|  |
| --- |
| Finite Element-based Software-in-the-Loop for Offline Post-processing and Real-time Simulations  Atta Oveisi[[1]](#footnote-1)\*1a, T. Arriessa Sukhairi1 and Tamara Nestorović1b  *1Mechanics of Adaptive Systems, Institute of Computational Engineering, Ruhr-Universität Bochum,*  *Universitätsstr. 150, 44801 Bochum, Germany.*  *(Received*  *keep as blank , Revised*  *keep as blank ,* *Accepted*  *keep as blank )9pt* |
| **Abstract.** In this paper, we introduce a new framework for running the finite element (FE) packages inside an online Loop together with MATLAB. Contrary to the Hardware-in-the-Loop techniques (HiL), in the proposed Software-in-the-Loop framework (SiL), the FE package represents a simulation platform replicating the real system which can be out of access due to several strategic reasons, e.g., costs and accessibility. Practically, SiL for sophisticated structural design and multi-physical simulations provides a platform for preliminary tests before prototyping and mass production. This feature may reduce the new product’s costs significantly and may add several flexibilities in implementing different instruments with the goal of shortlisting the most cost-effective ones before moving to real-time experiments for the civil and mechanical systems. The proposed SiL interconnection is not limited to ABAQUS as long as the host FE package is capable of executing user-defined commands in FORTRAN language. The focal point of this research is on using the compiled FORTRAN subroutine as a messenger between ABAQUS/CAE kernel and MATLAB Engine. In order to show the generality of the proposed scheme, the limitations of the available SiL schemes in the literature are addressed in this paper. Additionally, all technical details for establishing the connection between FEM and MATLAB are provided for the interested reader. Finally, two numerical sub-problems are defined for offline and online post-processing, i.e., offline optimization and closed-loop system performance analysis in control theory.  **Keywords:** software-in-the-loop; finite element; optimal placement; structural optimization; vibration control. |

**1. Introduction**

Intertwining with the passive behavior of the mechanical and civil structures towards smart structures and systems is a desirable feature that intrigues various researchers from separate fields of material science, civil/mechanical engineering, and instrumentation development. However, multi-domain nature of such case studies requires a suitable framework for the modeling of the system, physical analysis of the problem, and post-processing of the generated (input/output) data. For the physical analysis of the mechanical structures and the structural control as two case studies with predefined geometry and model properties, the finite element method (FEM) is an operational modeling technique. Leaving out the system identification techniques for now, the superiority of FEM as a modeling approach is due to the fact that the analytical/semi-analytical solutions for coupled systems are mostly limited to simple geometries. In order to put the FE model in a computationally affordable form with a limited number of dynamical states, a post-processing step is defined including a model reduction in terms of modal coordinates. This in turns makes the design/analyses tractable especially if the optimization or control of the structure is desirable.

In this paper, a new Software-in-the-Loop scheme (SiL) is constructed to address two families of problems: 1) the post-processing analyses of the solutions obtained from the FE package which may be used as a batch optimization tool or may be used for nonlinear modeling and uncertainty quantification. 2) To investigate the effects of the feedback loop in the time-domain analysis with application in control theory and online parameter optimization. The SiL presented in this paper is not limited to any particular physical domain and can be used for dynamics and vibration, structural health monitoring, fluid mechanics, thermoelastic analysis, and electro-/magneto-domains. As long as the problem under study can be defined in a step module (see (Puri, 2011; Nestorović and others, 2012)) of the commercial FE package of ABAQUS, it can be categorized as one of the applications of this paper. The italic terms here and after refer to the standard commands, e.g. step, in ABAQUS GUI. As another advantage of this scheme in comparison to those available in the literature ((Ray and others, 2000; Karagülle and others, 2004; Xu and Koko, 2004; Rahman and Alam, 2012; Gao and others, 2013; Bertagne and Hartl, 2014; Orszulik and Gabbert, 2016)), MATLAB toolboxes for robust control, global optimizations, neural networks, and fuzzy systems are accessible in the SiL which significantly increases the applicability of the method to general engineering problems. In this regards, the proposed technique is a candidate for non-parametric modeling of continuous nonlinear multi-domain structures with complex geometries where the real system is not accessible for measurements (Kerschen and others, 2006; Noël and Kerschen, 2017). Moreover, the proposed SiL can be used for the modeling of common benchmark problems in structural dynamics as a test platform for new control and optimization methods before moving to real-time measurements (Landau and others, 2013). Concerning the computation time, time-variability of the analysis, and the validation and verification of the proposed approach, detailed investigations are carried out.

Because the SiL approach is computationally demanding, it is not recommended for problems with simple geometries. Accordingly, analytical solutions or the methods that include system/parameter identification, model reduction in combination with offline design are recommended to be employed instead. However, for multi-physics problems without analytical models, systems with complicated geometries, benchmark problems where the real-time setup is out of access, and industrial problems where FE solutions are trusted, the presented method is an alternative to the field tests which are costly. ABAQUS is nominated over other packages as the dynamic simulator of the SiL configuration due to its capabilities in compiling FORTRAN subroutines. However, the proposed scheme can be applied to other commercial packages such as NASTRAN as long as the software provides a pool for including external commands.

The smart structural design based on the general FE approach is previously studied in the literature. For instance, Lim et al. (Lim and others, 1999) used 3D finite elements for modeling a multi-input-multi-output (MIMO) smart plate with discrete piezo-patches and designed an optimal controller on the reduced-order model by solving the algebraic Riccati equation (ARE). The performance of the designed controller for the vibration suppression of the clamped plate is presented for both the steady state and the transient cases. Ray et al. in a similar problem to the sub-problem (b) of this paper, used a FORTRAN subroutine to implement sensitivity enhancing control (SEC) for damaged smart beam (Ray and others, 2000). Karagülle et al. used ANSYS to integrate a PID control action into the solution of FE (Karagülle and others, 2004). Similar results are reported by (Xu and Koko, 2004). Following the same trend, Rahman and Alam compared their experimental active vibration control (AVC) of a cantilever beam based on PID controller with ABAQUS using 1D Finite element formulation (Rahman and Alam, 2012). Recently, Gao et al. used ABAQUS UAMP subroutine to include an active controller in the model of an aircraft’s vertical fin under dramatic buffet loads. They included a finite element model of macro fiber composite (MFC) actuators in ABAQUS implicit. The results are matched with those obtained from the experimental implementation of the controller on the prototype of the fin (Gao and others, 2013). The main limitations of implementing the control algorithm in SiL using standard ABAQUS scripting is the challenges that are introduced for matrix computations such as solving ARE for the optimal controller synthesis. The platform for ABAQUS coding is an application programming interface (API) that is realized per Python object-oriented language, and Python is not a well-established language for control algorithms (Bertagne and Hartl, 2014). This problem is also addressed in this paper as a solution to sub-problem (b). More recently, Orszulik and Gabbert presented an attractive interface for establishing a connection between the Simulink and ABAQUS for active vibration control of a cantilever beam (Orszulik and Gabbert, 2016; Gabbert and others, 2017).

The investigation of the passive structural vibration suppression is also carried out in the literature similar to sub-problem (a). Vel and Baillargeon utilized translational mass damper (TMD) in their physical system modeled in ABAQUS to evaluate the performance of a passive system (Vel and Baillargeon, 2004). Most recently, Shakeri and Younesian (Shakeri and Younesian, 2016) used multi-TMD (MTMD) in ABAQUS as well as in their analytical solution to examine the steady-state and transient acoustic radiation characteristics of the clamped-free annular plate. It should be indicated that the proposed methods in this paper are by no means limited to the structural optimization and structural vibration control, however, the applications of different SiL schemes in the literature are mostly concentrated on AVC (Omidi and others, 2015; Oveisi and Nestorović, 2016; Oveisi and others, 2016). Henceforth, the authors are mostly attentive in developing a new mechanism for uncertainty quantification in mechanical structures with complex geometries that can be used as an alternative to conventional methods (Soize, 2005). Uncertainty quantification regarding the unmodeled dynamics of high order nature is classically dealt with as a lumped stable bounded time-varying functions. In terms of controller synthesis (classical robust methods), such a view leads to conservative results. However, analytical modeling of simpler geometries under large vibration amplitudes hands the structure of uncertainty e.g. quadratic or cubic terms (Omidi and Mahmoodi, 2015; Stojanović, 2015; Oveisi and Nestorović, 2017). Next, by use of the parametric identification methods on the data obtained from the approaches that provide time-dependent responses of the nonlinear system (such as the SiL proposed in this paper) make an efficient tool for nonlinear system identification. This grey-box parameter identification approach as the center of intensive research in the identification community (see for instance (Paduart and others, 2010; Noël and Schoukens, 2017)) can be viewed as an alternative to some of the nonlinear system identification techniques based on discrete modeling of continuous mechanical structures reported in (Noël and Kerschen, 2017). Such a nonlinear nominal model can be later used for model-based controller synthesis in contrast to robust control methods which operate based on worst-case analysis. One should note that at the current stage in the literature, the lumped structural uncertainty quantification is obtained based on statistical analyses of an enormous number of experimental setups which is mostly limited because of the costs and difficulties regarding providing multiple identical systems (Adhikari and others, 2009).

