks associated with the intervention (?). Thus, optimal sample size and power analysis have become an important prerequisite for any quantitative research design. Not only are these required during the design phase of research, but it has also become mandatory for ethical, scientific, or economic justification in submissions to institutional review boards and research funding agencies.

Determining the right sample size for a study is not a straightforward task. Despite the plethora of sample size formulas for repeated measures (????), cluster repeated measures (?), multivariate repeated measures (?), longitudinal research designs (?), the tasks of gathering pilot estimates of the necessary parameters and getting the right software to carry out the computation can be challenging. Researchers commonly rely on formulas for very basic cross-sectional studies and adjust for attrition and other longitudinal design effects. Although such approaches can yield appropriate approximations, the ideal approach is to use a formula derived directly from the longitudinal model that researchers plan to eventually use on the study data.

? describe practical methods for the selection of appropriate sample size for repeated measures addressing issues of missing data, and the inclusion of more than one covariate to control for differences in response at baseline. Sample size formulas are refined depending on the specific situation and design features. For example, ? considered a sample size for longitudinal designs comparing two groups that accounted for participant attrition or drop-out. ? derived sample size formulas for continuous longitudinal data with time-varying exposure variables typical of observational studies. Ignoring time-varying exposure was demonstrated to lead to substantial overestimation of the minimum required sample size which can be economically disadvantageous. In non-traditional longitudinal designs such as designs for mediation analysis of the longitudinal study, further refinements to sample size formulas are needed to ensure that sufficient sample sizes are obtained (?). However, these formulas usual require additional parameters such as exposure mean, variance, and intraclass correlations (?), mediation effect, number of repeated measures (?), covariance structures (?), non-linear trends (?), missing, attrition or dropout rates (??), among others. Advanced sample size methods simultaneously handle several practical issues associated with the research design and complications that may arise during data collection. However, such methods are only available in commercial software (??).

As the analysis model and associated sample size formula becomes more sophisticated, estimating the parameters required by the formula becomes more challenging. A major hurdle to overcome is

the availability of pilot data to inform these parameters. To assist Alzheimer's researchers with this challenge, we have developed a power and sample size shiny app for Alzheimer's clinical trials. The app implements formulas for the linear mixed-effects model and Mixed Model for Repeated Measures (MMRM) (?) allowing user to input their own pilot estimates, or allow the app to generate pilot estimates using data from the Alzheimer's Disease Neuroimaging Initiative (ADNI; ?).

Review of methods

Continuous outcomes in clinical trial data collected longitudinally over time are commonly analyzed using linear mixed models (?) or MMRM (??). Prior to such trials, it is necessary to estimate the required sample size for a given treatment effect with desired power and Type I error. Various sample size approaches for longitudinal data have been proposed. We review a few of the most commonly used methods applied in Alzheimer's disease trials with continuous outcomes.

Sample size computation based on the linear mixed-effects model

Several sample size approaches have been developed by different authors. ? proposed sample size formulas for two approaches to continuous longitudinal outcome, one that assumes a constant mean over time and compare the average response over time between groups, and another that assumes a linear change over time and compares the mean rate of change or slope difference between groups. Suppose that Y_{ij} is the response for participant i taken at time j . To compare the average response between two groups (e.g. group A receiving active treatment and group B receiving control) across time, consider the model

$$Y_{ij} = \beta_0 + \beta_1 T_i + \epsilon_{ij}$$

where T_i is treatment indicator which is coded 1 for participants in group A and 0 for participants in group B . The sample size required per group to detect an average response between the two groups, δ is given by

$$m = \frac{2(Z_{1-\alpha/2} + Z_{1-\beta})^2 \sigma^2 (1 + (n-1)\rho)}{n\delta^2}$$

where α is the type I error rate, $1 - \beta$ is the power and $\text{corr}(Y_{ij}, Y_{ik}) = \rho$ for all $j \neq k$.

To test difference in the slopes or average rate of change between the two groups, consider the parameterization:

$$Y_{ij} = \beta_{0A} + \beta_{1A} t_{ij} + \epsilon_{ij}, i = 1, 2, \dots, m; j = 1, 2, \dots, n.$$

A similar parameterization can be specified for group B with parameters β_{0B} , and β_{1B} representing the intercept and slope. The parameters β_{1B} and β_{1A} are the rate of change of the outcome for group A and B , respectively. Assume that $\text{var}(\epsilon_{ij}) = \sigma^2$ and $\text{corr}(Y_{ij}, Y_{ik}) = \rho$ for all $j \neq k$. If the outcome of each participant is measured at the same time, t_j , then the sample size per group needed to detect a difference in the rate of change for each group, $\delta = \beta_A - \beta_B$, is given by

$$m = \frac{2(Z_{1-\alpha/2} + Z_{1-\beta})^2 \sigma^2 (1 - \rho)}{ns_t^2 \delta^2}$$

where α is the type I error rate, $1 - \beta$ is the power and $s_t^2 = \frac{\sum(t_j - \bar{t})^2}{n}$ is the within-participant variance of t_j .

