



Master's thesis  
Astrophysical Sciences

# Supermassive black holes and the cosmological formation of massive early-type galaxies (title not final)

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# Contents

<b>1</b>	<b>Introduction</b>	<b>1</b>
1.1	Information about galaxies, shortly . . . . .	1
1.2	Aim of the thesis . . . . .	1
<b>2</b>	<b>Background</b>	<b>2</b>
2.1	Cosmology . . . . .	2
2.1.1	Hubble parameter, Friedmann equations and so on . . . . .	2
2.1.2	Cosmological perturbations . . . . .	2
2.2	Early-type galaxies . . . . .	2
2.2.1	Types of ellipticals . . . . .	2
2.2.2	Photometric and kinematic profiles . . . . .	2
2.3	Feedback processes . . . . .	2
<b>3</b>	<b>GADGET-3 and KETJU</b>	<b>3</b>
3.1	Overview of GADGET-3 . . . . .	3
3.2	Smoothed Particle Hydrodynamics . . . . .	3
3.3	Gas cooling? . . . . .	3
3.4	Feedback? . . . . .	3
3.5	KETJU . . . . .	3
<b>4</b>	<b>Creating initial conditions for the cosmological simulations</b>	<b>4</b>

4.1	Zoom-in technique . . . . .	4
4.2	MUSIC . . . . .	6
4.2.1	Overview . . . . .	6
4.2.2	Generation of the seed density field . . . . .	6
4.2.3	Creation of nested grids . . . . .	9
4.2.4	Particle displacements and velocity fields . . . . .	10
4.2.5	Creating IC files . . . . .	10
4.3	GADGET-3 setup for the zoom-in -simulations . . . . .	11
4.3.1	Cosmological setup . . . . .	11
4.3.2	Low-resolution run . . . . .	11
4.3.3	Choosing the zoom-in regions . . . . .	11
4.3.4	Initial conditions . . . . .	11
<b>5</b>	<b>Cosmological GADGET-3 simulations</b>	<b>12</b>
5.1	Computational load of the simulations . . . . .	12
5.2	Locating galaxy centers: the shrinking sphere -method . . . . .	12
5.3	Properties of the galaxies . . . . .	12
5.3.1	Rotation curves . . . . .	12
5.3.2	Star formation history . . . . .	13
5.3.3	Colors and magnitudes . . . . .	16
<b>6</b>	<b>Simulations with KETJU</b>	<b>19</b>
<b>7</b>	<b>Conclusions</b>	<b>20</b>
	<b>Bibliography</b>	<b>20</b>

