## **PHY250**

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Digipen

Fall 2020

#### Electromagnetic waves

Introduction

Electric Field

Magnetic Field

Electromagnetic Radiation

ightharpoonup Changing Magnetic Field ightarrow Changing Electric Field

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- lacktriangle Changing Electric Field ightarrow Changing Magnetic Field

Electromagnetic Wave: Wave of Electric and Magnetic Field

- ightharpoonup Changing Magnetic Field ightarrow Changing Electric Field
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Electromagnetic Wave: Wave of Electric and Magnetic Field

Changing Electric Field  $\rightarrow$  Changing Magnetic Field  $\rightarrow$  Changing Electric Field

- ► Changing Magnetic Field → Changing Electric Field
- ightharpoonup Changing Electric Field ightarrow Changing Magnetic Field

Electromagnetic Wave: Wave of Electric and Magnetic Field

Changing Electric Field  $\rightarrow$  Changing Magnetic Field  $\rightarrow$  Changing Electric Field

The light is an electromagnetic wave that can propagate through space.

To describe an electromagnetic wave we have to know first:

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- what is an Electric Field?
- what is a Magnetic Field?

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#### Electric Field

Force between two point charged particles:

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$$F_{12} = \text{force on 1}$$
  $F_{21} = \text{force on 2}$  due to 1

 $\vec{\mathbf{F}}_{12} \longrightarrow \vec{\mathbf{F}}_{21}$ 

(a)

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Force between two point charged particles:

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$$\vec{F_{12}} = rac{1}{4\pi\epsilon_0} rac{Q_1 Q_2}{r_{12}^2} \hat{r}_{12}$$
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Where  $\epsilon_0$  is the permitivity of free space,

$$\epsilon_0 = 8.85 \times 10^{-12} \frac{C^2}{Nm^2}$$
 (2)

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## Electric Field

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charge  $\propto n \cdot e$ , *n* integer, it is quantized.



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Then, the electric field generated by a charge Q is:

$$E = \frac{1}{4\pi\epsilon_0} \frac{Q}{r^2} \tag{6}$$

Electric Field of more than one particle:

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#### Electric Field

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 (8)

Superposition principle.

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### Electric Field

$$dE = \frac{1}{4\pi\epsilon_0} \frac{dQ}{r^2}, \quad dQ = \rho dV \tag{9}$$

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$$E_{x} = \int dE cos\theta, \quad E_{y} = \int dE sin\theta$$
 (11)

#### Electric Potential

Work made by a constant force:

$$w = F \cdot d = qEd \tag{12}$$

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Definition of Electric Potential: Volt

$$V = \frac{U}{a} \tag{14}$$

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Unit:

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Unit:

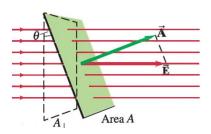
$$[V] = \frac{J}{C} \tag{16}$$

In general,

$$\Delta V = -\int \vec{E} \cdot d\vec{\ell} \tag{17}$$

Flux of a constant field through an area:

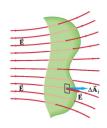
Flux of a constant field through an area:



$$\Phi_E = E \cdot A cos\theta = \vec{E} \cdot \vec{A}$$

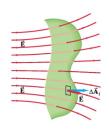
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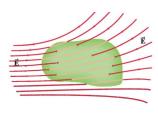
$$d\Phi_E = \vec{E} \cdot \vec{A} \rightarrow \Phi_E = \int \vec{E} \cdot \vec{A}$$

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## Electric Flux

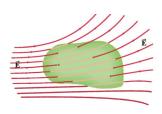
Electric flux through a closed surface.

Electric flux through a closed surface.



General case,

Electric flux through a closed surface.



General case,

$$\oint \vec{E} \cdot \vec{A} = 0$$

Gaus Law: Relates the Electric Flux with the total charge enclosed inside a closed surface.

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Basically, this law says that if the flux crossing a closed surface is different from zero, then it is generated by a charge inside the surface.

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### Gaus Law

 $\mathsf{Gaus} \to \mathsf{Coulomb}$ 

Gaus → Coulomb

Consider a point charge enclosed into an sphere,

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$$\oint \vec{E} \cdot d\vec{A} = E4\pi r^2 \to E = \frac{1}{4\pi r^2} \frac{Q}{\epsilon_0}$$
(19)

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 (19)

 $\mathsf{Coulomb} \to \mathsf{Gaus}$ 

$$\oint \vec{E} \cdot d\vec{A} = \oint \frac{1}{4\pi\epsilon_0} \frac{Q}{r^2} dA = \frac{Q}{4\pi r^2} 4\pi r^2 = \frac{Q}{\epsilon_0}$$
 (20)

#### Electric Current

Electric Current: is generated by charge in motion.

