

# PHY250

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Digipen

Fall 2021

## Electromagnetic waves

## Introduction

## Electric Field

## Magnetic Field

# Electromagnetic Radiation

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- ▶ Changing Magnetic Field → Changing Electric Field

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**Electromagnetic Wave:** Wave of Electric and Magnetic Field

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Changing Electric Field → Changing Magnetic Field → Changing Electric Field

The light is an electromagnetic wave that can propagate through space.

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- ▶ what is an Electric Field?
- ▶ what is a Magnetic Field?

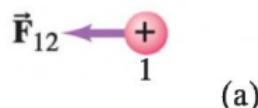
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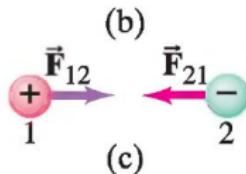
# Electric Field

Force between two point charged particles:

$F_{12}$  = force on 1  
due to 2



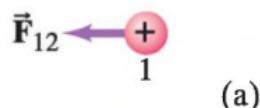
$F_{21}$  = force on 2  
due to 1



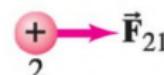
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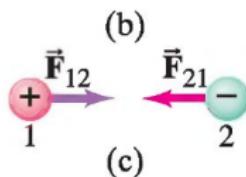
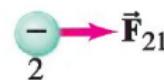
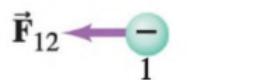
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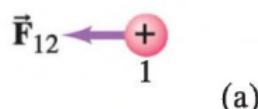
$$\vec{F}_{12} = \frac{1}{4\pi\epsilon_0} \frac{Q_1 Q_2}{r_{12}^2} \hat{r}_{12} \quad (1)$$



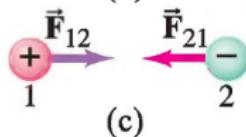
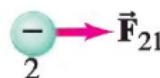
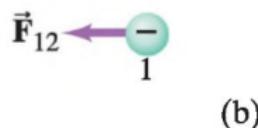
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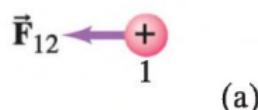
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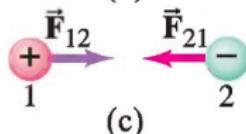
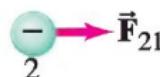
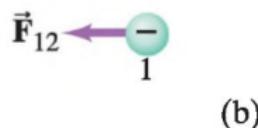
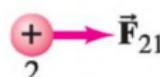
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$$\epsilon_0 = 8.85 \times 10^{-12} \frac{C^2}{Nm^2} \quad (2)$$

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charge  $\propto n \cdot e$ ,  $n$  integer, it is quantized.

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Then, the electric field generated by a charge  $Q$  is:

$$E = \frac{1}{4\pi\epsilon_0} \frac{Q}{r^2} \quad (6)$$

# Electric Field

Electric Field of more than one particle:

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$$E_x = \int dE \cos\theta, \quad E_y = \int dE \sin\theta \quad (11)$$

# Electric Potential

Work made by a constant force:

$$w = F \cdot d = qEd \quad (12)$$

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Definition of Electric Potential: Volt

$$V = \frac{U}{q} \quad (14)$$

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In general,

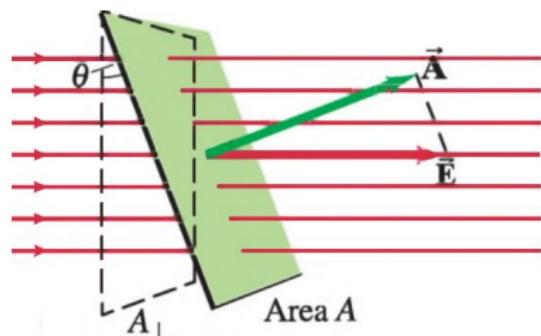
$$\Delta V = - \int \vec{E} \cdot d\vec{\ell} \quad (17)$$

# Electric Flux

Flux of a constant field through an area:

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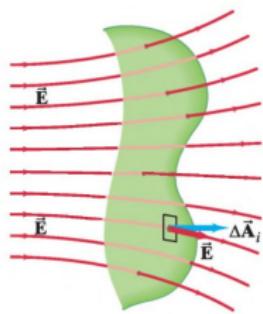
$$\Phi_E = E \cdot A \cos\theta = \vec{E} \cdot \vec{A}$$

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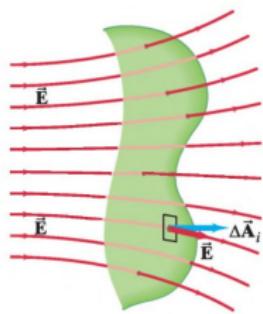
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General case,

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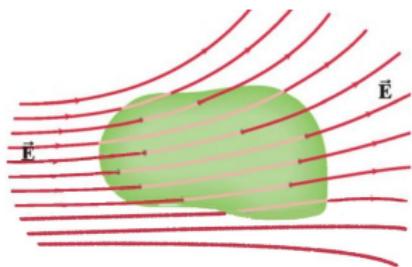
$$d\Phi_E = \vec{E} \cdot \vec{A} \rightarrow \Phi_E = \int \vec{E} \cdot \vec{A}$$

# Electric Flux

Electric flux through a closed surface.

# Electric Flux

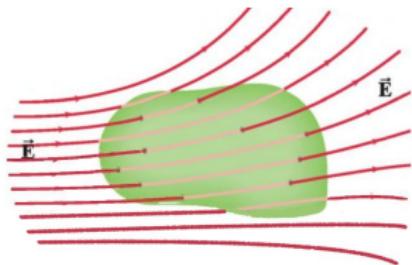
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General case,

$$\oint \vec{E} \cdot \vec{A} = 0$$

# Gaus Law

Gaus Law: Relates the Electric Flux with the total charge enclosed inside a closed surface.

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Basically, this law says that if the flux crossing a closed surface is different from zero, then it is generated by a charge inside the surface.

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$$\oint \vec{E} \cdot d\vec{A} = \oint \frac{1}{4\pi\epsilon_0} \frac{Q}{r^2} dA = \frac{Q}{4\pi r^2} 4\pi r^2 = \frac{Q}{\epsilon_0} \quad (20)$$

# Electric Current

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Units:

$$[I] = \frac{C}{s} = A, \text{ Ampere}$$

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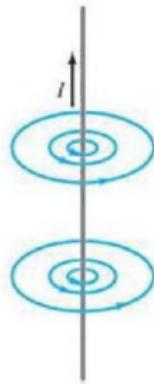
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Units:

$$[R] = \frac{V}{A} = \Omega, \quad Ohm \quad (23)$$

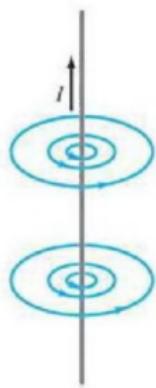
# Magnetic Field

## Sources of Magnetic Fields: Ampere's Law



# Magnetic Field

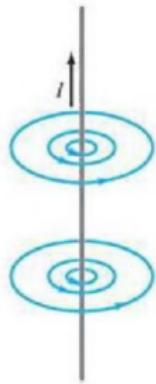
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The magnetic field generated  
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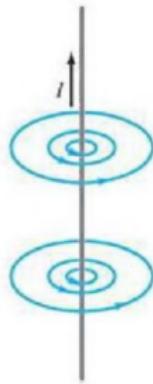


$$\oint \vec{B} \cdot d\vec{l} = \mu_0 I_{\text{enclosed}}$$

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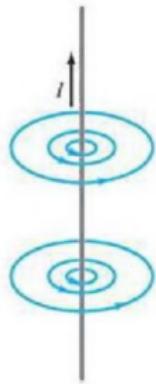
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$$\rightarrow= B = \frac{\mu_0 I}{2\pi r} \quad (24)$$

# Magnetic Field

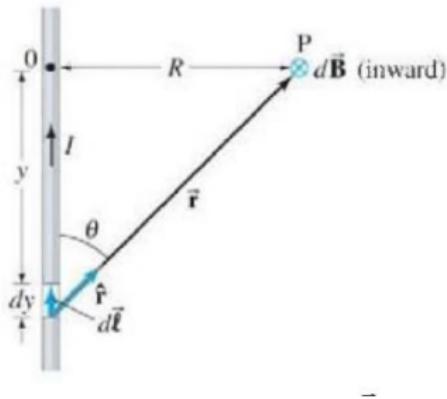
The unit of the magnetic field is Tesla,

$$[B] = \frac{N}{Am} \quad (25)$$

The constant  $\mu_0$  is the **Vacuum Magnetic Permeability**.

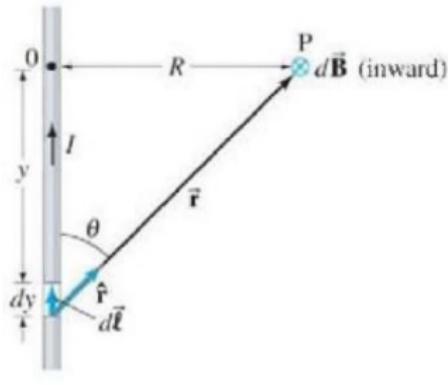
$$\mu_0 = 4\pi \times 10^{-7} \frac{T}{mA} \quad (26)$$

# Biot-Savat Law



$$d\vec{B} = \frac{\mu_0}{4\pi} I \frac{d\vec{l} \times \hat{r}}{r^2} \quad (27)$$

# Biot-Savat Law



$$d\vec{B} = \frac{\mu_0}{4\pi} I \frac{d\vec{l} \times \hat{r}}{r^2} \quad (27)$$

$$\rightarrow \vec{B} = \int \frac{\mu_0}{4\pi} I \frac{d\vec{l} \times \hat{r}}{r^2} \quad (28)$$

# Force due to a Magnetic Field

Force on a current due to a magnetic Field:

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Force on a point charge due to a magnetic Field:

$$\vec{F} = q\vec{v} \times \vec{B} \quad (30)$$

# Force due to a Magnetic Field

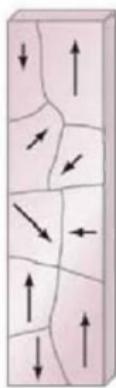
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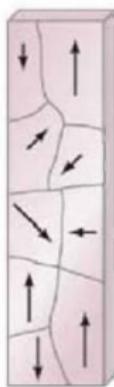
Total force due to an electric and magnetic field:

$$\vec{F} = q(\vec{E} + \vec{v} \times \vec{B}) \rightarrow \textit{Lorentz Equation} \quad (31)$$

Example: Magnet

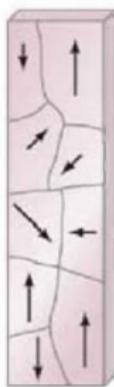


## Example: Magnet



In some materials called **Ferromagnetic**, the angular momentum of electrons are aligned so that they create a resultant macroscopic magnetic field.

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Iron - Cobalt - Nickel

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A changing magnetic field generates a changing electric field that generates a changing magnetic field.

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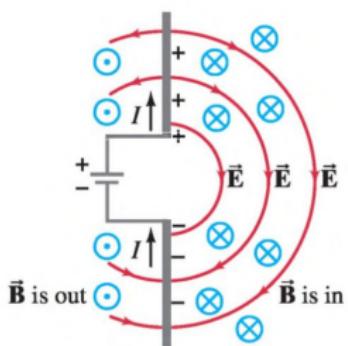
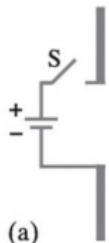
→ **Wave traveling in the space**

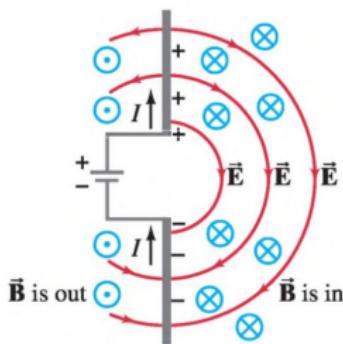
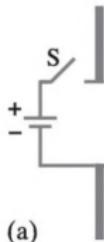
# Maxwell Equations

**TABLE E-1 Maxwell's Equations in Free Space<sup>†</sup>**

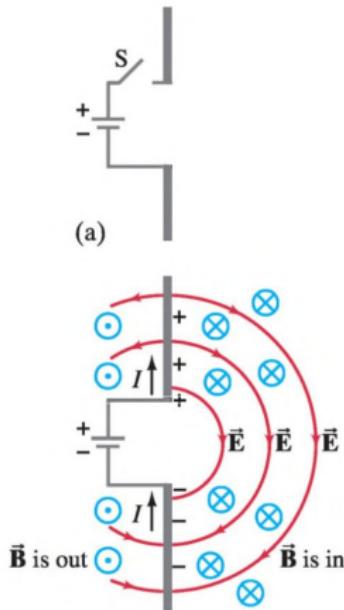
Integral form	Differential form
$\oint \vec{E} \cdot d\vec{A} = \frac{Q}{\epsilon_0}$	$\vec{\nabla} \cdot \vec{E} = \frac{\rho}{\epsilon_0}$
$\oint \vec{B} \cdot d\vec{A} = 0$	$\vec{\nabla} \cdot \vec{B} = 0$
$\oint \vec{E} \cdot d\vec{l} = - \frac{d\Phi_B}{dt}$	$\vec{\nabla} \times \vec{E} = - \frac{\partial \vec{B}}{\partial t}$
$\oint \vec{B} \cdot d\vec{l} = \mu_0 I + \mu_0 \epsilon_0 \frac{d\Phi_E}{dt}$	$\vec{\nabla} \times \vec{B} = \mu_0 \vec{j} + \mu_0 \epsilon_0 \frac{\partial \vec{E}}{\partial t}$

<sup>†</sup> $\vec{\nabla}$  stands for the *del operator*  $\vec{\nabla} = \hat{i} \frac{\partial}{\partial x} + \hat{j} \frac{\partial}{\partial y} + \hat{k} \frac{\partial}{\partial z}$  in Cartesian coordinates.