Finally, the structure of the paper is as follows: First, two numerical problems are briefly introduced and immediately after, the methodology of coupling ABAQUS and MATLAB is broken into two variants in accordance with these two numerical problems: 1) the coupling in which time-independent simulations are intended s. t. the post-processing through MATLAB only starts when the ABAQUS *jobs* are completed. For this purpose, Python scripting in ABAQUS is used to alter the model variables on the grounds of the decision made in a MATLAB m-file. In other words, if the resubmission of the *jobs* is required on a revised model, the input file of ABAQUS is altered by the MATLAB text editor. This method is already employed in the literature and is reported here for the sake of completeness (Kim and others, 1995; Ramesh Kumar and Narayanan, 2008). 2) The coupling of MATLAB/ABAQUS for designing systems within some time-dependent loops. For this purpose, the first coupling scheme is completely revised by employing the user-defined FORTRAN subroutines. To make the algorithm ready-to-use, the details of developing the required script are included, and the possible issues are carefully addressed. Finally, the multi-physics piezo-laminated structures in the aforementioned sub-problems are explained in more details.

Before moving to the methodology section in order to make the paper more readable, a brief description of the two numerical problems in association with two coupling schemes are presented as follows:

1. A constrained optimization problem without time- and frequency-dependence: The actuator and sensor placement optimization problem is investigated for a piezolaminated cylindrical panel shown in Fig. 1a. The structure is partitioned ten times in both of longitudinal and tangential directions of the cylindrical coordinate and as a result divided into one hundred sections. Each partition represents a candidate for the actuator/sensor placement as shown in this figure. The reason for selecting the optimal sensor and actuator positioning problem as the realization of the ABAQUS/MATLAB offline coupling scheme is due its relevance to sub-problem (b). Accordingly, the result of actuator/sensor placement reflect that the process of smart structure design including piezo-material selection, input/output (IO) optimization, and closed-loop tests can all fall into the application of this paper. The technical details of the performance requirements are deferred to section 3.
2. As an illustration of the second ABAQUS/MATLAB coupling scheme proposed in this paper, where a time-dependent loop is required, sub-problem (b) is defined. To this end, a regulation problem is investigated for AVC. In order to realize the feedback control as shown in Fig. 1b, methodology in section 2.2 is proposed. To keep the numerical example tractable an output feedback linear quadratic Gaussian (LQG) controller is synthesized on the nominal model of the system. The details of obtaining the reduced-order model are explained in sections 3.1.1 and 3.1.2.

**2. Methodology**

*2.1 Offline post-processing coupling scheme*

The process of optimal actuator/sensor positioning is defined in terms of the first coupling scheme. In this regards, the coupled ABAQUS/MATLAB automatically changes the actuator/sensor locations on the model in order to evaluate an objective function. In a more general view, when the ABAQUS-user submits a command in the graphic user interface (GUI) of CAE, Python script is generated/updated and then, passed through the interpreter and sent to the kernel.

|  |  |
| --- | --- |
| **(a)** |  |
| **(b)** |  |
|  | Fig. 1(a) Geometry of the simulation example. (b) The schematic definition of the sub-problem (b) |

A record of such actions in the form of a replay file “.rpy” is kept by ABAQUS. Additionally, a list of commands that are executed in GUI of ABAQUS/CAE is available in the journal file “.jnl” in the working directory. This journal file is the primary platform for scripting in Python and solving the sub-problem (a) in this paper. For offline post-processing, Python plays the role of a messenger to realize the alternations in ABAQUS model such as moving the actuator/sensor parts. In other words, the offline loop can be constructed by using MATLAB to change the numerical values of ABAQUS model in the “.py” file followed by resubmitting the list of ABAQUS *jobs*. Finally, the offline post-processing is carried out by inspecting the “.odb” file of the results produced by ABAQUS. If the design criteria are satisfied for the objective function, the loop is terminated. Otherwise, MATLAB continues to manipulate the “.py” file containing the model parameters and resubmits the *job* from the command line till the termination condition is met. The interconnection between MATLAB and ABAQUS in this form is presented in Fig. 2.

|  |
| --- |
|  |
| Fig. 2 Workflow of the program for sub-problem (a) |

*2.2 Coupling scheme with time-dependent loop*

In the second coupling scheme, a SiL is outlined that uses Python and FORTRAN as two messengers between the ABAQUS Kernel and MATLAB engine. For this purpose, the Python script is used to define the model geometry/material and model interactions e.g. boundary conditions, while the time-dependent external loads are realized by FORTRAN UAMP subroutine. Sensor elements (later referred to as SENUi) are defined on measurable physical variables e.g. electric potential in piezo-sensor of Fig. 1b in sub-problem (b) with the predefined frequency of data extraction from a particular nodal set in *history* output (seti) by using the command: \*Output, history, sensor, name=SENUi, frequency \*Node Output, nset=seti. All the terminologies here and after in Courier New font represent the commands used in Python and their syntax. Moreover, the time-varying amplitude of the user-defined load is generated by the command: \*Amplitude, name, definition=USER, variables. At this set of monitored points (seti) the solution-dependent data are extracted from the active elements. For instance, in the sub-problem (b), seti represents the nodal group on the top surface of piezo-actuator having the same applied electric potential.

UAMP subroutine determines the value of an amplitude in a time-dependent manner. This dependence is defined in terms of a function that takes the sensor values and current time increment for controlling the amplitude of a stimulus in *load* module of ABAQUS/CAE (see Fig. 1b). Since all information passed to the subroutine are updated at each time increment, ABAQUS is set to stall and waits for an update on previous value. In this stage, user-defined solution-dependent state variables (sensor values) are needed to be sent to MATLAB engine. This action requires a C compiler which takes the value, calls the MATLAB engine to open, executes a function (in an m-file), brings back the updated amplitude, closes the MATLAB engine, and finally waits for a recall. “Engine applications” are standalone C programs that permit the user to call MATLAB from another environment and then use it as the computation machine. These standalone programs in the proposed SiL framework are called within UAMP subroutine. The C compiler is therefore responsible for the Engine applications while the FORTRAN compiler handles UAMP. Moreover, the input array in MATLAB block of Fig. 1b is passed from engine application to UAMP subroutine and vice versa. For this purpose, ENGOPEN routine calls MATLAB computational engine, MXCREATEDOUBLEMATRIX creates an array, and MXCREATEDOUBLESCALAR creates a scalar double. All the routines in Consolas font here and after represent the commands in the FORTRAN subroutine. MXDESTROYARRAY is used to deallocate the memory occupied by the specified array, MXGETPR sets the pointer to the first component of the real data, MXCOPYREAL8TOPTR copies real values from the FORTRAN array into the MATLAB matrix. Furthermore, ENGPUTVARIABLE is employed to write an array to the MATLAB engine and assign a variable name for that array, while ENGEVALSTRING evaluates the expression contained in string for the engine session started by ENGOPEN, ENGGETVARIABLE reads the array from the engine session. Finally, MXCOPYPTRTOREAL8 is used to copy real values from the MATLAB array into the FORTRAN array, and ENGCLOSE routine terminates the current MATLAB session. This interconnection is presented in the flowchart of Fig. 3. In order to provide the technical details for the interested reader while maintaining the readability of the paper, the coupling script is separated from the problem definition/simulations and moved to the Appendix 1.

