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Problem Set 1

Problems 1-9 correspond to "Nearest neighbor classification"

Problem 1

1/1 point (graded)

A 10×10 greyscale image is mapped to a d-dimensional vector, with one pixel per coordinate. What is d?





Answer

Correct:

Each coordinate of the vector corresponds to one pixel of the image. Thus the total number of coordinates is just the overall number of pixels, 100.

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Problem 2

1/1 point (graded)

Which of these is the correct notation for 4-dimensional Euclidean space?





 4^{R}





R4



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Problem 3

1/1 point (graded)

What is the Euclidean (also known as L_2) distance between the following two points in ${\bf R}^3$?

2.82



Answer

Correct: The answer is $\sqrt{(1-3)^2 + (2-2)^2 + (3-1)^2} = \sqrt{8}$.

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Problem 4

1/1 point (graded)

The Euclidean (or L_2) length of a vector $x \in \mathbb{R}^d$ is

$$\|x\| = \sqrt{\sum_{i=1}^d x_i^2},$$

where x_i is the *i*th coordinate of x. This is the same as the Euclidean distance between xand the origin. What is the length of the vector which has a 1 in every coordinate?





 $\cdot x'$ has all coordinates equal to -1.







3/3 points (graded)

A particular data set has 4 possible labels, with the following frequencies:

Label	Frequency
A	50%
B	20%
C	20%
D	10%

a) What is the error rate of a classifier that picks a label (A,B,C,D) at random, each with probability 1/4? Give your answer as a number in the range [0,1].



Answer

Correct:

Whatever the correct label might be, the probability of randomly guessing it correctly is 1/4 = 0.25. Thus the probability of being wrong is 0.75.

b) One very simple type of classifier just returns the same label, always. What label should it return?



Answer

Correct: Yes, because this is the most frequently-occurring label.

c) What is the error rate of the classifier from b)? Give your answer as a number in the range [0, 1].



Answer

Correct:

The classifier from b) is wrong whenever the label happens to be something other than its prediction. We can look at the table of frequencies to see how often this happens.

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Problem 8

2/2 points (graded)

A nearest neighbor classifier is built using a large training set, and then its performance is also evaluated on a separate test set.

· Which is likely to be smaller:



· Which is likely to be a better predictor of future performance:

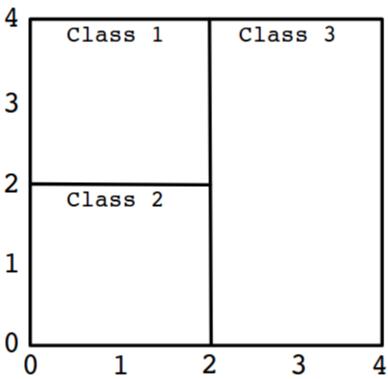
training error		
• test error?		



5/5 points (graded) In this problem,

- · The data space is $X = [0, 4]^2$: each point has two coordinates, and they lie between 0 and 4.
- The labels are $Y = \{1, 2, 3\}$.

The correct labels in different parts of *X* are as shown below.



a) What is the label of point (1, 1)? Your answer should be 1, 2, or 3.



Answer

Correct: This point lies squarely in the region of class 2.

For parts (b) through (e), assume you have a training set consisting of just two points, located at

b) What label will the nearest neighbor classifier assign to point (3, 1)?

Answer

Correct: The nearest neighbor to point (3, 1) is (1, 1), which has label 2.

c) What label will the nearest neighbor classifier assign to point (4, 4)?



Answer

Correct: The nearest neighbor to point (4, 4) is (1, 3), which has label 1.

d) Which label will this classifier never predict?



Answer

Correct:

There are only two data points in the training set, with labels 1 and 2. Thus no point will ever be assigned label 3.

e) Now suppose that when the classifier is used, the test points are uniformly distributed over the square X. What is the error rate of the 1-NN classifier? Give your answer as a number in the range [0, 1].