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Units:

$$[I] = \frac{C}{s} = A$$
, Ampere

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## Ohm's Law

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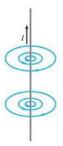
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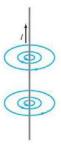
$$[R] = \frac{V}{A} = \Omega, \quad Ohm \tag{23}$$



Sources of Magnetic Fields: Ampere's Law

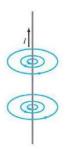


Sources of Magnetic Fields: Ampere's Law



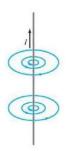


Sources of Magnetic Fields: Ampere's Law



$$\oint \vec{B} \cdot d\vec{\ell} = \mu_0 I_{enclosed}$$

Sources of Magnetic Fields: Ampere's Law

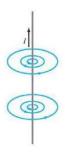


$$\oint \vec{\mathcal{B}} \cdot d\vec{\ell} = \mu_0 I_{enclosed}$$

$$\oint Bd\ell = B2\pi r = \mu_0 I$$



Sources of Magnetic Fields: Ampere's Law



$$\oint \vec{B} \cdot d\vec{\ell} = \mu_0 I_{enclosed}$$

$$\oint Bd\ell = B2\pi r = \mu_0 I$$

$$\rightarrow = B = \frac{\mu_0 I}{2\pi r} \qquad (24)$$

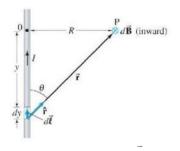
The unit of the magnetic field is Tesla,

$$[B] = \frac{N}{Am} \tag{25}$$

The constant  $\mu_0$  is the **Vacuum Magnetic Permeability**.

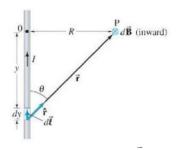
$$\mu_0 = 4\pi \times 10^{-7} \frac{T}{mA} \tag{26}$$

## Biot-Savat Law



$$d\vec{B} = \frac{\mu_0}{4\pi} I \frac{d\vec{\ell} \times \hat{r}}{r^2} \qquad (27)$$

## Biot-Savat Law



$$d\vec{B} = \frac{\mu_0}{4\pi} I \frac{d\vec{\ell} \times \hat{r}}{r^2} \qquad (27)$$

$$\rightarrow \vec{B} = \int \frac{\mu_0}{4\pi} I \frac{d\vec{\ell} \times \hat{r}}{r^2} \quad (28)$$

## Force due to a Magnetic Field

Force on a current due to a magnetic Field:

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$$\vec{F} = I\vec{\ell} \times \vec{B} \tag{29}$$

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Force on a point charge due to a magnetic Field:

Force on a current due to a magnetic Field:

$$\vec{F} = I\vec{\ell} \times \vec{B} \tag{29}$$

Force on a point charge due to a magnetic Field:

$$\vec{F} = q\vec{v} \times \vec{B} \tag{30}$$

Total force due to an electric and magnetic field:

Total force due to an electric and magnetic field:

$$\vec{F} = q(\vec{E} + \vec{v} \times \vec{B}) \rightarrow Lorentz \ Equation$$
 (31)

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### Example: Magnet



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In some materials called **Ferromagnetic**, the angular momentum of electrons are aligned so that they create a resultant macroscopic magnetic field.

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In some materials called **Ferromagnetic**, the angular momentum of electrons are aligned so that they create a resultant macroscopic magnetic field.

Iron - Cobalt - Nickel

When the electric and magnetic fields are static, the are separate entities. But when they are changing, we can not treat them separately When the electric and magnetic fields are static, the are separate entities. But when they are changing, we can not treat them separately

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A changing magnetic field generates a changing electric field that generates a changing magnetic field.

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### $\rightarrow \text{Maxwell Equations}$

A changing magnetic field generates a changing electric field that generates a changing magnetic field.