|  |
| --- |
|  |
| Fig. 3 ABAQUS kernel and MATLAB engine simulation workflow |

**3. Problem definition**

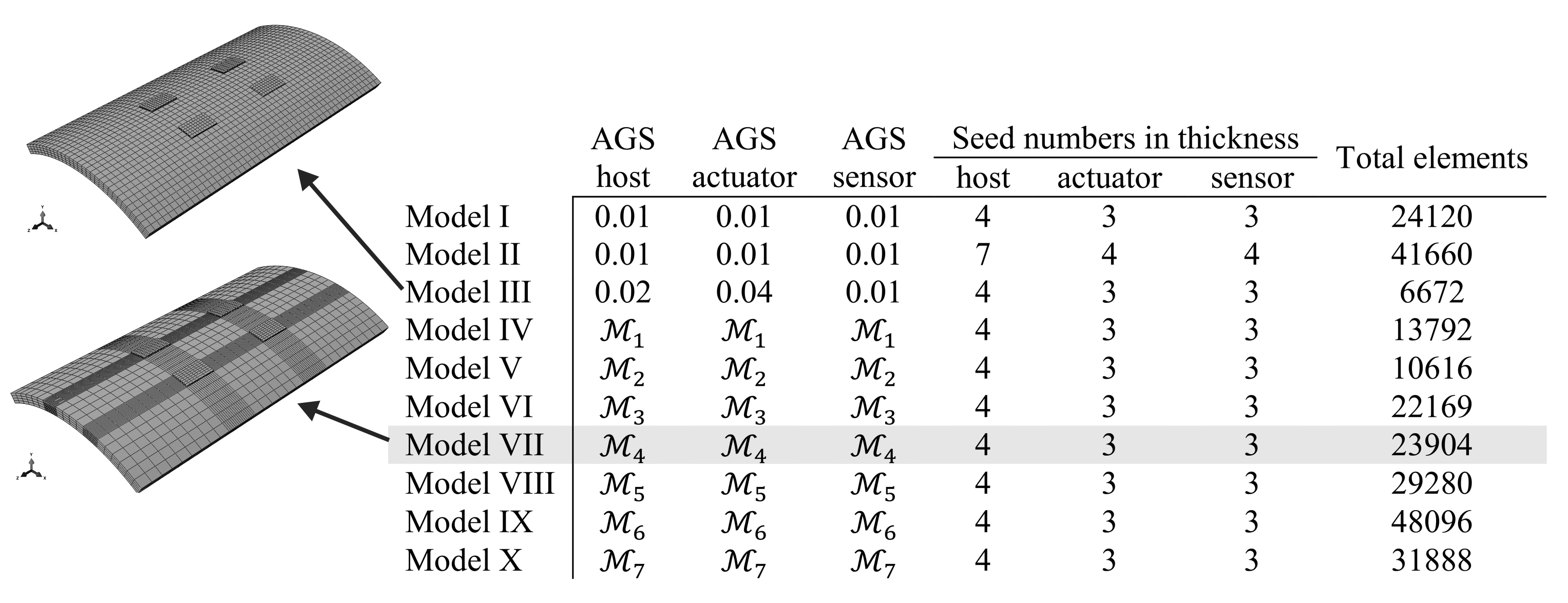
*3.1 Sub-problem (a): offline optimization*

In the first sub-problem, the cylindrical panel shown in Fig. 1a is used as the geometry of the structure. The main reason for selecting such a geometry is that: 1) Defining additional circular cylindrical coordinate system for the *material orientation* in orthotropic or anisotropic cases is required which makes the problem more general. 2) Non-conventional *assembly* and *interaction* constraints are required in sequential structure optimization. In this regards, each placement configuration includes the assembly of the piezo-sensor/-actuator patches with the host structure within a set of predefined partitions shown in Fig. 1a. 3) As pointed out later in the paper, the closed-loop investigations reflect more realistic issues which express the importance of the proposed coupling scheme in representing the real-time tests. While the piezo-patches are moved over these partitions on the host panel, the optimality of the smart structure is evaluated in terms of an objective function. At each simulation iteration, the next placement candidate (a partition of the structure geometry) is automatically selected by manipulating the parameters of the input file of ABAQUS from MATLAB. This procedure is controlled by selecting that specific partition to have two *tie* constraints for the actuator and sensor patches. The numerical implementation is carried out by finding a point inside a loop that defines the coordinates of the mid-point of the partition in cylindrical coordinate. Then, the calculated coordinates of the mid-point are stored in “.py” file (see Fig. 2). It is obvious that additional spatial constraints are needed to be automatically defined in the *assembly* module by using the *translate instance* command based on coinciding the corners of the partition of the host layer with the corners of the patches[[2]](#footnote-2).

*3.1.1 Mesh convergence and state space modeling*

It is assumed that the host structure has the mid-plain radius of , the thickness of , the length of , and arc angle of . Additionally, the piezo-patches are assumed to have the thickness of . The host structure is made of single layer orthotropic steel with density of , while the actuator and sensor are fabricated from PZT4 and , respectively. Elasticity matrix of the host, actuator, and sensor as well as the piezoelectric and dielectric matrices of the patches are presented in Appendix 2. It is also assumed that the host structure is perfectly bonded with the patches using the *tie* constraint by setting the lower surface of the piezo-actuator as the master surface and the upper surface of the sensor as the slave surface in relation to the bonding surface of the host. With a *tie* constraint, although the meshes on the master and slave surfaces may be dissimilar, the two tied regions are fused together. The master surface (actuator to the host and host to the sensor) is the surface that may penetrate into the slave and as a result the mesh on slave media is finer. For modeling the host structure and piezo-actuator/sensor, linear Hexahedral 8-node brick and 8-nodal piezoelectric brick elements are used, respectively. In addition, to minimize the computational burden without losing accuracy for sub-problem (a), mesh convergence analyses (MCAs) are carried out for two sets of mesh configurations: i) analyses for controlling the dimensionless approximate global size (AGS) of the elements ii) analyses for the seed size (local mesh refinement) in the radial, tangential, and longitudinal directions of the panel. Two series of investigations were performed: 1) Those with the finer mesh for the whole structure. 2) Analyses with some mesh modification at the location of the piezo-actuator/sensor. Accordingly, ten models for the piezolaminated structure are generated as shown in Table 1. In this table, , represent modifications in model in order to refine mesh on the paired master/slave surfaces of the *tie* constraints. These modifications can be understood by comparing Model III and Model VII in Table 1. A list of several modifications that are compared in MCAs of this paper are presented in Table 2. The subsequent standard mesh convergence procedure shows Model VII as the correct model.

Table 1 Mesh configuration in host structure, piezo-actuator, and piezo-sensor media



Following (Gawronski, 2004) and by appropriate selection of the modal coordinates (Nestorovic and others, 2015), the reduced order dynamical equation of motion for each actuator/sensor pair can be written as Eq. (1a, b). Equations (1a) and (1b) represent the ordinary differential equation of motion in state space form

|  |  |
| --- | --- |
|  | (1a) |

where,

|  |  |
| --- | --- |
| , , . | (1b) |

with , in which , , and are the modal mass, stiffness matrices, damping ratio associated with mode number , and the total number of mode-shapes considered in the modeling process, respectively. Additionally, , , and are the state, input, and output vectors, respectively while , , and are the state, control input, and output matrices, correspondingly. and are the modal coupling matrices of the piezo-actuator/-sensor, respectively. Finally, symbolizes the set of all real numbers.

Table 2 Mesh modification configuration (A: Actuator, H: Host, S: Sensor)

|  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- |
|  |  |  |  |  |  |  |  |  |
|  | AGS host | 0.04 | 0.04 | 0.04 | 0.03 | 0.02 | 0.01 | 0.04 |
| Actuator | # elements in | 6 | 5 | 8 | 8 | 8 | 8 | 10 |
| # elements in | 6 | 5 | 8 | 8 | 8 | 8 | 10 |
| Host | # elements in | 12 | 10 | 16 | 16 | 16 | 16 | 20 |
| # elements in | 12 | 10 | 16 | 16 | 16 | 16 | 20 |
| Sensor | # elements in | 24 | 20 | 32 | 32 | 32 | 32 | 40 |
| # elements in | 24 | 20 | 32 | 32 | 32 | 32 | 40 |

Technically, the state space model in Eq. (1a) is created by using the modal electrical potential coupling matrices which are calculated in ABAQUS/CAE and extracted by Python script using session.writeFieldReport command (Puri, 2011). The automatic process of constructing Eq. (1a) for all actuator/sensor configurations is carried out by reading this Python file in MATLAB for each placement scenario. Then, MATLAB program assigns new locations to the patches as the new decision variables. The m-file automatically and sequentially submits the analysis by: mo='noGUI'; system(['abaqus cae ',mo,'=MainFileAnalysis.py']);. In which MainFileAnalysis includes all definitions from the Python file for *geometry*, *assembly*, *interactions*, *mesh*, and *job* modules. The termination command should be activated accordingly.

This sub-problem is a candidate of all other case studies as long as the offline optimization process is intended in the solution method. Therefore, applicable and reliable resolutions for optimal structural design which is a demanding task in early development phases of a new product can be carried out in a similar manner as sub-problem (a). This makes it possible to test the feasibility and effectiveness in advance, before a prototype is available.