Another sample size computation approaches for correlated data is derived by ?. This approach derived sample size following the generalized estimating equation (?) approach. Thus, different outcomes types can be handled. A special case is for continuous response measured repeatedly over time and modeled using a linear model. Consider the model

$$Y_{ij} = \beta_0 + \beta_1 T_i + \epsilon_{ij}, i = 1, 2, \dots, N, j = 1, 2, \dots, n$$

where T_i is the treatment indicator, ϵ_{ij} is the error term assumed to follow a multivariate with a mean vector of zeros, $\mathbf{0}$ and covariance matrix, $\sigma^2 \mathbf{R}$, and \mathbf{R} is an $n \times n$ working correlation matrix. Different covariance structures such as independent, exchangeable, auto-regressive, and unstructured can be assumed. To estimate the total sample size required, N for a given significance level (α) and pre-specified nominal power ($1 - \beta$), the following formula is used:

$$N = \frac{(Z_{1-\alpha/2} + Z_{1-\beta})^2 \sigma^2}{\pi_0 \pi_1 (\beta_1^2 \mathbf{1R}^{-1} \mathbf{1})}$$

where π_0 and π_1 represents the proportion of observations in the control and treated group respectively. By assuming an exchangeable working correlation matrix, this formula reduces to

$$N = \frac{\left(Z_{1-\alpha/2} + Z_{1-\beta}\right)^2 \sigma^2 [1 + (n-1)\rho]}{\pi_0 \pi_1 \beta_1^2 n}.$$

It can be observed that for equal proportion of participants in each group i.e. $\pi_0 = \pi_1 = \frac{1}{2}$, the formula for the sample size per group is equivalent to the sample size formula for difference in average response between groups by ? above. An appealing aspect of ? approach is that it can allow for unequal allocation to the two groups, and different outcome types are considered.

Another approach is based on the linear mixed model analysis (?) comparing mean rate of change between groups (??). Consider the linear mixed model

$$Y_{ij} = X'_{ij}\beta + b_{0i} + b_{1i}t_{ij} + \epsilon_{ij}$$

where X_{ij} denotes a vector of indicator variables (treatment, time, and interaction terms), $b_i = (b_{0i}, b_{1i})' \sim N\left(\begin{pmatrix} 0 \\ 0 \end{pmatrix}, \begin{bmatrix} \sigma_{b_0}^2 & \sigma_{b_0, b_1} \\ \sigma_{b_0, b_1} & \sigma_{b_1}^2 \end{bmatrix}\right)$ are random participant-specific effects, and $\epsilon_{ij} \sim N(0, \sigma_e^2)$ are the residual errors. The random terms, b_i and ϵ_{ij} are assumed to be independent. Following this model specification, ? proposed a sample size formula per arm given by

$$\frac{N}{\text{arms}} = \frac{2 \left(Z_{1-\alpha/2} + Z_{1-\beta}\right)^2 \left[\sigma_{b_1}^2 + \frac{\sigma_e^2}{\sum(t_j - \bar{t})^2}\right]}{\Delta^2}$$

where t_i indexes the times at which measures are made assuming all participants are observed at the same time points, \bar{t} is the mean of the times, $\sigma_{b_1}^2$ is the variance of the participant-specific random slope, and Δ is the difference in mean rate of change in treatment versus control group to be detected. For a random-intercept mixed-effect model, the sample size formula reduces to

$$\frac{N}{\text{arms}} = \frac{2 \left(Z_{1-\alpha/2} + Z_{1-\beta}\right)^2 \left[\sigma_{b_1}^2 + \frac{\sigma_e^2}{\sum(t_j - \bar{t})^2}\right]}{\Delta^2}.$$

This sample size formula does not account for the correlation between the random intercept and slope, a limitation that can be mitigated by a recent approach by ?.

Sample size computation based on the mixed model for repeated measures (MMRM)

An alternative approach is to treat time as a categorical variable. This approach, common in trials of treatments of Alzheimer's and other therapeutic areas, is often referred to as the MMRM (???). The approach to fitting the MMRM is similar to that for other linear mixed-effect models for longitudinal or repeated measures except the unstructured modelling of time – treated as a categorical variable, and the specification of a within-participant correlation structure to account for association among the repeated measurements. The MMRM provides an estimate of the mean response for each time point category, for each group, and the resulting mean trajectory over time is unconstrained.

Suppose that Y_{ij} is the j th measurement taken of participant i ; $i = 1, 2, \dots, N$ at time, t_{ij} and T_i represents treatment or group indicator. Assuming we have two groups, $a; = (1, 2)$, let n_{aj} be the number of participants at time $j = 1, 2, \dots, J$ for group a . Thus, at time point 1, the total number of participants is $n_{11} + n_{21}$. The response variable is assumed to follow a multivariate normal with mean, variance-covariance and correlation matrix given respectively as

$$\begin{aligned} E(Y_{ij}|T_i = a) &= \mu_{aj} \\ \text{cov}(Y_{ij}, Y_{ik}|T_a = a) &= \sigma_{ajk} = \Sigma_a \\ \text{corr}(Y_{ij}, Y_{ik}|T_a = a) &= \frac{\sigma_{jk}}{\sigma_j \sigma_k} = R \end{aligned}$$

where $\sigma_j = \sigma_{jj}^{\frac{1}{2}}$. It is common to assume that the variance-covariance matrix is the same for each group in which case we can have $\Sigma_1 = \Sigma_2 = \Sigma$. Different correlation structures can be assumed (eg., compound symmetry, autoregressive and unstructured). The sample size formula for MMRM (?) can account for the attrition rate at each time point. Define the attrition rate $a_{aj} = 1 - r_{aj}$, where $r_{aj} = \frac{n_{aj}}{n_{a1}}$ is the retention rate at time point, j . The sample size for group A needed to achieve a power of $1 - \beta$ at

a significance level, α is given by

$$n_{11} = (\psi_1 + \lambda\psi_2)(Z_{1-\alpha/2} + Z_{1-\beta})^2 \frac{\sigma_J^2}{\delta_J}$$

where $\lambda = \frac{n_{11}}{n_{21}}$ is called the allocation ratio, δ_J is the effect size at the last time point, J , and ψ_a is the (J, J) th component of the variance inflation factor, I_a^{*-1} defined with respect to an estimation of the μ_{aj} for treatment group, a . Specifically, $\psi_a = [I_a^{*-1}]_{JJ}$ where

$$I_a^* = \sum_{j=1}^J (r_{a,j} - r_{a,j+1}) \begin{bmatrix} R_j^{-1} & 0_{j \times (J-j)} \\ 0_{(J-j) \times j} & 0_{(J-j) \times (J-j)} \end{bmatrix}$$