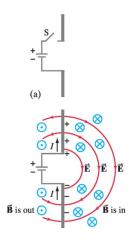
### $\rightarrow$ Wave traveling in the espace

# Maxwell Equations

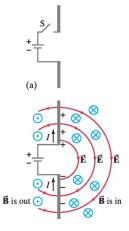
#### TABLE E-1 Maxwell's Equations in Free Space<sup>†</sup>

Integral form	Differential form
$\oint \vec{\mathbf{E}} \cdot d\vec{\mathbf{A}} = \frac{Q}{\epsilon_0}$	$ec{f  abla} \cdot ec{f E}  = rac{ ho}{\epsilon_0}$
$\oint \vec{\mathbf{B}} \cdot d\vec{\mathbf{A}} = 0$	$\vec{\nabla} \cdot \vec{\mathbf{B}} = 0$
$\oint \vec{\mathbf{E}} \cdot d\vec{\boldsymbol{\ell}} = -\frac{d\Phi_B}{dt}$	$\vec{\nabla} \times \vec{\mathbf{E}} = -\frac{\partial \vec{\mathbf{B}}}{\partial t}$
$\oint \vec{\mathbf{B}} \cdot d\vec{\boldsymbol{\ell}} = \mu_0 I + \mu_0 \epsilon_0 \frac{d\Phi_E}{dt}$	$\vec{\nabla} \times \vec{\mathbf{B}} = \mu_0 \vec{\mathbf{j}} + \mu_0 \epsilon_0 \frac{\partial \vec{\mathbf{E}}}{\partial t}$
$\vec{\nabla}$ stands for the delegarator $\vec{\nabla} = \hat{i} \frac{\partial}{\partial z} + \hat{i} \frac{\partial}{\partial z} + \hat{k} \frac{\partial}{\partial z}$ in Cartesian coordinates	

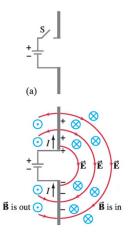
 $<sup>^{\</sup>dagger}\vec{\nabla}$  stands for the *del operator*  $\vec{\nabla} = \hat{\mathbf{i}} \frac{\partial}{\partial x} + \hat{\mathbf{j}} \frac{\partial}{\partial y} + \hat{\mathbf{k}} \frac{\partial}{\partial z}$  in Cartesian coordinates





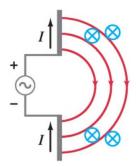


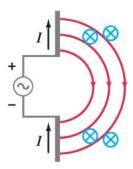
ightharpoonup We connect two rod to a battery ightarrowElectric Field



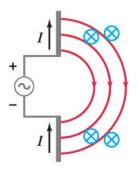
- $\hbox{$\stackrel{\bullet}{\blacktriangleright}$ We connect two rod to a battery} \rightarrow \\ \hbox{$\stackrel{\bullet}{\hbox{Electric Field}}$ }$
- lacktriangle The charge is re-distributed ightarrow Magnetic field

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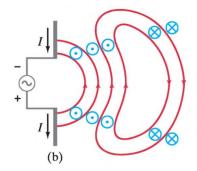


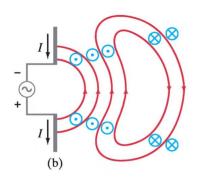


ightharpoonup sinusoidal voltage ightarrow Alternating Current

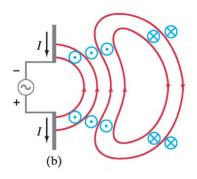


- lacktriangledown sinusoidal voltage o Alternating Current
- ightharpoonup variable Electric and Magnetic Fields.

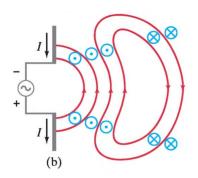




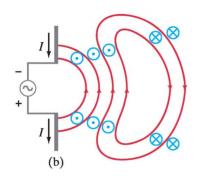
Old Field lines fold back to connect to some of the new lines → closed loops



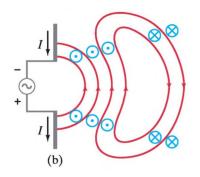
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- They are on their way to distant points.

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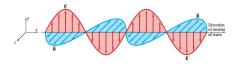
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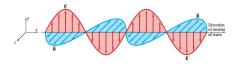
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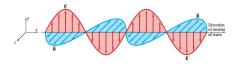
Transverse wave



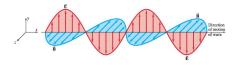
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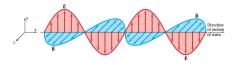


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EM waves are produced by electric charges that are oscillating

 $\rightarrow$  are undergoing into acceleration in general.

### Electromagnetic Waves



- Transverse wave
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EM waves are produced by electric charges that are oscillating  $\rightarrow$  are undergoing into acceleration in general.

