PHY115: Introduction

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Digipen

Spring 2023



General information of the course

Kinematics

Doing vector calculation using components

Unit Vectors

Review: Functions

General information of the course

Kinematics

Doing vector calculation using components Unit Vectors

Review: Functions

General information of the course

Grading Policy

- 1. Assigments (20 %)
- 2. Midterm exam (40%)
- 3. Final exam (40%)

Upon a successfully completion of this course the students will gain a fundamental understanding of basic physical principles including:

1. Kinematics (describe motion)

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- 2. Math basics

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 - vectors
 - trigonometry
 - algebra
 - functions

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- 3. Mechanics (understand what causes the motion)

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 - vectors
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- 3. Mechanics (understand what causes the motion)
- 4. Rotation of rigid bodies
- 5. Light and physics of shading



Why to study Physics?

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- Too many errors in the motion will distract viewers and remind them that it's just a story.

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- 2. Keep the suspension of Disbelief: The representation of any story succeeds only because of the audience's willingness to ignore the fact that it's just a story.
- Too many errors in the motion will distract viewers and remind them that it's just a story.
 - Wrong response of material to light
 - Objects that move as if they were heavier than they look
 - Different falling acceleration for different bodies
 - **.**..



General information of the course Kinematics Doing vector calculation using components Unit Vectors Review: Functions

What is Physics?

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- kinematics describes the motion path of objects (the timing and spacing)
- Dynamics describes what causes the motion

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Why do we want to do this?

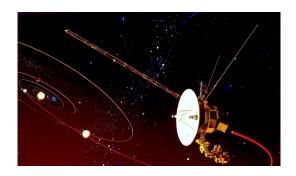
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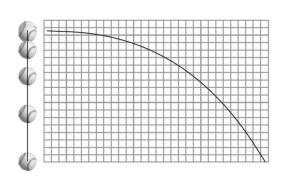
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General information of the course Kinematics Doing vector calculation using components Unit Vectors Review: Functions

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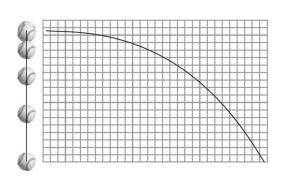
Knowing Dynamics can help us figure out accurate timing. Even if you plan to exaggerate your motion for effect, it helps to start with reality and work from there.

Kinematics



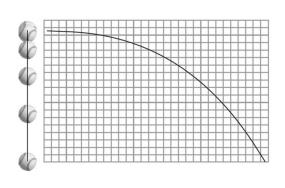
Describes the motion path: Position vs. time x(t), y(t) and $z(t) \rightarrow$ timing and spacing.

Kinematics



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- ► There are three main quantities that describe the motion: acceleration, velocity and position

Kinematics

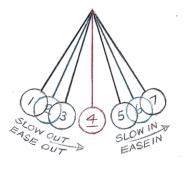


- Describes the motion path: Position vs. time x(t), y(t) and $z(t) \rightarrow$ timing and spacing.
- There are three main quantities that describe the motion: acceleration, velocity and position
- ➤ The position is related with velocity and the velocity is related with acceleration.

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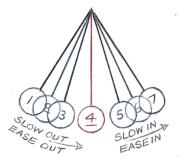
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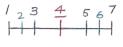


So our chart will look like this.

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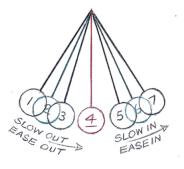


What is the right separation?

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You do this intuitively . . .

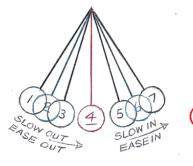
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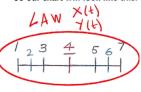
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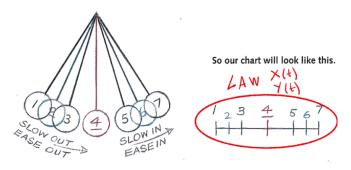


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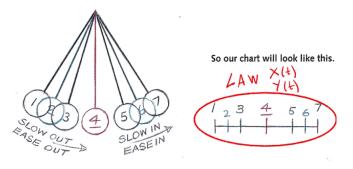
What generate that exact separation?

