PHY250: Review and Introduction

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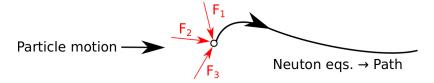
Digipen Institute

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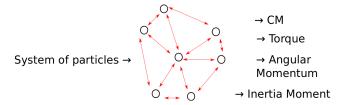


Introduction

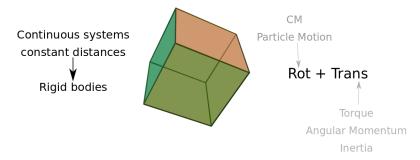
PHY250 in a nutshell Review of PHY200 In PHY 200 you studied:



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In PHY250 we are going to study fluids, we can think of them as systems of particles.



We also are going to study mechanics waves, energy traveling in a medium. We can think of them as the collective motion of the particles in a continuous system.



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- we are going to study how the energy is propagated
- finally, we are going to study the nature of light and how it interacts with different mediums

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$$\sum_{i} \vec{F}_{i} = m\vec{a} \tag{1}$$

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And you have proved that:

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Where

$$E_k = \frac{1}{2}mv^2 \tag{4}$$

is the kinetic energy.



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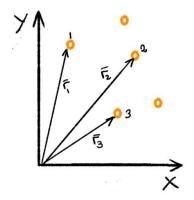
$$E = U + K = constant \tag{7}$$

So, when a force is conservative, that is, there is a function U(x) such that

$$F = -\frac{U(x)}{dx} \tag{8}$$

then, the energy of the particle is constant.

You also studied systems of N particles,:



$$\vec{p}_i = m_i \vec{v}_i$$

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$$ec{ au}_i = ec{r}_i imes ec{F}_i
ightarrow ec{ au} = \sum_i^N ec{ au}_i \quad (\textit{Torque})$$
 (11)

$$rac{d\vec{P}}{dt} = \bar{F}$$

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$$\frac{d\vec{L}}{dt} = \vec{\tau} \ (\textit{Conservation of Angular Momentum}) \tag{13}$$

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And you found the following expressions that relates the motion of the center of mass with the total external force:

$$\vec{P} = M \frac{d}{dt} (\vec{R}_{CM}) = M \vec{V}_{CM}$$
 (15)

$$\vec{F}^{\text{ext}} = M \frac{d^2}{dt^2} (\vec{R}_{CM}) = M \vec{a}_{CM} \tag{16}$$

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So the center of mass moves as a particle acted by the total external force.

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where I is the Moment of Inertia

$$I = \sum_{i}^{N} m_i r_i^2 \tag{19}$$

$$E_k = \sum_{i}^{N} E_{k,i}$$

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Tanslation of CM + Rotation Around CM

$$\vec{P} = M \vec{V}_{CM}$$

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$$\vec{F} = M\vec{a}_{CM} \leftrightarrow \vec{\tau} = I\vec{\alpha} \tag{22}$$

$$\vec{R}_{CM} = \frac{1}{M} \sum_{i}^{N} m_i \vec{r_i}$$

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