Accelerated electric charges give rise to electromagnetic waves

Let's consider a region of free space where there are no charges or conduction currents, Q = 0, I = 0

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- Plane waves
- Waves traveling in the x-direction,  $\vec{v} = v\hat{\imath}$

The Maxwell equation take the form:

$$\begin{split} & \oint \vec{\mathbf{E}} \cdot d\vec{\mathbf{A}} = 0 \\ & \oint \vec{\mathbf{B}} \cdot d\vec{\mathbf{A}} = 0 \\ & \oint \vec{\mathbf{E}} \cdot d\vec{\mathbf{\ell}} = -\frac{d\Phi_B}{dt} \\ & \oint \vec{\mathbf{B}} \cdot d\vec{\mathbf{\ell}} = \mu_0 \epsilon_0 \frac{d\Phi_E}{dt} . \end{split}$$

$$E = E_y = E_0 \sin(kx - \omega t) \tag{32}$$

$$B = B_z = B_0 \sin(kx - \omega t) \tag{33}$$

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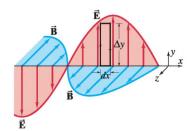
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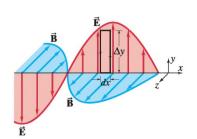
$$B = B_z = B_0 \sin(kx - \omega t) \tag{33}$$

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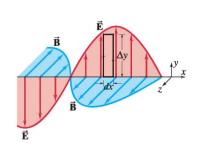
$$k = \frac{2\pi}{\lambda}, \quad \omega = 2\pi f, \quad f\lambda = \frac{\omega}{k} = v$$

Introduction
Electric Field
Magnetic Field
Electromagnetic Radiation



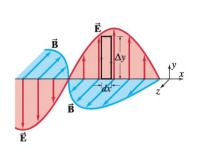


$$\oint \vec{E} d\vec{\ell} = \frac{-d\Phi_B}{dt}$$



$$\oint \vec{E} d\vec{\ell} = \frac{-d\Phi_B}{dt}$$

$$\oint \vec{E} d\vec{\ell} = (E + dE)\Delta y - E\Delta y = dE\Delta y$$

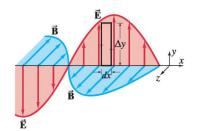


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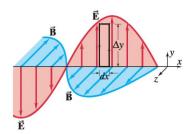
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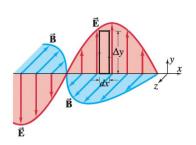
Introduction
Electric Field
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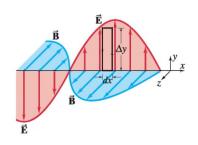
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The flux is,

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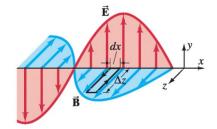
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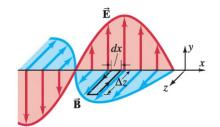
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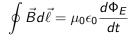
$$\rightarrow \frac{dE}{dx} = -\frac{dB}{dt} \rightarrow \frac{\partial E}{\partial x} = -\frac{\partial B}{\partial t} \quad (34)$$

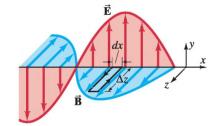
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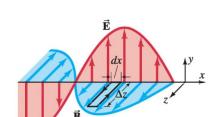
$$\oint \vec{B} d\vec{\ell} = \mu_0 \epsilon_0 \frac{d\Phi_E}{dt}$$







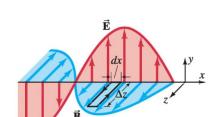
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$$\to v = \frac{1}{\mu_0 \epsilon_0} \frac{1}{v}$$

Then, the velocity of propagation of the wave is,

$$v^2 = \frac{1}{\epsilon_0 \mu_0} \to v = \frac{1}{\sqrt{\epsilon_0 \mu_0}} = c \tag{36}$$

c is the speed of light,

$$c = 3 \times 10^8 \ m/s \tag{37}$$

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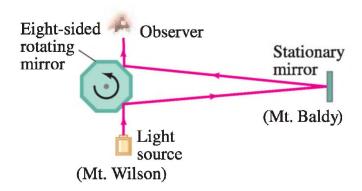
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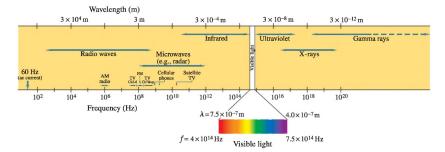


