Examples: Find domain and range of the following functions:

a)
$$f(x) = \frac{1}{x-2}$$
 b) $f(x) = \frac{1}{2x+1}$

Solution: a) Given that

$$f(x) = \frac{1}{x-3}$$

f(x) gives real values for all real values of x except x = 3

$$D_f = \mathbb{R} - \{3\}$$

Again,
$$y = f(x) = \frac{1}{x-3}$$

$$\Rightarrow x - 3 = \frac{1}{y}$$

$$\Rightarrow x = \frac{1}{y} + 3$$

x gives real values for all real values of y except 0.

$$R_f = \mathbb{R} - \{0\}$$

b) Given that

$$f(x) = \frac{1}{2x+1}$$

Here f(x) is not defined for 2x + 1 = 0 or $x = -\frac{1}{2}$ and f(x) gives real values for all real values of x except $x = -\frac{1}{2}$.

$$D_f = \mathbb{R} - \{-\frac{1}{2}\}$$

Again,
$$y = f(x) = \frac{1}{2x+1}$$

$$\Rightarrow 2x + 1 = \frac{1}{y}$$

$$\Rightarrow x = \frac{1}{2} \left(\frac{1}{y} - 1 \right)$$

x gives real values for all real values of y except y = 0.

$$R_f = \mathbb{R} - \{0\}$$