

# (g)ROOT

## Language Reference Manual

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# 1 Intro

[Ocaml LRM](#)

## 1.1 How to read manual

The syntax of the language will be given in BNF-like notation. Non-terminal symbol will be in italic font *like-this*, square brackets [ ... ] denote optional components, curly braces { ... } denote zero or more repetitions of the enclosed component, and parenthesis ( ... ) denote a grouping.

## 2 Lexical Convention

### 2.1 Blanks

The following characters are considered as **blanks**: space, horizontal tab (`\t`), newline character (`\n`), and carriage return (`\r`).

Blanks separate adjacent identifiers, literals, expressions, and keywords. They are otherwise ignored.

### 2.2 Comments

Comments are introduced with two adjacent characters (`;` and terminated by two adjacent characters `;`). Nested comments are currently not allowed.

```
(; This is a comment. ;)
```

### 2.3 Identifiers

Identifiers are sequences of letters, digits, and underscore characters (`_`), starting with a letter. Letters consist of the 26 lowercase and 26 uppercase characters from the ASCII set.

$$\langle \textit{ident} \rangle ::= \textit{letter} \ ( \ \textit{letter} \ | \ \textit{digit} \ | \ \_ \ )$$
$$\langle \textit{letter} \rangle ::= \text{a} \dots \text{z} \ | \ \text{A} \dots \text{Z}$$
$$\langle \textit{digit} \rangle ::= 0 \dots 9$$

### 2.4 Integer Literals

An integer literal is a decimal, represented by a sequence of one or more digits, optionally preceded by a minus sign.

$$\langle \textit{integer-literal} \rangle ::= [-] \ \textit{digit} \ \{ \ \textit{digit} \ \}$$
$$\langle \textit{digit} \rangle ::= 0 \dots 9$$

### 2.5 Boolean Literals

Boolean literals are represented by two adjacent characters; the first is the octothorp character (`#`), and it is immediately followed by either the `t` or the `f` character.

$$\langle \textit{boolean-literal} \rangle ::= \# \ ( \ \text{t} \ | \ \text{f} \ )$$

## 2.6 Character Literals

Character literals are a single character enclosed by two ' (single-quote) characters.

## 2.7 Operators

All of the following operators are prefix characters or prefixed characters read as single token. Binary operators are expected to be followed by two expressions, unary operators are expected to be followed by one expression.

$\langle operator \rangle ::= ( unary - operator \mid binary - operator )$

$\langle unary-operator \rangle ::= !$

$\langle binary-operator \rangle ::= + \mid - \mid * \mid / \mid \text{mod}$   
 $\mid == \mid < \mid > \mid \leq \mid \geq \mid !=$   
 $\mid \&\& \mid ||$

## 2.8 Keywords

The below identifiers are reserved keywords and cannot be used otherwise:

if	val	let
leaf?	elm	tree
cld	sib	lambda

The following character sequence are also keywords:

==	+	&&	>	'
!=	-		mod	#t
<=	*	!	(	#f
>=	/	<	)	

## 3 Values

### 3.1 Base Values

#### 3.1.1 Integer numbers

Integer values are integer numbers in range from  $-2^{32}$  to  $2^{32} - 1$ , similar to LLVM's integers, and may support a wider range of integer values on other machines, such as  $-2^{64}$  to  $2^{64} - 1$  on a 64-bit machine.

#### 3.1.2 Boolean values

Booleans have two values. `#t` evaluates to the boolean value `true`, and `#f` evaluates to the boolean value `false`.

#### 3.1.3 Characters

Character values are 8-bit integers between 0 and 255, and follow ASCII standard.

### 3.2 Functions

Functional values are mappings from values to value.

### 3.3 Leaf

### 3.4 N-Ary Tree Compound Type

A core feature of (g)ROOT is its n-ary tree compound value type. Every tree value consists of three components: an element, it's right-immediate sibling, and it's first child. This allows for the convenient implementation of robust recursive algorithms with an arbitrary branching factor.

Every tree value in (g)ROOT may be either a full tree instance with an element, sibling, and child, or a leaf. The leaf value in (g)ROOT represents the nullary, or empty, tree.