# Measuring the speed of light

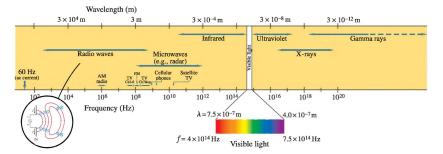
#### Michelson's Experiment



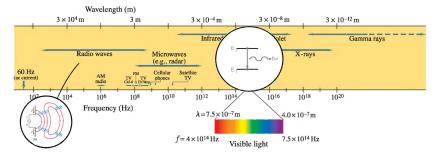
$$c = f\lambda$$



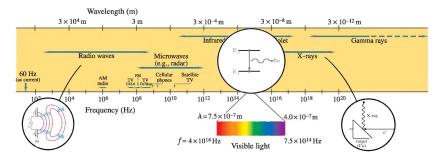
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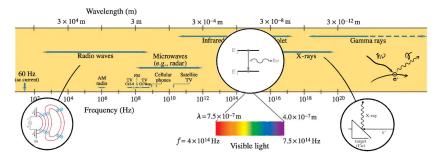
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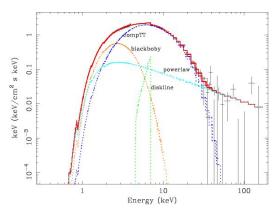


Example:

BB radiation 
$$o I \propto rac{1}{e^{rac{\hbar 
u}{kT}}-1}$$

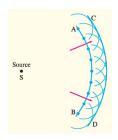
Synchrotron radiation  $ightarrow 
u^{lpha}$  Power Law

Application: knowing what process are occurring in an Astrophysical Object.



# Huygens' principle

Every point on a wave front can be considered as a source of tiny wavelets that spread out in the forward direction at the speed of the wave itself The new wave front is the envelope of all the wavelets— that is, the tangent to all of them.



What happens when waves impinge on an obstacle?

→ waves bend in behind an obstacle

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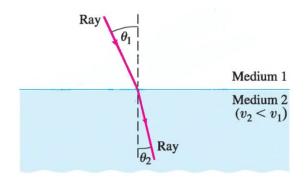
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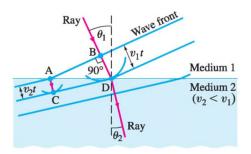
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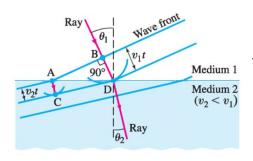


What happens when a waves front changes the medium?

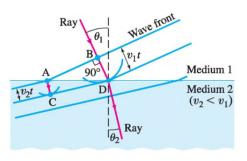
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is the refraction index.

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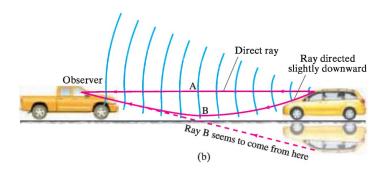
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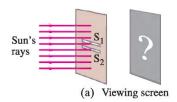
 $\mu \to {\sf The}$  resistance of a material to be penetrated by a magnetic field.

 $\epsilon o$  The resistance of a material to be penetrated by an electric field.

Example: Mirages



# Interference: Youn's double-slit Experiment









viewing screen (actual)

If light consists of tiny particles, we might expect to see two bright lines on a screen placed behind the slits as in (b). But instead a series of bright lines are seen, as in (c). Young was able to explain this result as a wave-interference phenomenon.

# Interference: Youn's double-slit Experiment

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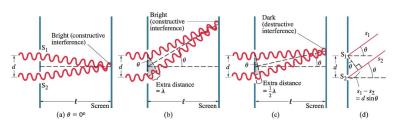
- plane waves
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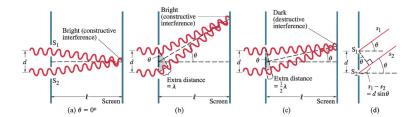
The waves leaving the two small slits spread out as shown:

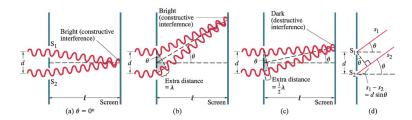
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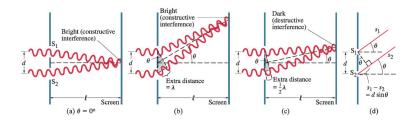
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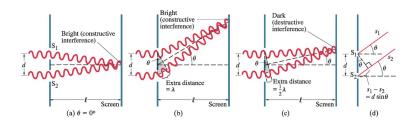




► Constructive interference  $\rightarrow$  the path of 2 rays differs in  $n\lambda$ , n integer.

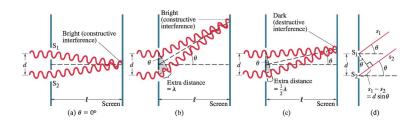


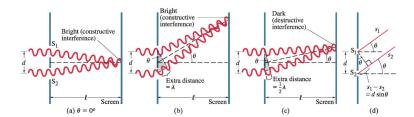
- ► Constructive interference  $\rightarrow$  the path of 2 rays differs in  $n\lambda$ , n integer.
- ▶ Destructive interference  $\rightarrow$  the path of 2 rays differs in  $(2n+1)\lambda/2$ , n integer.