# 1. Introduction

1.1 Information about galaxies, shortly

1.2 Aim of the thesis

## 2. Background

### 2.1 Cosmology

2.1.1 Hubble parameter, Friedmann equations and so on

2.1.2 Cosmological perturbations

### 2.2 Early-type galaxies

2.2.1 Types of ellipticals

2.2.2 Photometric and kinematic profiles

### 2.3 Feedback processes

## **3. GADGET-3 and KETJU**

- Haven't really thought about the contents of this chapter yet

### **3.1 Overview of GADGET-3**

### **3.2 Smoothed Particle Hydrodynamics**

### **3.3 Gas cooling?**

### **3.4 Feedback?**

### **3.5 KETJU**

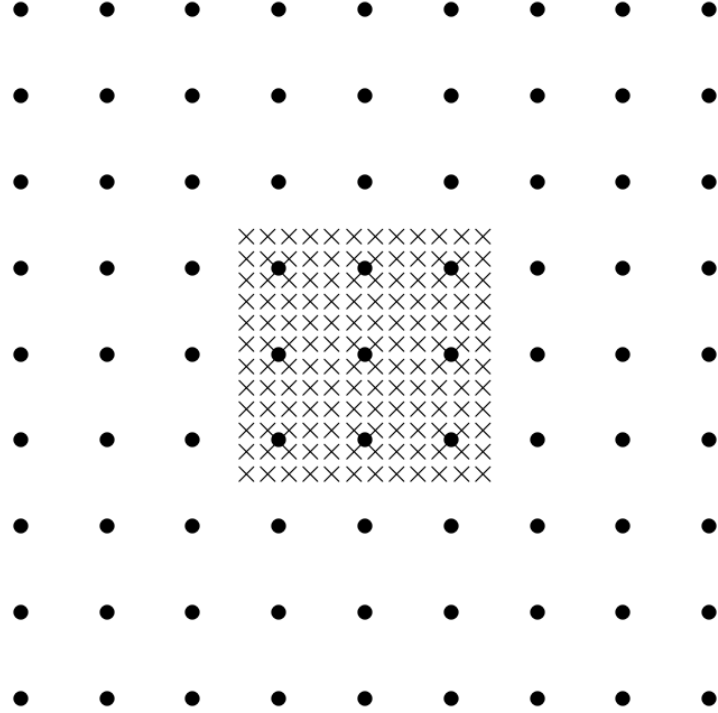


## 4. Creating initial conditions for the cosmological simulations

This chapter focuses on the methods used to create the necessary configuration files for the high resolution cosmological simulations. The first section focuses the so-called 'zoom-in' method, which allows us to have spatially large simulation boxes with high resolution regions. After this, the code MUSIC (MUlti-Scale initial conditions) is introduced, which is used to create a spatial volume with realistic velocity and density perturbations at an early redshift. Compared to earlier implementations, the errors in the velocity and displacement fields are improved by two orders of magnitude (Hahn & Abel, 2011). The created initial conditions (ICs) files are used for the performed GADGET-3 simulations. As the runs performed with GADGET-3 are the main focus of this thesis, the section for MUSIC is not as in-depth as the GADGET-3 discussion in chapter 3. The last part of this chapter focuses on the setup of the cosmological setup of the simulations, and on the preliminary low resolution run needed for the higher resolution simulations.

### 4.1 Zoom-in technique

To study galaxy formation and evolution in a proper cosmological context, the simulation box must have a large volume. To resolve the gravitational effects of a smaller scale structure, it is also required to have a high resolution, i.e. a large amount of particles with relatively low mass. Having a sufficient resolution on the whole simulation volume would result in an unreasonably large computational workload. Thus it is more sensible to implement a method, which has a high resolution in a single region of interest, surrounded by a large volume with a smaller resolution. This method, nowadays known as the 'zoom-in' technique, has been in use for multiple decades. One of the first simulations with a region of interest surrounded by low resolution background was performed by Navarro & White (1994), and later



**Figure 4.1:** An example of a zoom-in region, with one level of mesh refinement. The circles represent the particles on the coarse grid. The crosses represent the refined particles, with each coarse particle inside this region divided into  $4^3$  particles (Bertschinger, 2001).

implementations have been used by e.g. Power et al. (2003) and Marinacci et al. (2014).

An example of a zoom-in grid is shown in Figure 4.1. Here, the dots represent the large particles on a coarse grid, while the crosses represent the refined grid with finer, less massive particles. In this refinement, each massive particle in the refined region is divided into  $4^3$  particles. Modern implementations, such as the one used in this thesis, use zoom regions with multiple levels of refinement. This is discussed in 4.2.3.

To locate the regions of interest, we need to first perform a computationally light simulation without a high resolution volume (discussed in 4.3.2), and then choose the zoom-in region and perform the simulation again. The initial conditions (ICs) must also portray a realistic case, i.e. the fluctuations at a very high redshift must match the expected structure from theory. Fortunately, we can use a single program to create realistic ICs, with zoom-in box included.

## 4.2 Music

NOTE: some things might be mentioned without good explanations (like the power spectrum and two-point correlation), and I plan to explain them in chapter 2.

### 4.2.1 Overview

MUSIC (MUlti-Scale Initial Conditions) is a code by Hahn & Abel (2011), which can be used to create the ICs for GADGET-3 simulations. The program creates a simulation volume, with velocity and particle displacements calculated using a power spectrum and two-point correlation given as input. To take fluctuations of smaller scales into account, the program is also able to create a high resolution zoom-in region for the ICs. The zoom-in region can have multiple levels of refinement, and an example of an IC created using MUSIC is shown in Figure 4.2.

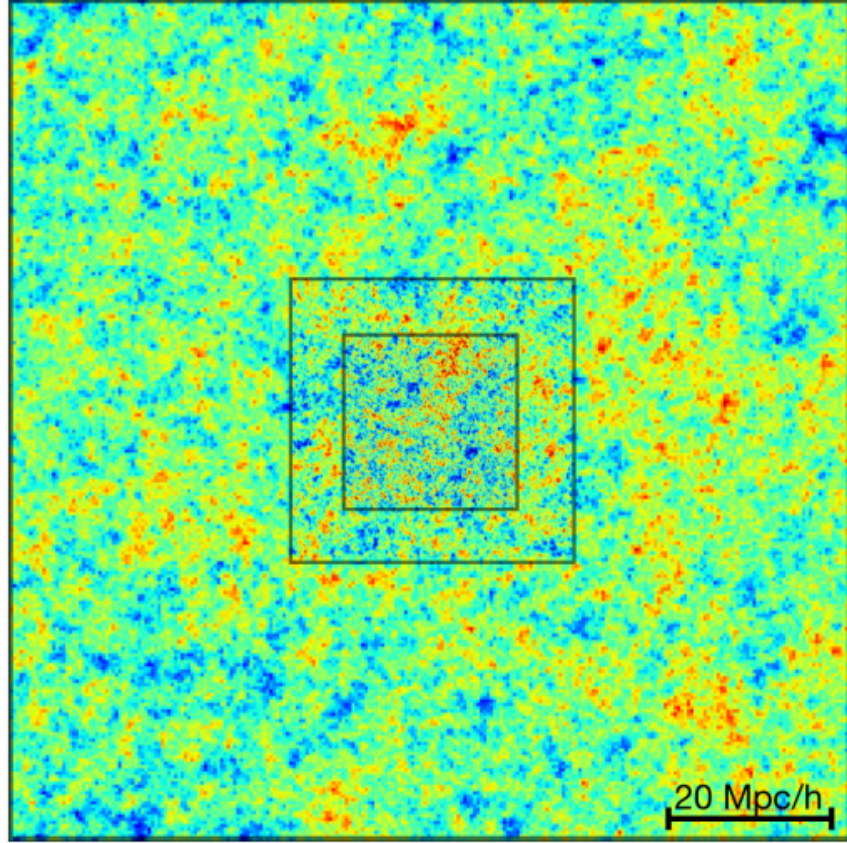
MUSIC extends the prior work, e.g. the GRAFIC-2 code made by Bertschinger (2001), which also produces ICs with multiple levels of resolution. The one of most notable upgrades of MUSIC compared to GRAFIC-2 is the way the transfer function is used to calculate the density perturbations, discussed in 4.2.2. Another improvement is the way different refinement levels constrain other levels (discussed in 4.2.3).

