

# PHY115

## Week2: Motion Along a Straight Line

Digipen

Spring 2021

## Motion Along a Straight Line

Displacement, Time, and Average Velocity

Instantaneous Velocity

Acceleration

Motion with Constant Acceleration

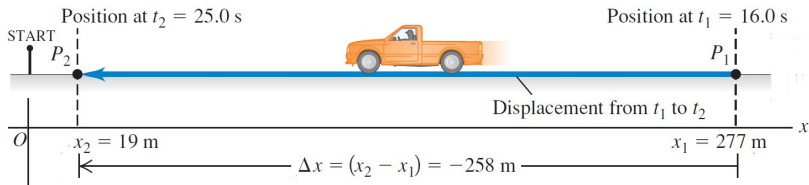
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- ▶ We introduce the physical quantities velocity and acceleration.
- ▶ Both are vectors, they have magnitude and direction.

## Average Velocity

$$v_{av} = \frac{x_2 - x_1}{t_2 - t_1} = \frac{\Delta x}{\Delta t} \quad (1)$$



## Position as a function of time

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- ▶ We can represent the variation of the position respect to the time as a function:  $x = x(t)$ .
- ▶  $x(t)$  *Does not* represent the object's path in space.
- ▶ Even for a straight-line motion,  $x(t)$  may not be a straight line.

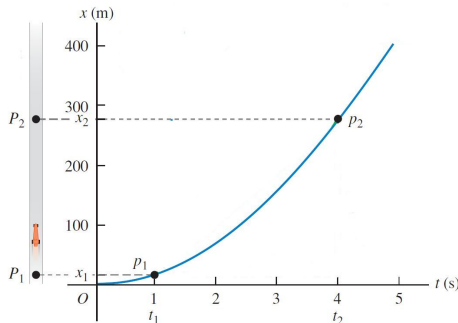


Figure: Position vs. time. Figure from Sears and Zemansky's University Physics with Modern Physics, 13th Edition.

## Plot of the average velocity

- ▶ The average velocity is the *slope* of the line  $p_1p_2$ .
- ▶ The average velocity depends only on the total displacement, not on the details of what happens inbetween.
- ▶ If distance is given in  $m$  and time in  $s$ , average velocity is measured in  $(m/s)$

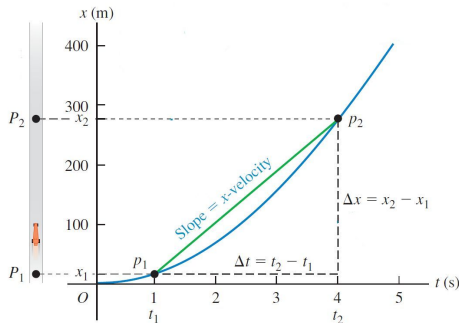


Figure: Position vs. time. Figure from Sears and Zemansky's University Physics with Modern Physics, 13th Edition.

Test your understanding.

Each of the following automobile trips takes one hour. The positive  $x$ -direction is to the east. Rank the five trips in order of average velocity from most positive to most negative. Which trips, if any, have the same average velocity? For which trip, if any, is the average  $x$ velocity equal to zero?

1. Automobile A travels 50 *km* due east.
2. Automobile B travels 50 *km* due west.
3. Automobile C travels 60 *km* due east, then turns around and travels 10 *km* due west.
4. Automobile D travels 70 *km* due east.
5. Automobile E travels 20 *km* due west, then turns around and travels 20 *km* due east.

## Instantaneous Velocity

- ▶ if we move the second point closer and closer to the first point
- ▶ the average velocity becomes the **instantaneous velocity** at point  $p_1$ .

$$v = \lim_{\Delta t \rightarrow 0} \frac{\Delta x}{\Delta t}$$

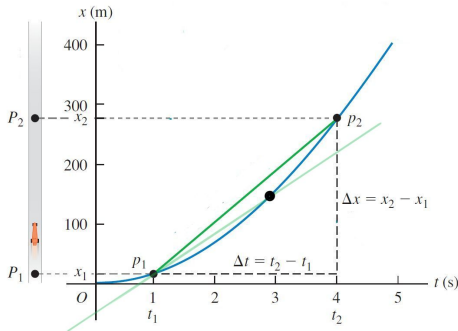


Figure: © University Physics with Modern Physics, 13th Edition.