The total sample size at the first time point is therefore given by

$$n_{11} + n_{21} = (1 + \lambda^{-1})(\psi_1 + \lambda\psi_2)(Z_{1-\alpha/2} + Z_{1-\beta})^2 \frac{\sigma_J^2}{\delta_J}.$$

The ‘longpower’ package

The aforementioned sample size approaches have been implemented in an R package, longpower (?), which can be found on CRAN via the URL <https://cran.r-project.org/web/packages/longpower/index.html>. The package also contains functions which translate pilot mixed effect model parameters (e.g. random intercept and/or slope) into marginal model parameters so that the formulas of ? or ? or ? formula can be applied to produce sample size calculations for two sample longitudinal designs assuming known variance.

A Web-based App

The interactive shiny (?) web application available from the URL <https://atrihub.shinyapps.io/power/> is an interface to the longpower package developed to easily generate sample size and conduct power analysis for a longitudinal study design with two-group comparisons for a continuous outcome. The app similarly implements the sample size formula of ? and ?? using functions in the longpower package. A novel feature of the app is that it can generate required pilot estimates by sourcing data from the Alzheimer’s Disease Neuroimaging Initiative (ADNI).

Illustrations

Illustration of the power package

ADNI is a population-based longitudinal cohort study that follows study participants to collect data on their clinical, cognitive, imaging including MRI and PET images, genetic, and biochemical biomarkers. The study was designed to discover, optimize, standardize, and validate clinical trial measures and biomarkers that are used in AD clinical research. This multi-site longitudinal study runs at about 63 sites in the US and Canada and began in 2004. All the data generated from the ADNI study are entered into a data repository hosted at the Laboratory of Neuroimaging (LONI) at the University of Southern California, the LONI Image & Data Archive (IDA). The data can be freely accessed upon request. Apart from the many uses of the data for advancing knowledge for AD trial (?), this big data resource can be used to improve study design. Specifically, in this paper, the data is used to generate pilot estimates for the computation of sample size and power.

We consider an Alzheimer’s disease example using ADAS-Cog (?) pilot estimates from the ADNI database. Suppose that we want to compute the sample size required to detect an effect of 1.5 at the 5% level of significance and 80% power. The linear mixed model fit to ADNI data has an estimated variance of random slope for group A (placebo or control group) of 74, and a residual variance of 10. Assuming study visits at 0.00 0.25 0.50 0.75 1.00 1.25 1.50 years, the sample size using the ‘edland’ approach can be obtained by using the `edland.linear.power()` functions in the ‘longpower’ R package as follows.

```
> t = seq(0, 1.5, 0.25)
> edland.linear.power(delta=1.5, t=t, sig2.s = 24, sig2.e = 10, sig.level=0.05,
power = 0.80)
```

Zhao and Edland, in process

```
N = 414.6202
n = 207.3101, 207.3101
delta = 1.5
t = 0.00, 0.25, 0.50, 0.75, 1.00, 1.25, 1.50
p = 0, 0, 0, 0, 0, 0, 1
p_2 = 0, 0, 0, 0, 0, 0, 1
sig2.int = 0
sig.b0b1 = 0
sig2.s = 24
sig2.e = 10
sig2.int_2 = 0
sig.b0b1_2 = 0
sig2.s_2 = 24
sig2.e_2 = 10
sig.level = 0.05
power = 0.8
alternative = two.sided
```

NOTE: N is *total* sample size and n is sample size in *each* group

An alternative approach is to use `lmpower()` and specify the argument `method="edland"` in the following way.

```
> lmpower(delta=1.5, t=t, sig2.s = 24, sig2.e = 10, sig.level=0.05,
power = 0.80,method="edland")
```

Zhao and Edland, in process

```
N = 414.6202
n = 207.3101, 207.3101
delta = 1.5
t = 0.00, 0.25, 0.50, 0.75, 1.00, 1.25, 1.50
p = 0, 0, 0, 0, 0, 0, 1
p_2 = 0, 0, 0, 0, 0, 0, 1
sig2.int = 0
sig.b0b1 = 0
sig2.s = 24
sig2.e = 10
sig2.int_2 = 0
sig.b0b1_2 = 0
sig2.s_2 = 24
sig2.e_2 = 10
sig.level = 0.05
power = 0.8
alternative = two.sided
```

NOTE: N is *total* sample size and n is sample size in *each* group

The Diggle and Liu & Liang approaches can be applied with the `diggle.linear.power()` and `lui.liang.linear.power()` functions, respectively. The `lmpower()` functions can be used for either approach with the appropriate specification of the 'method' argument.