Answer

Correct:

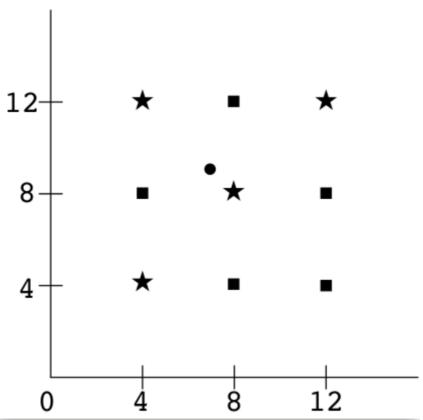
The 1-NN classifier correctly classifies all points in class 1 or 2, and incorrectly classifies all points in class 3. Since class 3 occurs half the time, the error rate of the classifier is 0.5.

Submit

Problems 10-16 correspond to "Improving nearest neighbor"

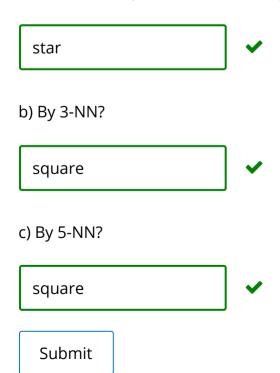
3/3 points (graded)

In the picture below, there are nine training points, each with label either square or star. These will be used to predict the label of a query point at (7, 9), indicated by a circle.



Suppose Euclidean (L_2) distance is used.

a) How will the point be classified by 1-NN? The options are square or star.



1/1 point (graded)

We decide to use 4-fold cross-validation to figure out the right value of k to choose when running k-nearest neighbor on a data set of size 10,000. When checking a particular value of k, we look at four different training sets. What is the size of each of these training sets?



Answer

Correct:

We divide the training set into four equal-sized chunks, and take turns using three of these chunks for training and one for testing. Thus the chunks are of size 2500 and the training sets are of size 7500.

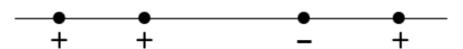
Submit

Problem 12

2/2 points (graded)

An extremal type of cross-validation is n-fold cross-validation on a training set of size n. If we want to estimate the error of k-NN, this amounts to classifying each training point by running k-NN on the remaining n-1 points, and then looking at the fraction of mistakes made. It is commonly called leave-one-out cross-validation (LOOCV).

Consider the following simple data set of just four points:



a) What is the LOOCV for 1-NN? Your answer should be a number in the range [0, 1].



Answer

Correct:

The two points on the left are correctly classified by doing 1-NN on the remaining points, while the two on the right are incorrectly classified.

b) What is the LOOCV for 3-NN?

0.25



Answer

Correct:

When doing 3-NN, every point is classified as +. Thus only one of them is misclassified.

Submit

Problem 13

2/2 points (graded)

An emergency room wishes to build a classifier that will use basic information about entering patients to decide which ones are at high risk and need to be prioritized. As soon as a patient enters the facility, the following information is collected:

- · age
- · temperature
- · heart rate
- · nine-digit identification number

Suppose a nearest neighbor classifier is used, with L_2 distance.

a) Which of these four features is least relevant to the classification problem?







b) Which of these four features is likely to have the greatest influence on the Euclidean distance function?

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age	
temperature	
heart rate	
nine-digit ider	ntification number
✓	
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Problem 14	
we do not use any	arest neighbor classification using a training set of n data points, and special data structures to speed up the classifier. Which of the describes the running time for classifying a single test point?
It does not de	pend on <i>n</i> .
lt is proportio	nal to logn.
It is proportio	nal to <i>n</i> .
lt is proportio	nal to n^2 .
✓	
Submit	
Problem 15	
0 points possible (ung	raded)

(This problem is ungraded and meant to be a thought exercise. You are not expected to enter an answer. Feel free to discuss on the forums.)

A bank decides to use nearest neighbor classification to decide which clients to offer a certain investment option. It has a database of clients that were already offered this product, along with information about whether these clients accepted or declined. This is the training set. It also has a long list of other clients who have not yet been offered this product; it wants to choose clients that are reasonably likely to accept, and will do so by using nearest neighbor using the training set.

Suppose the following information is available on each client:

- · age
- · annual income
- · amount in bank
- · zip code
- · driver license number

Which of these features do you think would be most relevant to the classification problem? Would it make sense to use Euclidean distance, or would something else be better?

Submit

Problem 16

0 points possible (ungraded)

(*This problem is ungraded and meant to be a thought exercise*. You are not expected to enter an answer. Feel free to discuss on the forums.)