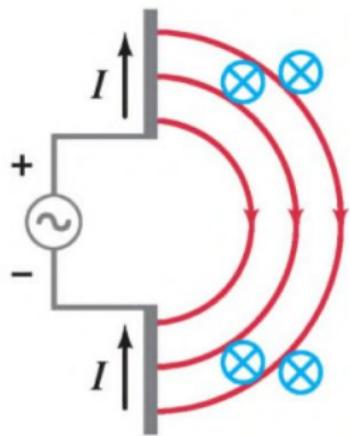


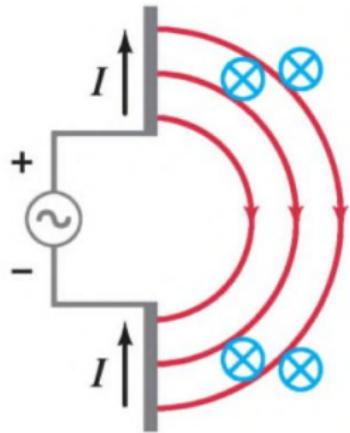


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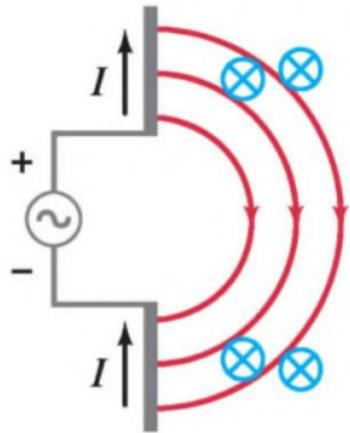


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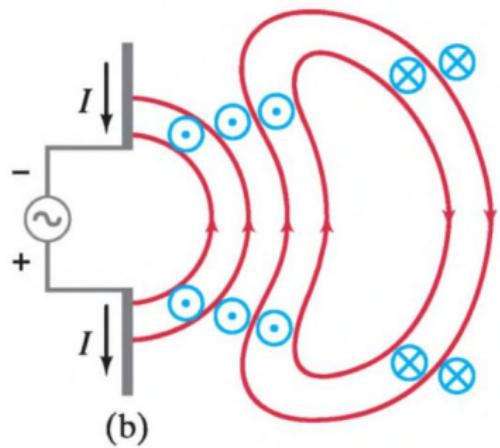




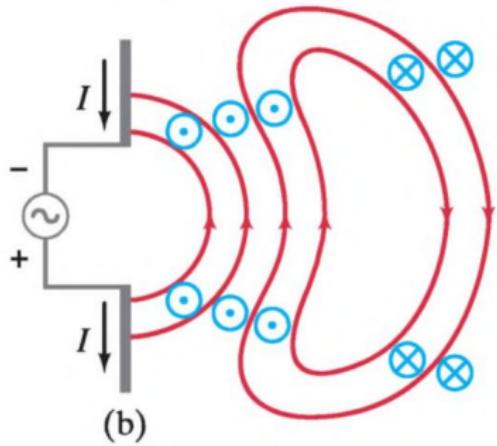
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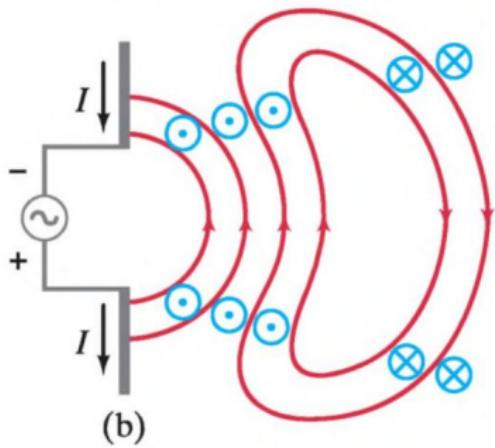


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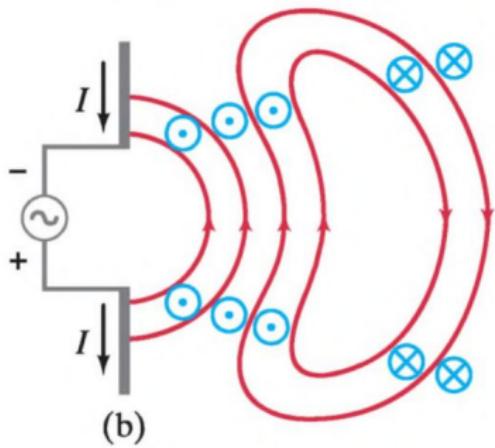


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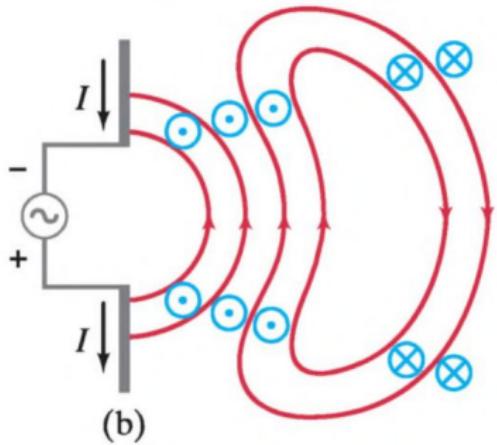




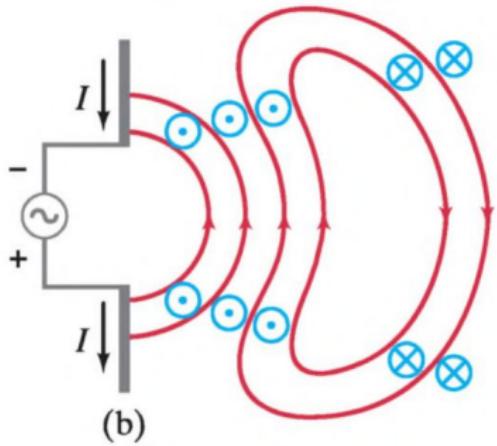
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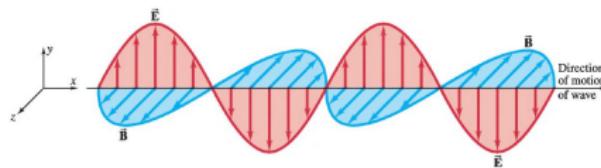
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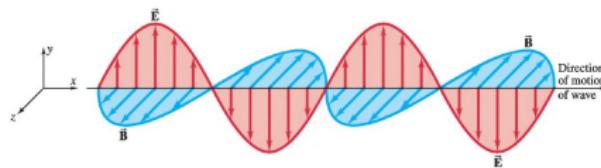
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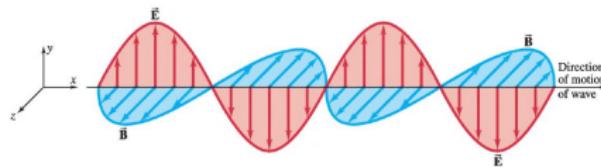
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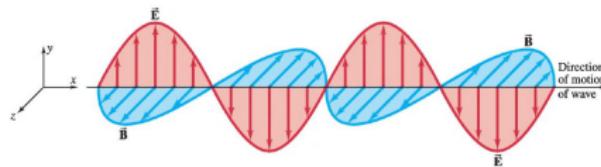
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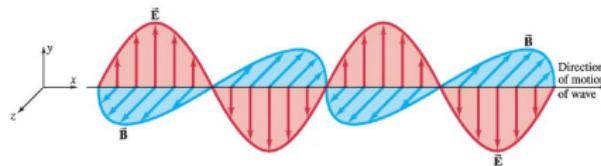
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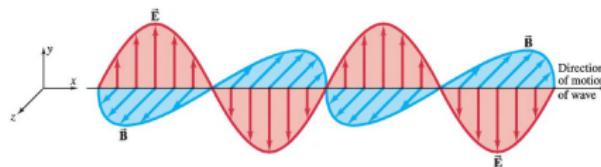
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**Accelerated electric charges give rise to electromagnetic waves**

# Mathematical Description

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- ▶ Waves traveling in the x-direction,  $\vec{v} = v\hat{i}$

# Mathematical Description

The Maxwell equation take the form:

$$\oint \vec{E} \cdot d\vec{A} = 0$$

$$\oint \vec{B} \cdot d\vec{A} = 0$$

$$\oint \vec{E} \cdot d\vec{l} = - \frac{d\Phi_B}{dt}$$

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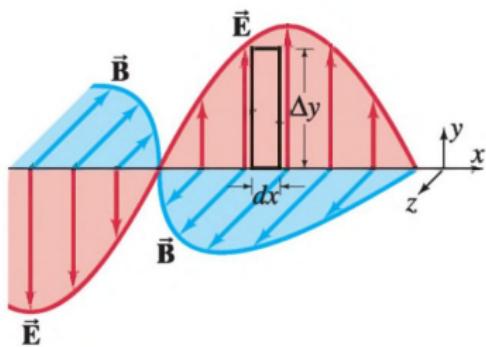
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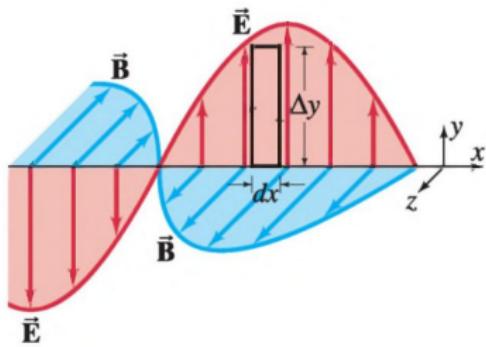
where,

$$k = \frac{2\pi}{\lambda}, \quad \omega = 2\pi f, \quad f\lambda = \frac{\omega}{k} = v$$

# Speed of light

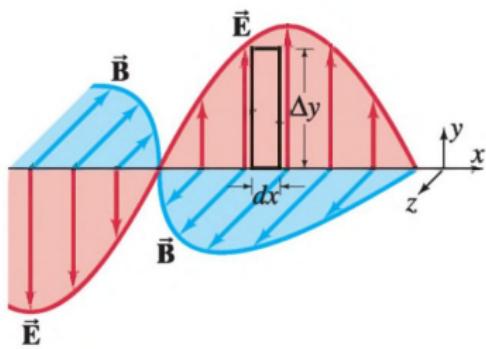


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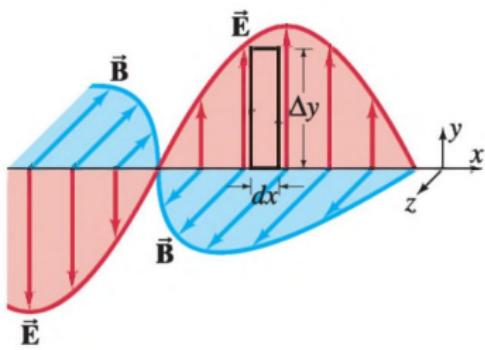
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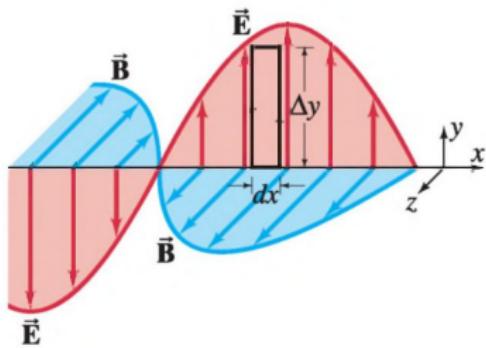


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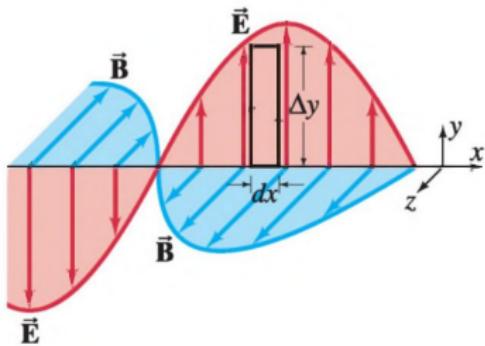
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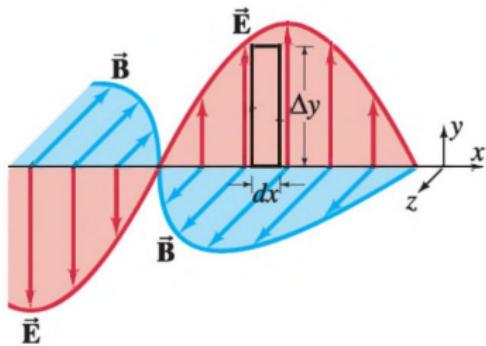
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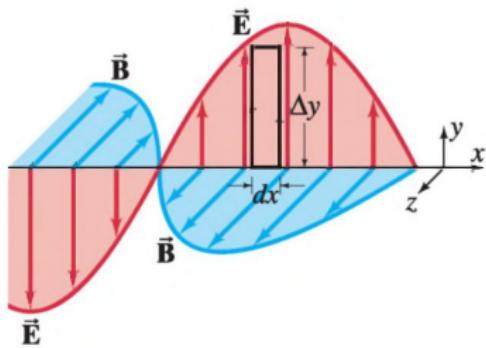