The initial conditions produced by the code best describe the real conditions when the redshift of the produced ICs lie on the linear perturbation regime. If the initial redshift  $z_i$  of the ICs is set to be too large (i.e. on the non-linear regime), the formation of the first haloes occurs at unrealistically late times and the formation of high-mass haloes is suppressed, as shown by Reed et al. (2013). Still, MUSIC gives relatively accurate ICs even at the mildly non-linear regime of  $z_i \sim 20$  (Hahn & Abel, 2011).

### 4.2.2 Generation of the seed density field

For the generation of particle velocities and locations, MUSIC first needs to create a density field, described by an over-density field  $\delta(\mathbf{r})$ . Using an a Power spectrum  $P(k)$  given as input, this field can be described completely, as the power spectrum of the field is

$$P(k) \equiv \langle \tilde{\delta}(\mathbf{k}) \tilde{\delta}^*(\mathbf{k}) \rangle, \quad (4.1)$$



**Figure 4.2:** An example of a density field created using MUSIC. The length of the simulation box is 100 Mpc/h. Two levels of refinement are included, with the two inner boxes showing the boundaries of the refined mesh grids (Hahn, 2013).

where  $*$  denotes the complex conjugate, and  $\tilde{\delta}(\mathbf{k})$  represents the Fourier transform of the over-density field, i.e.

$$\tilde{\delta}(\mathbf{k}) = \int \delta(\mathbf{x}) e^{-i\mathbf{k}\cdot\mathbf{x}} d^3\mathbf{x}. \quad (4.2)$$

The transfer function  $T(k)$  can also be used to express the power spectrum, defined as

$$P(k) = \alpha k^{n_s} T^2(k), \quad (4.3)$$

where  $\alpha$  is a normalization constant and  $n_s$  is the spectral index. The value of the spectral index is given to MUSIC in the configuration file, while  $\alpha$  is evaluated in using another, observable constant.

One way to normalize the spectrum estimate the amplitude of the via the observable variance of the galaxy distribution  $\sigma^2$  at a distance  $R$ . As shown in e.g.

Mo et al. (2010), the predicted variance is defined as

$$\sigma^2(R) = \frac{1}{2\pi^2} \int P(k) \tilde{W}^2(k) k^2 dk, \quad (4.4)$$

where  $\tilde{W}(k)$  is defined as the Fourier transform of a top-hat window function  $W(r)$ :

$$W(r) = \begin{cases} \frac{3}{4\pi R^3}, & r \leq R \\ 0, & r > R \end{cases} \quad (4.5)$$

The Fourier transform of this function is

$$\tilde{W}(k) = \frac{3}{(kR)^3} (\sin(kR) - kR \cos(kR)). \quad (4.6)$$

For historical reasons, the distance where the variance is usually measured is  $R = 8 \text{ Mpc/h}$ . At this distance,  $\sigma(8 \text{ Mpc/h}) \equiv \sigma_8$  is valued close to unity.  $\sigma_8$  is also the value MUSIC takes as input to normalize the power spectrum.

As the shape of the power spectrum are known and the spectrum is normalized, the generation of the density field is now possible. The goal is to create the density field from random noise values  $\mu(\mathbf{r})$ , while requiring that the amplitudes follow the power spectrum  $P(k)$ . The sample which random values  $\mu(\mathbf{r})$  create is called the white noise sample.

MUSIC generates the white noise sample using a Gaussian distribution. Discussion of Gaussian distributions can be found in multiple sources of literature, for example Mo et al. (2010). For a distribution to be Gaussian, the probability density function  $\varrho$  of random value  $x$  is

$$\varrho(x) = \frac{1}{\sqrt{2\pi}\sigma} \exp\left(-\frac{(x - \bar{x})^2}{2\sigma^2}\right), \quad (4.7)$$

where  $\bar{x}$  and  $\sigma^2$  are the mean and the variance, respectively. This can be generalized to higher dimensions, and for a  $n$ -dimensional random field  $\delta(\mathbf{x}) = (\delta_1, \delta_2, \dots, \delta_n)$  the distribution is Gaussian if the probability distribution function can be written as

$$\varrho(\delta_1, \delta_2, \dots, \delta_n) = \frac{1}{\sqrt{(2\pi)^n \det(\mathcal{M})}} e^{-\mathcal{L}}, \quad (4.8)$$

where  $\mathcal{M}$  is the covariance matrix,  $\mathcal{M}_{ij} = \langle \delta_i \delta_j \rangle$ , and

$$\mathcal{L} \equiv \frac{1}{2} \sum_{i,j} \delta_i (\mathcal{M}^{-1})_{ij} \delta_j. \quad (4.9)$$