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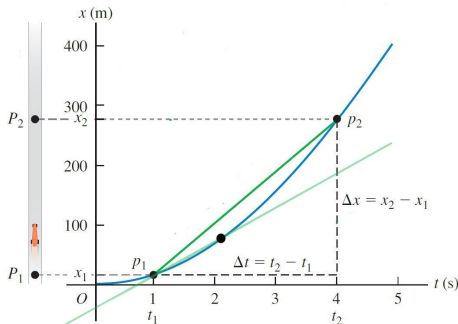


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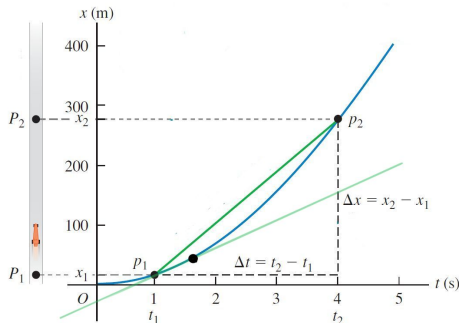


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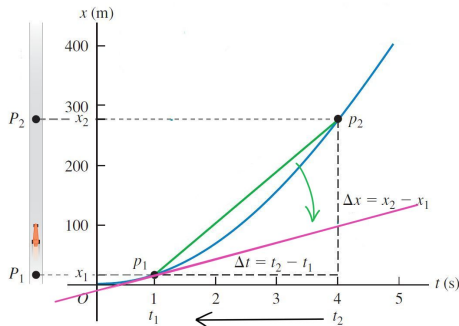


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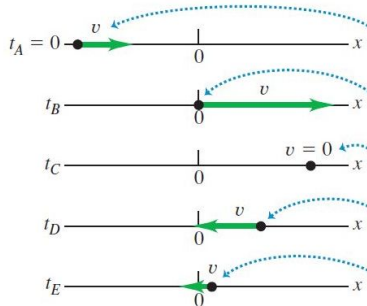
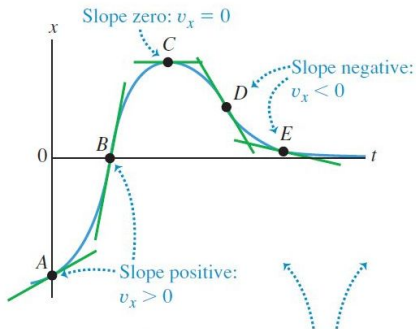
- ▶ The instantaneous velocity is a vector.
- ▶ It has the same sign than  $\Delta x$ .
- ▶ The instantaneous speed is the magnitude of the instantaneous velocity.

CAUTION!

The average speed is not the magnitude of the average velocity.

Finding Velocity on an  $x$ - $t$  Graph

- ▶ The instantaneous velocity is the slope of the curve.



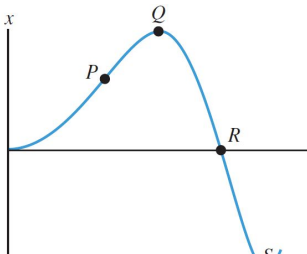
The steeper the slope (positive or negative) of an object's  $x$ - $t$  graph, the greater is the object's speed in the positive or negative  $x$ -direction.

Figure: © University Physics with Modern Physics, 13th Edition.

## Test your understanding

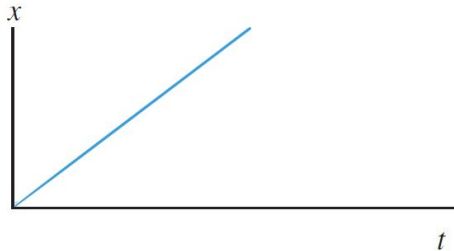
The figure is an  $x$ - $t$  graph of the motion of a particle.