*3.1.2 Actuator/senor placement objective*

The optimal placement of the actuator/sensor on the structure both in collocated and non-collocated configurations falls into the offline iterative post-processing scheme of Fig 2. Optimal placement for plate and panel structures was investigated previously in (Jae-Hung Han and In Lee, 1999; Bruant and others, 2010; Nestorovic and others, 2015; Hasheminejad and Oveisi, 2016) based on genetic algorithm (GA). Kumar and Narayanan (Ramesh Kumar and Narayanan, 2007) have applied their LQR controller based criteria to find optimal location of piezoelectric actuators/sensors in vibration control of plates using GA. In the paper by Peng et al. (Peng, 2005), the maximization of the controllability Gramian in combination with GA was used as the criterion for optimal placement of a clamped plate. A similar approach with modal controllability and observability Gramians and GA was also employed by Sadri et al. (Sadri and others, 1999, 2002). In this paper, the objective function is defined in terms of norm of input to output gains (Nestorović and Trajkov, 2013). Accordingly, the approximate -norm of the transfer function from each actuator to the sensor for mode number is calculated as Eq. (2) (Gawronski, 2004).

|  |  |
| --- | --- |
|  | (2) |

where are the Hankel singular values and are referred to as the half power frequencies. Additionally, the elements of and in Eq. (2) represent the values associated with the physical variables, e.g., electric potential at actuator and sensor nodes for each mode shape, respectively (see (Nestorović and Trajkov, 2013)). Using the additive property of in mode number for a set of actuator () and sensor () elements, Eq. (3) can be written.

|  |  |
| --- | --- |
|  | (3) |

where and are number of actuators and sensors, respectively. All of the results in multiple modes should be then normalized by and the normalized results are gathered in a matrix ().

|  |  |
| --- | --- |
|  | (4) |

Based on Eqs. (2)-(4) similar concept can be defined by norm . Then, by describing and similar to Eq. (4), the optimization function for multi-modal case is calculated as and for case as . The objective function based on these norm-valued scalars is defined similar to (Nestorović and Trajkov, 2013). The authors are aware of the other objective functions existing in the literature such as including a measure of unmodeled dynamics for spillover effect, simultaneous optimization of actuator/sensor placement and control system, etc. but the main thrust of this paper is to present the possibility of using an independent SiL framework which can realize various objectives as well. This goal is evaluated here by using a reasonably simple objective function for testing offline efficiency of the configuration in section 2.1.

*3.1.3 Sub-problem (a): Simulation results*

For the simulation example shown in Fig. 1b, neglecting the symmetricity of the structure, in the case of single-input single-output (SISO), 10000 possible configurations (collocated & non-collocated) are available in the discrete solution space. The fulfillment of optimality criteria is thus not restricted to a narrow set of predefined solution space and it relies on verifying a symmetrical portion of all candidates. For the sake of brevity in the single mode analyses, the optimization results in Fig. 4 are presented for two mode-shapes only: i) mode-shapes number two and four for actuator location. ii) mode-shapes number three and five for sensor location. Placement indices for various configurations are separately depicted based on Eqs. (2)-(4) for actuator/sensor elements. Each sub-plot in actuator placement is presented together with the modal strain contour plot associated with that mode. Locations with higher placement indices for both sensor and actuator specify the priority of them in the selection process of the final configuration. As it can be seen the best actuator locations are in agreement with the maximum strain values. On the other hand, for sensor placement, the modal Mises stress indicates the best location which is justified by the material behavior of piezo/PVDF elements. The forms of the placement curves for other mode-shapes are qualitatively similar as their modal parameters and for the sake of briefness are omitted in Fig. 4.

Next, based on and the feasibility of the proposed method in finding the optimal configuration in the case of multiple simultaneous eigenmodes consideration is presented in Fig. 5. For the sake of briefness, the multiple modes results are reported for two cases: i) Considering four simultaneous fundamental natural frequencies. ii) Considering nine fundamental natural frequencies. As it can be observed in Fig. 5, the results for and objective functions are not identical. The reason for having such a difference is the form of placement indices and , respectively.

|  |
| --- |
|  |
| Fig. 4 Objective function for single mode placement |

For the first case a weighted summation of the objective functions for each mode is affecting the placement index and for latter, only the maximum input-output (IO) gain for that location determines the multi-modal objective. In physical sense, the placement strategy provides an energy efficient configuration which results in models with correspondingly controllable and observable retained modes. However, the index sets the constraint for maximum amplitude of the transfer function and as a result the highest control authority can be achieved.

**Remark 1.** The numerical example in this subsection covers a broad spectrum in structural optimization which may not primarily be limited to the electrical potential in active elements of smart structures but systems with some integrated universal transducers, whose effect may be reflected by forces, moments, magnetic field, temperature, etc.

For the parallel actuator/sensor placement, the results of the evaluation of the objective matrices based on Eq. (3), are presented only for the -norm scheme in Fig. 6. By overlaying the contour plots of the modal strain and the Misses stress as the physical controlling variables of the placement index, it can be observed that unlike beam and plate structures, the optimal actuator and sensor may appear in non-identical places. This emphasizes the importance of using multiple-modal objectives, since the transient behavior of the system in general depends on a large number of the eigenmodes. Additionally, unlike lower mode numbers where the changes of the placement index are gradual, in higher mode-shapes, drastic changes may appear.

Finally, the results of the - and -norm schemes are compared for multiple-modal consideration case in Fig. 7. Accordingly, two sets of analyses are carried out for actuator/sensor pairs with collocated and non-collocated configurations. In order to emphasize the effect of placement in the parallel modal consideration, the analyses are performed for several modal combinations and two of them are presented: i)Including mode-shapes one through five, ii) Including mode-shapes one through ten.

The observations are as follows: 1) - norm scheme tends to keep the optimal location in the same trend as the number of included mode-shapes are increasing. This behavior can be observed by comparing two subplots for non-collocated configurations based on the inclusion of five and ten eigenmodes of system.

|  |
| --- |
|  |
| Fig. 5 Multi-modal optimization results for & |

Such a tendency is due to the fact that -based algorithm has a memory that takes into account the effect of all of the eigenmodes. One advantage of the method is then the globality of the optimal solution. However, since for real applications, not all of the frequencies are equally involved in final response of the system, this method is conservative. To overcome this drawback, a separate frequency-domain analysis for host structure should be carried out, preferably in real-time application under realistic working conditions, to calculate the frequency response function (FRF) of the system and indicate the effective mode-shapes. Then, a weighted -norm-based method will be more effective. 2) In contrast, the - norm scheme takes into consideration a measure of maximum placement indices. As a result, by including new dynamics of higher order nature into the calculations, the optimization outcome may diverge significantly. This can be observed by comparing the accumulative optimization indices for the actuator/sensor numbers around 50 (see Fig. 1a) in two cases of five and ten mode-shapes. Such an approach will result in an inaccurate assessment of the problem for the cases that the frequency range of the application may alter from time to time. This emphasizes the importance of combined -methods.

|  |
| --- |
|  |
| Fig. 6 objective function in single mode simultaneous actuator and sensor placement |

3) For the collocated formation, the results of - and -based optimization functions are qualitatively similar. As a result, in the applications where the transducer includes a pair of actuator/sensor, the results of the optimization are expected to coincide mostly for both procedures. However, if the application operates in a broadband frequency, the result of the -based method is less informative without appropriate weighting.

|  |
| --- |
|  |
| Fig. 7 Collocated/non-collocated configurations |

This can be observed by comparing the placement indices of the collocated form including ten eigenmodes for - and -objectives. For the sake of brevity, the rest of the results are presented in Table. 3 for four best symmetric locations of actuator/sensor placement. For sub-problem (b), two configurations are selected as shown in Fig. 8: 1) The non-optimal configuration with collocated actuators/sensors at locations 11, 20, 81, and 90 of Fig. 1b. 2) The optimal location based on multi-modal (1-10) placement result of -scheme: 34, 37, 64, and 67 of Fig. 1b.

|  |  |
| --- | --- |
|  |  |
| Configuration 1 | Configuration 2 |
| Fig. 8 Symmetrical configurations for optimal (2) and non-optimal (1) actuator/sensor placement | |

Next, the simulation sub-problem (b) is outlined in details to illustrate the applicability of the methodology in section 2.2 and Appendix 1 for time-dependent online analysis namely, the closed-loop system design.