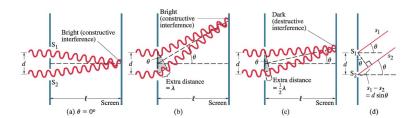


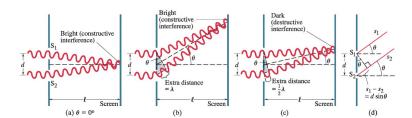
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Thus, there will be a series of bright and dark lines (or fringes) on the viewing screen.

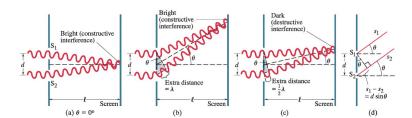






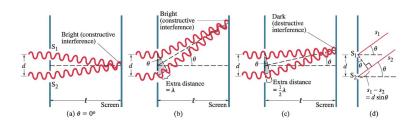


- ▶ *d* << ℓ
- ► The rays are essentially parallel.



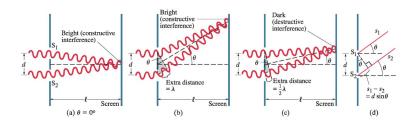
- ▶ d << ℓ</p>
- ► The rays are essentially parallel.
- $\blacktriangleright$   $\theta$  is the angle they make with the horizontal.

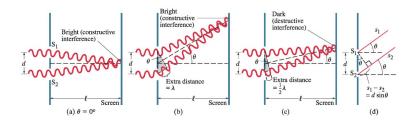


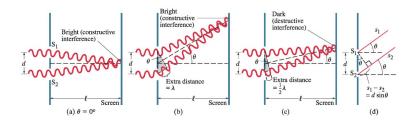


- ▶ d << ℓ</p>
- ► The rays are essentially parallel.
- ightharpoonup heta is the angle they make with the horizontal.
- ▶ The extra distance traveled by the lower ray is  $dsin\theta$



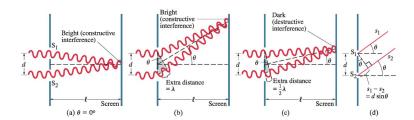






Where the bright lines fall?

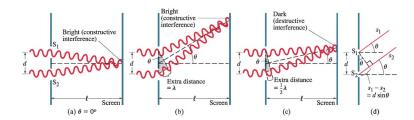
Constructive interference:



Where the bright lines fall?

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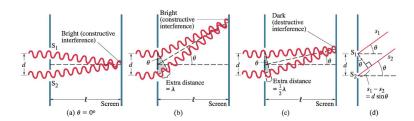
$$sin\theta = \frac{n\lambda}{d} = \frac{X}{\ell}$$
 (44)

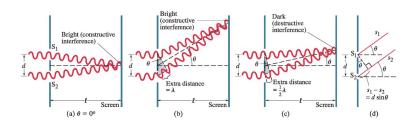


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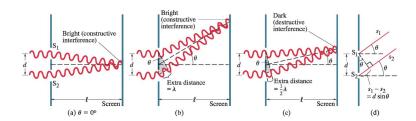
Constructive interference:

$$sin\theta = \frac{n\lambda}{d} = \frac{X}{\ell} \to X = \ell \frac{n\lambda}{d}$$
 (45)





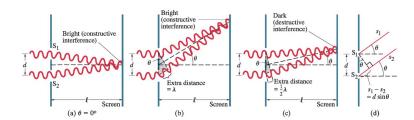
Destructive interference:



Destructive interference:

$$\sin\theta = \frac{(2n+1)\lambda}{d} = \frac{X}{\ell} \tag{46}$$





Where the bright lines fall?

Destructive interference:

$$sin\theta = \frac{(2n+1)\lambda}{d} = \frac{X}{\ell} \to X = \ell \frac{(2n+1)\lambda}{d}$$
 (47)

#### Conceptual Example:

(a) Will there be an infinite number of points on the viewing screen where constructive and destructive interference occur, or only a finite number of points?

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- (a) Will there be an infinite number of points on the viewing screen where constructive and destructive interference occur, or only a finite number of points?
- (b) Are neighboring points of constructive interference uniformly spaced, or is the spacing between neighboring points of constructive interference not uniform?

#### Conceptual Example:

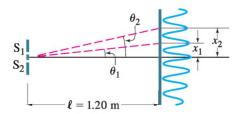
(a) The maximum value of n is the integer closest in value but smaller than d/X.