You do this intuitively . . .



What generate that exact separation? FORCES

You do this intuitively . . .



What generate that exact separation? FORCES Dynamics

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- Frames of Reference
- escalar and vectors
- funcions
- trigonometry

Frame of reference

When we want to describe the motion of a body, the first thing we need to define is a coordinate system.

Frame of reference

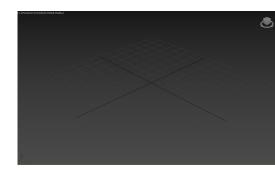
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- Defining these 3 numbers plus a time scale we can represent the position vs time.



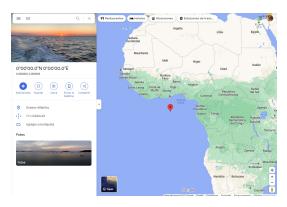
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Another example of a reference system ...



Vectors

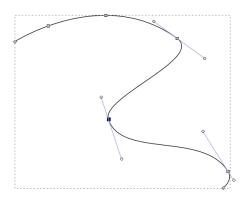
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Vectors

- Some physical quantities, such as time, temperature, mass, and density, can be described completely by a single number with a unit.
- But many other important quantities in physics have a direction associated with them and cannot be described by a single number

For example, you use vectors to determine the direction of a curve in vectorial illustration. . .

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Another examples of vectors?

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- velocity
- acceleration
- ► force

Another examples of vectors?

- velocity
- acceleration
- ► force
- **.**..

How do we use them?

Vectors

► When a physical quantity is described by a single number, we call it a **scalar quantity**.

Vectors

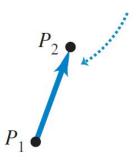
- When a physical quantity is described by a single number, we call it a scalar quantity.
- ► A **vector quantity** has both a magnitude and a direction in space.

Review: Functions

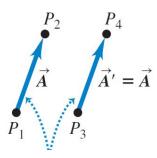
Vectors

- When a physical quantity is described by a single number, we call it a scalar quantity.
- ► A **vector quantity** has both a magnitude and a direction in space.
- We represent a vector quantity by a single letter, italic type with an arrow above it: \vec{v}

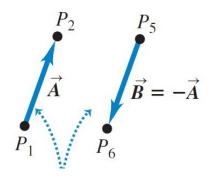
- Vectors are represented by arrows in diagrams.
- the magnitude is just the length of the arrow.
- $ightharpoonup \vec{A} = \vec{A'}$



- If two vectors have the same magnitude and the same direction, they are equal, no matter where they are located in space.
- $ightharpoonup \vec{A} = \vec{A}'$



- We define the negative of a vector as a vector having the same magnitude as the original vector but the opposite direction.
- $\vec{A} = -\vec{B}$
- When two vectors are parallel and have opposite directions, we say that they are antiparallel.



Introduction

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Review: Functions

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Review: Functions

- ► The magnitude of a vector is a positive scalar (a positive number).
- ➤ A vector can never be equal to a scalar because they are different kind of quantities.

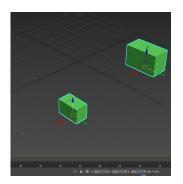
Displacement

Displacement is simply a change in the position of an object.



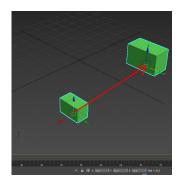
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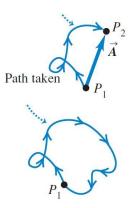
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- The displacement only depend on the initial and final positions.



