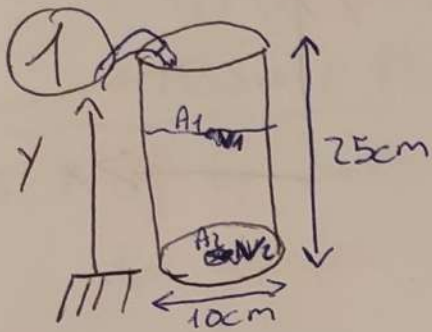


# PHY 250

## HW-2



$$Q = 2.4 \cdot 10^{-4} \text{ m}^3/\text{s} \quad A_2 = 1.5 \cdot 10^{-4} \text{ m}^2$$

Volume flow rate from the tube

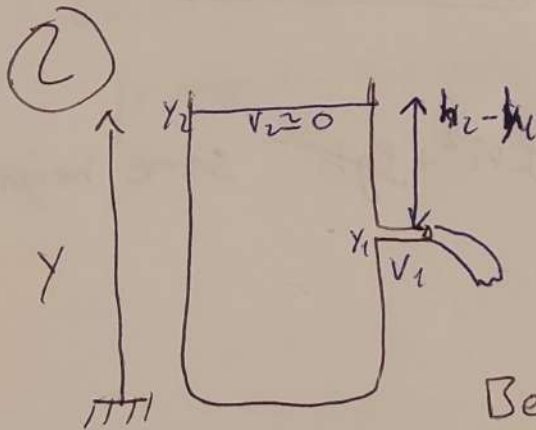
$$Q = A_2 V_2 \Rightarrow V_2 = \frac{2.4 \cdot 10^{-4} \text{ m}^3/\text{s}}{1.5 \cdot 10^{-4} \text{ m}^2} = 1.6 \text{ m/s}$$

$$Q = A_1 V_1 \Rightarrow V_1 = \frac{Q}{A_1} \approx 0 \text{ m/s} \quad (\text{since } A_1 \text{ is so big that } V_1 \text{ is almost } 0 \text{ m/s})$$

Bernoulli's Equation

$$P_0 + \frac{1}{2} \rho V_1^2 + \rho g h_1 = P_0 + \frac{1}{2} \rho V_2^2 + \rho g h_2$$

$$g h_1 = \frac{V_2^2}{2} \Rightarrow h_1 = \frac{V_2^2}{2g} = \boxed{0.13 \text{ m}}$$



From the equation of continuity we have

$$A_1 V_1 = A_2 V_2$$

$$V_2 = \frac{A_1 V_1}{A_2}$$

Bernoulli's Equation

$$P_0 + \frac{1}{2} \rho V_1^2 + \rho g h_1 = P_0 + \frac{1}{2} \rho V_2^2 + \rho g h_2$$

$$g(h_2 - h_1) = \frac{1}{2} (V_1^2 - V_2^2)$$

$$2g(h_2 - h_1) = V_1^2 - V_2^2$$

$$V_1^2 - \frac{A_1^2 V_1^2}{A_2^2} = 2gh$$

$$V_1^2 \left(1 - \frac{A_1^2}{A_2^2}\right) = 2gh$$

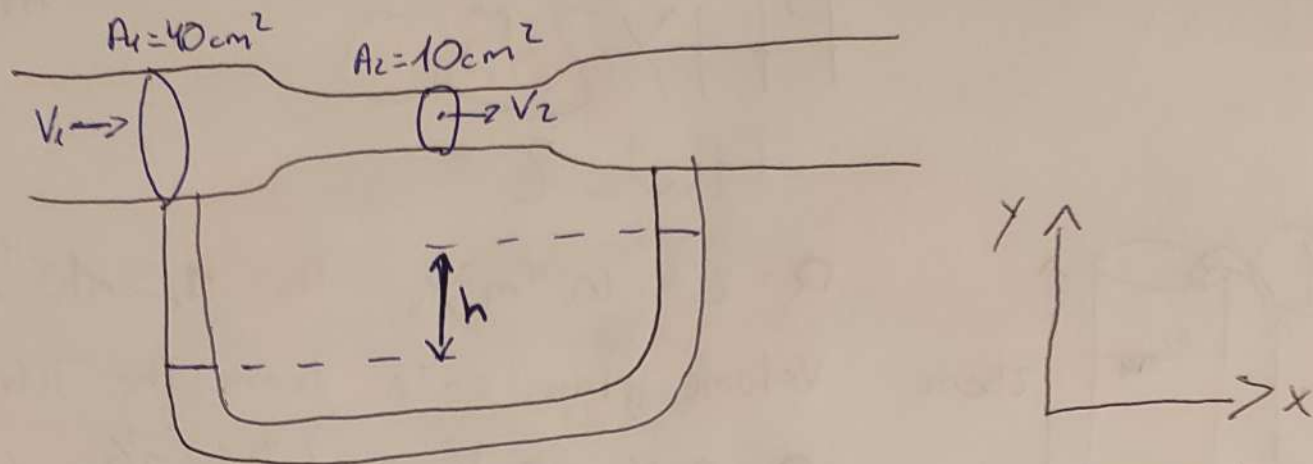
$$V_1 = \sqrt{\frac{2gh}{\left(1 - \frac{A_1^2}{A_2^2}\right)}}$$