*3.2 Sub-problem (b): SiL in closed-loop investigates*

In this section, the application of the real-time SiL described in section 2.2 is shown for AVC of two piezo-laminated panels in Fig. 8. Sensor values as predefined time-varying physical measures in the *output history* of the system response are collected in nodal level and as shown in Fig. 3 are sent to be processed inside “Engine application” (Refer to Appendix 1). The control law (feedback signal) is generated by using arbitrary linear/nonlinear controller synthesized in MATLAB. As long as the structure of the controller can be formulated in an m-file in the form of a system of ordinary differential equations (ODE), the proposed coupling scheme can handle the implementation of the controller inside a loop with ABAQUS/CAE. For the simulation example in sub-problem (b), the designed controller is parameterized in a function that takes a vector of inputs (see Fig. 1b) including the previous output of the plant, sensor values, current time step, time increment, and amplitude generated from MATLAB in the previous step. This vector is imported as the input data for the fixed-step ODE solver. As a results, it is essential to create a set that records the amplitude of the plant inside FORTRAN and provides the data at each increment for MATLAB. To keep the problem tractable, an optimal controller is designed based on the reduced order nominal model from sub-problem (a) for the two final configurations. The details of the output feedback linear quadratic Gaussian regulator as a classical method is briefly presented in Appendix 3.

*3.2.3 System identification and closed-loop analyses*

A reduced-order plant is required for the LQG controller design in Appendix 1. For this purpose, first the system response in frequency-domain as a nonparametric model is obtained by *Steady-state dynamics, Direct* *step* in the frequency range of [1350 8000] Hz.

|  |
| --- |
| Table 3 The four best actuator/sensor placement numbers based on different criteria |
| |  |  |  |  |  |  |  | | --- | --- | --- | --- | --- | --- | --- | |  | **Separate placement** | | | | **collocated placement** | | |  | **actuator** | | **Sensor** | |  | | | **Mode number** |  |  |  |  |  |  | | **1** | 45, 46, 55, 56 | 45, 46, 55, 56 | 15, 16, 85, 86 | 15, 16, 85, 86 | 45, 46, 55, 56 | 45, 46, 55, 56 | | **2** | 35, 36, 65, 66 | 35, 36, 65, 66 | 5, 6, 95, 96 | 5, 6, 95, 96 | 35, 36, 65, 66 | 35, 36, 65, 66 | | **3** | 43, 48, 53, 58 | 43, 48, 53, 58 | 3, 8, 93, 98 | 3, 8, 93, 98 | 43, 48, 53, 58 | 43, 48, 53, 58 | | **4** | 33, 38, 63, 68 | 33, 38, 63, 68 | 33, 38, 63, 68 | 33, 38, 63, 68 | 33, 38, 63, 68 | 33, 38, 63, 68 | | **5** | 43, 48, 53, 58 | 43, 48, 53, 58, | 3, 8, 93, 98 | 3, 8, 93, 98 | 43, 48, 53, 58 | 43, 48, 53, 58 | | **1-2** | 35, 36, 65, 66 | 35, 36, 65, 66 | 5, 6, 95, 96 | 5, 6, 95, 96 | 35, 36, 65, 66 | 35, 36, 65, 66 | | **1-5** | 33, 38, 63, 68 | 33, 38, 63, 68 | 4, 7, 94, 97 | 33, 38, 63, 68 | 33, 38, 63, 68 | 33, 38, 63, 68 | | **1-8** | 32, 39, 62, 69 | 22, 29, 72, 79 | 32, 39, 62, 69 | 22, 29, 72, 79 | 34, 37, 64, 67 | 42, 49, 52, 59 | | **1-10** | 25, 26, 75, 76 | 25, 26, 75, 76 | 25, 26, 75, 76 | 45, 46, 55, 56 | 34, 37, 64, 67 | 42, 49, 52, 59 | |

The frequency response function (FRF) of the system from the control input and disturbance input to the measurement signals are presented in Fig. 9. Then, the state space matrices including the disturbance matrix is parameterized via frequency-domain subspace system identification method following (Favoreel and others, 2000; Wills and others, 2009).

|  |
| --- |
|  |
| Fig. 9 The frequency response function in nominal range compared to wide-band obtained from ABAQUS |

The frequency range is limited to a narrow band compared to the steady-state analysis in ABAQUS for two main reasons: 1) to express the efficiency of the SiL configuration in detecting the spillover effect when the nominal model is selected to be narrow band. In other words, compared to conventional methods of implementing the designed control system on the reduced order model which is in contrast with the nature of real-time implementations, it is observed that for disturbance signals with broadband frequency content the control system is unable to suppress the vibrations or even cause instability due to the spillover effect. Additionally, due to the unconventional geometry of the problem compared to the results in the literature of FE-based control (mostly clamped-free beam), the higher order modes can significantly affect the dynamic response. 2) To show that as long as the disturbance signal is activated in the nominal frequency range, the designed controller is able to attenuate vibration amplitude.

Before moving to the closed-loop performance evaluation, it should be pointed out that since the transient simulations are performed in *dynamic implicit* scheme, the time integration damping generated by ABAQUS is automatically introduced due to Hilber-Hughes-Taylor as an extension of Newmark’s -method time integration. The parameters corresponding to the transient fidelity are selected to be , , and such that the numerical energy dissipation is kept minimal. This operator has an advantage that it is unconditionally stable for a linear system (Puri, 2011). Next, the vibration suppression performance is investigated in the frequency range of the reduced-order system. Accordingly, the panel is excited by a uniformly distributed time-varying pressure that acts over partitions 44, 45, 54, and 55 simultaneously with a chirp profile: magnitude of and frequency swept between [1350 2500] Hz within 1 sec. The open loop and closed-loop system responses are compared at an observation nodal point in the center of the host layer’s top surface in Figs. 10a and 10b for configurations 1 and 2, respectively. For the results in Fig. 10a (case 1) and Fig. 10b, it is assumed that and while and (see Appendix 3).

|  |
| --- |
|  |
| Fig. 10 Comparison of the open loop and closed-loop systems in time domain: (a) non-optimal configuration. (b) optimal configuration |

It is obvious that due to the placement of active elements, applying the same weighting for two configurations lead to widely different results; one of which is instable. The optimal configuration 2 in Fig. 8 suppresses the vibration in the nominal frequency range while the non-optimal configuration leads to instability (Case 1 of Fig. 10a). Additionally, the spatial vibration suppression of the system can be observed for any specific time-step e.g. the snapshot of the open loop and closed-loop systems in Fig. 11 for (see Fig. 10b) which is an advantage of the SiL method. In order to investigate the main reason for instability of the system in configuration 2, fast Fourier transformation (FFT) is applied on the control signal as shown in Fig. 12a, Case 1. It is observed that due to the spillover effect, the system dynamic at 5414 Hz is excited by the controller.

|  |  |
| --- | --- |
|  |  |
| Fig. 11 Comparison of spatial displacement of open loop and closed-loop systems in contour plot of isosurfaces in deformed panel at 0.3785 sec snapshot | |

However, as shown in Fig. 9 (configuration 1, Case 1), the dynamics of the plant with higher frequency than 4450 Hz are neglected. To address this issue the process of identification and control synthesis are re-performed by increasing the nominal frequency range up to 5850 Hz as Case 2 in Configuration 1 (see Fig. 9: dashed green line). Vibration attenuation quality assessment in Fig. 10a Case 2 reveals that the control system is unable to suppress the vibration. Additionally, the control effort in AVC that results in suppressing the vibration amplitude in Figs. 10a (Case 2) and 10b are presented in Figs. 12a (Case 2) and 12b, respectively.

|  |
| --- |
|  |
| Fig. 12 Applied control input on the piezo-actuators bonded on top surface of the host panel |

Two main observations are as follows: 1) Although the results of the control implementation on the nominal reduced-order plant are suppressed, it is seen that the closed-loop system is stable and suppresses the vibration. Therefore, the importance of the SiL framework proposed in this paper is emphasized in providing a realistic evaluation of the controller performance when implemented on an approximation of the full-order system. This feature is especially emphasized for the cases that real-time experimental implementations are costly, hazardous, or in the phase of structural design and prototyping where there is no access to the real plant.

2) Comparing Figs. 12a (Case 2) and 12b for optimal and non-optimal configurations shows that although the amplitude of control law is higher in non-optimal scenario and Case 2 covers a broader frequency range, it is unable to match the same vibration suppression performance as in the optimal case. Using the SiL technique may reveal reasonable resolutions for that matter: 2a) The delay in the system: Sub-figures in Figs. 12a (Case 2) and 12b show that for non-optimal configuration, there exists sec time-delay from disturbance to the sensor which is neglected in control synthesis. Accordingly, for real applications such as flexible manipulators used in Space Robotic Arms with large geometries and non-collocated actuator/sensor placement such time-delays in actuator/sensor elements as mentioned in (Bossi and others, 2011) may lead to performance degradation. 2b) Although the actuator/sensor size optimization is neglected in this study, by looking at the contour plot of isosurfaces in the deformed panel in -directions at 5414 Hz in Fig. 13, for non-optimal configuration, the inability of closed-loop system in suppressing the vibration amplitude is evident.

|  |
| --- |
|  |
| Fig. 13 The deformation contour plot in -directions at 5414 Hz |

The results in Fig. 11 are presented only for configuration 2 for the sake of brevity. One remark is that if the simulations need a large number of increments (), then the obtained results may be affected by round-off errors. A possible solution is executing the ABAQUS *Job* module with double precision entries.