Introduction

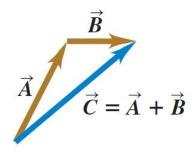
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Operations with vector: Addition and subtraction

Review: Functions

Operations with vector: Addition and subtraction

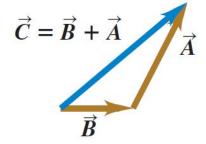
Suppose a particle undergoes a displacement \vec{A} followed by a second displacement \vec{B} . The final result is the same as if the particle had started at the same initial point and undergone a single displacement \vec{C} .



Operations with vector: Addition and subtraction

$$\vec{C} = \vec{A} + \vec{B}$$

- vector addition obeys the commutative law
- $\vec{A} + \vec{B} = \vec{B} + \vec{A}$
- ▶ note that the magnitude of $|C| \le |A| + |B|$

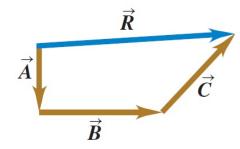


Sum of more than two vector:

$$\vec{R} = (\vec{A} + \vec{B}) + \vec{C} = \vec{D} + \vec{C}$$

or

$$\vec{R} = \vec{A} + (\vec{B} + \vec{C}) = \vec{A} + \vec{E}$$



We define the difference of two vectors \vec{A} and \vec{B} to be the vector sum of \vec{A} and $-\vec{B}$:

$$\vec{A} - \vec{B} = \vec{A} + (-\vec{B})$$

Subtracting
$$\vec{B}$$
 from \vec{A} ...

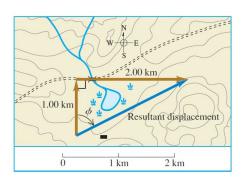
$$\vec{A} - \vec{B} = \vec{A} + \vec{B}$$
... is equivalent to adding $-\vec{B}$ to \vec{A} .

A vector can be multiplied by a positive (negative) scalar quantity. The result is a vector in the same direction (opposite) as the vector but with a different magnitud. The magnitude is $|c||\vec{A}|$

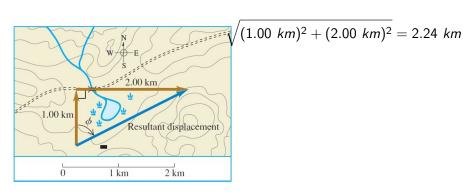
EXAMPLE 1: Adding two vectors that are perpendicular

A cross-country skier skis $1.00 \ km$ north and then $2.00 \ km$ east on a horizontal snowfield. How far and in what direction is she from the starting point?

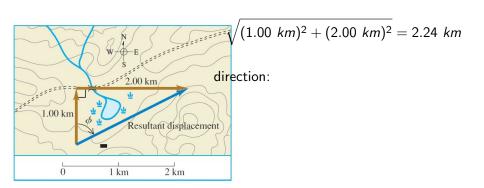
Distance from the starting point:



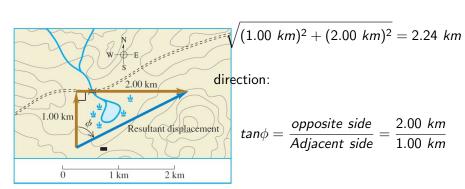
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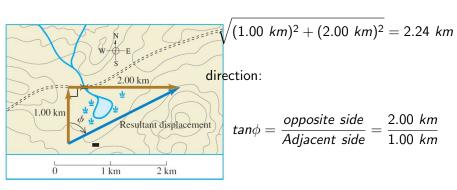
Distance from the starting point:



Distance from the starting point:



Distance from the starting point:



$$(1.00 \text{ km})^2 + (2.00 \text{ km})^2 = 2.24 \text{ km}$$

direction:

$$tan\phi = rac{opposite\ side}{Adjacent\ side} = rac{2.00\ km}{1.00\ km}$$

$$\phi = 63.4^{\circ}$$



Review: Functions

EXAMPLE 2: Test Your Understanding

Two displacement vectors, \vec{u} and \vec{v} have magnitudes 3 and 4. Which of the following could be the magnitude of the difference vector (There may be more than one correct answer.)

