

# PHY115: Final Exam

Spring 2021

Deadline: Wednesday the 21th

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## Theory Questions (30 p)

### 1. Newton's Laws

- When are Newton's Laws valid?
- Can you use the second Law of Newton to explain the first one? How?
- Is the normal force the reaction pair of the weight? Why not? or why yes?

### 2. Linear Momentum

- Define Linear Momentum.
- Write the 2nd Law of Newton in terms of the linear momentum.
- When is the linear momentum conserved?
- When is a component conserved?
- Give an example in which the linear momentum is not conserved, but one of its coordinates is.
- EXTRA CREDIT (5 p): Find a scene on a Movie or in your animation short to illustrate the previous point, attach the link to the scene.

### 3. Angular Momentum

- Define Torque and Angular Momentum.
- Write the equation that relates the angular momentum and torque.
- Write the equation for Angular Momentum that is equivalent to the definition of Linear Momentum.
- Write the equation for Torque that is equivalent to the 2nd Law of Newton.
- When is the Angular Momentum conserved?
- Give an example in which the Angular Momentum is conserved.
- EXTRA CREDIT (5 p): Find a scene on a Movie or in your animation short to illustrate the previous point, attach the link to the scene.

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## Test your understanding (20 p)

1. A helicopter has a large main rotor that rotates in a horizontal plane and provides lift. There is also a small rotor on the tail that rotates in a vertical plane. What is the purpose of the tail rotor? (Hint: If there were no tail rotor, what would happen when the pilot changed the angular speed of the main rotor?).
2. A bullet spins on its axis as it emerges from a rifle. Explain how this prevents the bullet from tumbling and keeps the streamlined end pointed forward.
3. A client brings a treasured ball to your engineering firm, wanting to know whether the ball is solid or hollow. Design a simple, inexpensive experiment that you could perform quickly, without injuring the precious ball, to find out whether it is solid or hollow.

## Exercises (50 p)

### 1: Billiard Physics

A cue ball (a uniform solid sphere of mass  $m$  and radius  $R$ ) is at rest on a level pool table. Using a pool cue, you give the ball a sharp, horizontal hit of magnitude  $F$  at different heights (see figure 1 panels a-d) In panel (a)  $h$  is defined so that the ball will roll without slipping. In panel (b), the hit height is higher than  $h$ . In panel (c) the hit is right in the center of the ball, and in panel (d) the hit height is lower than  $h$ .

- In panels 1-4 of the figure 1, we can observe how the ball will move after the hit. Match each one of the panels a-d with the corresponding motion after the hit shown in panels 1-4.
- What is the acceleration of the center of mass after the hit in terms of the friction force and  $m$ ?
- What is the torque after the hit in terms of the friction force and  $R$ ?