The geometry of the simulation problems in this paper is more complicated than in previous studies such as beams with a couple of natural frequencies below 100 Hz. Such a geometry is intentionally selected to show the efficiency of the SiL scheme in detecting the realistic behavior of the closed-loop system in complicated structures. The experimental analyses carried out in (Oveisi and Nestorović, 2016; Oveisi and Nestorovic, 2016) show an agreement in the behavior of AVC performance evaluation observed in the proposed SiL configuration.

Analyzing the vibration suppression for higher frequencies is out of the scope of this paper which requires large system memory, higher processing power, and CPU time due to the higher required mesh density and lower time-increment (Bossi and others, 2011). The SiL framework can be used as a tool for extracting the time-domain response of geometrically nonlinear mechanical structures (open loop and closed-loop) for complex geometries where analytical solutions are nonexistent and experiments are costly. New uncertainty quantification methods can be established based on the combination of recent developments in covariance matrix adaptation evolution strategy (CMA-ES) (Claeys and others, 2014; Noël and Kerschen, 2017) and the modeling framework proposed in this paper. Also, Additional FORTRAN subroutines may be combined with UAMP e.g. user-defined finite elements can be incorporated within ABAQUS e.g. authors used UEL subroutine to implement Mindlin-type nine-node shell element for the piezoelectric domain (Nestorović and others, 2012).

**4. Conclusions**

In this paper, a stable interconnection between ABAQUS and MATLAB is developed and tested for both offline post-processing and online simulation of time-varying amplitudes. A detailed ready-to-use scheme is prepared in a step-by-step manner that makes the software-in-the-loop framework flexible in terms of adding/changing additional FORTRAN subroutines. Possible issues in establishing this connection are remarked. In order to investigate some of the key features of such interconnection, two design problems are defined for a mechanical structure with relatively complex geometry. Comprehensive analyses are carried out in terms of observing the behavior of the framework.

**Acknowledgments**

The authors would like to thank Jim Dempsey CEO, CTO at QuickThread Programming and Steve Lionel, the senior technical staff at Intel Corporation for their productive comments on developing the proposed SiL technique.

**Appendix 1.**

In order to arrange a ready-to-use interface for the reader, the revised form of standard UAMP is broken into some script blocks. This increases the readability of the script in comparison to a batch entrance. Let’s name the revised UAMP subroutine “general block” which starts with general block **part 1** in Fig. A1.

|  |
| --- |
| general block **part 1** |
| Subroutine uamp(  C passed in variables  \* ampName, time, ampValueOld, dt, nProps, props, nSvars, svars,  \* lFlagsInfo, nSensor, sensorValues, sensorNames,  \* jSensorLookUpTable,  C to be defined (if needed)  \* ampValueNew,  \* lFlagsDefine,  \* AmpDerivative, AmpSecDerivative, AmpIncIntegral,  \* AmpIncDoubleIntegral)  include 'aba\_param.inc' |

Fig. A1. The general FORTRAN subroutine’s first block: subroutine declaration and UAMP’s variable definition

For brevity, the standard UAMP is not explained in this paper, and the interested reader may refer to ABAQUS user subroutine reference manual. Next, in contrast to standard UAMP, an interface should be defined including the signatures of some functions and additional subroutines. The interface in FORTRAN is declared with the interface keyword after general block **part 1**, and then ends before defining the class of sensorValues in the program block of Fig. A2by end interface keyword. This block in the rest of the appendix is referred to as “interface block”.

|  |
| --- |
| interface block**part 1** |
| interface  function ENGOPEN (command) bind(C,name="ENGOPEN")  integer(INT\_PTR\_KIND()) :: ENGOPEN  character, dimension(\*), intent(in) :: command  end function ENGOPEN  end interface |

Fig. A2. The first part of the interface block as the language-binding-spec attribute

At this point, MATLAB engine should be called inside the main subroutine, and since FORTRAN compiler is used for ABAQUS/CAE kernel, any function/subroutine inside the interface block should be bound with the language-binding-spec attribute, using the keyword bind. Such an entity in FORTRAN processor is treated as its conforming object in the companion C compiler. Note that the engine applications in visual studio (VS) environment are straight-forward to be compiled. However, the harvested features of VS in ABAQUS require the interface block which serves as the recognition platform between the case-sensitive commands of FORTRAN and C. As an example, ENGOPEN routine is presented as the first entity to interface blockin Fig. A2.

Such a function needs the declaration of the class of its input and output variables. To increase the readability, the rest of interface block is presented at the end of Appendix 1. After ending the interface block, the variables together with their classes are defined in a similar manner to MATLAB function definition syntax and then followed by general block **part 2** which is partially shown in Fig. A3.

|  |
| --- |
| general block **part 2** |
| ! Time vector parameters  double precision timestep1, timestep2  C time indices  parameter (iStepTime = 1,  \* iTotalTime = 2,  \* nTime = 2)  timestep1 = time(iStepTime)  timestep2 = timestep1 + dt |

Fig. A3. General block for time indices and various information flags

The general block **part 2** may contain the time indices, definition/activation of various information flags, the definition of sensor values at the end of the previous increment (sensorValues), and description of the array of the solution-dependent state variables (svars). These variables should be written in FORTRAN language intrinsic data types. Then, iGetSensorID('SENUi', jSensorLookUpTable) would deliver the user-defined solution-dependent state variables which should be passed through MATLAB engine.

Note that independent of the numerical example of sub-problem (b) in Fig. 1a, the current steps are general for other applications mentioned in the introduction section as long as they can be formulated in terms of a time-dependent step module of ABAQUS with a series of external loads or time-varying boundary conditions. At this point, MATLAB engine is opened, a double array of the desired size is defined (forvar) for the variables that are going to be processed in MATLAB engine (matlabsession), a time vector is created in MATLAB, and the vector is copied from FORTRAN array to MATLAB array using MXGETPR. This completes the general block **part 3** as illustrated in Fig. A4.

|  |
| --- |
| general block **part 3** |
| integer\*8 matlabsession  matlabsession = ENGOPEN('matlab')  ! Check point 1:  T = MXCREATEDOUBLEMATRIX(Mi, Ni, 0)  Call MXCOPYREAL8TOPTR(forvar, MXGETPR(T), Ni)  status = ENGPUTVARIABLE(ep, 'TT', T)  if (status .ne. 0) then  write(6,\*) 'ENGPUTVARIABLE failed: Check point 1'  stop  endif |

Fig. A4. The general program for opening the engine and evaluating the MATLAB function for the vector defined in UAMP subroutine

Next, a MATLAB function (m-file) which controls the execution of the online post-processing algorithm is called. This function (matlabfunc) is a gateway to the MATLAB toolboxes such as signal processing, control design, fuzzy systems, etc. The m-file initiates the commands at the beginning of each time increment while the ABAQUS/CAE kernel is in a wait state. User-defined functions can be called only if the current directory includes a copy of the function, however, since the MATLAB engine still needs to be called from ABAQUS, the only possibility is to add the directory containing the m-file to permanent MATLAB directory using “pathtool”. Since the function called in the global MATLAB directory cannot save the variables, it is recommended to create a dummy vector in UAMP and assign the generated results from MATLAB iteratively to its elements. This action has three advantages: 1) the simulations can be terminated using some if-conditions on ampValueNew (see Fig. A1) in the case of violation of a physical constraint or performance index. In application of AVC of sub-problem (b), this criterion can be the maximum control effort generated from the controller exceeding the piezo-patch depolarization voltage or maximum displacement of a shaker baffle. 2) During the simulation, the visualization module can be executed over the resulted “.odb” file for observing the generated amplitudes in UAMP. 3) An additional advantage is the possibility to have access to these variables in Tecplot Software.

At this point, the MATLAB function is called from FORTRAN subroutine, the resulted array in MATLAB is read by the messenger of FORTRAN interface, and the obtained array is copied from MATLAB array to FORTRAN array as in general block **part 4** in Fig. A5.

|  |
| --- |
| general block **part 4** |
| ! Check point 2:  if (ENGEVALSTRING(matlabsession, 'out1 = matlabfunc(TT);') .ne. 0) then  write(6,\*) 'ENGEVALSTRING failed: check point 2'  stop  endif  out2 = ENGGETVARIABLE(matlabsession, 'out1')  call MXCOPYPTRTOREAL8(MXGETPRS(out2), out3, No) |

Fig. A5. The general program for bringing back the MATLAB function’s output using the FORTRAN messenger

It is evident that variables out1, out2, and out3 are classified in general block **part 2** (suppressed for the sake of brevity). Finally, the amplitude is updated in FORTRAN subroutine based on the values of out3, and the array is deallocated as: call MXDESTROYARRAY(T) for the new increment.