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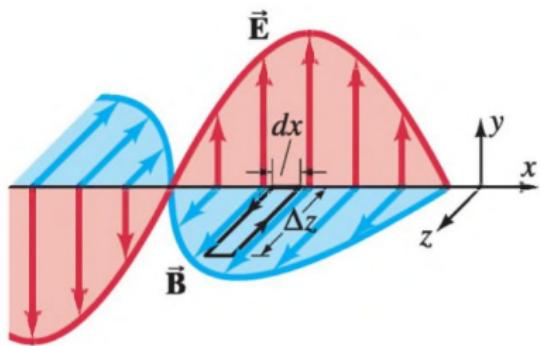


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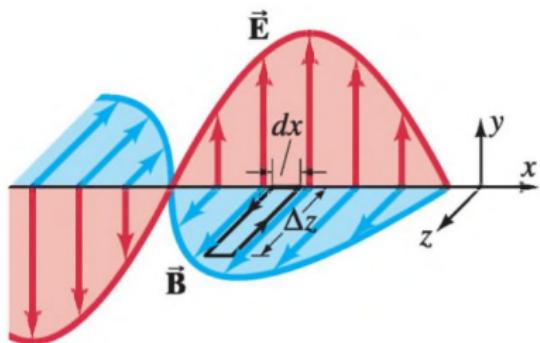
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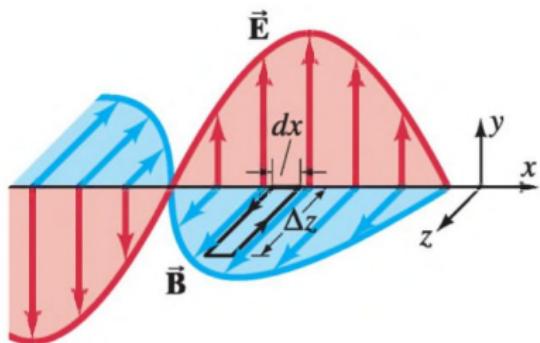
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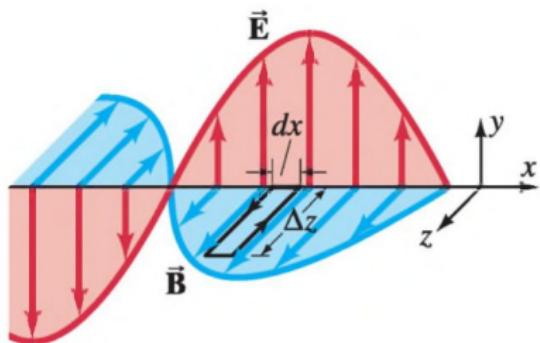


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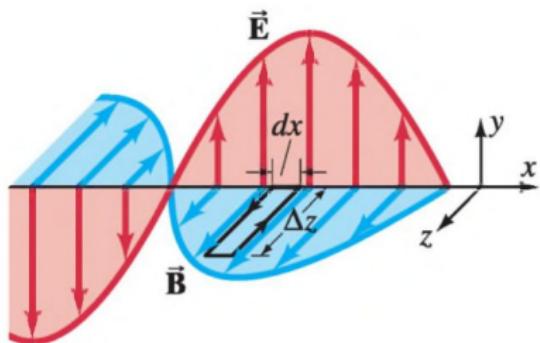
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$$\rightarrow v = \frac{1}{\mu_0 \epsilon_0} \frac{1}{\omega}$$

# Speed of light

Then, the velocity of propagation of the wave is,

$$v^2 = \frac{1}{\epsilon_0 \mu_0} \rightarrow v = \frac{1}{\sqrt{\epsilon_0 \mu_0}} = c \quad (36)$$

$c$  is the speed of light,

$$c = 3 \times 10^8 \text{ m/s} \quad (37)$$

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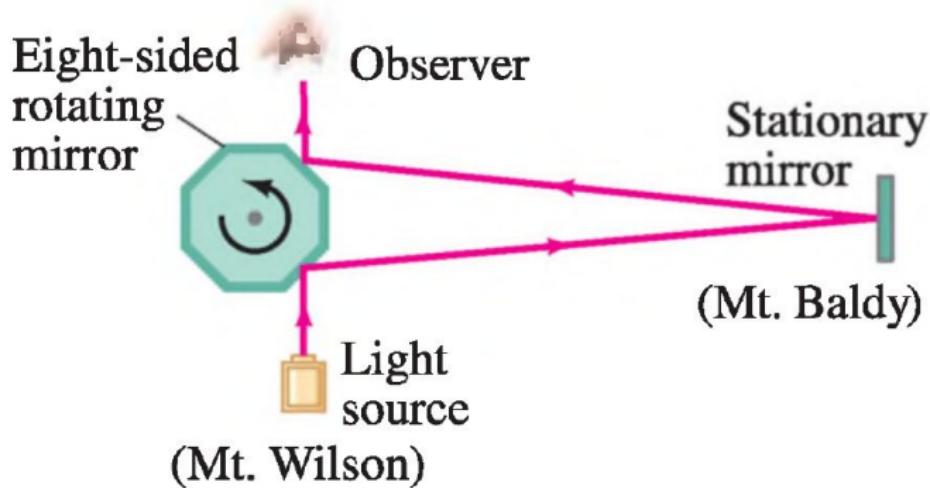
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# Measuring the speed of light

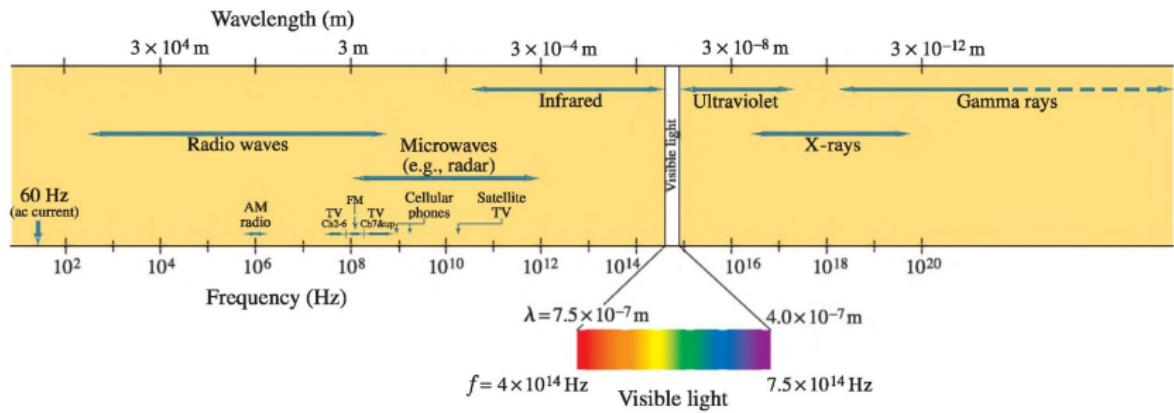
## Michelson's Experiment



# Electromagnetic spectrum

The frequency of light is related with its speed thought the expression,

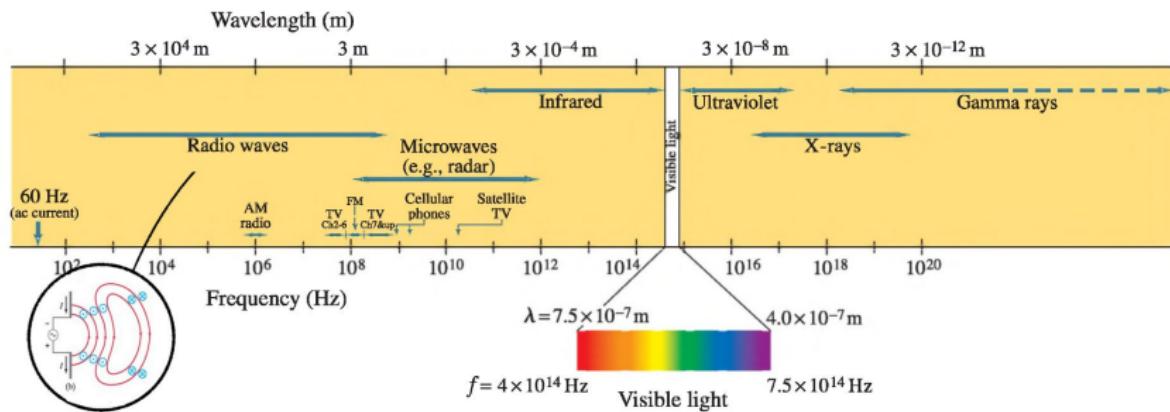
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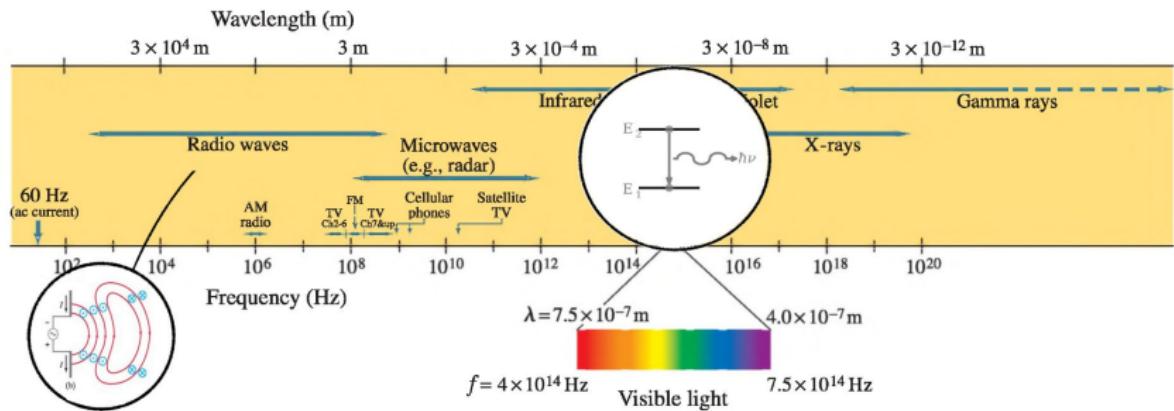
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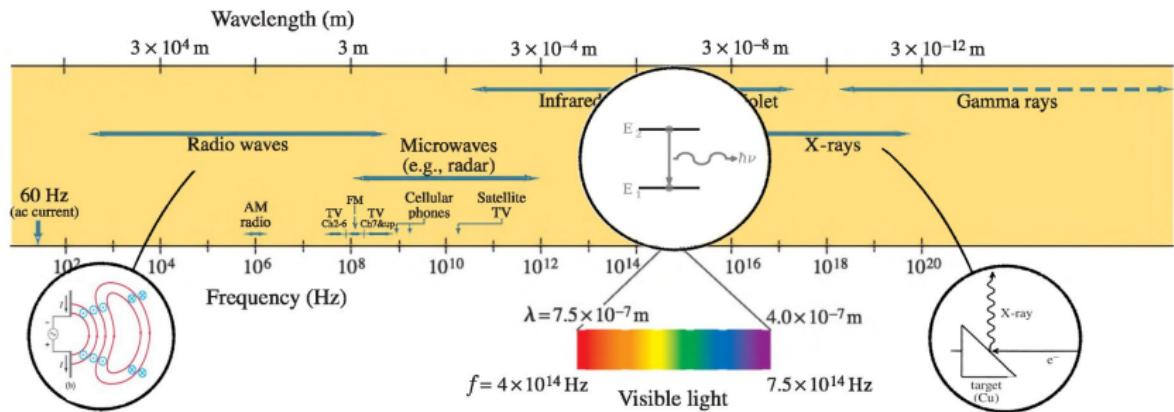
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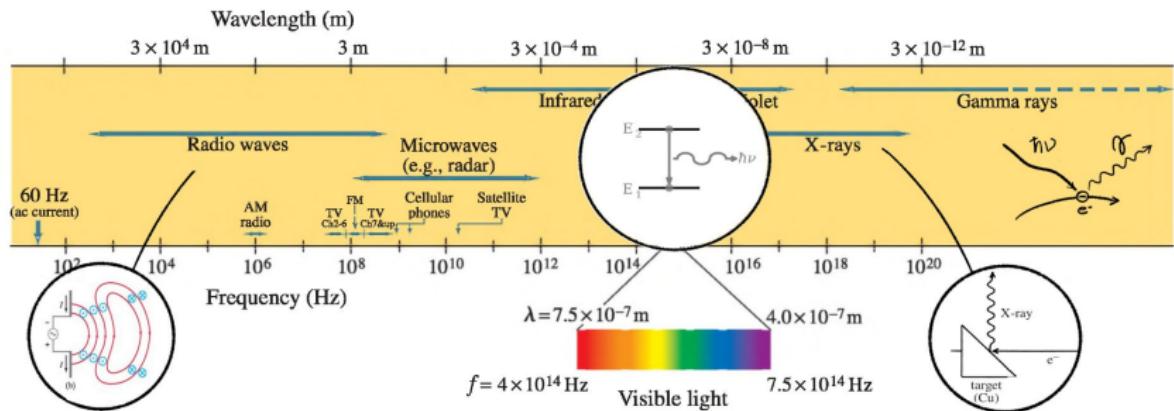
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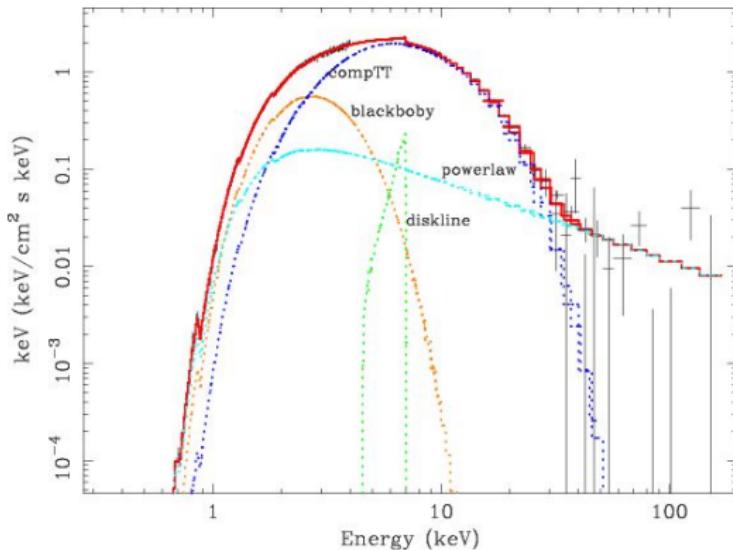
Example:

$$\text{BB radiation} \rightarrow I \propto \frac{1}{e^{\frac{h\nu}{kT}} - 1}$$

Synchrotron radiation  $\rightarrow \nu^\alpha$  Power Law

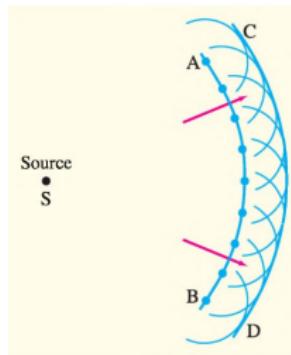
# Electromagnetic spectrum

Application: knowing what process are occurring in an Astrophysical Object.



# Huygens' principle

*Every point on a wave front can be considered as a source of tiny wavelets that spread out in the forward direction at the speed of the wave itself. The new wave front is the envelope of all the wavelets—that is, the tangent to all of them.*



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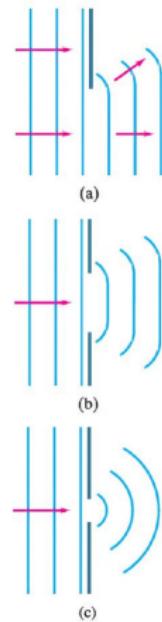
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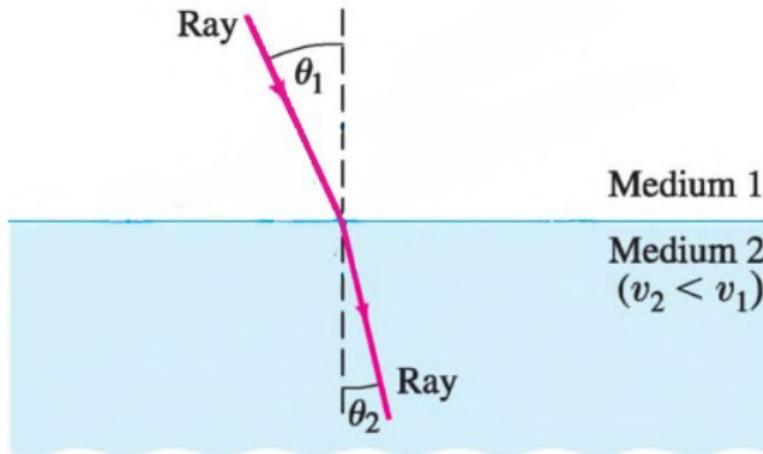


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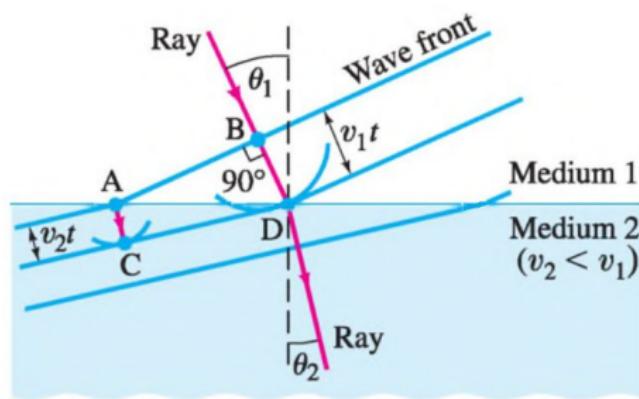


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We are going to use the Huygens' principle to explain this...

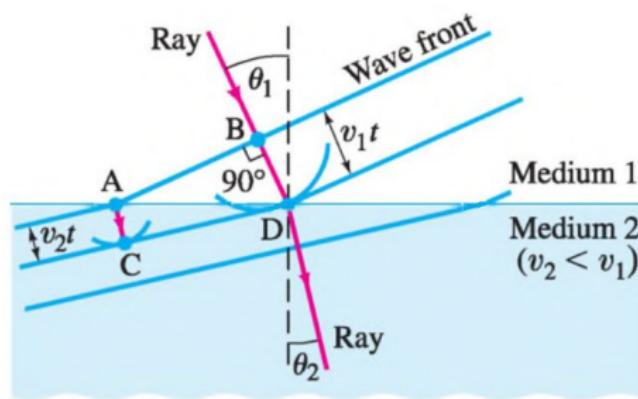
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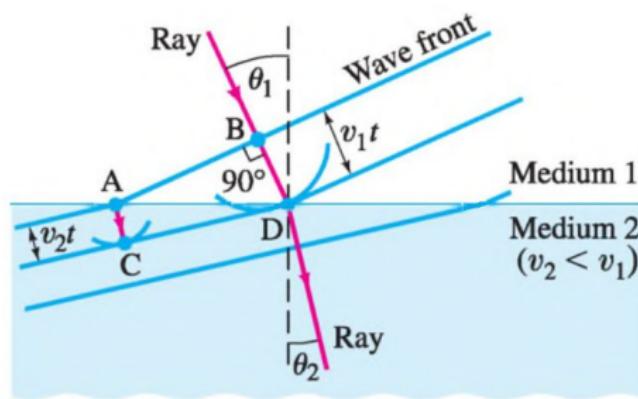
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$$\sin\theta_1 = \frac{v_1 t}{AD}, \quad \sin\theta_2 = \frac{v_2 t}{AD}$$

# Refraction

We are going to use the Huygens' principle to explain this...



$$\sin\theta_1 = \frac{v_1 t}{AD}, \quad \sin\theta_2 = \frac{v_2 t}{AD}$$

$$\rightarrow \frac{\sin\theta_1}{\sin\theta_2} = \frac{v_1}{v_2}$$

# Refraction

The frequency does not change, but the wavelength does,

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$$\frac{\lambda_2}{\lambda_1} = \frac{v_2}{v_1} = \frac{n_1}{n_2}$$

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$$n = \frac{c}{v} \quad (41)$$

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where,

$$n = \frac{c}{v} \quad (41)$$

is the **refraction index**.

# Refraction

Why the velocity change?

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$$v = \frac{1}{\sqrt{\epsilon\mu}} \quad (42)$$

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$\epsilon \rightarrow$  The resistance of a material to be penetrated by an electric field.

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$$v = \frac{1}{\sqrt{\epsilon\mu}} \quad (43)$$

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# Refraction

Why the velocity change?

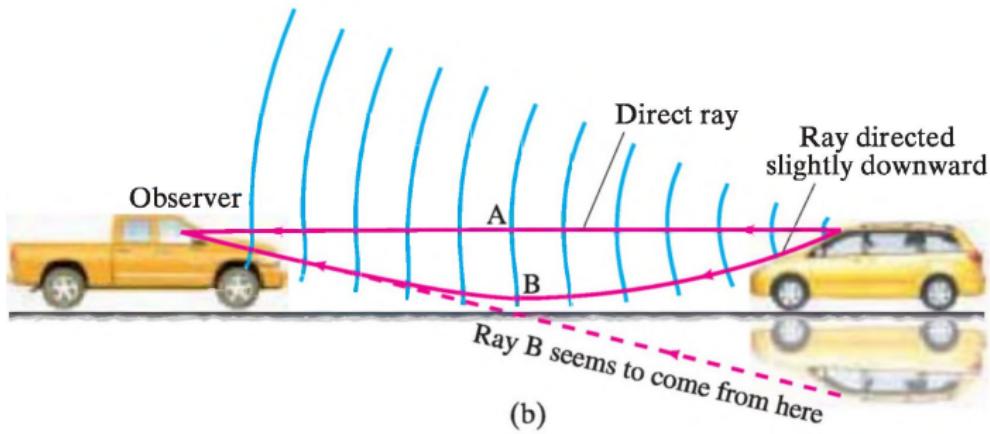
$$v = \frac{1}{\sqrt{\epsilon\mu}} \quad (43)$$

$\mu \rightarrow$  The resistance of a material to be penetrated by a magnetic field.

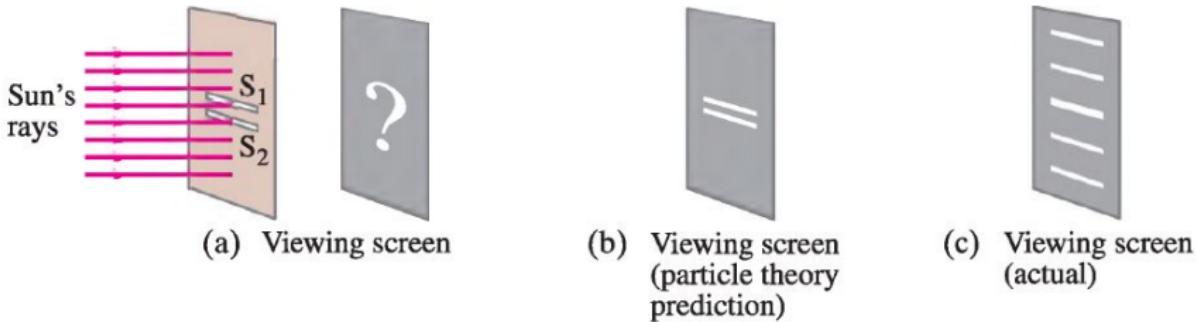
$\epsilon \rightarrow$  The resistance of a material to be penetrated by an electric field.

# Refraction

Example: Mirages



# Interference: Youn's double-slit Experiment



If light consists of tiny particles, we might expect to see two bright lines on a screen placed behind the slits as in (b). But instead a series of bright lines are seen, as in (c). Young was able to explain this result as a wave-interference phenomenon.

# Interference: Youn's double-slit Experiment

To understand why, we consider:

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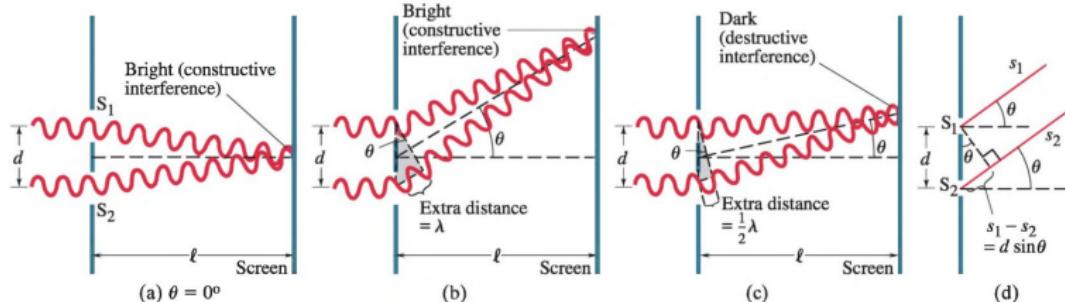
The waves leaving the two small slits spread out as shown:

# Interference: Youn's double-slit Experiment

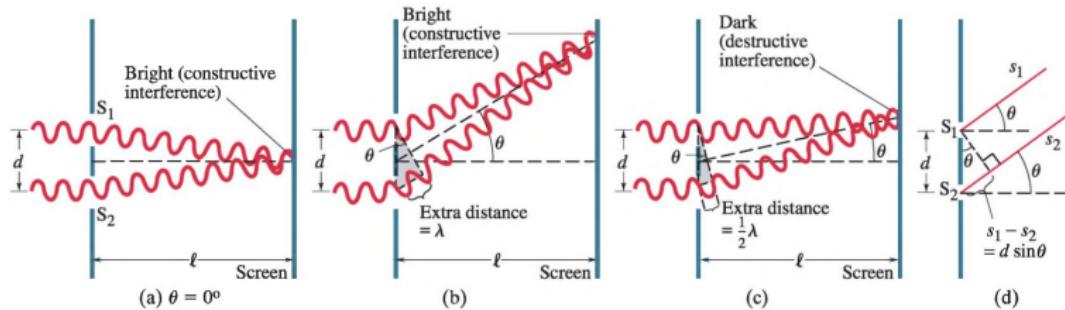
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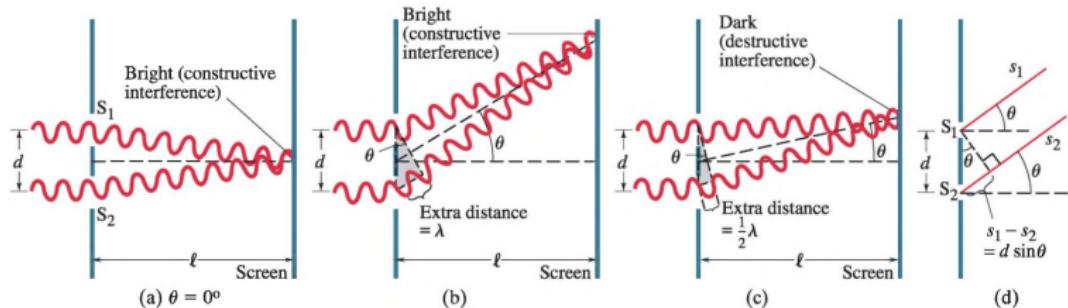
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## Interference: Youn's double-slit Experiment