#### Conceptual Example:

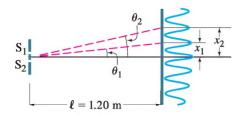
- (a) The maximum value of n is the integer closest in value but smaller than d/X.
- (b) For small values of  $\theta$  the spacing is nearly uniform. For non-small values  $\to$  the spacing gets larger as  $\theta$  gets larger.

#### Example:

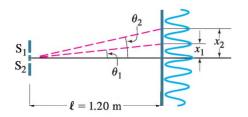
A screen containing two slits 0.100 mm apart is 1.20 m from the viewing screen. Light of wavelength A=500 nm falls on the slits from a distant source. Approximately how far apart will adjacent bright interference fringes be on the screen?



#### Example:

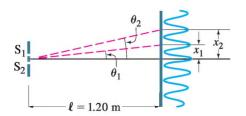


#### Example:



$$\sin\theta_1 = \frac{m\lambda}{d} = \frac{(1)(500 \times 10^{-9} \ m)}{1.00 \times 10^{-4} \ m} = 5.00 \times 10^{-3} \tag{48}$$

#### Example:



$$\sin\theta_1 = \frac{m\lambda}{d} = \frac{(1)(500 \times 10^{-9} \ m)}{1.00 \times 10^{-4} \ m} = 5.00 \times 10^{-3}$$
 (48)

 $\theta << 1 \rightarrow sin\theta \sim \theta$  and  $x_1/\ell = tan\theta_1 \sim \theta_1$ 

Example:

then,

$$x_1 \sim \ell \theta_1 = (1.20 \ m)(5.00 \times 10^{-3}) = 6.00 \ mm$$
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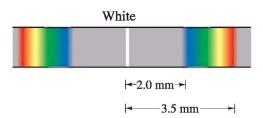
$$x_2 \sim \ell \theta_2 = \ell \frac{2\lambda}{d} = 12.00 \text{ mm} \tag{50}$$

Thus the lower order fringes are 6.00 mm apart.

#### Conceptual Example:

(a) What happens to the interference pattern, if the incident light (500 nm) is replaced by light of wavelength 700 nm? (b) What happens instead if the wavelength stays at 500 nm but the slits are moved farther apart?

Except for the zeroth-order fringe at the center, the position of the fringes depends on wavelength.



$$ightharpoonup E_{\theta} = E_1 + E_2$$

$$\triangleright$$
  $E_{\theta} = E_1 + E_2$ 

$$ightharpoonup E_1 = E_{10} sin\omega t$$

- ►  $E_{\theta} = E_1 + E_2$
- $ightharpoonup E_1 = E_{10} sin\omega t$
- $E_2 = E_{20} sin(\omega t + \delta), \ \frac{\delta}{2\pi} = \frac{dsin\theta}{\lambda}$

We can work with this expression and prove that:

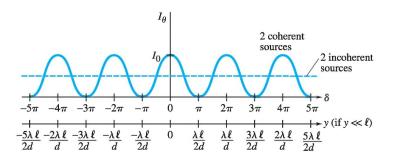
$$\frac{I_{\theta}}{I_0} = \frac{E_{\theta 0}^2}{(2E_0)^2} = \cos^2 \frac{\delta}{2}$$
 (51)

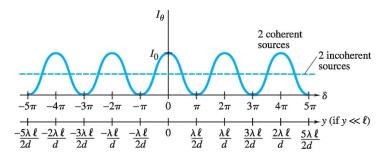
$$I_{\theta} = I_0 \cos^2 \left( \frac{\pi d \sin \theta}{\lambda} \right) \tag{52}$$

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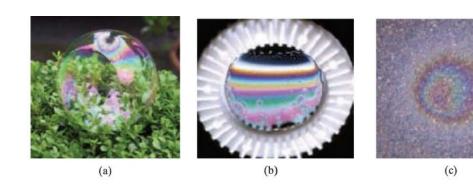
small  $\theta$ ,  $sin\theta = \frac{y}{\ell}$ 

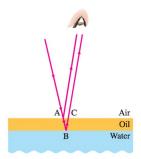
$$I_{\theta} = I_0 \left[ \cos \left( \frac{\pi d}{\lambda \ell} y \right) \right]^2 \tag{53}$$





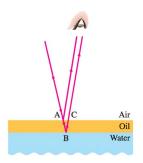
The intensity pattern shows a series of maxima of equal height, and is based on the assumption that each slit (alone) would illuminate the screen uniformly. This is never quite true, if we consider diffraction.