The tree type in (g)ROOT is modeled after a left-child right-sibling binary tree, where each node contains a reference to its first child and reference to its next sibling. This allows each node in Groot to have any number of children, while constraining the maximum number of fields per tree instance to three (element, sibling, and child).

The tree type is very similar in usage to the one-dimensional list type present in many other functional languages, but enforces two additional invariants that empower programmers to shoot themselves in their feet less often.

1. The element of a tree instance may not be itself a tree. An element may be a value of any other type. This enforces a consistent structure among all trees that could be created in (g)ROOT.

**Note:** it is possible to circumvent this requirement by wrapping a tree instance in a no-args lambda closure. This is a reasonable means of achieving nested data structures as it prevents the accidental creation of nested values; programmers who wrap tree instances in lambda closures likely did not with intention

2. Every tree node must have a single immediate sibling and a single immediate child. This forces programmers to think in a purely recursive manner about their solutions.

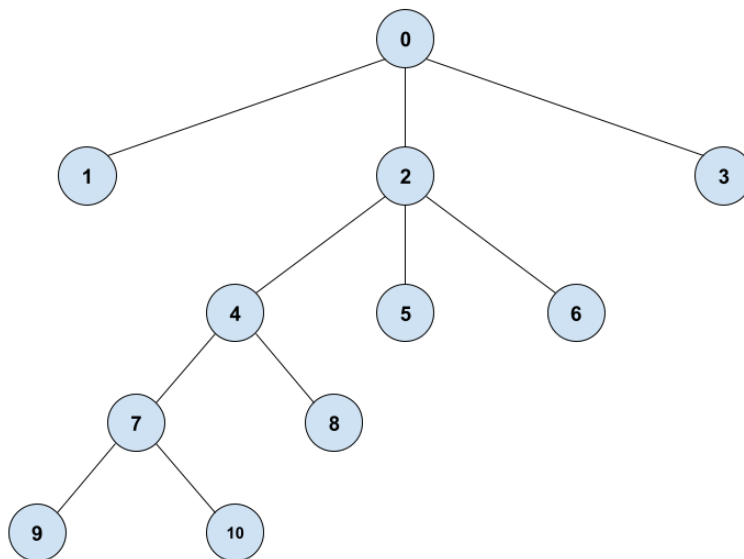
Trees may be conveniently constructed in-place using the following construction syntax:

```
'(value left-tree right-tree)
```

For example:

```
'(0 leaf (1 (2 (3 leaf leaf) (4 (5 (6 (leaf leaf)) leaf))) (7 (8 leaf leaf) (9 (10 leaf leaf) leaf))))
```

represents the following tree:



## 4 Names

### 4.1 Base Values

### 4.2 Functions

## 5 Constants

## 6 Expressions

$\langle expr \rangle$	$::=$	$literal$
		$ident$
		$unary-operator\ expr$
		$(\ binary-operator\ expr\ expr)$
		$(\ ident\ expr-list\ )$
		$(\ val\ ident\ expr\ )$
		$(\ let\ ident\ expr\ expr\ )$
		$(\ if\ expr\ expr\ expr\ )$
		$(\ lambda\ (\{arguments\})\ expr\ )$
$\langle literal \rangle$	$::=$	$integer-literal\  \ boolean-literal\  \ character\  \ leaf$
$\langle arguments \rangle$	$::=$	$\epsilon$
		$ident\ ::\ arguments$

### 6.1 Literals

### 6.2 Lambda Expression



## 7 Functions

### 7.1 Built-In Functions

**Note:** Throughout this section, the character pair “tr” is used as shorthand to represent a tree value, an identifier bound to a tree value.

There are four built-in functions which are integral to the tree data type:

1. **elm**

Usage: (**elm** tr)

Purpose: returns the element of the provided tree value (**tr**)

2. **sib**

Usage: (**sib** tr)

Purpose: returns the sinbling tree of the provided tree value (**tr**)

3. **cld**

Usage: (**cld** tr)

Purpose: returns the child tree of the provided tree value (**tr**)

4. **tree**

Usage: (**tree** ELEMENT SIBLING CHILD)

Purpose: constructs a tree value containing the value ELEMENT, with sibling SIBLING and child CHILD.

### 7.2 Standard Library Functions

**Note:** Throughout this section, the character pair “tr” is used as shorthand to represent a tree value, an identifier bound to a tree value.