The second illustrative example is the hypothetical clinical trial discussed in ?. Suppose that we are interested in testing the effect of a new treatment in reducing blood pressure through a clinical trial. The investigator is interested in randomizing participants between a control and active treatment group to have equal size. Three visits are envisaged with assessments planned at years 0, 2, and 5. Thus, $n = 3$ and $s_x^2 = 4.22$. Assuming a type I error rate of 5%, power of 80% and smallest meaningful difference of 0.5 mmHg/year, we want to determine the number of participants needed for both treated and control groups for varying correlation (0.2, 0.5 and 0.8) and response variance (100, 200, 300).

```

> n <- 3
> t <- c(0,2,5)
> rho <- c(0.2, 0.5, 0.8)
> sigma2 <- c(100, 200, 300)
> tab = outer(rho, sigma2,
+             Vectorize(function(rho, sigma2){
+               ceiling(diggle.linear.power(
+                 delta=0.5,
+                 t=t,
+                 sigma2=sigma2,
+                 R=rho,
+                 alternative="one.sided",
+                 power = 0.80)$n[1]))))
> colnames(tab) = paste("sigma2 =", sigma2)
> rownames(tab) = paste("rho =", rho)
> tab
sigma2 = 100 sigma2 = 200 sigma2 = 300
rho = 0.2      313      625      938
rho = 0.5      196      391      586
rho = 0.8       79      157      235

```

The above codes reproduces the table on page 29 of ?. These results can also be reproduced using the method by ? difference in average response between groups as follows:

```

> u = list(u1 = rep(1,n), u2 = rep(0,n)) #a list of covariate vectors or
+   matrices associated with the parameter of interest
> v = list(v1 = rep(1,n), v2 = rep(1,n)) #a respective list of covariate
+   vectors or matrices associated with the nuisance parameter
> rho = c(0.2, 0.5, 0.8) #correlations
> delta = c(20, 30, 40, 50)/100
> tab = outer(rho, delta, Vectorize(function(rho, delta){
+   ceiling(liu.liang.linear.power(
+     delta=delta, u=u, v=v,
+     sigma2=1,
+     R=rho, alternative="one.sided",
+     power=0.80)$n[1]))))
> colnames(tab) = paste("delta =", delta)
> rownames(tab) = paste("rho =", rho)
> tab
delta = 0.2 delta = 0.3 delta = 0.4 delta = 0.5
rho = 0.2      145      65      37      24
rho = 0.5      207      92      52      33
rho = 0.8      268     120      67      43

```

The sample size formula for the MMRM approach is also implemented in the 'longpower' package's `mmrm()` function. To illustrate how this approach is implemented, consider a hypothetical example with a correlation matrix having 0.25 as off-diagonal entries (exchangeable), a retention vector (1, 0.90, 0.80, 0.70) and standard deviation of 1, for group A. Assuming these values to be the same for group B, then the sample size required to detect an effect size of 0.5 at 5% level of significance and 80% power is computed as follows:

```

> Ra <- matrix(0.25, nrow = 4, ncol = 4)
> diag(Ra) <- 1 #exchangeable correlation matrix for group A
> ra <- c(1, 0.90, 0.80, 0.70) #retention in group A
> sigmaa <- 1 #standard deviation for group A
> power.mmrn(Ra = Ra, ra = ra, sigmaa = sigmaa, delta = 0.5, power = 0.80)

Power for Mixed Model of Repeated Measures (Lu, Luo, & Chen, 2008)

n1 = 86.99175
n2 = 86.99175
retention1 = 1.0, 0.9, 0.8, 0.7
retention2 = 1.0, 0.9, 0.8, 0.7
delta = 0.5

```

```
sig.level = 0.05
power = 0.8
alternative = two.sided
```

Suppose allocation ratio is 2, then the function argument ‘lambda=2’ can be added.

Illustration of the Shiny web-App

We demonstrate how the App is used to perform power analysis by inputting user-specified values and a specific sample size approach. We make use of the values shown in Table ???. For the MMRM method, we specify the options assuming an exchangeable correlation structure.

Table 1: Input values

Parameter	LMM	MMRM
Start time	0	1
End time	1.5	4
Timestep	0.5	1
Type I error rate	0.05	0.05
Effect size	1.5	-
Estimate of variance of random intercept	55	-
Estimate of variance of random slope	22	-
Estimate of covariance of random intercept and slope	29	-
Estimate of the error variance	10	-
Standard deviation of observation in group A	-	1
Standard deviation of observation in group B	-	1
Exchangeable correlation	-	0.25
Allocation ratio	1	2

For the ADNI-based generator for pilot estimates, we select full range of values for some selected variables (See Figure ??).

App menus and contents

The app has three main menus on the sidebar. The first menu has two sub-menus which let the user perform power and sample size calculations based on the longitudinal design. The first submenu, the default, accepts user-specified inputs and generates a graphical output and summary of the inputs. In the ‘input’ box, as shown in Figure ??a, users are aided with the selection of their inputs through widgets such as select input, numerical input, slider input, and radio button to facilitate the user selection. The select input for ‘Analysis Type’ allows the user to select whether the user desires to determine power or sample size. Input parameters that are not applicable for a given selection or are not applicable for the selected sample size method are grayed out to enhance the user experience. For example, the allocation ratio input widget is grayed out when the ‘diggle’ and ‘liuliang’ procedures are selected. The ‘output’ box, shown in Figure ??b, displays a graph of power versus sample size, a note on the method for the sample size computation, and a summary of the selected inputs by the user. The second submenu enables the user to conduct power analysis based on the MMRM methodology. Widgets such as select inputs, slider inputs, numerical inputs, and radio buttons display the current values of the model parameter in the ‘input’ box (See Figure ??a). As the MMRM requires the specification of an association structure and a vector of the retention rates, the app display vectors, and matrix inputs widgets. The size of these widgets depends on users’ choice on the number of time points for the study. However, these widgets are not reactive, and therefore the user must use the “Update/Enter” action button when changes are made to the number of time points to update the vector and matrix input widgets. The corresponding graphical and summary outputs are reactively displayed within the ‘output’ box, immediately below the ‘input’ box (See Figure ??b).

