

Summary

Commutativity:

$$p \vee q \Leftrightarrow q \vee p \quad p \wedge q \Leftrightarrow q \wedge p$$

Associativity:

$$p \vee (q \vee r) \Leftrightarrow (p \vee q) \vee r$$

$$p \wedge (q \wedge r) \Leftrightarrow (p \wedge q) \wedge r$$

Idempotence:

$$p \vee p \Leftrightarrow p \text{ and } p \wedge p \Leftrightarrow p$$

Distributivity:

$$p \vee (q \wedge r) \Leftrightarrow (p \vee q) \wedge (p \vee r)$$

$$p \wedge (q \vee r) \Leftrightarrow (p \wedge q) \vee (p \wedge r)$$

De Morgan's Laws:

$$\neg(p \vee q) \Leftrightarrow \neg p \wedge \neg q$$

$$\neg(p \wedge q) \Leftrightarrow \neg p \vee \neg q$$

Double Negation Law:

$$\neg(\neg p) \Leftrightarrow p;$$

Tautology Laws:

$$p \vee \text{true} \Leftrightarrow \text{true}$$

$$p \wedge \text{true} \Leftrightarrow p$$

Contradiction Laws:

$$p \vee \text{false} \Leftrightarrow p \quad p \wedge \text{false} \Leftrightarrow \text{false}$$

Excluded Middle Laws:

$$p \vee \neg p \Leftrightarrow \text{true}$$

$$p \wedge \neg p \Leftrightarrow \text{false}$$

Absorption Laws:

$$p \vee (p \wedge q) \Leftrightarrow p \quad p \wedge (p \vee q) \Leftrightarrow p$$

Implication Law:

$$p \Rightarrow q \Leftrightarrow \neg p \vee q$$

Contrapositive Law:

$$p \Rightarrow q \Leftrightarrow \neg q \Rightarrow \neg p$$

Equivalence Law:

$$(p \Leftrightarrow q) \Leftrightarrow (p \Rightarrow q) \wedge (q \Rightarrow p)$$