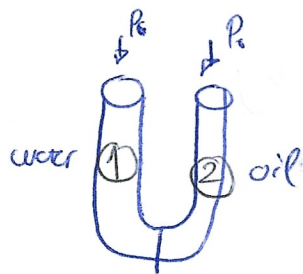


①

water

$$0,25\text{m} \rightarrow 25\text{cm}$$

$$\rho = 1\text{ g/cm}^3$$

oil

$$0,25\text{m} \rightarrow 25\text{cm}$$

$$\rho = 0,80\text{ g/cm}^3$$

- a) The water is more dense than oil, this means that water will "push" the oil, as the oil "sits" on top of water. The level of water will decrease by h and the level of oil will increase by the same amount.

We know that the pressure at a certain height is $P = \rho g y + P_0$ due to Pascal's Principle. We also know that the pressure at the center is constant (is the same for the oil and water).

$$P_0 + \rho_w g(y_1 - h) = P_0 + \rho_o g(y_2 + h) + P_0$$

$$y_1 - h = 0,8 y_2 + 0,8 h$$

$$y_1 - 0,8 y_2 = 1,8 h; \text{ In this case } y_1 = y_2 \text{ (} \approx 25\text{cm)}$$

$$y - 0,8 y = 1,8 h; \quad y(1 - 0,8) = 1,8 h; \quad h = \frac{0,2 y}{1,8} = 0,11 y$$

$$y = 25\text{cm}; \quad h = 0,11 \cdot 25 = 2,777\text{cm}$$

Solution: The level of water will ~~increase~~ decrease by $2,777\text{cm} \rightarrow 25 - 2,777 = 22,22\text{cm}$
and level of oil ~~decreases~~ increases by $2,777\text{cm} \rightarrow 25 + 2,777 = 27,77\text{cm}$

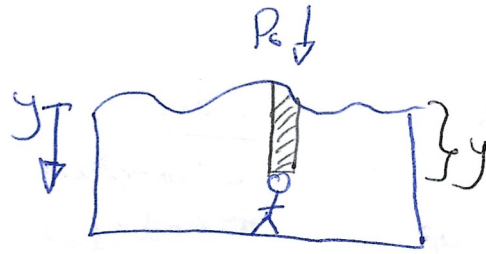
- b) ~~II~~ If both had equal densities the level would remain the same as both liquids would be almost the same (for example, water on both sides). The pressure on both sides would be the same.

II) If the density was less, the water would "push" the oil much more. The height of oil would increase significantly and the height of water decrease to compensate the difference in density.

② Eardrum diameter = $8.2 \text{ mm} = 8,2 \cdot 10^{-3} \text{ m}$

" radius = $4,1 \cdot 10^{-3} \text{ m}$

$\rho_{\text{water}} = 1,03 \cdot 10^3 \text{ kg/m}^3$



Pascal's Principle: $P = \rho g h + P_0$

$P = \frac{F}{A}$

if the force is $1,5 \text{ N} + P_0 \rightarrow$

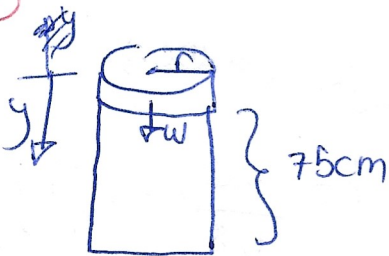
~~$P = 1,5 \text{ N} + P_0$~~ , $\Delta P = 1,5 \text{ N}$

$F_i = 1,5 + F_{\text{atm. pressure}}$; $\Delta F = 1,5 \text{ N}$

$P = \frac{\Delta F}{A}$; $\Delta F = P \cdot A$; $\Delta F = \rho g y \cdot A$

$\Delta F = \rho g y \cdot \pi r^2$; $y = \frac{\Delta F}{\rho g \pi r^2} = \frac{1,5}{(1,03 \cdot 10^3) \cdot 9,8 \cdot \pi \cdot (4,1 \cdot 10^{-3})^2}$
 $= 2,8 \text{ m}$

③



$\rho_{\text{oil}} = 0,850 \text{ g/cm}^3 = 850 \text{ kg/m}^3$

$r = 0,15 \text{ cm} = 0,15 \text{ m}$

$W = m \cdot g$

a) $A_{\text{disk}} = \pi \cdot r^2 = 706,5 \text{ cm}^2 = 0,07 \text{ m}^2$

Gauge Pressure $P = \frac{F}{A}$; $P = \frac{45 \text{ N}}{0,07 \text{ m}^2} = \underline{642,85 \text{ Pa}}$

b) I) 83 N applied $\rightarrow 83 + 45 = 128 \text{ N}$

New gauge Pressure $\rightarrow P_g = \frac{128}{0,07} = 1828,6 \text{ Pa}$

At bottom of tank height = $0,75 \text{ m}$; Pascal's Principle: $P = \rho g y + P_g$

$P = 850 \cdot 9,8 \cdot 0,75 + 1828,6 = \underline{8076,1 \text{ Pa}}$

II) At middle of tank the height = $0,75/2 = 0,375 \text{ m}$

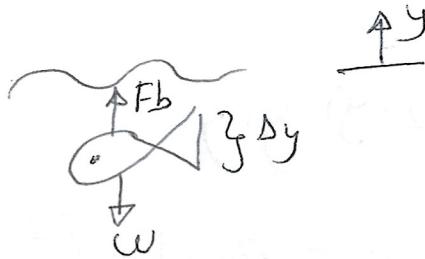
$P = 850 \cdot 9,8 \cdot 0,375 + 1828,6 = \underline{4952,35 \text{ Pa}}$

④ a) If fish float it's because they have similar density to water (they are submerged)

$$\rho_{\text{fish}} \approx \rho_{\text{water}}$$

b) 2.75 kg fish increases volume by 10% $\rightarrow +10\%$

Net force?