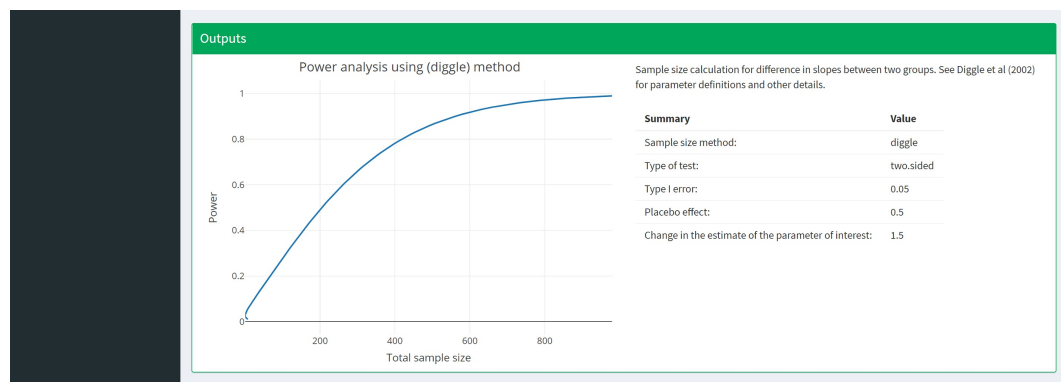
The second menu item also has two sub-menus for the linear mixed model and the mixed model repeated measures methods, respectively. In this menu, the app enables the user to generate pilot estimates from the Alzheimer’s Disease Neuroimaging Initiative (ADNI) data that is fed into the application to perform the power calculations.

In the box for ‘baseline selection’, the user can select variables that define their study population. By default, all variables are selected, utilizing all the data in the ADNI. A variable can be deselected

The screenshot shows the 'Inputs' section of the 'Power and Sample Size for Longitudinal Study' application. The interface includes a sidebar on the left with options like 'Power Analysis Based on Linear Mixed Model (LMM)', 'Power Analysis with ADNI-based pilot estimate generator', and 'About'. The main area contains several input fields and sliders:

- Analysis type:** A dropdown menu set to 'Sample size'.
- Sample size (n):** A slider ranging from 0 to 5,000, with a current value of 1,000.
- Power:** A slider ranging from 0 to 1, with a current value of 0.8.
- Start time (in years):** A text input field set to 0.
- End time (in years):** A text input field set to 1.5.
- Time step (in years):** A text input field set to 0.5.
- Type I error (sig.level):** A slider ranging from 0 to 1, with a current value of 0.05.
- Type of test:** Radio buttons for 'two.sided' (selected) and 'one.sided'.
- Estimate available:** Radio buttons for 'delta' (selected) and 'percent change'.
- Pilot estimate of the placebo change (beta):** A text input field set to 0.5.
- Percent change in the pilot estimate of the parameter of interest (pct.change):** A slider ranging from 0 to 1, with a current value of 0.5.
- Target treatment effect size (delta):** A text input field set to 1.5.
- Pilot estimate of variance of random intercept (sig2.i):** A text input field set to 55.
- Pilot estimate of variance of random slope (sig2.s):** A text input field set to 22.
- Pilot estimate of covariance of random slope and intercept (cov.s.i):** A text input field set to 29.
- Pilot estimate of residual variance (sig2.e):** A text input field set to 10.
- Method:** Radio buttons for 'diggle' (selected), 'liuliang', and 'edland'.
- Allocation ratio (lambda):** A slider ranging from 0 to 5, with a current value of 1.

(a) LMM Input window



(b) LMM Output window

Figure 1: User-specified MMRM windows

from the left side of the box with a click. After the user selection of the variable, the user can submit by clicking on the 'submit selected criteria' action button to activate the corresponding widgets in the next box. The 'Inclusion/exclusion criteria' box is made of a slider and select input widgets which allow the user to select a range of values for the selected population characteristics (See Figure ??). Baseline summaries are produced by the app according to the selections of the user. Summaries by gender, education, ethnicity and race are provided for the selected population. For continuous variables, the number of observations, number of missing observations, mean, median, lower and upper quantiles are displayed, while for categorical variables, the total and level-specific number of observations, and percentages are displayed. These bivariate summaries give the user a clear presentation of the data per the selected inclusion and exclusion criteria.

Next, the user can choose a primary outcome from among some that are commonly used for Alzheimer's disease studies. Pilot estimates are obtained from fitting a linear mixed model for the selected outcome for the power analysis. The estimates of the model can be adjusted with some user-selected covariate options. Data on the selected outcome from baseline to the selected number of years of the study are presented by individual-level and smooth mean profile plots. The app allows the selection of options for selecting the sample size method, type of test, type I error rate, percentage change, and allocation ratio as inputs for the power analysis (see Figure ??). Finally, the graphical output for the power analysis and summary of the inputs used are displayed in the 'output' box. The summary of the linear mixed model is also shown (see Figure ??).

The interface of the second sub-menu is very similar to the first except that the sample size methodology is based on the MMRM. Additionally, the model fitting options include specifying an association structure, allocation ratio, and percentage retention for the two groups.

