Create a Python class named FourierSeriesExpansion that performs the following tasks:

- ullet \_\_init\_\_ method should take a mathematical sympy function f(x) and an interval [a,b] as input parameters.
- Implement a method called calculate\_fourier\_series that uses sympy 's fourier\_series function to compute the Fourier series expansion of the function on the specified interval. The method should allow the user to specify the number of terms to which the series should be truncated.
- Implement another method called plot\_function\_and\_series that uses the matplotlib library to plot both the original function f(x) and its Fourier series expansion.
- Use  $f(x) = x^2 \sin(x)$  and [a, b] = [-1, 1] as a test function and interval respectively.

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In [ ]: import sympy as sp
        import numpy as np
        import matplotlib.pyplot as plt
        class FourierSeriesExpansion:
            def __init__(self, f, a, b):
                self.f = f
                self.a = a
                self.b = b
                self.x = sp.symbols("x")
            def calculate fourier series(self, n terms):
                fourier series = sp.fourier series(self.f, (self.x, self.a, self.b)).truncate
                    n=n terms
                return fourier series
            def plot function and series(self, n terms):
                fourier_series = self.calculate_fourier_series(n_terms)
                x vals = np.linspace(self.a, self.b, 400)
                f lambda = sp.lambdify(self.x, self.f, ["numpy", "sympy"])
                series lambda = sp.lambdify(self.x, fourier series, ["numpy", "sympy"])
                fig = plt.figure(figsize=(10, 6))
                plt.plot(x vals, f lambda(x vals), label="Original Function", color="blue")
                plt.plot(
                    x vals,
                    series_lambda(x_vals),
                    label=f"Fourier Series (n={n terms})",
                    color="red",
                    linestyle="--",
                plt.title("Function and its Fourier Series Expansion")
                plt.xlabel("x")
                plt.ylabel("f(x)")
                plt.legend()
                plt.grid()
                plt.show()
                plt.close(fig)
        x = sp.symbols("x")
        f = x**2 * sp.sin(x)
        a = -1
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b = 1
fourier_expansion = FourierSeriesExpansion(f, a, b)
fourier_expansion.plot_function_and_series(n_terms=22)
```