If they float then $F_b = w$ (Net force: $F_b - w = 0$)

$$w = 2.75 \cdot 9.8 = 26.95 \text{ N}$$

Archimedes principle: $F_b = \rho_w \cdot g \cdot \underbrace{A \cdot \Delta y}_{\text{volume}}$

$$\text{As } F_b = w; |F_b| = 26.95 \text{ N}$$

The volume is increased by 10% = 0.1

$$F_b = \rho_w g \cdot 0.1 \text{ vol} + \text{vol} = \rho_w g \cdot 1.1 \text{ Volume} = 1.1 F_b$$

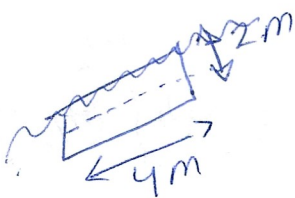
$$\cancel{F_b = w = m g} \quad 1.1 F_b = 1.1 \cdot 26.95 = \underline{29.7 \text{ N}}$$

c) Net external force?

Water exerts 29.7 N up and weight 26.95 N down

~~net force of Newton~~: $F_b - w = 29.7 - 26.95 = 2.75$ upwards

⑤



top view side view We need to calculate torque at every point

$$P = \frac{F}{A}; \quad F = PA; \quad dF = p \cdot dA$$

$$dF = \rho g y \cdot dA$$

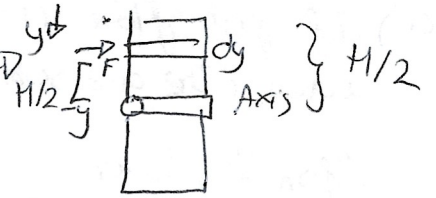
base height = $4 \cdot dy$
= $b \cdot dy$

$$dF = \rho g y \cdot b dy$$

$\vec{\tau} = \vec{r} \times \vec{F}$; In this case \vec{r} = distance from axis of rotation to where the force is applied

~~$\rho = 1000$~~

As the hinge is at the center $\rightarrow r = (H/2 - y)$



$$\tau_{\text{of upper part}} = \int_0^{H/2} d\tau = \int_0^{H/2} \rho g b \cdot r y \cdot dy$$

$$= \tau_1 = \rho g b \int_0^{H/2} (H/2 - y) \cdot y dy$$

$$= \rho g b \int_0^{H/2} \left(\frac{H}{2} y - y^2 \right) dy = \rho g b \left[\frac{H}{2} \int_0^{H/2} y dy - \int_0^{H/2} y^2 dy \right]$$

$$= \rho g b \left[\frac{H}{2} \cdot \frac{y^2}{2} \Big|_0^{H/2} - \frac{y^3}{3} \Big|_0^{H/2} \right]$$

$$= \rho g b \left[\frac{H}{4} y^2 \Big|_0^{H/2} - \frac{y^3}{3} \Big|_0^{H/2} \right]$$

$$= \rho g b \left[\left(\frac{H}{4} \cdot \frac{H^2}{4} \right) - \left(\frac{H}{4} \cdot 0 \right) \right] - \left[\frac{H^3}{8} - 0 \right]$$

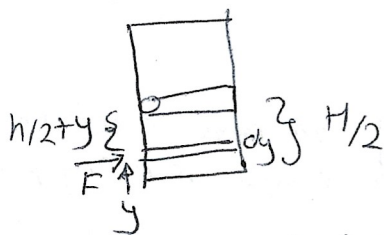
$$= \rho g b \left[\frac{H^3}{16} - 0 \right] - \left[\frac{H^3}{8} \right] = \rho g b \left[\frac{3H^3}{48} - \frac{2H^3}{48} \right]$$

$$= \rho g b \left[\frac{H^3}{48} \right] \Rightarrow \rho_{\text{water}} = \frac{1 \text{ kg}}{1000 \text{ m}^3} \Rightarrow 1000 \cdot 9.8 \cdot 4 \cdot \frac{8}{48}$$

$$= -6533.3 \text{ N}\cdot\text{m}$$

clockwise direction

Lower part



$$r = (H/2 + y)$$

Apply same as before: $\tau_2 = \int_0^{H/2} \rho g b (H/2 + y) \cdot y dy = \rho g b \int_0^{H/2} (H/2 + y) \cdot y dy$

$$= \rho g b \int_0^{H/2} \left(\frac{H}{2} y + y^2 \right) dy = \rho g b \left[\frac{H}{2} \frac{y^2}{2} \Big|_0^{H/2} + \frac{y^3}{3} \Big|_0^{H/2} \right]$$

$$= \rho g b \left[\frac{H}{4} y^2 \Big|_0^{H/2} + \frac{y^3}{3} \Big|_0^{H/2} \right] = \rho g b \left[\left(\frac{H}{4} \cdot \frac{H^2}{4} \right) + \frac{H^3}{8} \right] = \rho g b \left[\frac{H^3}{16} + \frac{H^3}{24} \right]$$

$$= \rho g b \left[\frac{3H^3}{48} + \frac{2H^3}{48} \right] = \rho g b \cdot \frac{5H^3}{48} = 1000 \cdot 9.8 \cdot 4 \cdot \frac{5 \cdot 2^3}{48} = +32666.66 \text{ N}\cdot\text{m}$$

Solution: $\tau_{\text{total}} = \tau_1 + \tau_2 = -6533.33 + 32666.66$

$$= 26133.33 \text{ N}\cdot\text{m}$$

\rightarrow counter clockwise direction