1. Rank the values of the particle's velocity at the points P, Q, R, and S from most positive to most negative.
2. At which points  $v$  is positive?
3. At which points  $v$  is negative?
4. At which points  $v$  is zero?
5. Rank the values of the particle's speed at the points P, Q, R, and S from fastest to slowest.



When the velocity is constant, the average velocity is equal to the instantaneous velocity.

$$v = \frac{\Delta x}{\Delta t} \rightarrow x(t) = vt + x_0 \quad (2)$$



How is the velocity vs. time plot?

## Average and Instantaneous Acceleration

- ▶ The average acceleration is the change of the velocity in the time interval  $\Delta t$



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$$a = \frac{dv}{dt} \quad (4)$$

## Finding Acceleration on a v-t Graph

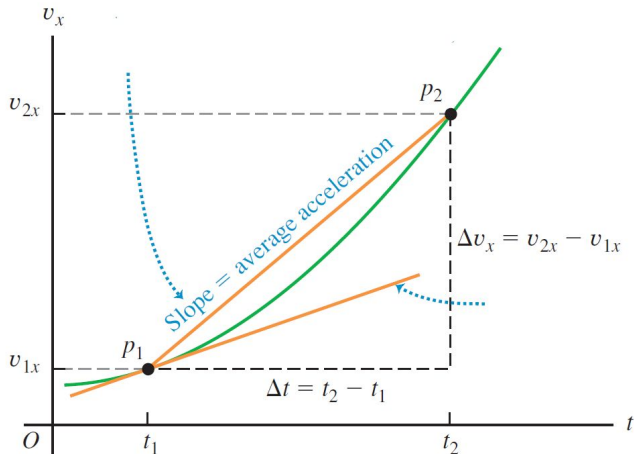
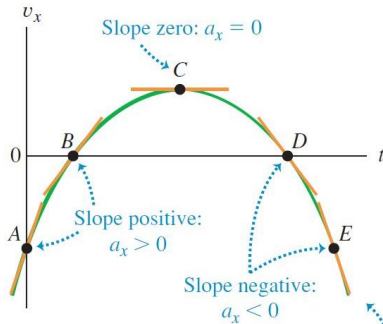


Figure: © University Physics with Modern Physics, 12th Edition

The acceleration is the slope of  $v(t)$



The steeper the slope (positive or negative) of an object's  $v_x$ - $t$  graph, the greater is the object's acceleration in the positive or negative  $x$ -direction.

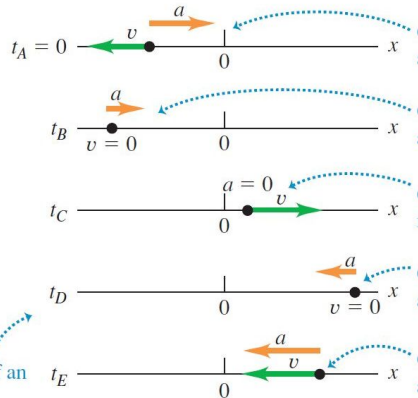
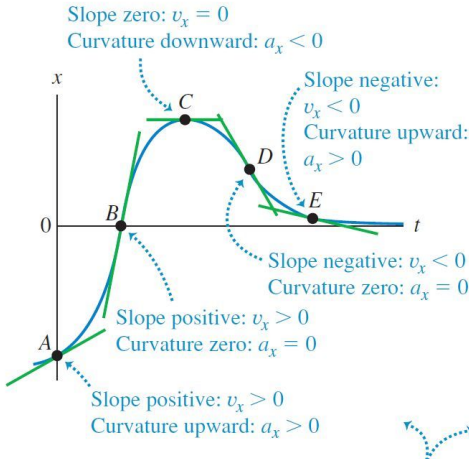


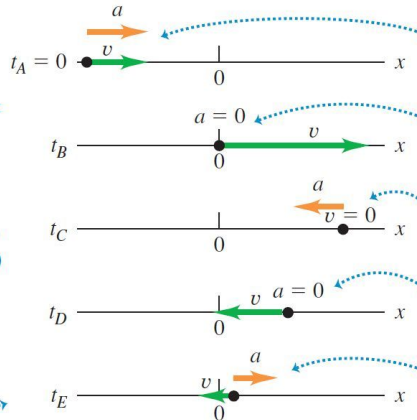
Figure: © University Physics with Modern Physics, 13th Edition.