- ▶ 9 m
- ▶ 7 m
- ▶ 5 m
- ▶ 1 m
- ▶ 0 m
- ► -1 m



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- Measuring a diagram offers only very limited accuracy.
- So we need a simple but general method for adding vectors.
- This is called the method of components.

COMPONENTS OF VECTORS

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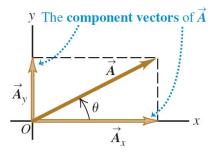
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Review: Functions

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We represent \vec{A} using its components as:

$$\vec{A} = (A_x, A_y) \tag{3}$$

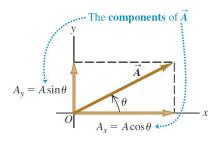


▶ If we know the direction and the magnitude of a vector, we can know the components.

$$\frac{A_x}{A} = \cos\theta$$
, and $\frac{A_y}{A} = \sin\theta$

$$A_x = A\cos\theta$$
, and $A_y = A\sin\theta$

$$\rightarrow \vec{A} = \vec{A}_x + \vec{A}_y$$



Finding a vector's magnitude and direction from its components.

$$A = \sqrt{A_x^2 + A_y^2} \tag{4}$$

$$tan\theta = \frac{A_y}{A_x}$$
 and $\theta = arctan(\frac{A_y}{A_x})$ (5)

Review: Functions

Multiplying a vector by a scalar.

$$\vec{D} = c\vec{A} \tag{6}$$

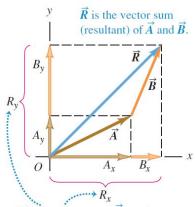
$$D_x = cA_x$$
 and $D_y = cA_y$ (7)

Using the components to calculate the vector sum

$$\vec{R} = \vec{A} + \vec{B}$$

$$R_x = A_x + B_x$$

$$R_y = A_y + B_y$$

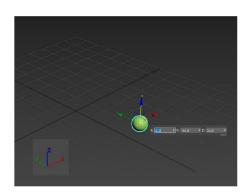


The components of \vec{R} are the sums of the components of \vec{A} and \vec{B} :

$$R_y = A_y + B_y \qquad R_x = A_x + B_x$$

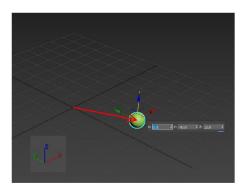
EXAMPLE:

You are using vector sums to move objects in 3ds Max all the time...



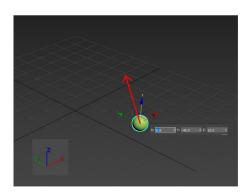
EXAMPLE:

Position vector



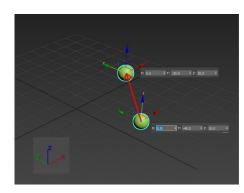
EXAMPLE:

Displacement Vector



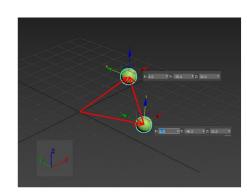
EXAMPLE:

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EXAMPLE:

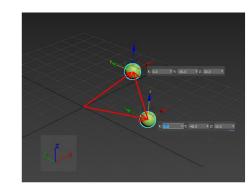
Final Position=Position Vector + Displacement Vector



EXAMPLE:

A more elegant notation...

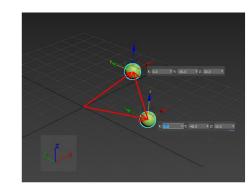
$$\vec{r}_f = \vec{r}_i + \Delta \vec{r} \tag{8}$$



EXAMPLE:

so, the displacement vector is...

$$\Delta \vec{r} + = \vec{r}_f - \vec{r}_i \qquad (9)$$

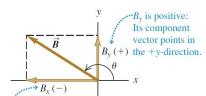


Introduction

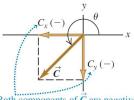
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In general, we use the symbol Δ to represent the change of a magnitude...