The final menu on the sidebar is the 'About' menu, which provides brief information of the dashboard, data description and acknowledgment of the ADNI resources, packages used for developing

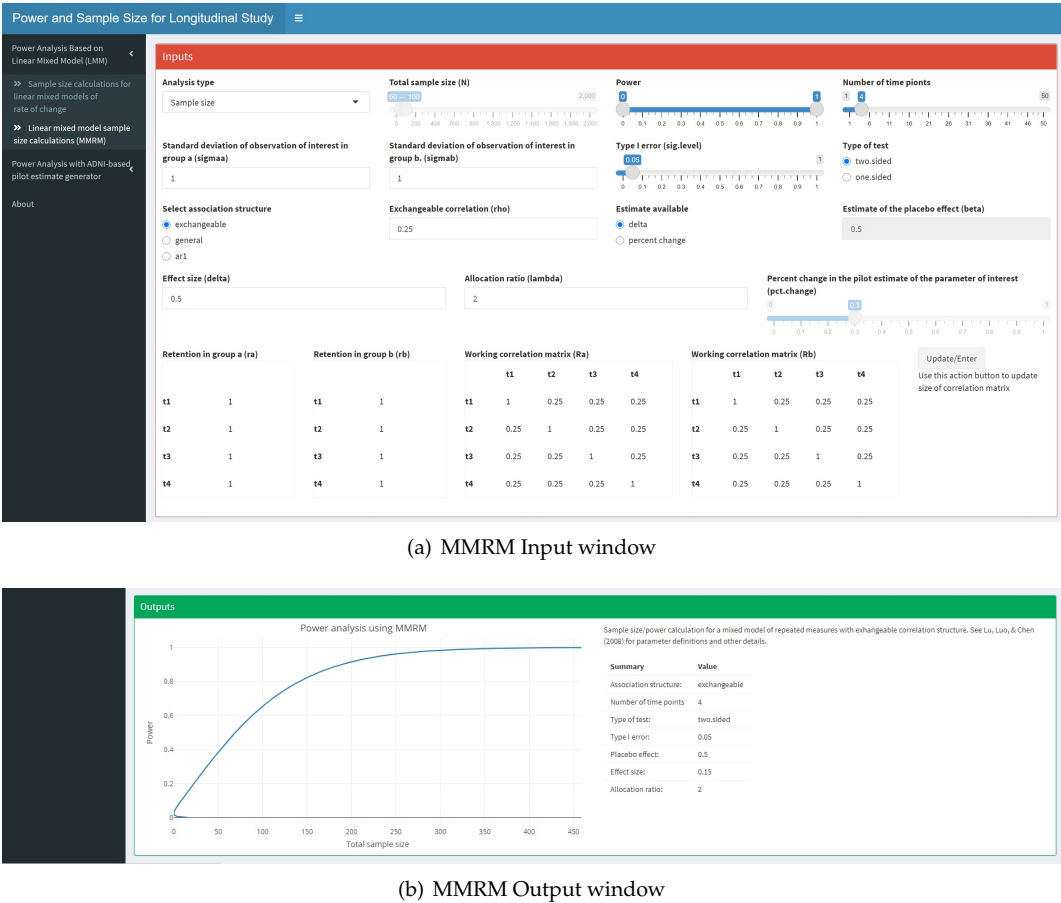


Figure 2: User-specified MMRM windows

the dashboard, and contact information of the developers of the dashboard.

Discussion

In this manuscript, we have presented the longpower R package, and a Shiny app dashboard that facilitatessample size and power analysis for a longitudinal study design with two-group comparisons of a continuous outcome. The app implements the sample size formulas of ?, ??, ? and ? using functions in the ‘longpower’ package. The package also handles models in which time is treated either as continuous (e.g. with random intercepts and slopes) or categorical (MMRM).

The longpower package was created to allow R users easy access to sample size formulas for longitudinal data that were already available in the literature. Many of the earlier papers on the topic provided no software, and so considerable effort was required by each reader to program implementations of the formulas. Collecting these formulas into an R package makes the methods more accessible and easy to compare. The package includes unit tests to ensure the software can adequately reproduce published results, and alternative approaches for the same study design are validated against each other.

A novel feature of the app is the ability to source pilot data for Alzheimer’s disease trials to generate required parameter estimates. We focus on Alzheimer’s data as our primary area of interest, but future work could bring in data from other disease areas. Other future directions include accommodating other outcome types, and keeping up with the evolving landscape of model parameterizations.

Acknowledgments

We are grateful to the ADNI study volunteers and their families. This work was supported by Biomarkers Across Neurodegenerative Disease (BAND-14-338179) grant from the Alzheimer’s As-sociation, Michael J. Fox Foundation, and Weston Brain Institute; and National Institute on Aging