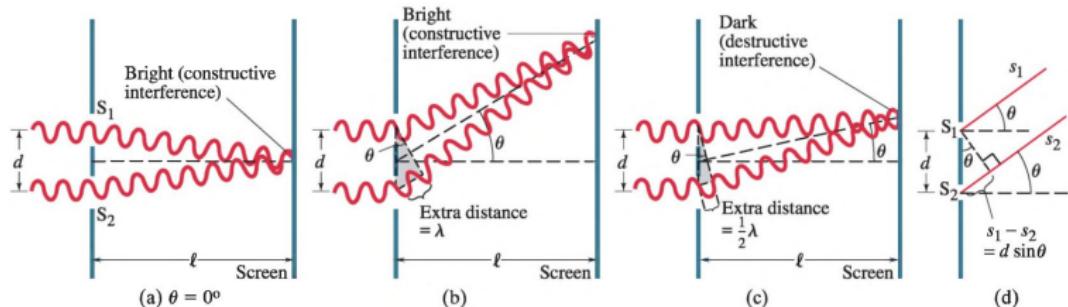


## Interference: Youn's double-slit Experiment



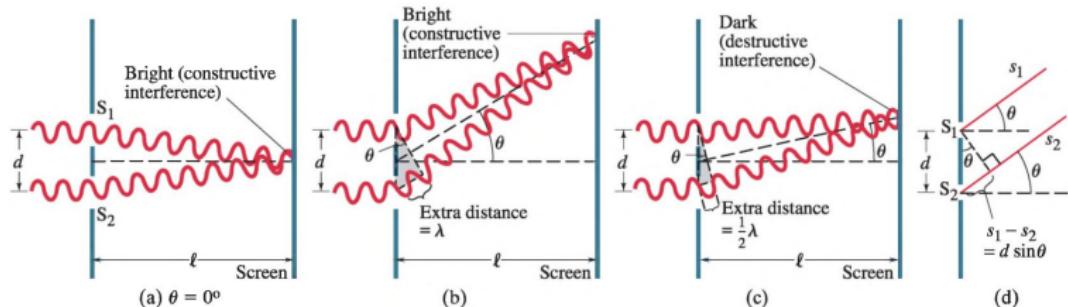
- ▶ Constructive interference → the path of 2 rays differs in  $n\lambda$ , n integer.

# Interference: Youn's double-slit Experiment



- ▶ Constructive interference → the path of 2 rays differs in  $n\lambda$ ,  $n$  integer.
- ▶ Destructive interference → the path of 2 rays differs in  $(2n + 1)\lambda/2$ ,  $n$  integer.

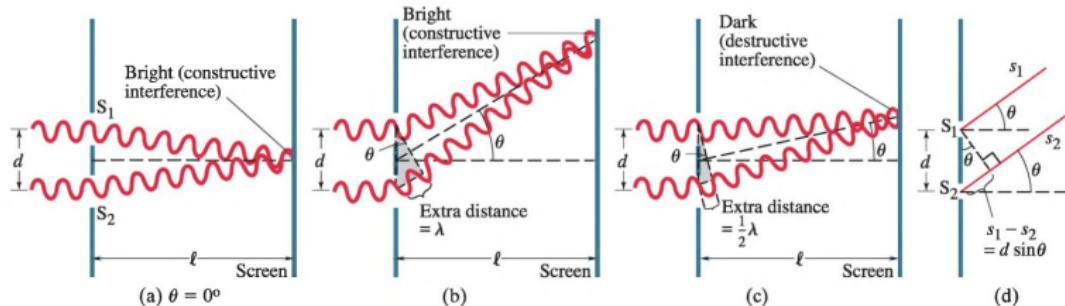
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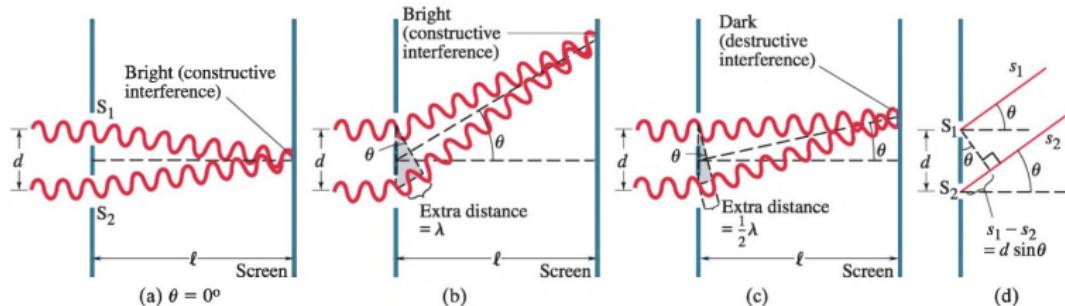
- ▶ Constructive interference → the path of 2 rays differs in  $n\lambda$ , n integer.
- ▶ Destructive interference → the path of 2 rays differs in  $(2n + 1)\lambda/2$ , n integer.

Thus, there will be a series of bright and dark lines (or fringes) on the viewing screen.

## Interference: Youn's double-slit Experiment

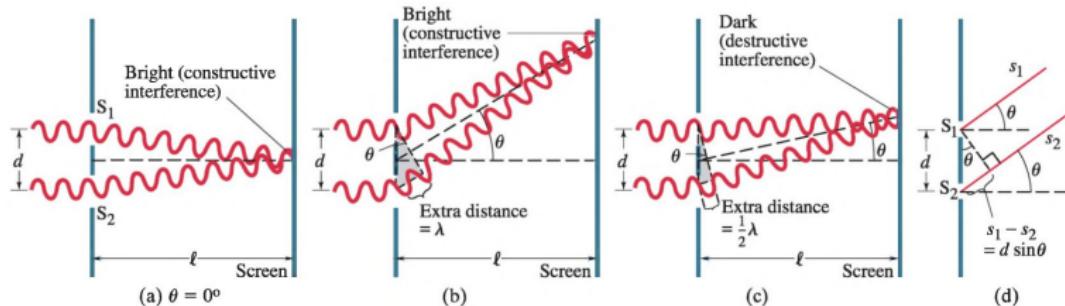


## Interference: Youn's double-slit Experiment



Where the bright lines fall?

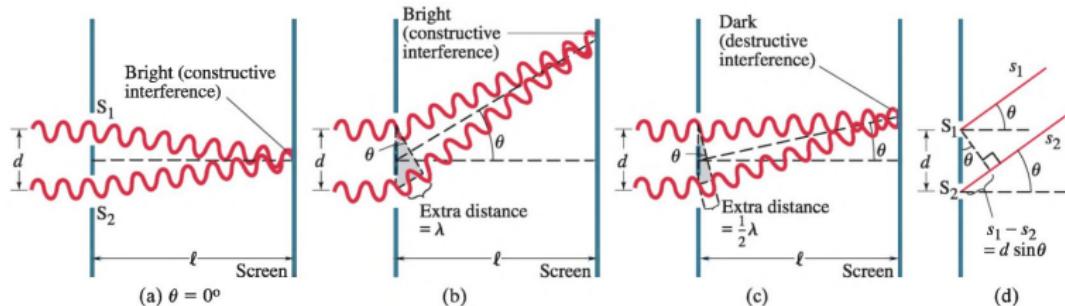
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Where the bright lines fall?

- ▶  $d \ll \ell$

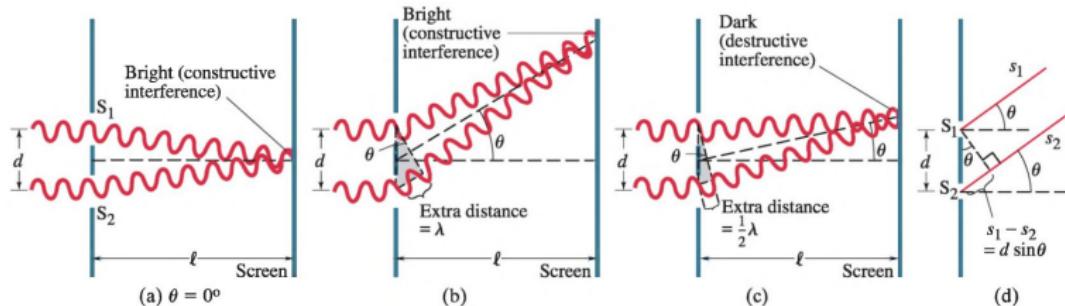
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Where the bright lines fall?

- ▶  $d \ll \ell$
- ▶ The rays are essentially parallel.

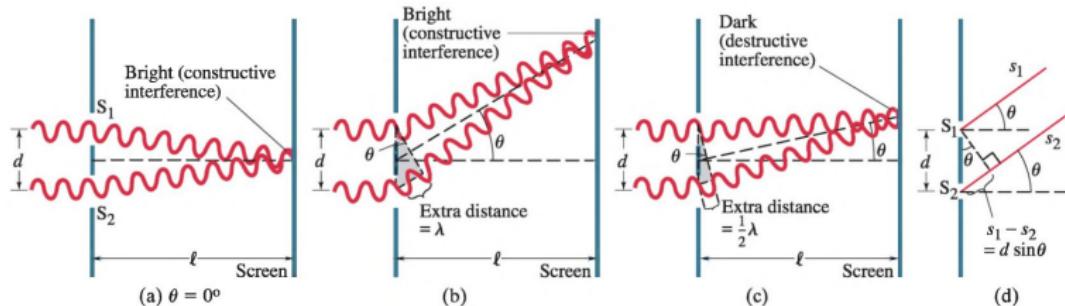
# Interference: Youn's double-slit Experiment



Where the bright lines fall?

- ▶  $d \ll \ell$
- ▶ The rays are essentially parallel.
- ▶  $\theta$  is the angle they make with the horizontal.

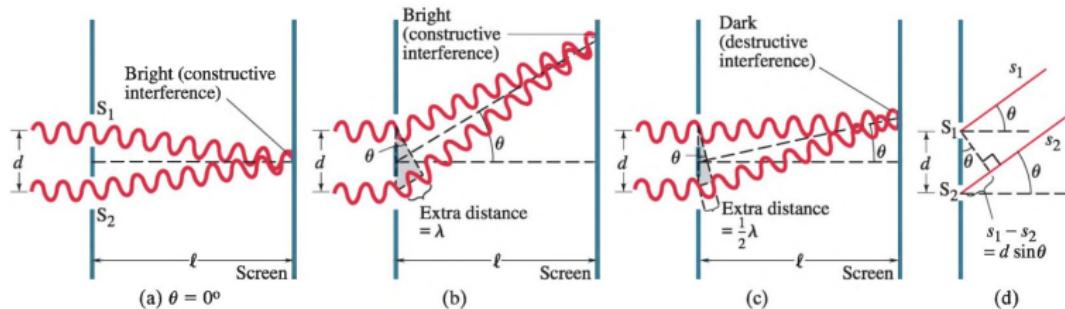
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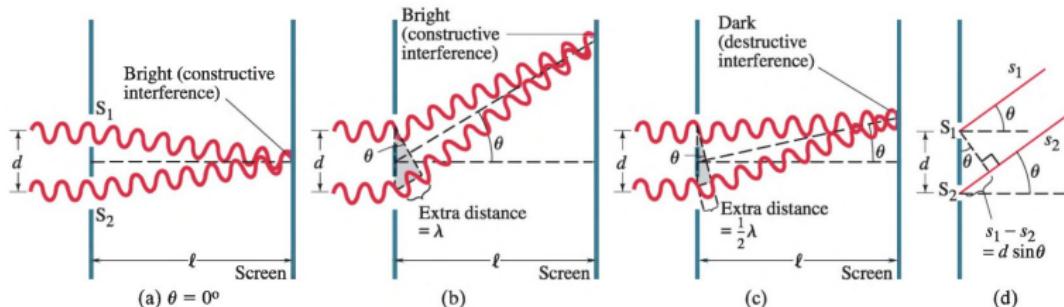
Where the bright lines fall?