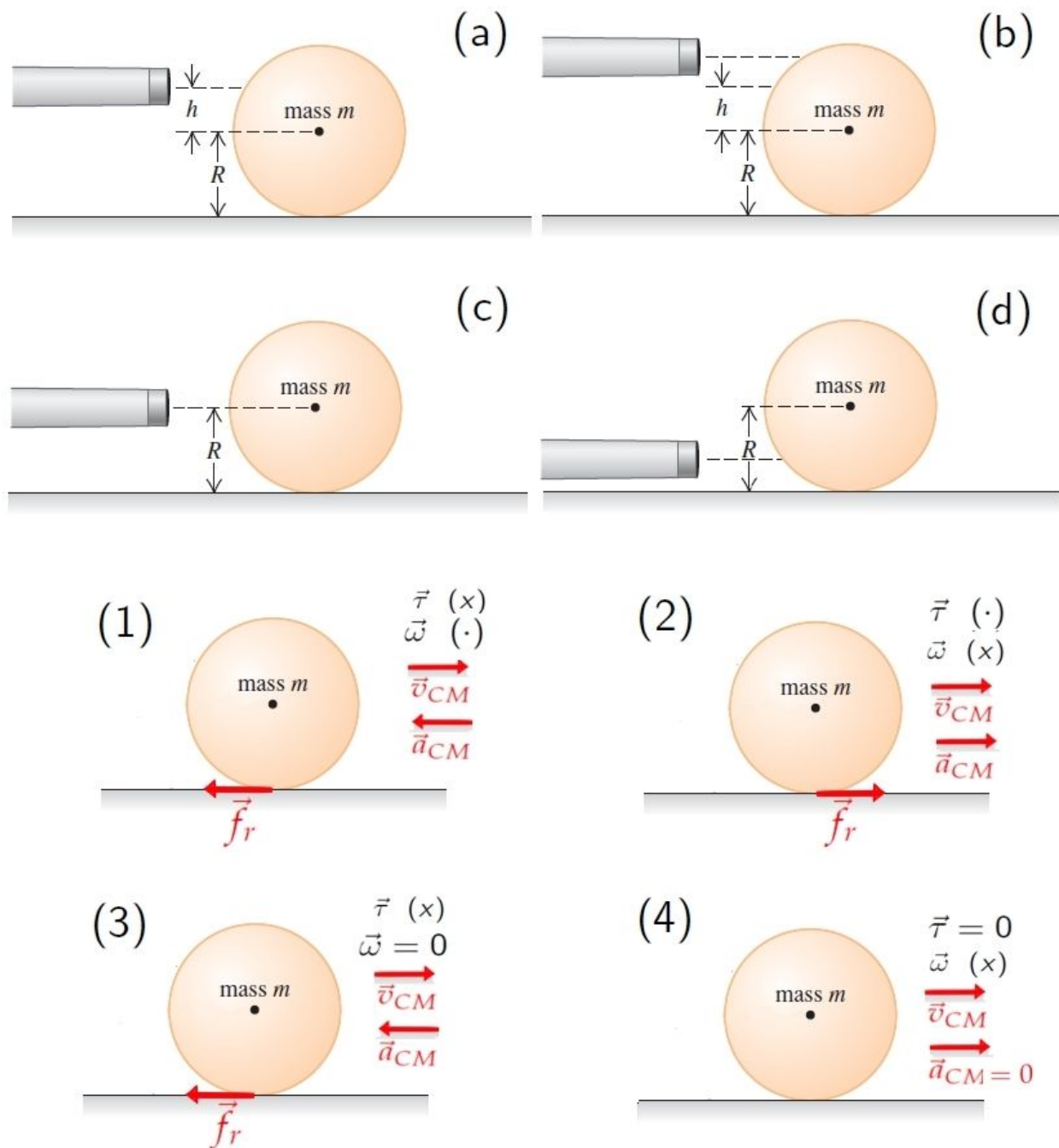


Figure 1: Panels (a) to (d):  $h$  is defined so that the ball will roll without slipping. In panel (b), the hit height is higher than  $h$ . In panel (c) the hit is right in the center of the ball, and in panel (d) the hit height is below. Panels (1) to (4): motion after the hit .

## 2: Elastic Collision

Consider a ball that bounces with a wall on a horizontal surface without friction. If the collision is elastic, the kinetic energy of the ball is conserved, and the magnitude of the

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linear momentum after the collision is equal to the initial:

$$|\vec{p}_f| = |\vec{p}_i| \quad (1)$$

Proof that the initial angle ( $\theta_i$ ) is equal to the final angle ( $\theta_f$ ).

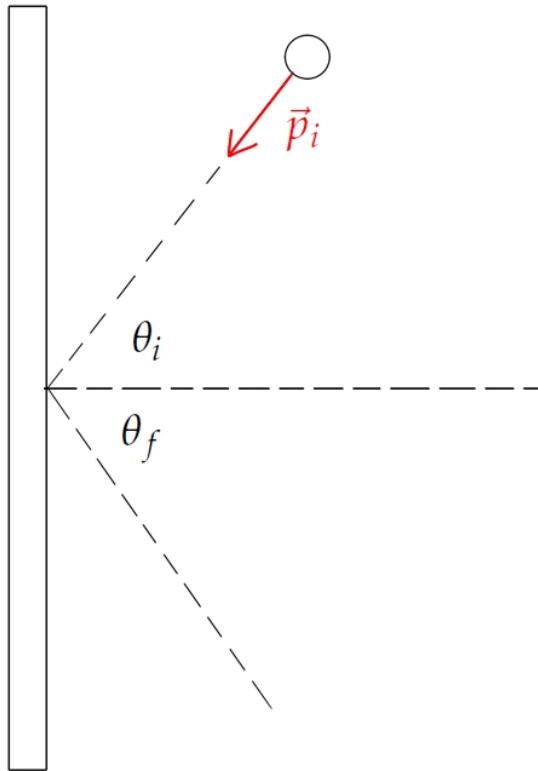


Figure 2: Ball bouncing with a wall in an horizontal surface without friction.