The first set of function introduced in the standard library allow for programmers to use some of their beloved list functions present in other languages:

1. (**cons** a b)

Creates a 1-ary tree approximating the functionality of single-dimensional list in other functional languages.

2. (**car** tr)

Extracts the first value in the pair.

3. (**cdr** tr)

Extracts the second value in the pair.

4. `(null? tr)`

A predicate function that evaluates to true iff the pseudo-list is empty.

5. `(val nil leaf)`

A value `nil` that mirrors the built-in keyword `leaf`.

6. `(append xs ys)`

Append the list of elements in `ys` to the end of `xs`.

7. `(revapp xs ys)`

Append the list of elements in `ys` to the reverse of `xs`.

Now some useful tree functions!

1. `(graft oak fir)`

Appends a sibling tree `fir` to some other tree `oak`. The result of calling this function is a new tree in which `fir` is the rightmost sibling of `oak`. This function is extremely useful when re-shaping trees.

2. `(level-flatten tr)`

Flattens the provided tree to a 1-ary tree, arranging elements in level-order.

3. `(pre-flatten tr)`

Flattens the provided tree to a 1-ary tree, arranging elements in pre-order.

4. `(post-flatten tr)`

Flattens the provided tree to a 1-ary tree, arranging elements in post-order.

5. `(map f tr)` Maps a function `f` over every element of the provided tree `tr`.

6. `(filter p? tr)`

Constructs a new tree containing only elements that satisfy the predicate function `p?`, which must return a boolean value.

7. `(level-fold fn base tr)`

Folds a tree, visiting each element in a level-order traversal. Note that the accumulation function `fn` must take TWO arguments, the first of which is the current element, and second is the rest of the tree.

8. `(pre-fold fn base tr)`

Folds a tree, visiting each element in a pre-order traversal. Note that the accumulation function `fn` must take TWO arguments, the first of which is the current element, and second is the rest of the tree.

9. `(post-fold fn base tr)`

Folds a tree, visiting each element in a post-order traversal. Note that the accumulation function `fn` must take TWO arguments, the first of which is the current element, and second is the rest of the tree.

10. `(fold fn base tr)`

Folds a tree, in a more intuitively tree-like manner. Note that the accumulation function `fn` must take THREE arguments: the value of the current node, the sibling accumulator, and the child accumulator.

11. `(node-count tr)`

Evaluates to the number of nodes in the provided tree.

12. `(height tr)`

Evaluates to the height of the provided tree.

Higher-Order Functions:

1. `(curry f)`

Allows for the partial application of a two-argument function.

2. `(uncurry f)`

Uncurries a previously curried function such that both of its arguments must be provided at the same time.

3. `(o f g)`

Given two single-argument functions, returns a single function which is the composition of `f` and `g`.

4. `(flip f)`

Given a two argument function, reverses the order in which the arguments are evaluated and passed to the function.

5. `(flurry f)`

Given a two argument function, reverses the order in which the arguments are evaluated and passed to the function, and allows for the partial application of that function. This function both flips and curries `f` (hence the fun name).

## 8 Appendix

```
(*
 * We can define standard list functions with our tree
 * data type! Fun!
 *)
(define (cons a b) (tree a leaf (tree b leaf leaf)))
(define (car tr) (elm tr))
(define (cdr tr) (cld tr))
(define (nil ) leaf)
(define (null? tr) (leaf? tree))

;; a list function!
(define append (xs ys)
  (if (null? xs)
      ys
      (cons (car xs) (append (cdr xs) ys))
  )
)

;; another list function!
(define revapp (xs ys) ; (reverse xs) followed by ys
  (if (null? xs)
      ys
      (revapp (cdr xs) (cons (car xs) ys))
  )
)

;; appends a sibling tree (fir) to tree (oak)
(define (graft oak fir)
  (if (leaf? oak)
      fir
      (tree (elm oak) (graft (sib oak) fir) (cld oak))
  )
)

;; attempt 4
;; this function flattens a tree, level-order
(define (level-flatten tr)
  (if (leaf? tr)
      leaf
      (tree
        (elm tr)
        leaf
        (level-flatten (graft (sib tr) (cld tr)))
      )
  )
)
```

```

    )
  )
)

;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;
;;
;; flattening functions!
;;

;; this function flattens a tree, pre-order
(define (pre-flatten tr)
  (if (leaf? tr)
      leaf
      (tree
        (elm tr)
        leaf
        (pre-flatten (graft (cld tr) (sib tr)))
      )
  )
)

;; this function flattens a tree, post-order
(define (post-flatten tr)
  (if (leaf? tr)
      leaf
      (if (leaf? (cld tr))
          (tree
            (elm tr)
            leaf
            (post-flatten (sib tr)))
          (post-flatten (graft
                        (graft
                          (cld tr)
                          (tree (elm tr) leaf leaf))
                        (sib tr))
          )
      )
  )
)

;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;
;;
;; Let's create some higher order functions! Yay!
;;

(define (curry f) (lambda (x) (lambda (y) (f x y))))