It is assumed that the field is homoeoneous and isotropic, meaning under spatial translation or rotation, the multivariant Gaussian distribution functions are invariant. Therefore the two-point correlation function  $\xi(x)$  completely determines the distribution functions. Specifically, the field's one-point distribution function is

$$\varrho(\delta)d\delta = \frac{1}{\sqrt{2\pi\sigma^2}}e^{-\frac{\delta^2}{2\sigma^2}}d\delta, \quad (4.10)$$

where the variance of the field is  $\sigma^2 = \xi(0)$ .

Returning to the white noise sample, the amplitudes of the random values  $\mu(\mathbf{r})$  can be generated to follow the power spectrum  $P(k)$  by considering the Fourier transformed random field  $\tilde{\mu}(\mathbf{k})$ . With this, the Fourier transformed field  $\tilde{\delta}(\mathbf{k})$  can be written as

$$\tilde{\delta}(\mathbf{k}) = \sqrt{P(|\mathbf{k}|)}\tilde{\mu}(\mathbf{k}) = \alpha|\mathbf{k}|^{n_s/2}T(|\mathbf{k}|)\tilde{\mu}(\mathbf{k}). \quad (4.11)$$

**NOTE: The MUSIC paper has  $\alpha$  in this equation, why isn't it  $\sqrt{\alpha}$ ?**

A common procedure to evaluate the real-space density field is to perform an inverse Fourier transform to  $\tilde{\delta}(\mathbf{k})$ , as is done in e.g. Bertschinger (2001). MUSIC uses a different approach, and calculates the real-space density field as

$$\delta(\mathbf{r}) = \mathcal{T}_R(|\mathbf{r}|) * \mu(\mathbf{r}), \quad (4.12)$$

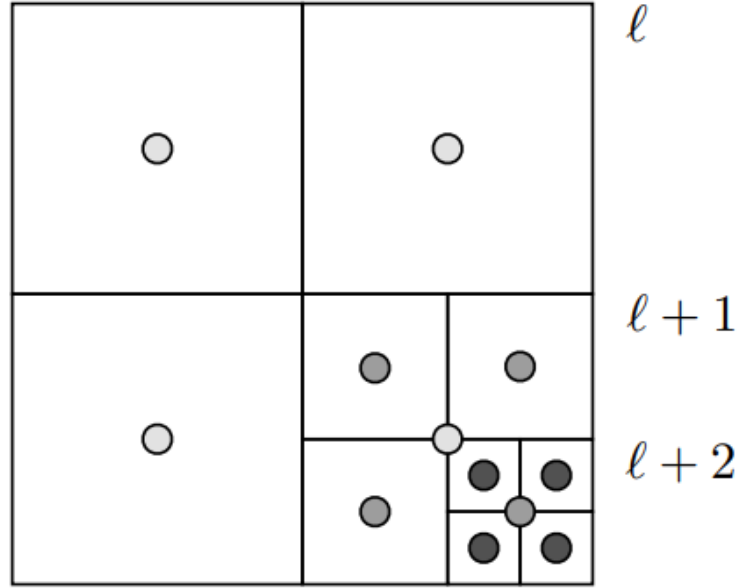
where  $\mathcal{T}_R(r)$  is the real-space counterpart of  $\tilde{\mathcal{T}}(k) \equiv \alpha k^{n_s/2}T(k)$  and "\*" is denoting convolution, discussed thoroughly by Salmon (1996). In short, the white noise  $\mu(\mathbf{x})$  is realised as density perturbations in real space using the convolution operator. This method has previously been used by e.g. Pen (1997) and Sirko (2005). Hahn & Abel (2011) also show that previous implementations that use the inverse Fourier transform of  $\delta(\mathbf{k})$  leads to too small values for two-point correlation function.

To calculate the  $\delta(\mathbf{r})$  via convolution, it is still required to transform  $\tilde{\mathcal{T}}(k)$  into real space, which MUSIC achieves by calculating (assuming that  $\tilde{\mathcal{T}}(k)$  is spherically symmetric)

$$\mathcal{T}_R(r) = \frac{1}{(2\pi)^3} \int_{\mathbb{R}} \tilde{\mathcal{T}}(k) e^{i\mathbf{x} \cdot \mathbf{k}} d^3\mathbf{k} \quad (4.13)$$

$$= \frac{1}{2\pi^2} \int_0^\infty \tilde{\mathcal{T}}(k) \frac{\sin(kr)}{kr} dk. \quad (4.14)$$

### 4.2.3 Creation of nested grids



**Figure 4.3:** A two dimensional example layout of multiple scale nested grid (Hahn & Abel, 2011). The figure shows parent cells on level  $\ell$ , and children cells on two higher levels. The center of the children cells is not in the same position as the center of the parent cell.