Additional notes:

* Since the routines in the interface block are mixed-case, the declarations in Fig. A6 are needed before interface.

|  |
| --- |
| Pre-interface block |
| **!DEC$ OBJCOMMENT LIB:"libeng.lib"**  **!DEC$ OBJCOMMENT LIB:"libmx.lib"**  **!DEC$ OBJCOMMENT LIB:"libmat.lib"** |
| Fig. A6. Intel-style pre-processing directives |

where the **OBJCOMMENT LIB** directive postulates a library in an object heading. In this case, the “linker” looks for the character constant **.lib** by the **OBJCOMMENT** directive in the command line of the script. The reason behind this obligatory declaration is that FORTRAN is not case-sensitive. However C is, and the routines in MATLAB libraries are mixed-case. As a result, Intel-style pre-processing directives are required. The three libraries mentioned above are available by installing the MATLAB software.

* If C code correctly links with the external libraries but “unresolved external symbol reference” error appears, assembler output should be checked. For Microsoft Windows operating systems (OS), some changes should be applied: low case, up case, and mixed case. A list of such changes is available for the linker in the header file “fintrf.h” provided by Mathworks which contains the declaration of the pointer type needed by the MATLAB/FORTRAN interface. Since this header file is not readable for ABAQUS compiler, those changes should be found and applied manually from the assembler output. One should note that only Windows linker has this feature. For instance, in this paper, mxCopyReal8ToPtr is replaced with MXCOPYREAL8TOPTR730 along with some other modifications. These changes are different from one OS to another. This is a common approach when one needs to write an assembly program to interface with a C application using decorated function names. Then, in order to figure out the problematic name mangling, an empty shell subroutine in C is recommended to be written. The produced assembly output, gives the correct form to be referred to in subroutine that should be applied manually.

As it can be seen in the interface block**part 2**, additional subroutines are MXDESTROYARRAY, MXCOPYREAL8TOPTR, and MXCOPYPTRTOREAL8, which all require **DECORATE** attribute on a mixed-language application. Additionally, unlike the functions, no return values should be assigned to them.

**Appendix 2.**

The material properties of the composite structure are provided for the host structure:

and the piezo-actuator/sensor (density: )

|  |  |
| --- | --- |
|  | |
|  |  |
|  |  |

where , , , and represent the piezoelectricity matrices (stress coefficients) and the dielectric matrices for actuator and sensor, respectively.

|  |
| --- |
| interface block**part. 2** |
| function MXCREATEDOUBLEMATRIX (a1,b1,c1)  \* bind(C,name="MXCREATEDOUBLEMATRIX")  integer\*8 :: a1,b1,c1  integer\*8 :: MXCREATEDOUBLEMATRIX  intent(in) :: a1,b1,c1  end function MXCREATEDOUBLEMATRIX    function MXCREATEDOUBLESCALAR (a2)  \* bind(C,name="MXCREATEDOUBLESCALAR")  real\*8 :: a2  integer\*8 :: MXCREATEDOUBLESCALAR  intent(in) :: a2  end function MXCREATEDOUBLESCALAR    Subroutine MXDESTROYARRAY (a3)  **!DEC$ ATTRIBUTES DECORATE, ALIAS:"MXDESTROYARRAY" :: MXDESTROYARRAY**  integer\*8, dimension(\*) :: a3  end Subroutine MXDESTROYARRAY  function MXGETPR(a4) result(ptr) bind(C, name='MXGETPR')  import  implicit none  integer\*8, dimension(\*), intent(in) :: a4  integer\*8 :: ptr  end function MXGETPR    Subroutine MXCOPYREAL8TOPTR (a5,b5,c5)  **!DEC$ ATTRIBUTES DECORATE, ALIAS:"MXCOPYREAL8TOPTR" :: MXCOPYREAL8TOPTR**  real\*8 a5(\*)  integer\*8 b5  integer\*8 c5  end Subroutine MXCOPYREAL8TOPTR    function ENGPUTVARIABLE (a6,b6,c6)  \* bind(C,name="ENGPUTVARIABLE")  integer\*8, intent(in) :: a6  character, dimension(\*), intent(in) :: b6  integer\*8, dimension(\*), intent(in) :: c6  end function ENGPUTVARIABLE    function ENGEVALSTRING (a7,b7)  \* bind(C,name="ENGEVALSTRING")  integer(INT\_PTR\_KIND()) :: ENGEVALSTRING  integer\*8, intent(in) :: a7  character, dimension(\*), intent(in) :: b7  end function ENGEVALSTRING    function ENGGETVARIABLE (a8,b8)  \* bind(C,name="ENGGETVARIABLE")  integer\*8 :: ENGGETVARIABLE  integer\*8, intent(in) :: a8  character, dimension(\*), intent(in) :: b8  end function ENGGETVARIABLE    Subroutine MXCOPYPTRTOREAL8 (a9,b9,c9)  **!DEC$ ATTRIBUTES DECORATE, ALIAS:"MXCOPYPTRTOREAL8" :: MXCOPYPTRTOREAL8**  integer\*8 a9  real\*8 b9  integer\*8 c9  end Subroutine MXCOPYPTRTOREAL8    function engClose (a10) bind(C,name="engClose")  integer(INT\_PTR\_KIND()) :: engClose  integer\*8, intent(in) :: a10  end function engClose |

Fig. A7. The second part of the interface block after Fig. A2

**Appendix 3.**

In optimal control design for the output regulation problem, the feedback law is synthesized by minimizing a time-dependent function that includes the measure of system output (sensor measurement) and control effort to achieve an optimal tradeoff between reduction in the plant response and injected control energy. Following the conventional linear quadratic output regulator (LQRY) technique in (Gawronski, 2004) for the system in Eq. (1) and given initial condition , the control input signal () is constructed by optimizing the objective function in Eq. (C1) such that within a specific time window (in steady state ), the system outputs converge to origin.

|  |  |  |
| --- | --- | --- |
|  |  | (C1) |

where and are user-defined time-independent weighting matrices selected by control engineer. Following Lewis and Syrmos (Lewis, 1996), the LQRY can be converted to linear quadratic regulation problem (LQR) by translating the weighting matrices as Eq. (C2)

|  |  |  |
| --- | --- | --- |
|  |  | (C2) |

In order to add to the generality of the problem, the strictly proper system is assumed to be under the effect of unknown input disturbance and output measurement noise as formulated in Eq. (C3) instead of (1)

|  |  |  |
| --- | --- | --- |
|  |  | (C3) |

in which, , and represent the real-values unknown-input matrix with appropriate dimensions, output measurement noise, and unknown but -bounded mismatch disturbance signal. Additionally, and are assumed to be the result of some uncorrelated zero-mean Gaussian stochastic processes with constant power spectral density matrices ( and , respectively). Since, in practical problems generally the states of the system are unavailable for measurement, an observer based on Kalman filter is combined with the deterministic LQR to formulate the control synthesis in linear quadratic Gaussian (LQG) framework. As a result, the control input is proposed in terms of observed states () as under the assumption that the pair () is observable where with being the unique positive-semi definite solution of the ARE of (Macijejowski, 1989). Moreover, the dynamics of the state observer in the presence of measurement noise is assigned as such that is minimized. represents the expectation operator, while with 0. The steady state solution of the latter optimization problem is proven to be obtained by solving ARE: . It is obvious that the behavior of the closed-loop system obtained based on LQG configuration can be determined by analyzing the closed-loop poles based on Separation theorem (Skogestad and Postlethwaite, 2007).

**References**

Adhikari S., Friswell MI., Lonkar K. and Sarkar A. (2009), "Experimental case studies for uncertainty quantification in structural dynamics", *Probabilistic Eng. Mech.,* **24**(4), 473–492.

Bertagne C. and Hartl D. (2014), "Feedback control applied to finite element models of morphing structures", *ASME 2014 Conf. Smart Mater. Adapt. Struct. Intell. Syst. SMASIS 2014,* **1**, 1–10.

Bossi L., Rottenbacher C., Mimmi G. and Magni L. (2011), "Multivariable predictive control for vibrating structures: An application", *Control Eng. Pract.,* **19**(10), 1087–1098.