► In the previous definitions we measure the angles as in the figure.

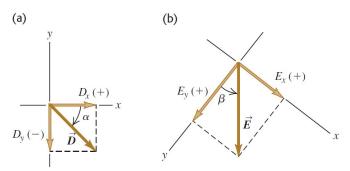


 \vec{B}_x is negative: Its component vector points in the -x-direction.



Both components of \vec{C} are negative.

EXAMPLE: (a) What are the x and y components of vector in the figure? The magnitude of the vector \vec{D} is D=3.00~m, and the angle $\alpha=45^\circ$. (b) What are the x- and y-components of vector \vec{E} in? The magnitude of the vector is E=4.50~m, and the angle $\beta=45^\circ$



Adding more than one vector:

$$\vec{R} = \vec{A} + \vec{B} + \vec{C}$$

$$\to R_x = A_x + B_x + C_y$$

$$\rightarrow R_y = A_y + B_y + C_y$$

$$\rightarrow R_y = A_z + B_z + C_z$$

Magnitude of a vector with 3 components:

$$|\vec{A}| = \sqrt{A_x^2 + A_y^2 + A_z^2}$$

Review: Functions

Test your understanding:

Two vectors \vec{A} and \vec{B} both lie in the xy-plane.

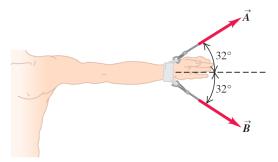
- ls it possible for \vec{A} to have the same magnitude as \vec{B} but different components?
- Is it possible for \vec{A} to have the same components as \vec{B} but a different magnitude?

Let's solve some exercises from Sears & Zemansky's Book¹:

A disoriented physics professor drives $3.25\ km$ north, then $2.90\ km$ west, and then $1.5\ km$ south. Find the magnitude and direction of the resultant displacement, using the method of components. In a vector-addition diagram (roughly to scale), show that the resultant displacement found from your diagram is in qualitative agreement with the result you obtained using the method of components.

¹Sears & Zemansky with modern physics 13th edition. (♂) (≥) (≥) (≥) () ()

A patient with a dislocated shoulder is put into a traction apparatus as shown in the figure². The pulls and have equal magnitudes and must combine to produce an outward traction force of 5.60 N on the patient's arm. How large should these pulls be?



▶ A unit vector is a vector that has a magnitude 1 with no units

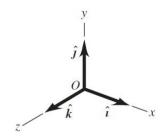
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- the unit vectors that point into the direction of the coordinate axes are:

 \hat{i} , \hat{j} , and \hat{k}



We can represent component vectors like this:

$$\rightarrow \vec{A_x} = A_x \hat{\imath}$$

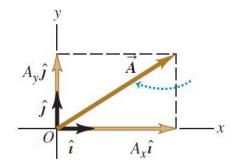
$$\rightarrow \vec{A_y} = A_y \hat{\jmath}$$

$$\rightarrow \vec{A_z} = A_z \hat{k}$$

We can represent a vector using this notation:

$$\vec{A} = \vec{A}_x + \vec{A}_y$$

$$\rightarrow \vec{A} = A_x \hat{\imath} + A_y \hat{\jmath}$$



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How can we represent the sum of two vectors using this notation? Guess!

Test your understanding

Arrange the following vectors in order of their magnitude, with the vector of largest magnitude first.

$$1. \vec{A} = (3\hat{\imath} + 5\hat{\jmath} - 2\hat{k})$$

2.
$$\vec{A} = (-3\hat{\imath} + 5\hat{\jmath} - 2\hat{k})$$

3.
$$\vec{A} = (3\hat{\imath} - 5\hat{\jmath} - 2\hat{k})$$

4.
$$\vec{A} = (3\hat{\imath} + 5\hat{\jmath} + 2\hat{k})$$

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Functions

Functions

➤ A function is a binary relation between two sets that associates every element of the first set to exactly one element of the second set

Functions

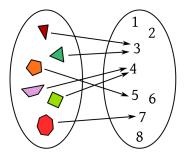
- ➤ A function is a binary relation between two sets that associates every element of the first set to exactly one element of the second set
- some useful functions:
 - 1. linear functions
 - 2. quadratic functions
 - 3. sin, cos
 - 4. exponential, logarithmic function

Introduction

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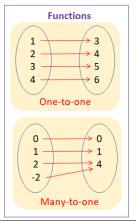
Examples . . .