#### 4.2.4 Particle displacements and velocity fields

- Lagrangian perturbation theory (might be explained already in earlier chapters?)
- Poisson's equation and its multi-grid solution
- MUSIC can use a hybrid Poisson solver
- Differences between baryons and DM

#### 4.2.5 Creating IC files

- Step by step explanation of creating the IC file with a zoom-in region

## 4.3 GADGET-3 setup for the zoom-in -simulations

### 4.3.1 Cosmological setup

### 4.3.2 Low-resolution run

### 4.3.3 Choosing the zoom-in regions

- FoF -algorithm
- Conditions of the chosen halos
- Figure showing the zoom-in regions from the low res run

### 4.3.4 Initial conditions

$h_0$	$\Omega_m$	$\Omega_b$	$\Omega_\Lambda$	$\sigma_8$	$\rho_{\text{crit}}$
70.3	0.276	0.045	0.724	0.811	$9.28 \times 10^{-27} \text{ kg/m}^3$

**Table 4.1:** Cosmological parameters used for the simulations. If a simulation doesn't include baryons, the dark matter density parameter  $\Omega_{\text{DM}}$  is equal to the matter density parameter  $\Omega_m$ . If baryons are included,  $\Omega_{\text{DM}} = \Omega_m - \Omega_b$ .

- Information from GADGET3 config files



## 5. Cosmological GADGET-3 simulations

### 5.1 Computational load of the simulations

- Quick overview: CPUs used, time elapsed, where simulations were run

### 5.2 Locating galaxy centers: the shrinking sphere -method

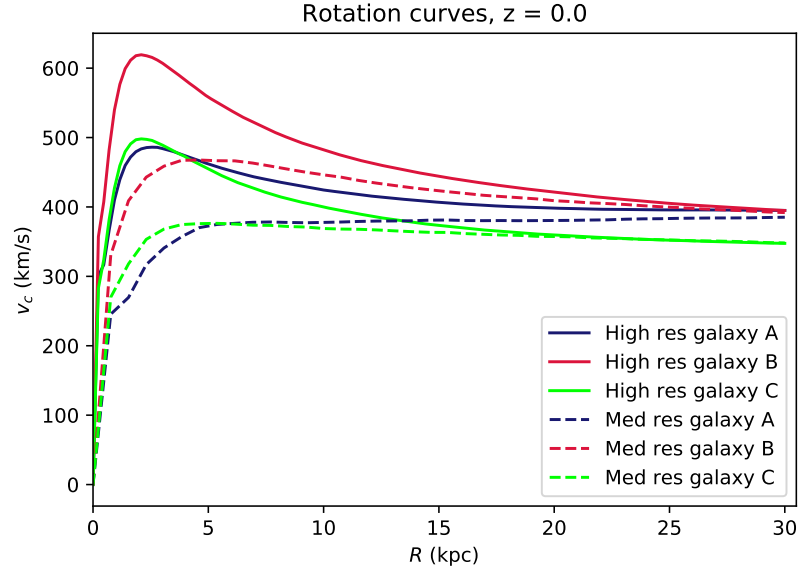
### 5.3 Properties of the galaxies

Simulation	$r_{\text{vir}}$ (kpc)	$M_*$ ( $M_{\odot}$ )	$M_V$ (mag)	$M_{*,\text{gal}}/M_{\text{vir}}$	$M_{\text{bh}}$ ( $M_{\odot}$ )
Med res, A	517	$3.98 \times 10^{11}$	-22.4	0.025	$5.82 \times 10^9$
Med res, B	574	$5.16 \times 10^{11}$	-22.7	0.024	$6.23 \times 10^9$
Med res, C	400	$2.56 \times 10^{11}$	-22.0	0.035	$3.96 \times 10^9$
High res, A	526	$5.31 \times 10^{11}$	-22.6	0.032	$3.64 \times 10^9$
High res, B	578	$6.38 \times 10^{11}$	-22.8	0.029	$4.54 \times 10^9$
High res, C	400	$3.46 \times 10^{11}$	-22.2	0.047	$2.80 \times 10^9$

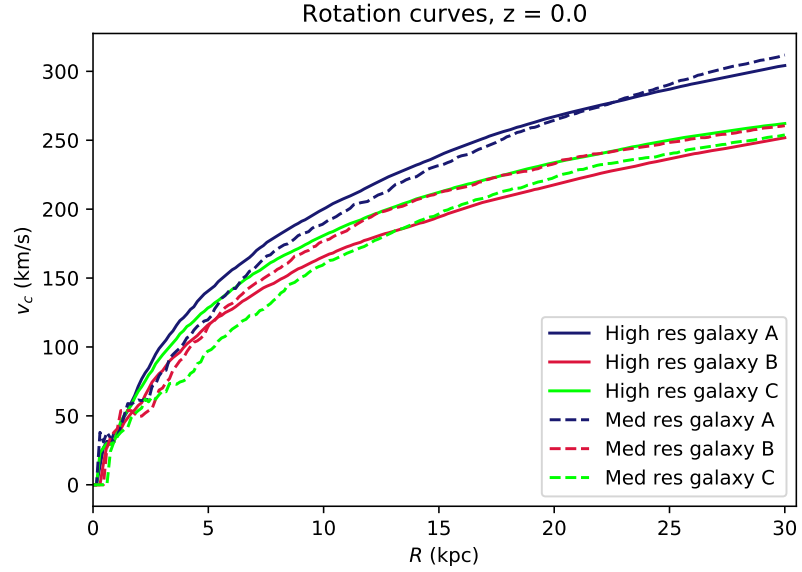
**Table 5.1:** Properties of the zoomed-in galaxies at redshift  $z = 0$ .