Bruant I., Gallimard L. and Nikoukar S. (2010), "Optimal piezoelectric actuator and sensor location for active vibration control, using genetic algorithm", *J. Sound Vib.,* **329**(10), 1615–1635.

Claeys M., Sinou J-J., Lambelin J-P. and Alcoverro B. (2014), "Multi-harmonic measurements and numerical simulations of nonlinear vibrations of a beam with non-ideal boundary conditions", *Commun. Nonlinear Sci. Numer. Simul.,* **19**(12), 4196–4212.

Favoreel W., De Moor B. and Van Overschee P. (2000), "Subspace state space system identification for industrial processes", *J. Process Control,* **10**(2), 149–155.

Gabbert U., Duvigneau F. and Ringwelski S. (2017), "Noise control of vehicle drive systems", *Facta Univ. Ser. Mech. Eng.,* **15**(2), 183.

Gao L., Lu QQ., Fei F., Liu LW., Liu YJ. and Leng JS. (2013), "Active vibration control based on piezoelectric smart composite", *Smart Mater. Struct.,* **22**(12)

Gawronski WK. (2004), *Dynamics and Control of Structures: A Modal Approach.*

Hasheminejad SMM. and Oveisi A. (2016), "Active vibration control of an arbitrary thick smart cylindrical panel with optimally placed piezoelectric sensor/actuator pairs", *Int. J. Mech. Mater. Des.,* **12**(1), 1–16.

Jae-Hung Han and In Lee. (1999), "Optimal placement of piezoelectric sensors and actuators for vibration control of a composite plate using genetic algorithms", *Smart Mat. Struct.,* **8**(2), 257.

Karagülle H., Malgaca L. and Öktem HF. (2004), "Analysis of active vibration control in smart structures by ANSYS", *Smart Mater. Struct.,* **13**(4), 661–667.

Kerschen G., Worden K., Vakakis AF. and Golinval J-C. (2006), "Past, present and future of nonlinear system identification in structural dynamics", *Mech. Syst. Signal Process.,* **20**(3), 505–592.

Kim J., Varadan V V. and Varadan VK. (1995), "Finite element-optimization methods for the active control of radiated sound from a plate structure", *Smart Mater. Struct.,* **4**(4), 318–326.

Landau ID., Castellanos Silva A., Airimitoaie T-B., Buche G. and Noe¨ M. (2013), "Benchmark on adaptive regulation—rejection of unknown/time-varying multiple narrow band disturbances", *Eur. J. Control,* **19**(4), 237–252.

Lewis FL. (1996), *Optimal Control.*

Lim Y-H., Gopinathan S V., Varadan V V. and Varadan VK. (1999), "Finite element simulation of smart structures using an optimal output feedback controller for vibration and noise control", *Smart Mater. Struct.,* **8**(3), 324–337.

Macijejowski JM. (1989), *Multivariable Feedback Design.*

Nestorović T., Marinković D., Chandrashekar G., Marinković Z. and Trajkov M. (2012), "Implementation of a user defined piezoelectric shell element for analysis of active structures", *Finite Elem. Anal. Des.,* **52**, 11–22.

Nestorović T. and Trajkov M. (2013), "Optimal actuator and sensor placement based on balanced reduced models", *Mech. Syst. Signal Process.,* **36**(2), 271–289.

Nestorovic T., Trajkov M. and Garmabi S. (2015), "Optimal placement of piezoelectric actuators and sensors on a smart beam and a smart plate using multi-objective genetic algorithm", *Smart Struct. Syst.,* **15**(4), 1041–1062.

Noël JP. and Kerschen G. (2017), "Nonlinear system identification in structural dynamics: 10 more years of progress", *Mech. Syst. Signal Process.,* **83**, 2–35.

Noël JP. and Schoukens J. (2017), "Grey-box state-space identification of nonlinear mechanical vibrations", *Int. J. Control,*, 1–22.

Omidi E. and Mahmoodi SN. (2015), "Sensitivity analysis of the Nonlinear Integral Positive Position Feedback and Integral Resonant controllers on vibration suppression of nonlinear oscillatory systems", *Commun. Nonlinear Sci. Numer. Simul.,* **22**(1), 149–166.

Omidi E., Mahmoodi SN. and Shepard WS. (2015), "Vibration reduction in aerospace structures via an optimized modified positive velocity feedback control", *Aerosp. Sci. Technol.,* **45**, 408–415.

Orszulik RR. and Gabbert U. (2016), "An interface between Abaqus and Simulink for high-fidelity simulations of smart structures", *IEEE/ASME Trans. Mechatronics,* **21**(2), 879–887.

Oveisi A. and Nestorovic T. (2016), "Robust nonfragile observer-based H2/H∞ controller", *J. Vib. Control,*, 1077546316651548.

Oveisi A. and Nestorović T. (2016), "Robust observer-based adaptive fuzzy sliding mode controller", *Mech. Syst. Signal Process.,* **76**–**77**, 58–71.

Oveisi A. and Nestorović T. (2017), "Transient response of an active nonlinear sandwich piezolaminated plate", *Commun. Nonlinear Sci. Numer. Simul.,* **45**, 158–175.

Oveisi A., Nestorović T. and Nguyen NL. (2016), "Semi-analytical modeling and vibration control of a geometrically nonlinear plate", *Int. J. Struct. Stab. Dyn.,*, 1771003.

Paduart J., Lauwers L., Swevers J., Smolders K., Schoukens J. and Pintelon R. (2010), "Identification of nonlinear systems using Polynomial Nonlinear State Space models", *Automatica,* **46**(4), 647–656.

Peng F. (2005), "Actuator placement optimization and adaptive vibration control of plate smart structures", *J. Intell. Mater. Syst. Struct.,* **16**(3), 263–271.

Puri GM. (2011), *Python scripts for Abaqus : learn by example.*, 1st edn. Charleston, South Carolina

Rahman N. and Alam MN. (2012), "Active vibration control of a piezoelectric beam using PID controller : Experimental study", *Lat. Am. J. Solids Struct.,* **9**(May), 657–673.

Ramesh Kumar K. and Narayanan S. (2007), "The optimal location of piezoelectric actuators and sensors for vibration control of plates", *Smart Mater. Struct.,* **16**(6), 2680–2691.

Ramesh Kumar K. and Narayanan S. (2008), "Active vibration control of beams with optimal placement of piezoelectric sensor/actuator pairs", *Smart Mater. Struct.,* **17**(5), 055008.

Ray LR., Koh B-H. and Tian L. (2000), "Damage detection and vibration control in smart plates: Towards multifunctional smart structures", *J. Intell. Mater. Syst. Struct.,* **11**(9), 725–739.

Sadri AM., Wright JR. and Wynne RJ. (1999), "Modelling and optimal placement of piezoelectric actuators in isotropic plates using genetic algorithms", *Smart Mater. Struct.,* **8**(4), 490–498.

Sadri AM., Wright JR. and Wynne RJ. (2002), "LQG control design for panel flutter suppression using piezoelectric actuators", *Smart Mater. Struct.,* **11**(6), 834–839.

Shakeri R. and Younesian D. (2016), "Broad-band noise mitigation in vibrating annular plates by dynamic absorbers", *Int. J. Struct. Stab. Dyn.,* **16**(06), 1550014.

Skogestad S. and Postlethwaite I. (2007), "Multivariable feedback control: analysis and design", *lavoisier.fr,*

Soize C. (2005), "Random matrix theory for modeling uncertainties in computational mechanics", *Comput. Methods Appl. Mech. Eng.,* **194**(12–16), 1333–1366.

Stojanović V. (2015), "Geometrically nonlinear vibrations of beams supported by a nonlinear elastic foundation with variable discontinuity", *Commun. Nonlinear Sci. Numer. Simul.,* **28**(1–3), 66–80.

Vel SS. and Baillargeon BP. (2004), Active vibration suppression of smart structures using piezoelectric shear actuators. *Proceedings of the 15th International Conference on Adaptive Structures and Technologies*.

Wills A., Ninness BM. and Gibson S. (2009), "Maximum Likelihood Estimation of state space models from frequency domain data", *IEEE Trans. Automat. Contr.,* **54**(1), 19–33.

Xu SX. and Koko TS. (2004), "Finite element analysis and design of actively controlled piezoelectric smart structures", *Finite Elem. Anal. Des.,* **40**(3), 241–262.

1. \*Corresponding author,

   E-mail: [atta.oveisi@rub.de](mailto:atta.oveisi@rub.de)

   aResearch associate.

   bPROF. DR.-ING. [↑](#footnote-ref-1)
2. Reader may contact the corresponding author to obtain all the Python files which may be adapted for other case studies. [↑](#footnote-ref-2)