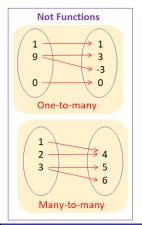
Examples . . .



Relations

A relation shows a relationship between two values. A function is a relation where each input has only one output.







Anabela R. Turlione

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Instead of using diagrams, we can use a law to draw the function in the x-y axes \dots

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$$y = f(x)$$

Linear Functions:

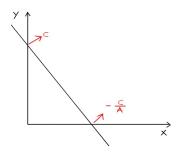
$$f(x) = Ax + C$$

Linear Functions:

$$f(x) = Ax + C$$

Representation in the xy axes coordinates:

$$y = Ax + C$$



Cuadratic Functions:

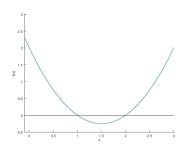
$$f(x) = ax^2 + bx + c$$

Cuadratic Functions:

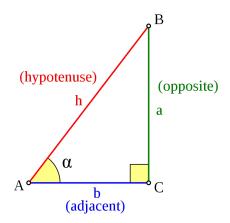
$$f(x) = ax^2 + bx + c$$

Representation in the xy axes coordinates:

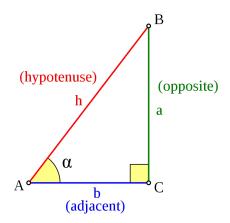
$$y = ax^2 + bx + c$$



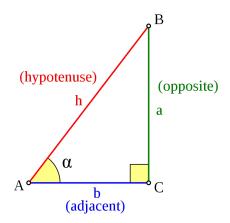
$$\mathit{sin}(\alpha) = \frac{\mathit{opposite}}{\mathit{hypotenuse}}$$

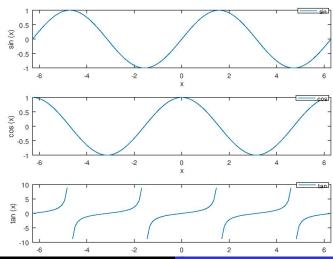


$$cos(\alpha) = \frac{adjacent}{hypotenuse}$$

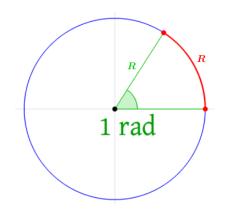


$$tan(\alpha) = \frac{opposite}{adjacent}$$





Measuring angles: radians



Introduction

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Radians to degrees

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$$radians = \frac{arc\ length}{radious}$$

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 rad \rightarrow 360deg

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Radians to degrees

$$radians = \frac{arc\ length}{radious} = \frac{2\pi}{1}$$

$$2\pi$$
 rad \rightarrow 360deg

$$x \ rad \rightarrow \frac{360}{2\pi}x = \frac{180}{\pi}x$$

$$sin(30) = 0.5$$

$$\textit{sin}(30) = 0.5 \rightarrow \textit{asin}(0.5) = 30$$

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Review: Functions

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$$tan(30) = 0.57735026919 \rightarrow atan(0.57735026919) = 30$$

Review: Functions

How do I calculate the angle if I know the sin/cos/tan?

$$sin(30) = 0.5 \rightarrow asin(0.5) = 30$$

$$cos(30) = 0.86602540378 \rightarrow acos(0.86602540378) = 30$$

$$tan(30) = 0.57735026919 \rightarrow atan(0.57735026919) = 30$$

You have to check what are the units of the angles. . .