#### 5.3.1 Rotation curves

- Med res galaxy A simulation is performed with single precision, I'm currently doing the simulation in double precision
- Rotation curves do not have the same limits on the y-axis



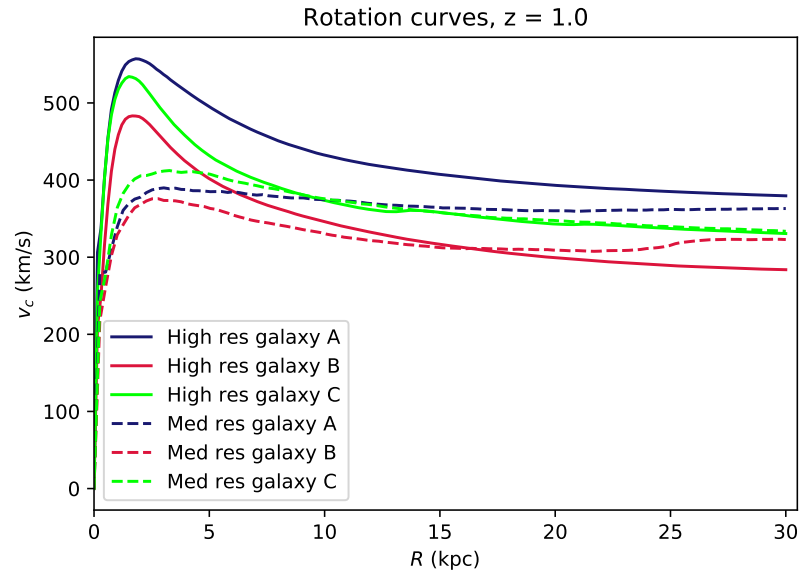
**Figure 5.1:** Rotation curves for each galaxy including baryons, at redshift 0. The continuous lines represent the high resolution simulations and the dashed lines represent the medium resolution simulations.



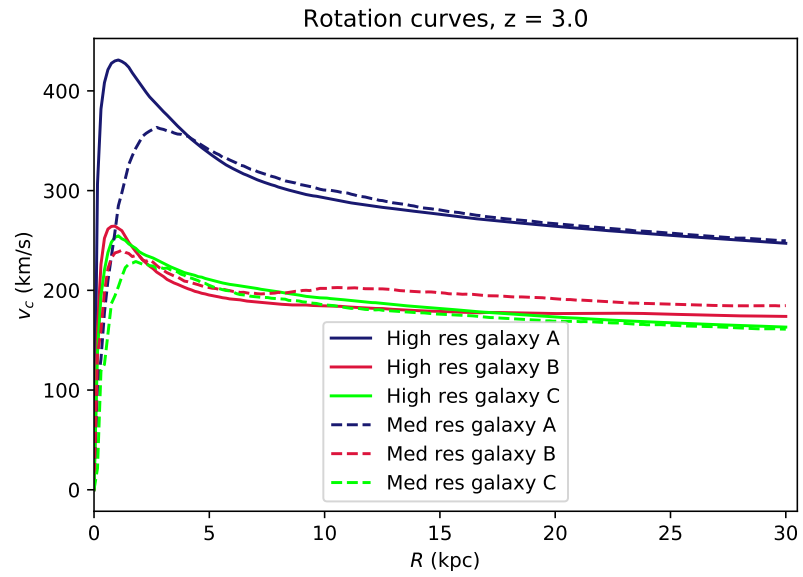
**Figure 5.2:** Rotation curves for each galaxy including only dark matter, at redshift 0. The continuous lines represent the high resolution simulations and the dashed lines represent the medium resolution simulations.

### 5.3.2 Star formation history

- The stellar mass evolution plot is not yet done for high res simulations.