## Finding Acceleration on a $x$ - $t$ Graph

(a)  $x$ - $t$  graph



(b) Object's motion



- ▶ If the curve is concave up, the acceleration is positive.

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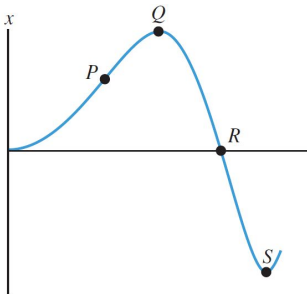


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## Test your understanding

1. At which of the points P, Q, R, and S is the x-acceleration positive?
2. At which points is the x-acceleration negative?
3. At which points does the x-acceleration appear to be zero?
4. At each point state whether the velocity is increasing, decreasing, or not changing.



- ▶ straight-line motion with constant acceleration

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- ▶ the velocity changes at the same rate throughout the motion.

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- ▶ the velocity changes at the same rate throughout the motion.
  - ▶ falling body when the effects of the air are not important.

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if  $t_1 = 0$ ,  $v_1 = v_0$  and  $v_2 = v \rightarrow v = at + v_0$

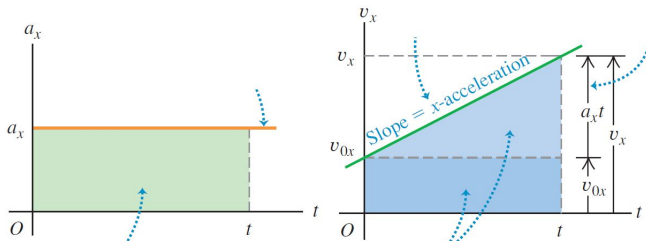


Figure: © University Physics with Modern Physics, 13th Edition.

What is  $x(t)$ ?

Let's use the expression for the average velocity,

$$v_{av} = \frac{x - x_0}{t}$$

When the acceleration is constant, the average velocity is also

$$v_{av} = \frac{v + v_0}{2}$$

And..we already know that  $v = at + v_0$

Then...

$$x = x_0 + v_0 t + \frac{1}{2}at^2 \quad (6)$$

What is  $x(t)$ ? Example: object motion,  $v_0 = 0$  and  $x_0 = 0$

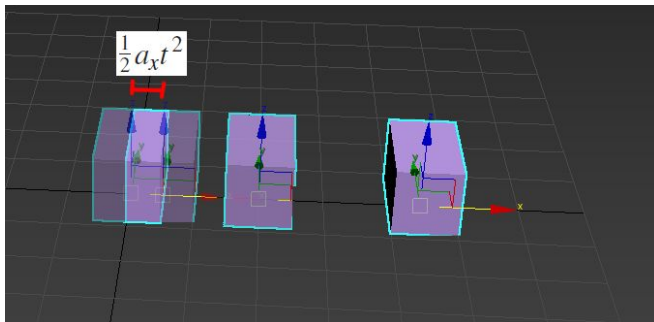


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$x(t)$  is a parababola

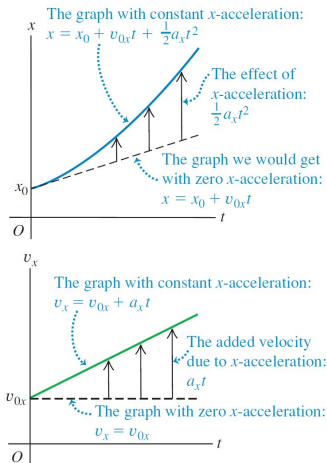


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Example: Let's analyze the motion for the following graphs