```

```

(define (uncurry f) (lambda (x y) ((f x) y)))
(define (o      f g) (lambda (x) (f (g x))))
(define (flip  f)  (lambda (x) (lambda (y) (f y x))))

;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;
;;
;; function: (flurry func)
;;
;; precondition:
;;   func is a function that takes exactly two args
;;
;; evaluation:
;;   evaluates to a curried form of func, where:
;;     1) the first value passed to the curried function
;;        is treated as the second argument to (func)
;;     2) the second value passed to the curried function
;;        is treated as the first argument to (func)
;;
;; note:
;;   flurry is a contraction of "flip & curry",
;;   and I'm very proud of the wordplay there
;;
;;

(define flurry (func)
  (curry (lambda (a b) (func b a)))
)

;;
;; mapping function!
;;
(define (map f tr)
  (if (leaf? tr)
      leaf
      (tree
        (f (elm tr))
        (map f (sib tr))
        (map f (cld tr))
      )
  )
)

;;
;; filter function!
;;

```

```

(define filter (p? tr)
  (if (leaf? tr)
      leaf
      (if (p? (elm tr))
          (tree (elm tr) (filter p? (sib tr)) (filter p? (cld tr)))
          (filter p? (graft (cld tr) (sib tr)))
      )
  )
)

;;
;; folding functions!
;;

;; attempt 4
;; this function folds a tree, level-order
(define (level-fold fn base tr)
  (if (leaf? tr)
      base
      (fn
        (elm tr)
        (level-fold (graft (sib tr) (cld tr)))
      )
  )
)

;; this function folds a tree, pre-order
(define (pre-fold fn base tr)
  (if (leaf? tr)
      base
      (fn
        (elm tr)
        (pre-fold (graft (cld tr) (sib tr)))
      )
  )
)

;; this function folds a tree, post-order
(define (post-fold fn base tr)
  (if (leaf? tr)
      base
      (if (leaf? (cld tr))
          (fn (elm tr) (post-fold (sib tr)))
          (post-fold (graft
                        (graft (cld tr) (tree (elm tr) leaf leaf))

```

```

                                (sib tr)
                            )
                        )
                    )
                )
            )

;; once we implement first-class functions, we
;; should find that the behaviors of these three
;; functions are exactly equivalent to their
;; lower-class cousins
(define (level-fold-flatten tr) (level-fold cons nil tr))
(define (pre-fold-flatten tr) (pre-fold cons nil tr))
(define (post-fold-flatten tr) (post-fold cons nil tr))

;; this function folds a tree, in a more intuitively
;; tree-like manner
;; fn must take in three params:
;;   - the current value
;;   - the sibling accumulator
;;   - the child accumulator
(define (fold fn base tr)
  (if (leaf? tr)
      base
      (fn
        (elm tr)
        (fold fn base (sib tr))
        (fold fn base (cld tr))
      )
  )
)

;;
;; some more fun folding functions!
;;
(define (node-count tr)
  (pre-fold (lambda (elem count) (+ 1 count)) 0 tr)
)

;; this uses the tree fold to calculate the height!
(define (height tr)
  (fold
    (lambda (elem clds sibs) (+ 1 (max clds sibs)))
    0 tr
  )
)

```



```
(define (height-no-fold tr)
  (if (leaf? tr)
      0
      (max (height (sib tr))
            (+ 1 (height (cld tr)))
           )
  )
)
```