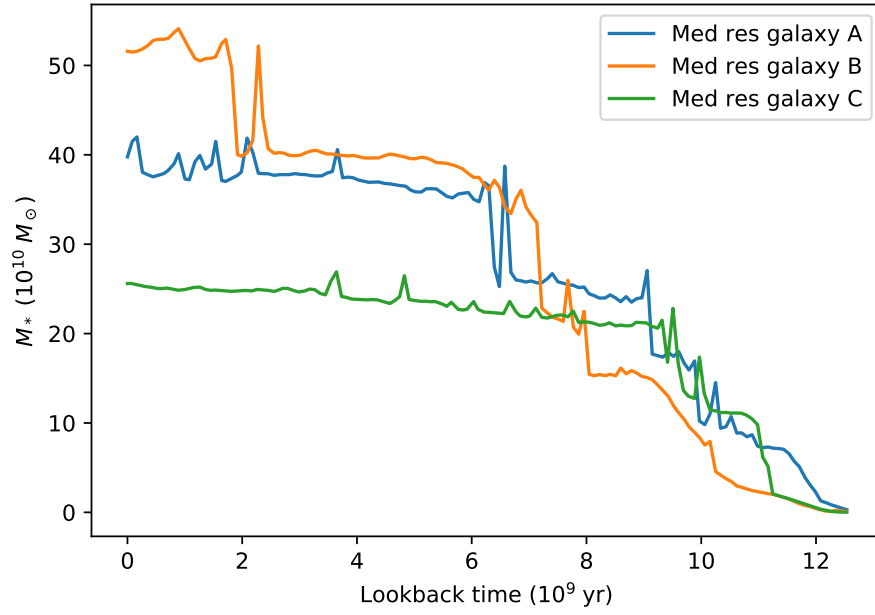


**Figure 5.3:** Rotation curves for each galaxy including baryons, at redshift 1. The continuous lines represent the high resolution simulations and the dashed lines represent the medium resolution simulations.



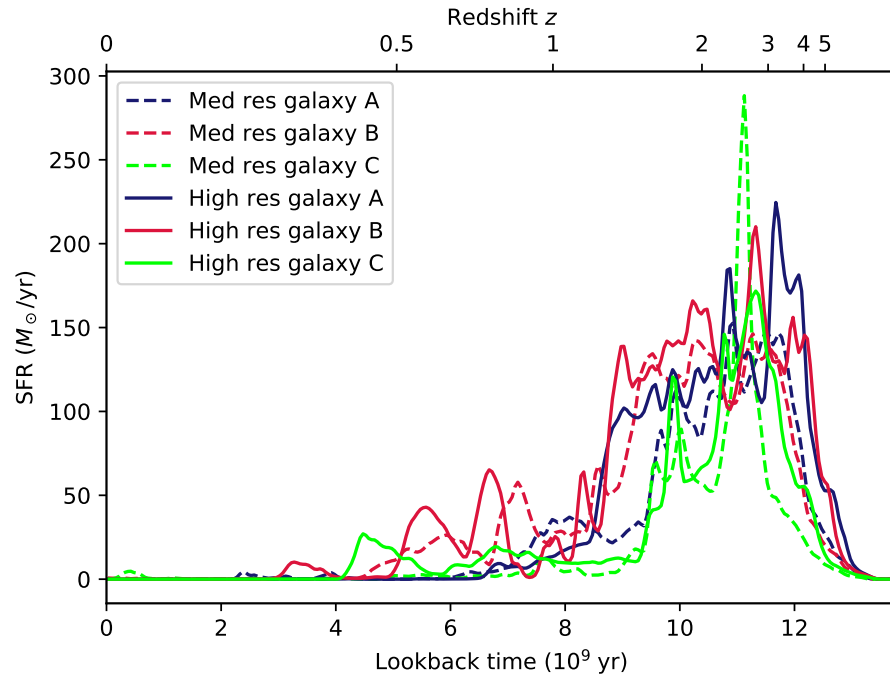
**Figure 5.4:** Rotation curves for each galaxy including baryons, at redshift 3. The continuous lines represent the high resolution simulations and the dashed lines represent the medium resolution simulations.

- Redshifts missing from the stellar mass evolution plot
- SFRs, also histograms?



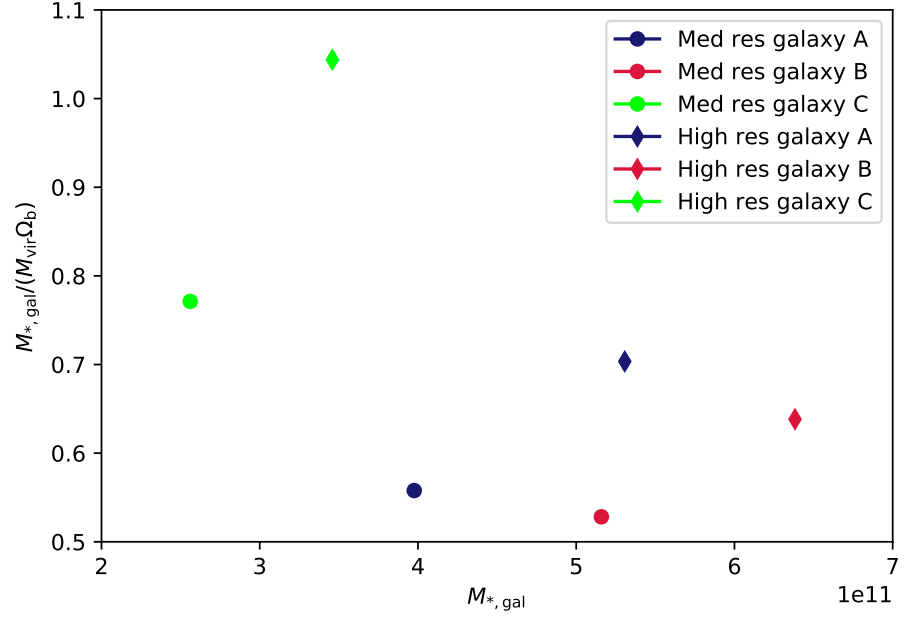
**Figure 5.5:** Stellar mass evolution for the medium resolution galaxies. The calculated stellar mass is the stellar mass within  $r_{\text{gal}} = r_{\text{vir}}/10$ .