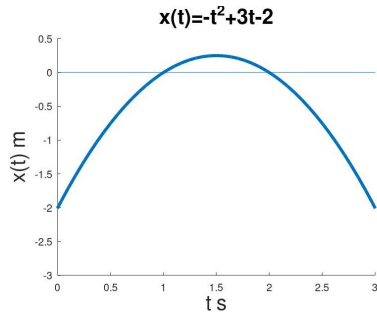
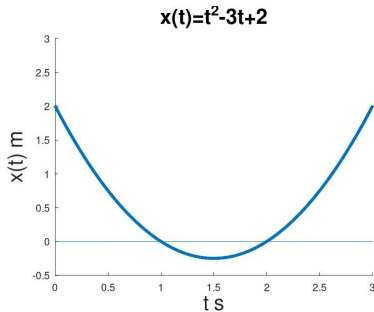


Figure: © University Physics with Modern Physics, 13th Edition.

## DISCUSSION QUESTIONS

The top diagram in the figure represents a series of highspeed photographs of an insect flying in a straight line from left to right (in the positive  $x$ -direction). Which of the graphs of the bottom graphs most plausibly depicts this insect's motion?

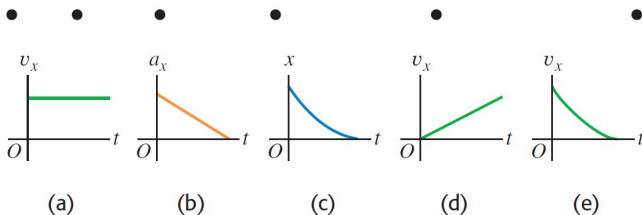


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Another useful expression valid for constant acceleration motion:

$$v = at + v_0 \rightarrow t = \frac{v - v_0}{a}$$



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$$v = at + v_0 \rightarrow t = \frac{v - v_0}{a}$$

$$\rightarrow x = \frac{1}{2}a\left(\frac{v - v_0}{a}\right)^2 + v_0\left(\frac{v - v_0}{a}\right) + x_0$$

Another useful expression valid for constant acceleration motion:

$$v = at + v_0 \rightarrow t = \frac{v - v_0}{a}$$

$$\rightarrow x = \frac{1}{2}a\left(\frac{v - v_0}{a}\right)^2 + v_0\left(\frac{v - v_0}{a}\right) + x_0$$

$$\rightarrow 2a(x - x_0) = 2v_0v - 2v^2 + v^2 - 2v_0v + v_0^2$$

By using these equations, we can solve any problem involving straight-line motion of a particle with constant acceleration.

Equation	Includes Quantities			
$v_x = v_{0x} + a_x t$	$t$		$v_x$	$a_x$
$x = x_0 + v_{0x} t + \frac{1}{2} a_x t^2 \quad (2.12)$	$t$	$x$		$a_x$
$v_x^2 = v_{0x}^2 + 2a_x(x - x_0)$		$x$	$v_x$	$a_x$
$x - x_0 = \left( \frac{v_{0x} + v_x}{2} \right) t$	$t$	$x$	$v_x$	

Figure: © University Physics with Modern Physics, 13th Edition.

## Exercise:

A motorist traveling with a constant speed of  $15 \text{ m/s}$  passes a school-crossing corner, where the speed limit is  $10 \text{ m/s}$ . Just as the motorist passes the schoolcrossing sign, a police officer on a motorcycle stopped there starts in pursuit with a constant acceleration of  $3 \text{ m/s}^2$

1. How much time elapses before the officer passes the motorist?
2. What is the officer's speed at that time?
3. At that time, what distance has each vehicle traveled?

## Testing your understanding

- ▶ Can an object with constant acceleration reverse its direction of travel? Can it reverse its direction twice?
- ▶ Under what conditions is average velocity equal to instantaneous velocity?
- ▶ Is it possible for an object to be slowing down while its acceleration is increasing in magnitude?
- ▶ To be speeding up while its acceleration is decreasing? +98