- ▶  $d \ll l$
- ▶ The rays are essentially parallel.
- ▶  $\theta$  is the angle they make with the horizontal.
- ▶ The extra distance traveled by the lower ray is  $d \sin\theta$

## Interference: Youn's double-slit Experiment

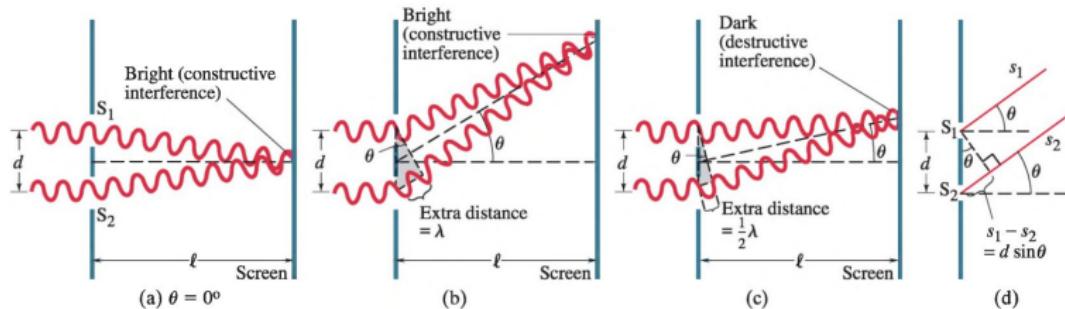


## Interference: Youn's double-slit Experiment



Where the bright lines fall?

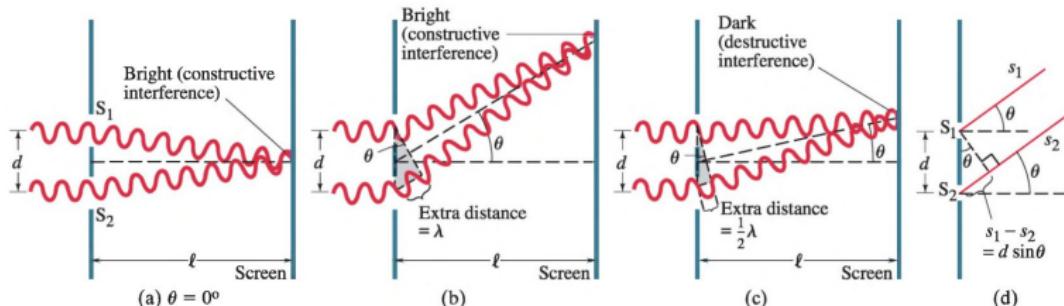
## Interference: Youn's double-slit Experiment



Where the bright lines fall?

Constructive interference:

# Interference: Youn's double-slit Experiment

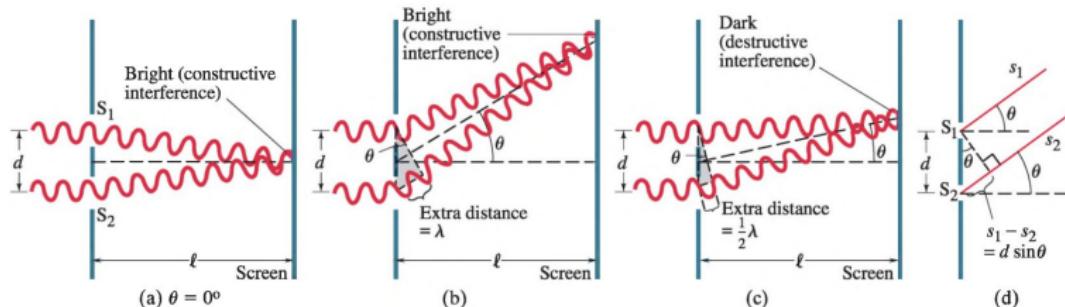


Where the bright lines fall?

Constructive interference:

$$\sin\theta = \frac{n\lambda}{d} = \frac{X}{l} \quad (44)$$

## Interference: Youn's double-slit Experiment

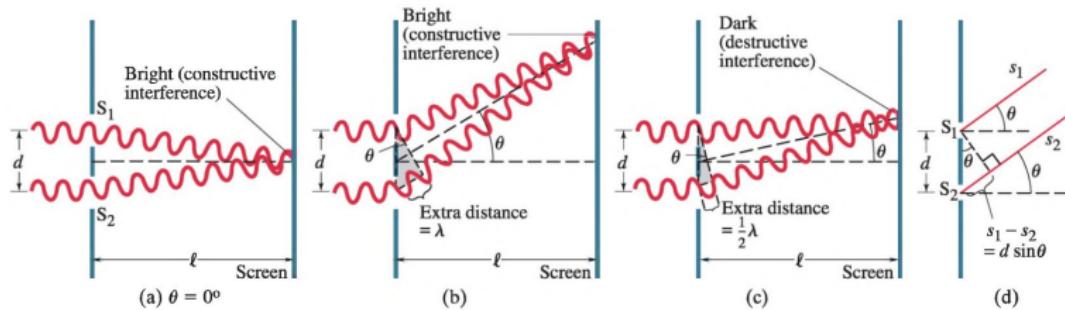


Where the bright lines fall?

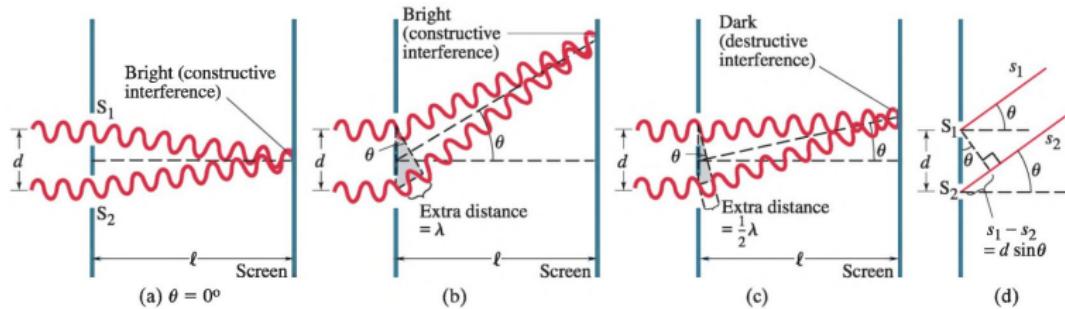
Constructive interference:

$$\sin \theta = \frac{n\lambda}{d} = \frac{X}{\ell} \rightarrow X = \ell \frac{n\lambda}{d} \quad (45)$$

## Interference: Youn's double-slit Experiment

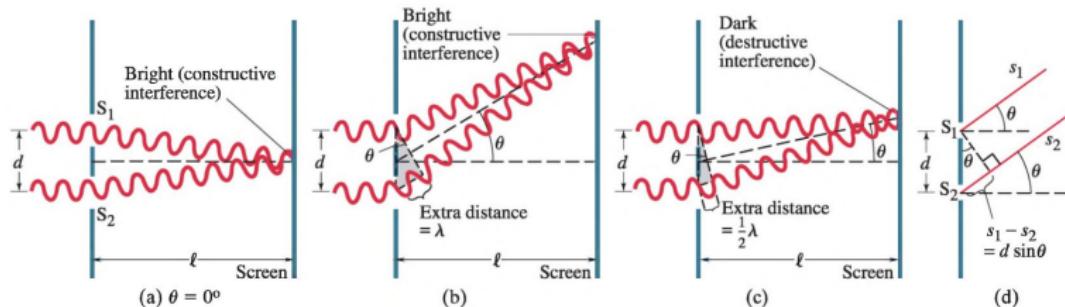


## Interference: Youn's double-slit Experiment



Destructive interference:

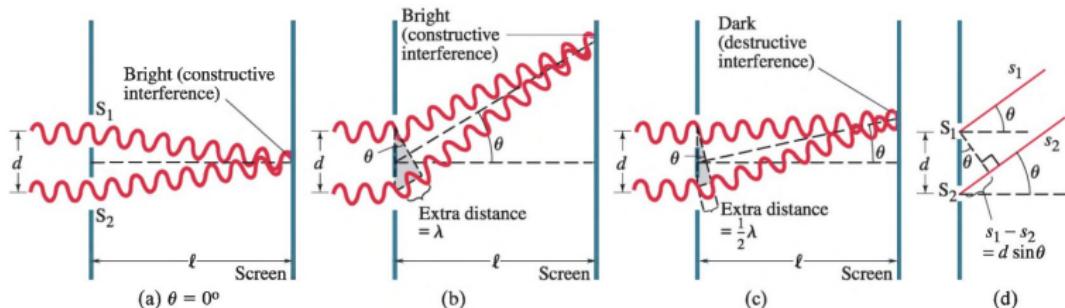
# Interference: Youn's double-slit Experiment



Destructive interference:

$$\sin\theta = \frac{(2n+1)\lambda}{d} = \frac{X}{\ell} \quad (46)$$

# Interference: Youn's double-slit Experiment



Where the bright lines fall?

Destructive interference:

$$\sin\theta = \frac{(2n+1)\lambda}{d} = \frac{X}{\ell} \rightarrow X = \ell \frac{(2n+1)\lambda}{d} \quad (47)$$

# Interference: Youn's double-slit Experiment

Conceptual Example:

- (a) Will there be an infinite number of points on the viewing screen where constructive and destructive interference occur, or only a finite number of points?

# Interference: Youn's double-slit Experiment

Conceptual Example:

- (a) Will there be an infinite number of points on the viewing screen where constructive and destructive interference occur, or only a finite number of points?
- (b) Are neighboring points of constructive interference uniformly spaced, or is the spacing between neighboring points of constructive interference not uniform?

# Interference: Youn's double-slit Experiment

Conceptual Example:

- (a) The maximum value of  $n$  is the integer closest in value but smaller than  $d/X$ .

# Interference: Youn's double-slit Experiment

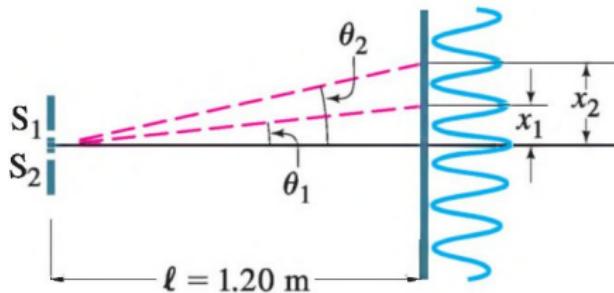
Conceptual Example:

- (a) The maximum value of  $n$  is the integer closest in value but smaller than  $d/X$ .
- (b) For small values of  $\theta$  the spacing is nearly uniform. For non-small values  $\rightarrow$  the spacing gets larger as  $\theta$  gets larger.

# Interference: Youn's double-slit Experiment

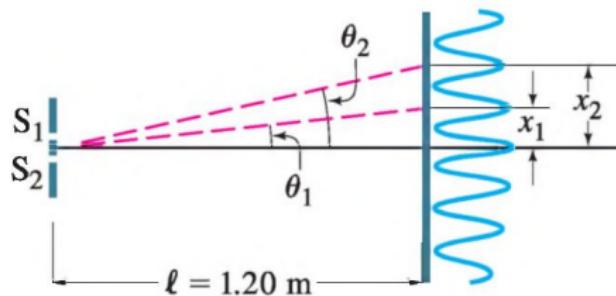
Example:

A screen containing two slits 0.100 mm apart is 1.20 m from the viewing screen. Light of wavelength  $\lambda = 500 \text{ nm}$  falls on the slits from a distant source. Approximately how far apart will adjacent bright interference fringes be on the screen?



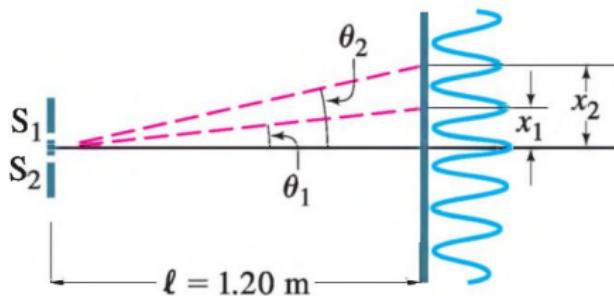
# Interference: Youn's double-slit Experiment

Example:



# Interference: Youn's double-slit Experiment

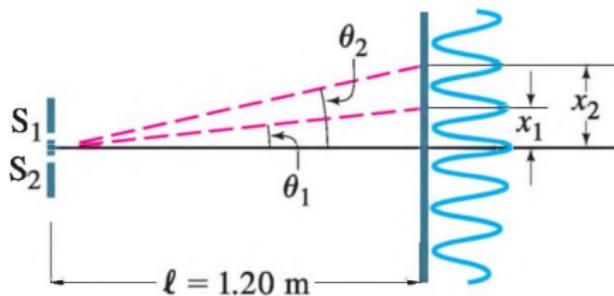
Example:



$$\sin\theta_1 = \frac{m\lambda}{d} = \frac{(1)(500 \times 10^{-9} \text{ m})}{1.00 \times 10^{-4} \text{ m}} = 5.00 \times 10^{-3} \quad (48)$$

## Interference: Youn's double-slit Experiment

Example:



$$\sin\theta_1 = \frac{m\lambda}{d} = \frac{(1)(500 \times 10^{-9} \text{ m})}{1.00 \times 10^{-4} \text{ m}} = 5.00 \times 10^{-3} \quad (48)$$

$$\theta \ll 1 \rightarrow \sin\theta \sim \theta \text{ and } x_1/\ell = \tan\theta_1 \sim \theta_1$$

# Interference: Youn's double-slit Experiment

Example:

then,

$$x_1 \sim \ell\theta_1 = (1.20 \text{ m})(5.00 \times 10^{-3}) = 6.00 \text{ mm} \quad (49)$$

# Interference: Youn's double-slit Experiment

Example:

then,

$$x_1 \sim \ell\theta_1 = (1.20 \text{ m})(5.00 \times 10^{-3}) = 6.00 \text{ mm} \quad (49)$$

$$x_2 \sim \ell\theta_2 = \ell \frac{2\lambda}{d} = 12.00 \text{ mm} \quad (50)$$

# Interference: Youn's double-slit Experiment

Example:

then,

$$x_1 \sim \ell\theta_1 = (1.20 \text{ m})(5.00 \times 10^{-3}) = 6.00 \text{ mm} \quad (49)$$

$$x_2 \sim \ell\theta_2 = \ell \frac{2\lambda}{d} = 12.00 \text{ mm} \quad (50)$$

Thus the lower order fringes are 6.00 mm apart.