How might nearest neighbor be used in a recommender system? Suppose a movie streaming service keeps track of which movies its users watch and what their ratings are. Is there a way to use this information to make movie recommendations to users? What would the data space be, and what kind of distance function would be suitable?

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Problems 17-22 correspond to "Useful distance functions for machine learning"

3/3 points (graded)

Consider the two points x = (-1, 1, -1, 1) and x' = (1, 1, 1, 1).

What is the L_2 distance between them?

2.82



Answer

Correct: It is
$$\sqrt{(-1-1)^2 + (1-1)^2 + (-1-1)^2 + (1-1)^2} = \sqrt{8}$$
.

What is the L_1 distance between them?

4

Answer

Correct: It is |-1-1| + |1-1| + |-1-1| + |1-1| = 4.

What is the L_{∞} distance between them?

2

Answer

Correct: It is $\max(|-1-1|, |1-1|, |-1-1|, |1-1|) = 2$.

Submit

Problem 18

3/3 points (graded)

For the point x = (1, 2, 3, 4) in \mathbb{R}^4 , compute the following.

a) $||x||_{1}$

10

Λ	n	SI	^,	۵	r
A	п	•	w	e	r

Correct: This is |1| + |2| + |3| + |4|.

b) $||x||_2$

5.477

Answer

Correct: This is $\sqrt{1^2 + 2^2 + 3^2 + 4^2}$.

c) $\|x\|_{\infty}$

4

Answer

Correct: This is max (1, 2, 3, 4).

Submit

Problem 19

3/3 points (graded)

For each of the following norms, consider the set of points with length ≤ 1 . In each case, state whether this set is shaped like a *ball*, a *diamond*, or a *box*.

a) ℓ_2



b) ℓ₁



c) ℓ_{∞}

box

~

Submit

Problem 20

1/1 point (graded)

How many points in \mathbb{R}^2 have $||x||_1 = ||x||_2 = 1$?

4



Submit

Problem 21

3/3 points (graded)

Which of these distance functions is a *metric*? If it is not a metric, select which of the four metric properties it violates (possibly more than one of them).

- a) Let X = R and define d(x, y) = x y.
 - this function is a metric
 - not a metric; violates non-negativity (i.e. $d(x, y) \ge 0$)
 - not a metric; violates symmetry (i.e. d(x, y) = d(y, x))
 - not a metric; violates identity (i.e. d(x, y) = 0 iff x = y)
 - not a metric; violates triangle inequality (i.e. $d(x, z) \le d(x, y) + d(y, z)$)

~

b) Let Σ be a finite set and $X = \Sigma^m$. The *Hamming distance* on X is

d(x, y) = # of positions on which x and y differ.

this function is a metric

not a metric; violates non-negativity

not a metric; violates symmetry

not a metric; violates identity

not a metric; violates triangle inequality



c) Squared Euclidean distance on R^m , that is,

$$d(x, y) = \sum_{i=1}^{m} (x_i - y_i)^2$$
.

(It might be easiest to consider the case m = 1.)

this function is a metric

not a metric; violates non-negativity

not a metric; violates symmetry

not a metric; violates identity

✓ not a metric; violates triangle inequality



Submit

Problem 22

1/1 point (graded)

Suppose d_1 and d_2 are two metrics on a space X. Define d to be their sum:

$$d(x, y) = d_1(x, y) + d_2(x, y).$$

Is *d* necessarily a metric? If not, which of the four metric properties might it violate?

- this function is a metric
- not a metric; violates non-negativity (i.e. $d(x, y) \ge 0$)
- not a metric; violates symmetry (i.e. d(x, y) = d(y, x))
- not a metric; violates identity (i.e. d(x, y) = 0 iff x = y)
- not a metric; violates triangle inequality (i.e. $d(x, z) \le d(x, y) + d(y, z)$)



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Problem 23 corresponds to "A host of prediction problems"

Problem 23

4/4 points (graded)

For each of the following prediction tasks, state whether it is best thought of as a classification problem or a regression problem.

a) Based on sensors in a person's cell phone, predict whether they are walking, sitting, or running.



classification



regression



classif	ïcation	
• regres	sion	
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) Based on ollege.	a student's high-school SAT score, predict their GPA during freshm	nan year c
classif	ication	
• regres	sion	
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l) Based on ollege.	a student's high-school SAT score, predict whether or not they will	l complete
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