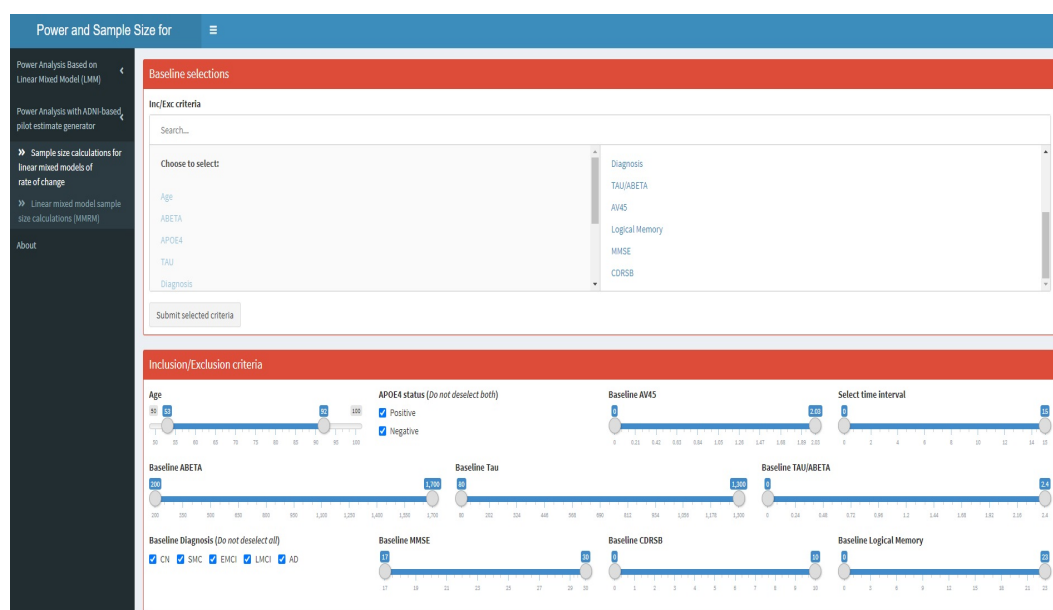


Figure 3: Range of baseline values

grant R01-AG049750. Data collection and sharing for this project was funded by the Alzheimer's Disease Neuroimaging Initiative (ADNI) (National Institutes of Health Grant U01 AG024904) and DOD ADNI (Department of Defense award number W81XWH-12-2-0012). ADNI is funded by the National Institute on Aging, the National Institute of Biomedical Imaging and Bioengineering, and through generous contributions from the following: AbbVie, Alzheimer's Association; Alzheimer's Drug Discovery Foundation; Araclon Biotech; BioClinica, Inc.; Biogen; Bristol-Myers Squibb Company; CereSpir, Inc.; Eisai Inc.; Elan Pharmaceuticals, Inc.; Eli Lilly and Company; EuroImmun; F. Hoffmann-La Roche Ltd and its affiliated company Genentech, Inc.; Fujirebio; GE Healthcare; IXICO Ltd.; Janssen Alzheimer Immunotherapy Research & Development, LLC.; Johnson & Johnson Pharmaceutical Research & Development LLC.; Lumosity; Lundbeck; Merck & Co., Inc.; Meso Scale Diagnostics, LLC.; NeuroRx Research; Neurotrack Technologies; Novartis Pharmaceuticals Corporation; Pfizer Inc.; Piramal Imaging; Servier; Takeda Pharmaceutical Company; and Transition Therapeutics. The Canadian Institutes of Health Research is providing funds to support ADNI clinical sites in Canada. Private sector contributions are facilitated by the Foundation for the National Institutes of Health (www.fnih.org). The grantee organization is the Northern California Institute for Research and Education, and the study is coordinated by the Alzheimer's Therapeutic Research Institute at the University of Southern California. ADNI data are disseminated by the Laboratory for Neuro Imaging at the University of Southern California. *Conflict of Interest:* None declared.

Summary

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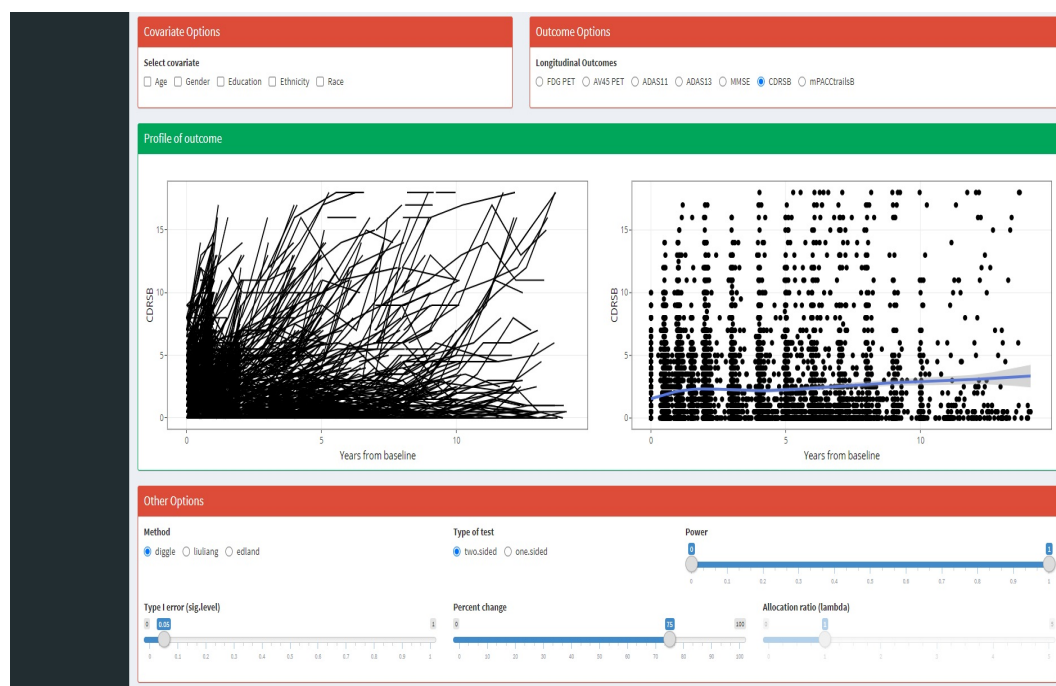