- Again, med res A results will probably change a bit when double precision run is finished.
- Formation efficiencies, comparing to the cosmological parameter

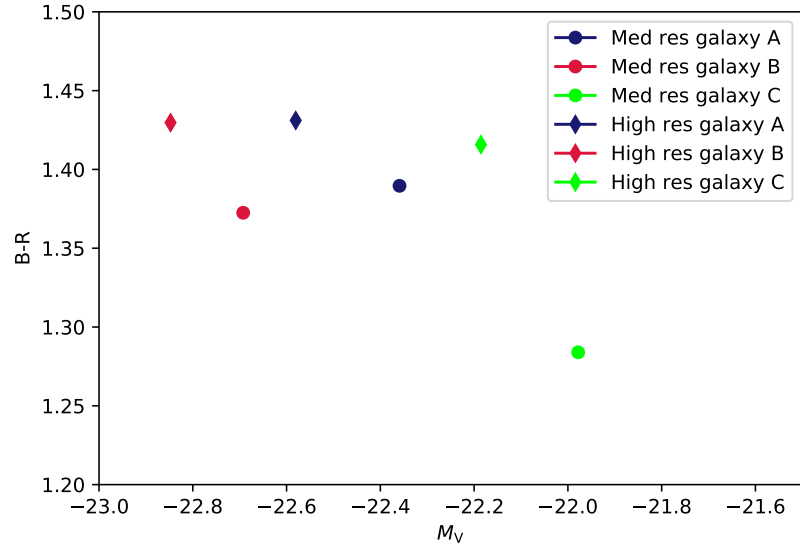


**Figure 5.6:** Stellar formation rates for each zoomed-in galaxy, plotted as a function of lookback time. The lines are created from histograms having a length of 5 Myr, which are then smoothed. The continuous lines represent the high resolution simulations and the dashed lines represent the medium resolution simulations.

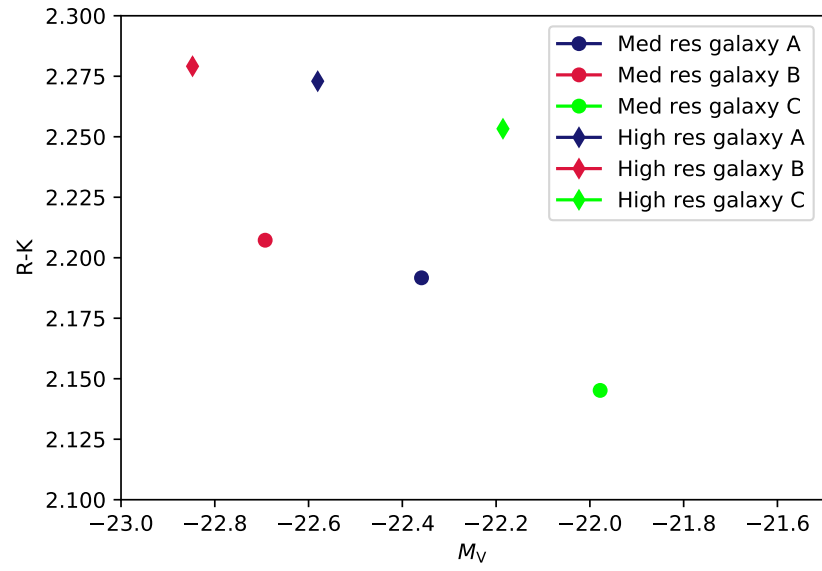
### 5.3.3 Colors and magnitudes



**Figure 5.7:** Galaxy formation efficiencies for each galaxy, plotted with their stellar masses. The cosmological baryon density  $\Omega_b$  is set to 0.045 in the simulations. The diamond and circular markers show the results of the high resolution and the medium resolution zoom-in simulations, respectively.



**Figure 5.8:** B-R colors for each simulated galaxy, plotted with each galaxy's absolute magnitude in the V-band. The diamond and circular markers show the results of the high resolution and the medium resolution zoom-in simulations, respectively.



**Figure 5.9:** R-K colors for each simulated galaxy, plotted with each galaxy's absolute magnitude in the V-band. The diamond and circular markers show the results of the high resolution and the medium resolution zoom-in simulations, respectively.

## **6. Simulations with KETJU**



## 7. Conclusions

- recap on what was written/studied
- more own thoughts on results
- future missions
- how could the simulations be more realistic (higher resolution, more feedback stuff?)

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