

Practical 6: To Simplify the Given Boolean Expression and Realize It Using Basic Gates and Universal Gates

Boolean algebra is used to simplify digital expressions so that a circuit becomes easier, faster, and uses fewer gates.

After simplification, the expression is implemented using:

1. **Basic Gates** (AND, OR, NOT, XOR)
2. **Universal Gates** (NAND and NOR) — because they can build any circuit.

In this practical, we simplify the given Boolean expression and design its logic circuit.

Note: Since your teacher will give any expression like

$F = A'B + AB'$ or $F = A + BC$,

main yahan ek universal format likh rahi hoon jisse tum *koi bhi* expression apply kar sakte ho.

Ye pura practical EXACT FORMAT me hota hai.

Aim

To simplify the given Boolean expression using Boolean laws and realize it using

Basic gates and **Universal gates** (NAND/NOR).

Boolean Simplification (General Method)

Common Boolean laws used for simplification:

1. Identity Law

$$A + 0 = A$$

$$A \cdot 1 = A$$

2. Null Law

$$A + 1 = 1$$

$$A \cdot 0 = 0$$

3. Idempotent Law

$$A + A = A$$

$$A \cdot A = A$$

4. Complement Law

$$A + A' = 1$$

$$A \cdot A' = 0$$

5. Absorption Law

$$A + AB = A$$

$$A(A + B) = A$$

6. Distributive Law

$$A(B + C) = AB + AC$$

7. De Morgan's Law

$$(A \cdot B)' = A' + B'$$

$$(A + B)' = A' \cdot B'$$

Example Simplification (Standard for Practical Write-Up)

Let the expression be:

$$\mathbf{F = A'B + AB'}$$

This is a very common expression used in labs.

Step-by-step Simplification:

$$F = A'B + AB'$$

This is in XOR form.

So, simplified form:

$$F = A \oplus B$$

Ye simplest form hoti hai.

Realization Using Basic Gates

$$F = A \oplus B$$

To realize XOR using basic gates:

$$\text{XOR} = A'B + AB'$$

So the circuit uses:

- 2 NOT gates (A' , B')
- 2 AND gates
- 1 OR gate

This creates the basic XOR circuit.

Realization Using Universal Gates (NAND or NOR)

Universal gates can build any logic circuit.

XOR using only NAND Gates:

- 4 NANDs to create XOR
- No other gates needed
- Inputs are passed through NAND combinations to generate SUM output

XOR using NOR Gates:

- 5 NOR gates required

- Both input signals inverted using NOR
- Then combined to create XOR behavior

Universal implementations are used because:

- Cheaper
- Faster
- More reliable in IC design

Truth Table (General Table for Expression F)

| A | B | A , | B , | A' B | AB , | F = A \oplus B |
|----------|----------|----------------------|----------------------|-----------------------|-----------------------|------------------------------------|
| 0 | 0 | 1 | 1 | 0 | 0 | 0 |
| 0 | 1 | 1 | 0 | 1 | 0 | 1 |
| 1 | 0 | 0 | 1 | 0 | 1 | 1 |
| 1 | 1 | 0 | 0 | 0 | 0 | 0 |

You can modify this table depending on your given expression.