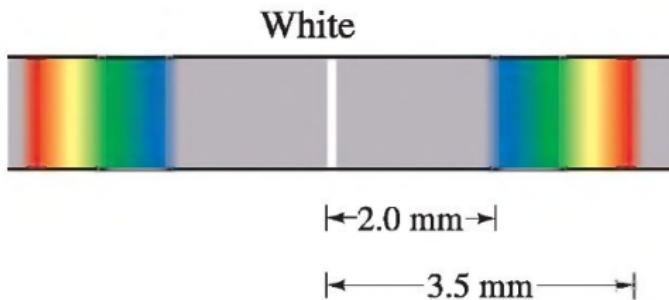
# Interference: Youn's double-slit Experiment

Conceptual Example:

- (a) What happens to the interference pattern, if the incident light (500 nm) is replaced by light of wavelength 700 nm? (b) What happens instead if the wavelength stays at 500 nm but the slits are moved farther apart?

# Interference: Youn's double-slit Experiment

Except for the zeroth-order fringe at the center, the position of the fringes depends on wavelength.



# Intensity in the Interference Pattern

- ▶  $E_\theta = E_1 + E_2$

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- ▶  $E_\theta = E_1 + E_2$
- ▶  $E_1 = E_{10} \sin \omega t$

# Intensity in the Interference Pattern

- ▶  $E_\theta = E_1 + E_2$
- ▶  $E_1 = E_{10} \sin \omega t$
- ▶  $E_2 = E_{20} \sin(\omega t + \delta)$ ,  $\frac{\delta}{2\pi} = \frac{ds \sin \theta}{\lambda}$

We can work with this expression and prove that:

$$\frac{I_\theta}{I_0} = \frac{E_{\theta 0}^2}{(2E_0)^2} = \cos^2 \frac{\delta}{2} \quad (51)$$

# Intensity in the Interference Pattern

$$I_\theta = I_0 \cos^2 \left( \frac{\pi d \sin \theta}{\lambda} \right) \quad (52)$$

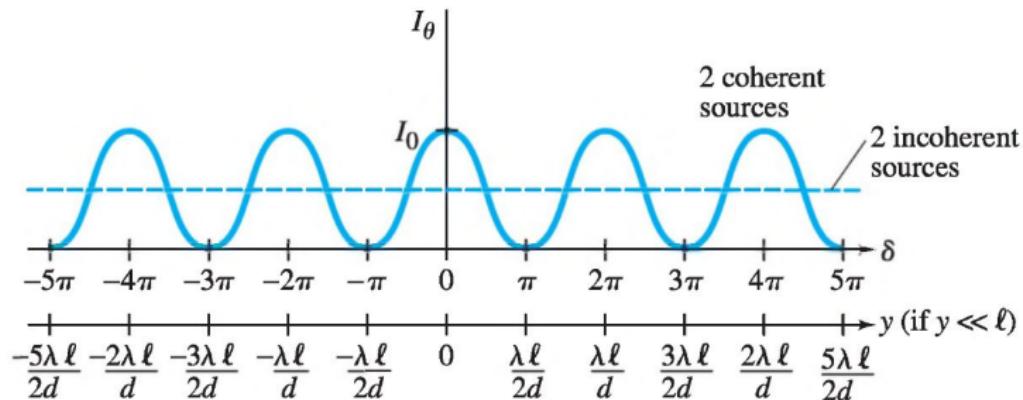
# Intensity in the Interference Pattern

$$I_\theta = I_0 \cos^2 \left( \frac{\pi d \sin \theta}{\lambda} \right) \quad (52)$$

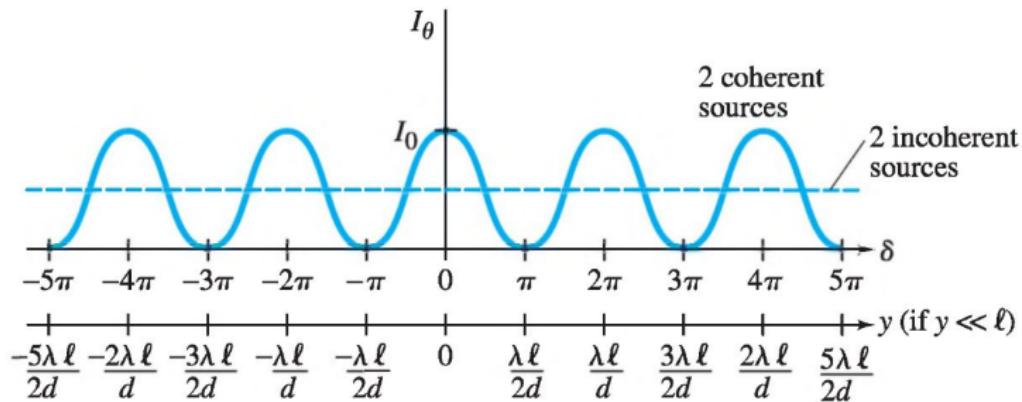
small  $\theta$ ,  $\sin \theta = \frac{y}{\ell}$

$$I_\theta = I_0 \left[ \cos \left( \frac{\pi d}{\lambda \ell} y \right) \right]^2 \quad (53)$$

## Intensity in the Interference Pattern



## Intensity in the Interference Pattern



The intensity pattern shows a series of maxima of equal height, and is based on the assumption that each slit (alone) would illuminate the screen uniformly. This is never quite true, if we consider diffraction.

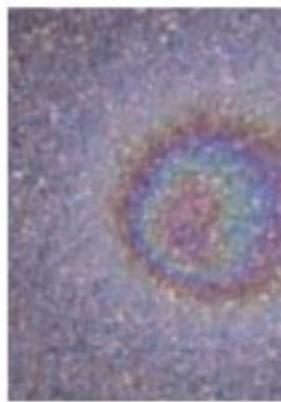
# Interference in Thin Films



(a)

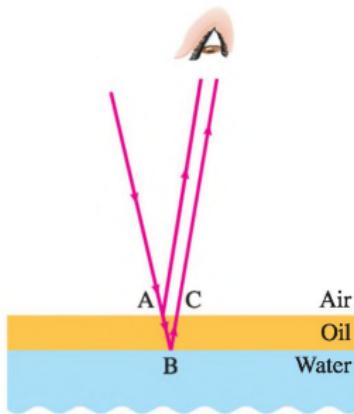


(b)



(c)

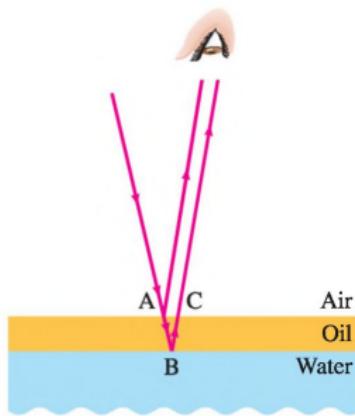
# Interference in Thin Films



If path difference  $ABC$  is,

- ▶ equals  $m\lambda_n \rightarrow$  constructive interference

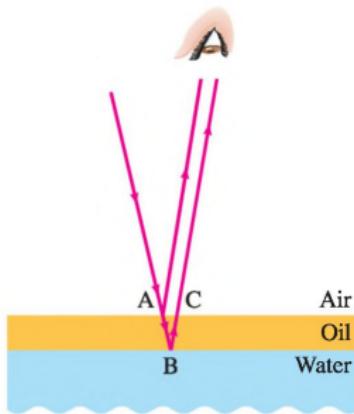
# Interference in Thin Films



If path difference  $ABC$  is,

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- ▶ equals  $(2m + 1)\lambda_n \rightarrow$  destructive interference

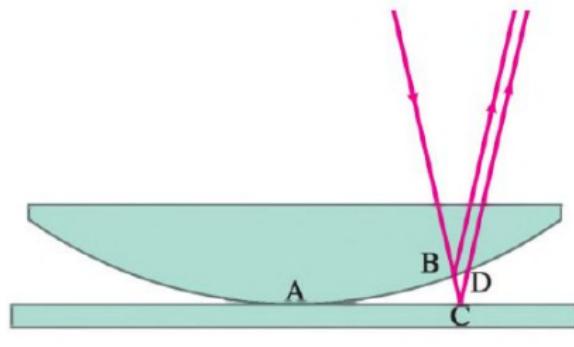
# Interference in Thin Films



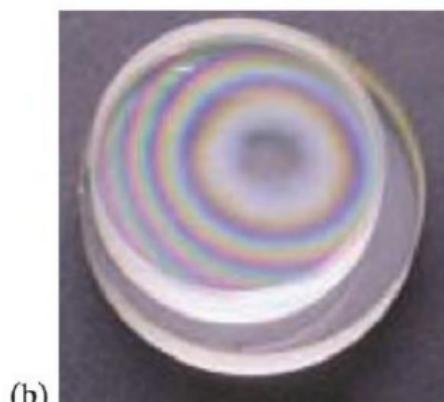
If path difference  $ABC$  is,

- ▶ equals  $m\lambda_n \rightarrow$  constructive interference
- ▶ equals  $(2m + 1)\lambda_n \rightarrow$  destructive interference
- ▶  $\lambda_n = \lambda/n$ ,  $n$  is the index of refraction

# Newton's Rings



(a)



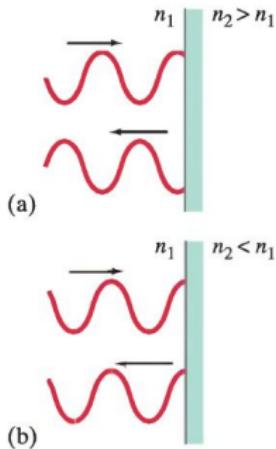
(b)

# Newton's Rings

Why is the center dark?

# Newton's Rings

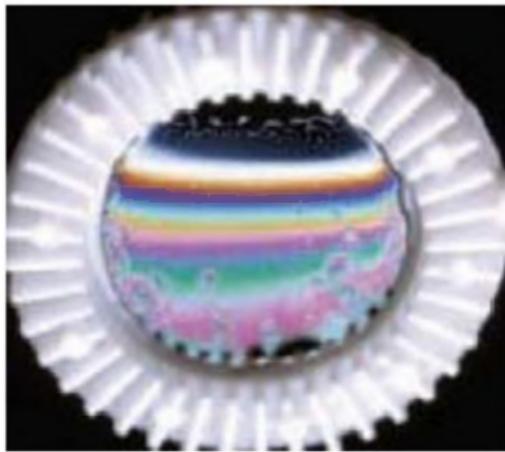
Why is the center dark?



**a beam of light reflected by a material with index of refraction greater than that of the material in which it is traveling, changes phase by  $180^\circ$  or  $\frac{1}{2}$  cycle;**

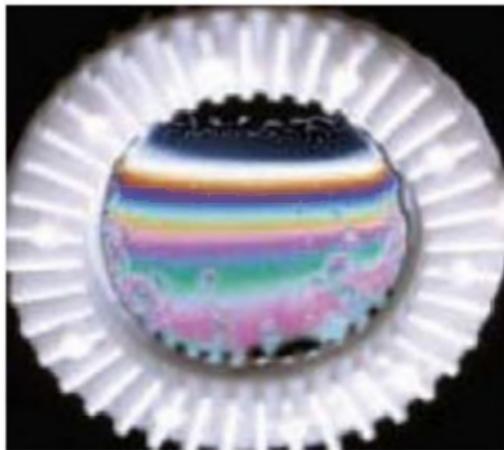
## Colors in a Thin Soap Film

- ▶ The thin film stood vertically.

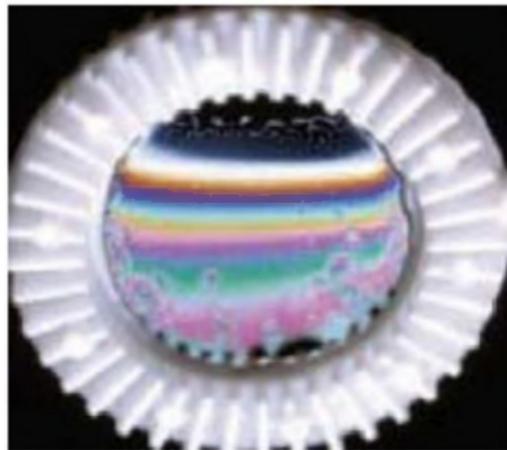


## Colors in a Thin Soap Film

- ▶ The thin film stood vertically.
- ▶ Gravity has pulled much of the soapy water toward the bottom.

