

Exercise 4: Solution

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Loss: BCE - Forward method

```
def forward(self, y out, y truth):
Performs the forward pass of the binary cross entropy loss function.
:param y_out: [N, ] array predicted value of your model.
     y truth: [N, ] array ground truth value of your training set.
:return: [N, ] array of binary cross entropy loss for each sample of your training set.
result = None
# TODO:
# Implement the forward pass and return the output of the BCE loss.
result = -y truth * np.log(y out) - (1 - y truth) * np.log(1 - y out)
FND OF YOUR CODE
```

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return result

Loss: BCE - Backward method

```
def backward(self, y_out, y_truth):
 Performs the backward pass of the loss function.
 :param y out: [N, ] array predicted value of your model.
     y truth: [N, ] array ground truth value of your training set.
 :return: [N, ] array of binary cross entropy loss gradients w.r.t y out for
       each sample of your training set.
 gradient = None
 # TODO:
 # Implement the backward pass. Return the gradient wrt y out
 gradient = - (y truth / y out) + (1 - y truth) / (1 - y out)
                    END OF YOUR CODE
 return gradient
```

Classifier: Sigmoid

```
def sigmoid(self, x):
Computes the ouput of the sigmoid function
:param x: input of the sigmoid, np.array of any shape
:return: output of the sigmoid with same shape as input vector x
out = None
# TODO:
# Implement the sigmoid function, return out
out = 1 / (1 + np.exp(-x))
                END OF YOUR CODE
return out
```

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Classifier: Forward method

```
def forward(self, X):
Performs the forward pass of the model.
:param X: N x D array of training data. Each row is a D-dimensional point.
:return: Predicted labels for the data in X, shape N x 1
       1-dimensional array of length N with classification scores.
0.00
assert self.W is not None, "weight matrix W is not initialized"
# add a column of 1s to the data for the bias term
batch_size, _ = X.shape
X = np.concatenate((X, np.ones((batch_size, 1))), axis=1)
# save the samples for the backward pass
self.cache = X
# output variable
y = None
# TODO:
# Implement the forward pass and return the output of the model. Note #
# that you need to implement the function self.sigmoid() for that
y = X.dot(self.W)
y = self.sigmoid(y)
END OF YOUR CODE
```

Classifier: Backward method

```
def backward(self, v):
Performs the backward pass of the model.
:param y: N x 1 array. The output of the forward pass.
:return: Gradient of the model output (y=sigma(X*W)) wrt W
assert self.cache is not None, "run a forward pass before the backward pass"
dW = None
# TODO:
# Implement the backward pass. Return the gradient wrt W, dW
# The data X is stored in self.cache. Be careful with the dimensions
# of W, X and y and note that the derivative of the sigmoid fct can be #
# expressed by sigmoid itself
X = self.cache
N, _ = X.shape
\# dz/dW, where z = X * W
dW = X
# dsigmoid/dz, where z = X * W
dz = y * (1 - y)
\# dy/dW = dsigmoid/dz * dz/dW
dW *= dz
END OF YOUR CODE
```

Keep the dimensions of the arrays in mind:

X: [N, D]

y: [N, 1],

dW should be of shape [N, D] as it contains a gradient of the output w.r.t. W for each sample (N: number of samples). The average over all samples is taken in the solver step.

return dW



Optimization

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Optimizer: Step method

```
def step(self, dw):
 :param dw: [D+1,1] array gradient of loss w.r.t weights of your linear model
 :return weight: [D+1,1] updated weight after one step of gradient descent
 weight = self.model.W
 # TODO:
 # Implement the gradient descent for 1 step to compute the weight
 weight -= self.lr * dw
                        END OF YOUR CODE
 self.model.W = weight
```

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Solver: Step method

```
def _step(self):
 Make a single gradient update. This is called by train() and should not
 be called manually.
 model = self.model
 loss func = self.loss func
 X train = self.X train
 v train = self.v train
 opt = self.opt
       Get the gradients dhat{y}/dW and dLoss/dhat{y}.
    Combine them via the chain rule to obtain dLoss / dW.
    Proceed by performing an optimizing step using the given
    optimizer (by calling opt.step() with the gradient wrt W)
    Hint: don't forget to divide number of samples when computing the
    gradient!
 model forward, model backward = model(X train)
 loss, loss grad = loss func(model forward, y train)
 grad = loss_grad.T.dot(model_backward) / loss_grad.shape[0]
 opt.step(grad.T)
 END OF YOUR CODE
```

Model and loss_func return (forward, backward) when called, cf. __call__() in their base classes.

Mind the dimensions of all elements. In particular, we want to update W (via opt.step()) with an array of the same shape, i.e., [1, D]



Questions? Campuswire

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