Figure 4: Input options and profiles of outcome

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Data used in preparation of this article were obtained from the Alzheimer's Disease Neuroimaging Initiative (ADNI) database (adni.loni.usc.edu). As such, the investigators within the ADNI contributed to the design and implementation of ADNI and/or provided data but did not participate in analysis or writing of this report. A complete listing of ADNI investigators can be found at: http://adni.loni.usc.edu/wp-content/uploads/how_to_apply/ADNI_Acknowledgement_List.pdf

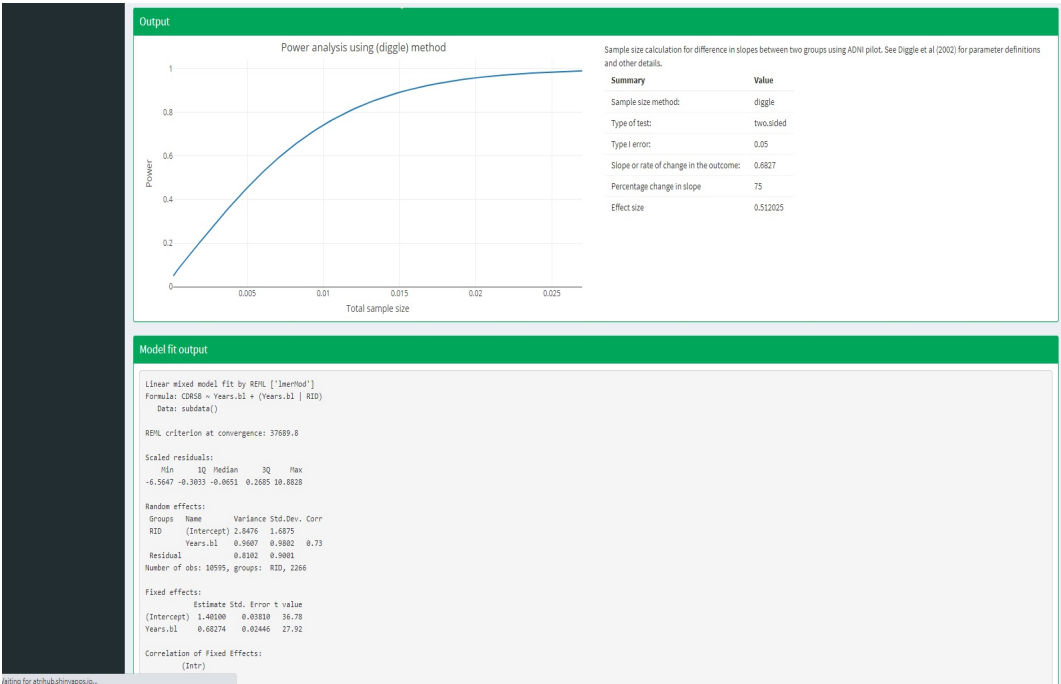


Figure 5: Output of power analysis and model fit for LMM

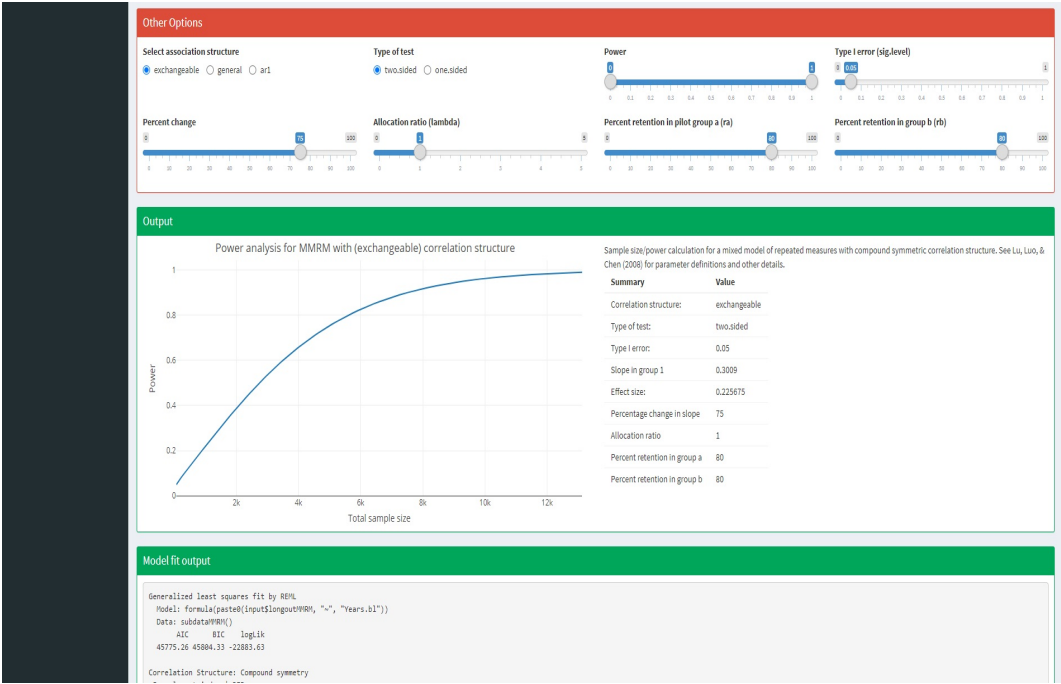


Figure 6: Some input options, output of power analysis and model fit for MMRM