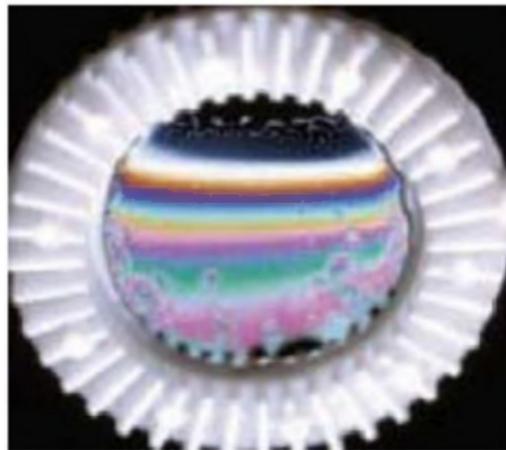


## Colors in a Thin Soap Film



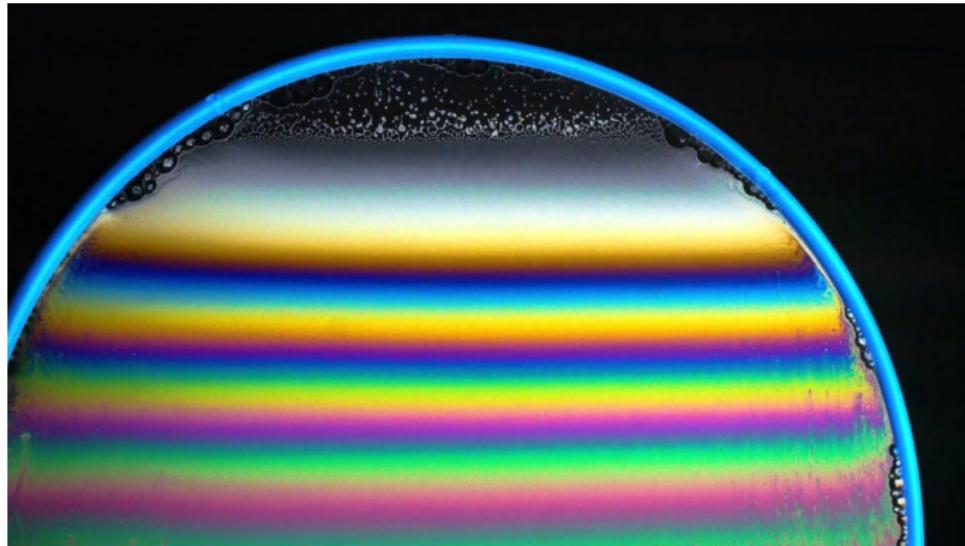
- ▶ The thin film stood vertically.
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- ▶ The top section is so thin → light reflected from the front and back surfaces have almost no path difference.

# Colors in a Thin Soap Film

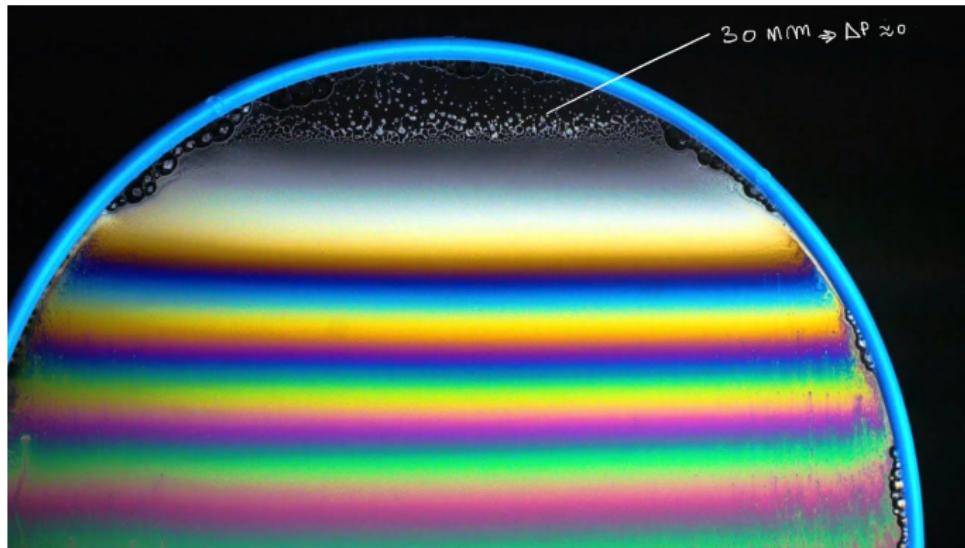


- ▶ The thin film stood vertically.
- ▶ Gravity has pulled much of the soapy water toward the bottom.
- ▶ The top section is so thin → light reflected from the front and back surfaces have almost no path difference.
- ▶  $180^\circ$  → two reflected waves are out of phase for all wavelengths.

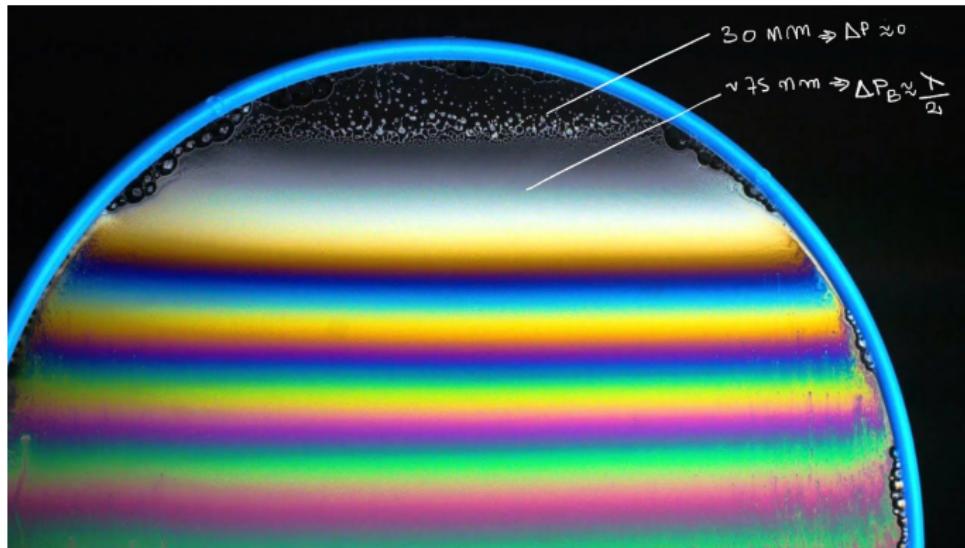
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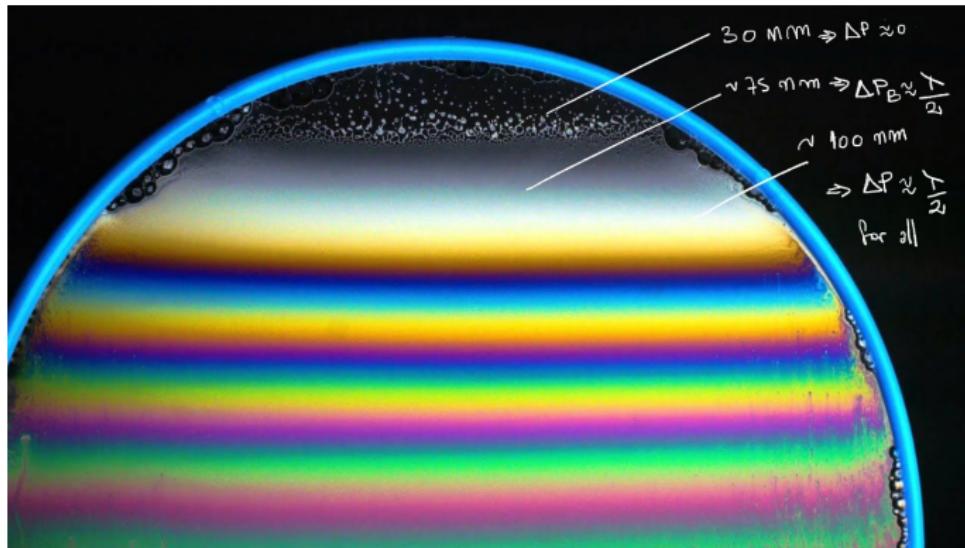
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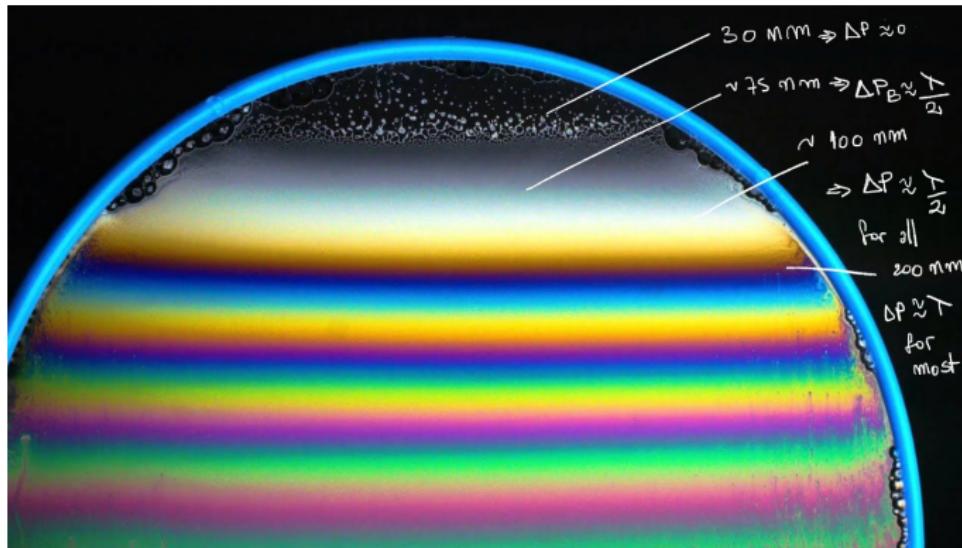
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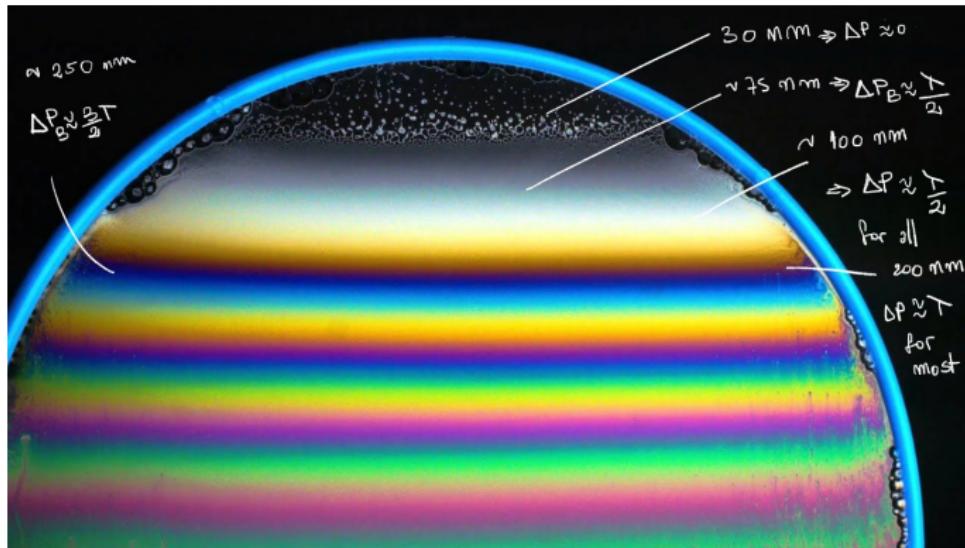
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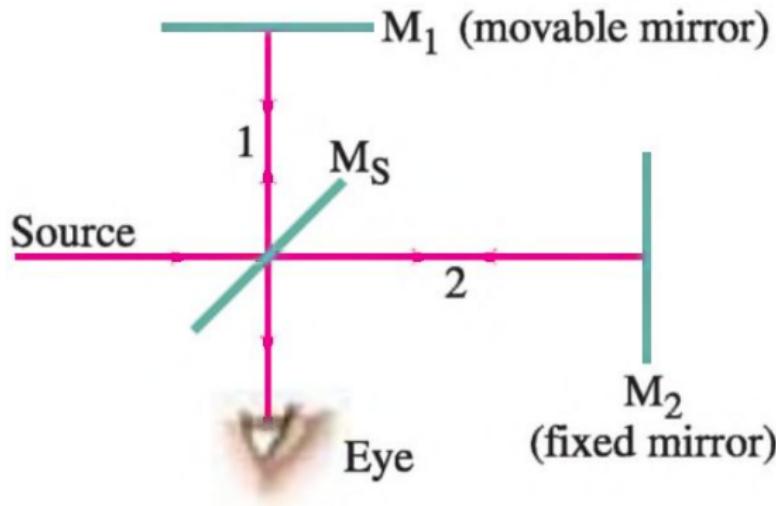
# Colors in a Thin Soap Film



# Colors in a Thin Soap Film



# Michelson Interferometer



# Questions

- ▶ Does Huygens' principle apply to sound waves? To water waves?

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# Questions

- ▶ Does Huygens' principle apply to sound waves? To water waves?
- ▶ We can hear sounds around corners but we cannot see around corners; yet both sound and light are waves. Explain the difference.
- ▶ Two rays of light from the same source destructively interfere if their path lengths differ by how much?

# Questions

- ▶ Monochromatic red light is incident on a double slit and the interference pattern is viewed on a screen some distance away. Explain how the fringe pattern would change if the red light source is replaced by a blue light source.

# Questions

- ▶ Monochromatic red light is incident on a double slit and the interference pattern is viewed on a screen some distance away. Explain how the fringe pattern would change if the red light source is replaced by a blue light source.
- ▶ Compare a double-slit experiment for sound waves to that for light waves. Discuss the similarities and differences.