$$A_1 \ll A_2$$

$$V_1 = \sqrt{2gh}$$

where  $h = h_2 - h_1$

3



$$Q = 6 \cdot 10^{-3} \frac{\text{m}^3}{\text{s}}$$

$$\rho_w = 997 \frac{\text{kg}}{\text{m}^3} \quad \rho_{Hg} = 13600 \frac{\text{kg}}{\text{m}^3}$$

a) Continuity Equation

$$A_1 V_1 = 6 \cdot 10^{-3} \text{ m}^3/\text{sec}$$

$$V_1 = \frac{6 \cdot 10^{-3} \text{ m}^3/\text{sec}}{40 \cdot 10^{-4} \text{ m}^2}$$

$$\boxed{V_1 = 1,5 \text{ m/s}}$$

$$A_2 V_2 = 6 \cdot 10^{-3} \text{ m}^3/\text{sec}$$

$$V_2 = \frac{6 \cdot 10^{-3} \text{ m}^3/\text{sec}}{10 \cdot 10^{-4} \text{ m}^2}$$

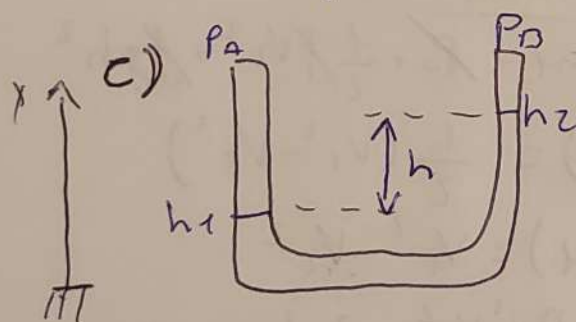
$$\boxed{V_2 = 6 \text{ m/sec}}$$

b) Bernoulli's Equation

$$P_1 + \frac{1}{2} \rho V_1^2 + \cancel{\rho g h} = P_2 + \frac{1}{2} \rho V_2^2 + \cancel{\rho g h} \quad \text{same height}$$

$$(P_1 - P_2) = \frac{\rho_w}{2} (V_2^2 - V_1^2)$$

$$\boxed{\Delta P = 16874 \text{ Pa}}$$



Bernoulli's Equation

$$P_1 + \rho_{Hg} g h_1 + \cancel{\frac{1}{2} \rho V_1^2} = P_2 + \rho_{Hg} g h_2 + \cancel{\frac{1}{2} \rho V_2^2}$$

No velocities in this situation  
(They are static)

$$(P_1 - P_2) = \rho_{Hg} \cdot g \cdot (h_2 - h_1)$$

$$\frac{\Delta P}{\rho_{Hg} \cdot g} = \Delta h$$

$$\boxed{0,126 \text{ m} = \Delta h}$$

4

Since the liquid is in free fall motion, we can use  $V^2 = V_0^2 + 2gy$  (we would reach the same conclusion using Bernoulli's equation, since pressure is constant).

Continuity equation:  $A_1 V_1 = A_2 V_2$       $A = \pi r^2$

$$V_0 \pi r_0^2 = \sqrt{V_0^2 + 2gy} \cdot \pi r^2$$

$$r = \sqrt{\frac{V_0 r_0^2}{\sqrt{V_0^2 + 2gy}}} = \sqrt{\frac{V_0}{\sqrt{V_0^2 + 2gy}}} r_0$$

b) Given  $V_0 = 1,2 \text{ m/s}$  and  $r = \frac{r_0}{2}$ , solve for  $y$

$$\frac{r_0}{2} = \sqrt{\frac{V_0}{\sqrt{V_0^2 + 2gy}}} r_0$$

$$\left(\frac{1}{2}\right)^2 = \left(\sqrt{\frac{V_0}{\sqrt{V_0^2 + 2gy}}}\right)^2$$

$$\left(\frac{1}{4}\right)^2 = \left(\frac{V_0}{\sqrt{V_0^2 + 2gy}}\right)^2$$

$$\frac{1}{16} = \frac{V_0^2}{V_0^2 + 2gy}$$

$$\frac{V_0^2 + 2gy}{16(V_0^2 + 2gy)} = \frac{16V_0^2}{16(V_0^2 + 2gy)}$$

$$y = \frac{15(1,2 \text{ m/s})^2}{2 \cdot 9,8 \text{ m/s}^2} \Rightarrow \boxed{y = 1,1 \text{ m}}$$