Hint= Which component of  $\vec{p}$  is conserved?

### 3: Light and materials

Find and explain the difference in the parameters for the materials shown in the figure 2.

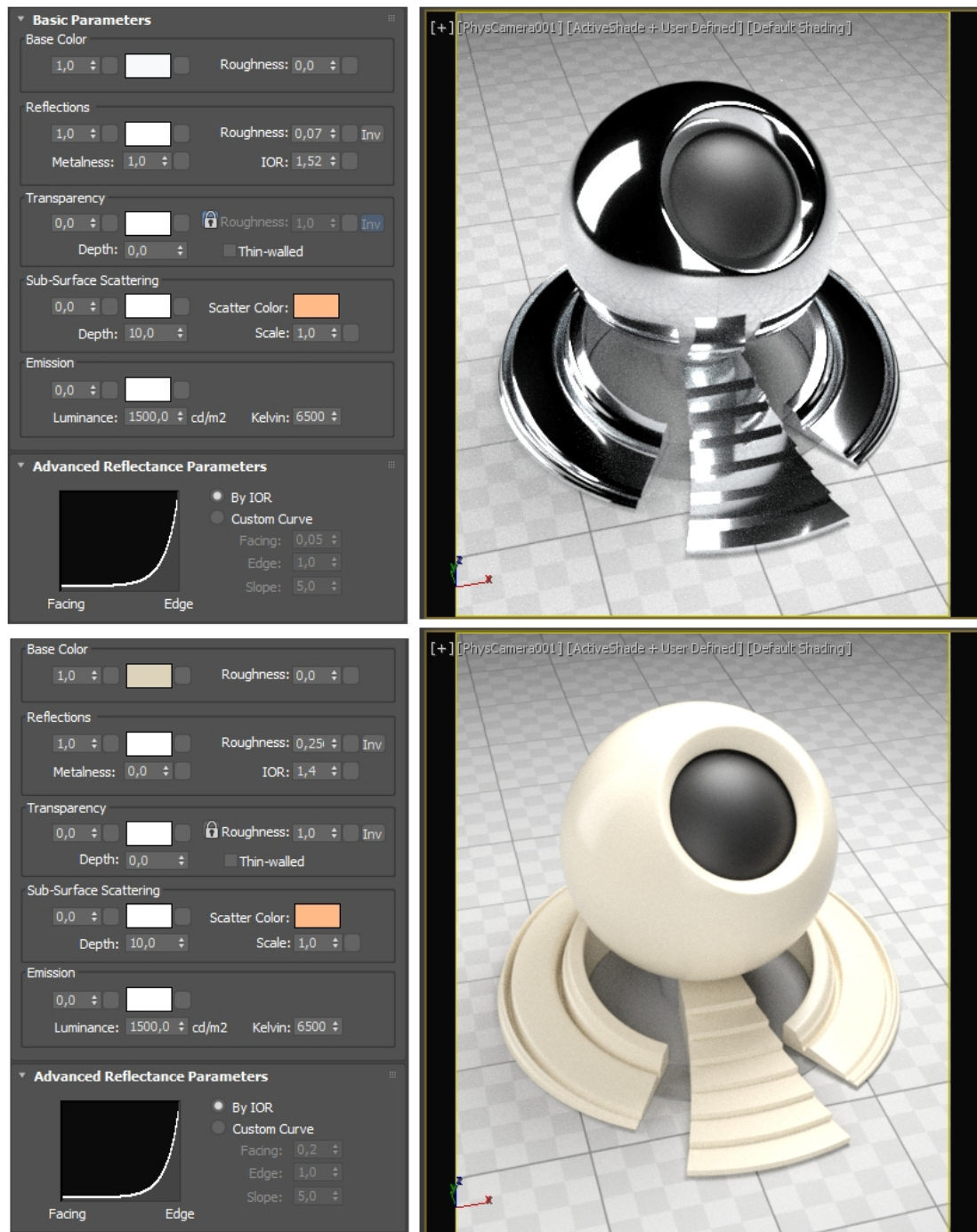


Figure 3: Interaction of light with a metal (top panel) and a non-metallic material (lower panel).