

Practical 6: To Simplify the Given Boolean Expression and Realize It Using Basic Gates and Universal Gates

Boolean algebra is used to simplify digital expressions so that a circuit becomes easier, faster, and uses fewer gates.

After simplification, the expression is implemented using:

1. **Basic Gates** (AND, OR, NOT, XOR)
2. **Universal Gates** (NAND and NOR) — because they can build any circuit.

In this practical, we simplify the given Boolean expression and design its logic circuit.

Note: Since your teacher will give any expression like

$$F = A'B + AB' \text{ or } F = A + BC,$$

main yahan ek universal format likh rahi hoon jisse tum *koi bhi* expression apply kar sakte ho.

Ye pura practical EXACT FORMAT me hota hai.

Aim

To simplify the given Boolean expression using Boolean laws and realize it using

Basic gates and Universal gates (NAND/NOR).

Boolean Simplification (General Method)

Common Boolean laws used for simplification:

1. Identity Law

$$A + 0 = A$$

$$A \cdot 1 = A$$

2. Null Law

$$A + 1 = 1$$

$$A \cdot 0 = 0$$

3. Idempotent Law

$$A + A = A$$

$$A \cdot A = A$$

4. Complement Law

$$A + A' = 1$$

$$A \cdot A' = 0$$

5. Absorption Law

$$A + AB = A$$

$$A(A + B) = A$$

6. Distributive Law

$$A(B + C) = AB + AC$$

7. De Morgan's Law

$$(A \cdot B)' = A' + B'$$

$$(A + B)' = A' \cdot B'$$

Example Simplification (Standard for Practical Write-Up)

Let the expression be:

$$F = A'B + AB'$$

This is a very common expression used in labs.

Step-by-step Simplification:

$$F = A'B + AB'$$

This is in XOR form.

So, simplified form:

$$F = A \oplus B$$

Ye simplest form hoti hai.

Realization Using Basic Gates

$$F = A \oplus B$$

To realize XOR using basic gates:

$$\text{XOR} = A'B + AB'$$

So the circuit uses:

- 2 NOT gates (A' , B')
- 2 AND gates
- 1 OR gate

This creates the basic XOR circuit.

Realization Using Universal Gates (NAND or NOR)

Universal gates can build any logic circuit.

XOR using only NAND Gates:

- 4 NANDs to create XOR
- No other gates needed
- Inputs are passed through NAND combinations to generate SUM output

XOR using NOR Gates:

- 5 NOR gates required

- Both input signals inverted using NOR
- Then combined to create XOR behavior

Universal implementations are used because:

- Cheaper
- Faster
- More reliable in IC design

Truth Table (General Table for Expression F)

A	B	A'	B'	AB	F = A ⊕ B
0	0	1	1	0	0
0	1	1	0	1	0
1	0	0	1	0	1
1	1	0	0	0	0

You can modify this table depending on your given expression.