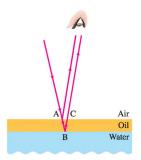
If path difference ABC is,

• equals  $m\lambda_n \rightarrow$  constructive interference



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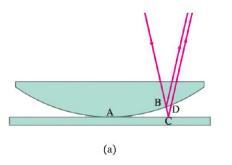
- equals  $m\lambda_n \rightarrow$  constructive interference
- equals  $(2m+1)\lambda_n \rightarrow$  destructive interference

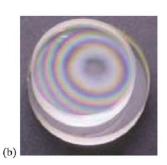


If path difference ABC is,

- equals  $m\lambda_n \rightarrow$  constructive interference
- equals  $(2m+1)\lambda_n \rightarrow$  destructive interference
- $\lambda_n = \lambda/n$ , n is the index of refraction

## Newton's Rings





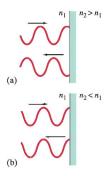
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Electric Field
Magnetic Field
Electromagnetic Radiation

# Newton's Rings

Why is the center dark?

# Newton's Rings

Why is the center dark?



a beam of light reflected by a material with index of refraction greater than that of the material in which it is traveling, changes phase by  $180^{\circ}$  or  $\frac{1}{2}$  cycle;



► The thin film stood vertically.



- The thin film stood vertically.
- Gravity has pulled much of the soapy water toward the bottom.

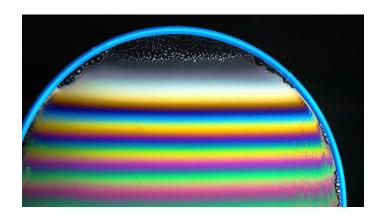


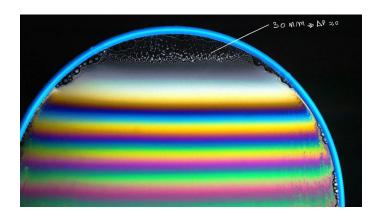
- The thin film stood vertically.
- Gravity has pulled much of the soapy water toward the bottom.
- The top section is so thin → light reflected from the front and back surfaces have almost no path difference.

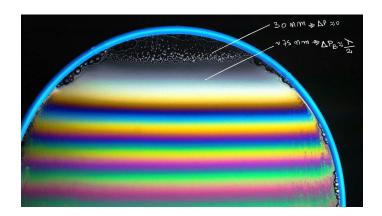


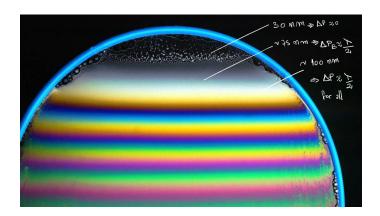
- The thin film stood vertically.
- Gravity has pulled much of the soapy water toward the bottom.
- ➤ The top section is so thin → light reflected from the front and back surfaces have almost no path difference.
- ▶  $180^{\circ}$  → two reflected waves are out of phase for all wavelengths.

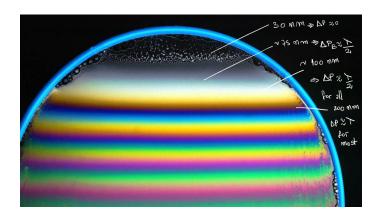
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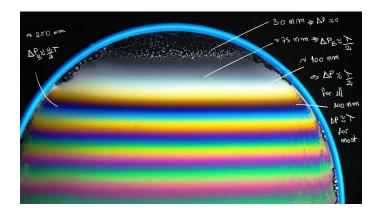




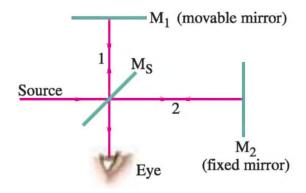








#### Michelson Interferometer



Does Huygens' principle apply to sound waves? To water waves?

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- We can hear sounds around corners but we cannot see around corners; yet both sound and light are waves. Explain the difference.

- Does Huygens' principle apply to sound waves? To water waves?
- We can hear sounds around corners but we cannot see around corners; yet both sound and light are waves. Explain the difference.
- ► Two rays of light from the same source destructively interfere if their path lengths differ by how much?

Monochromatic red light is incident on a double slit and the interference pattern is viewed on a screen some distance away. Explain how the fringe pattern would change if the red light source is replaced by a blue light source.

- Monochromatic red light is incident on a double slit and the interference pattern is viewed on a screen some distance away. Explain how the fringe pattern would change if the red light source is replaced by a blue light source.
- Compare a double-slit experiment for sound waves to that for light waves. Discuss the similarities and differences.