

# Efficient Configuration Space Representation in Path Planning

Akhil Avula, Aidan Cookson, Calvin Chang, Daniel Truong

[aavula@g.ucla.edu](mailto:aavula@g.ucla.edu), [aucookson@g.ucla.edu](mailto:aucookson@g.ucla.edu), [calvinchang33@g.ucla.edu](mailto:calvinchang33@g.ucla.edu), [dktruong@g.ucla.edu](mailto:dktruong@g.ucla.edu)

UCLA ECE 209AS Fall 2020

# Overview

- Introduction to Path Planning
- Previous Research
- Shortcomings of Research
- Problem Statement
- Procedural Map Generation
- Quadtrees Design Process
- Implementation
- Expected Results
- Conclusion and Future Works

# Path Planning Problem

- Automated traveling from point A to point B
- Feasible and Optimal Path
- Assume holonomic robot

Configuration space:  $C$

Obstacles:  $C_{obs} \in C$

Feasible robot states:  $C_{feasible} \in C$

$$C_{feasible} \cup C_{obs} = C$$

$$C_{feasible} \cap C_{obs} = \emptyset$$

Starting state:  $s_i \in C_{feasible}$

Goal state:  $s_f \in C_{feasible}$



Taken from National Stone, Sand, and Gravel Association [8]



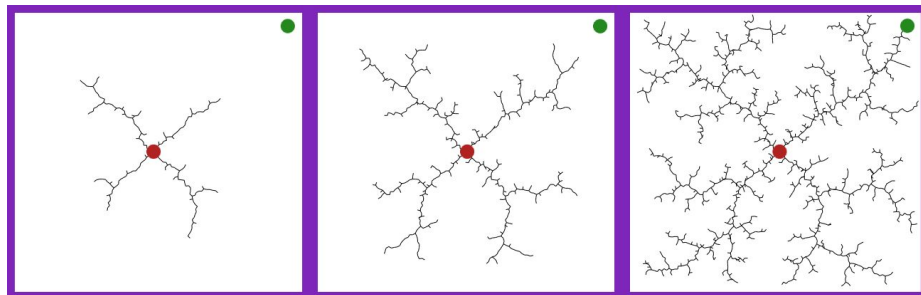
Taken from Wikipedia: user Dtom [9]

How to represent configuration  
space?

# Previous Research

- Mapping configuration space into graph

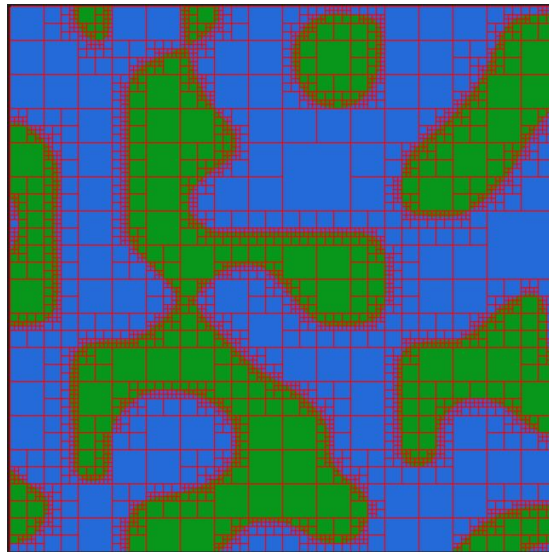
- Grid
- Probabilistic Roadmap<sup>[1]</sup>
- Quadtrees<sup>[2]</sup>
- Visibility Graph<sup>[3]</sup>
- Triangulation<sup>[4]</sup>
- Rapidly Exploring Random Test<sup>[5]</sup>



From RRT paper by LaValle [5]

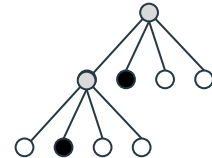
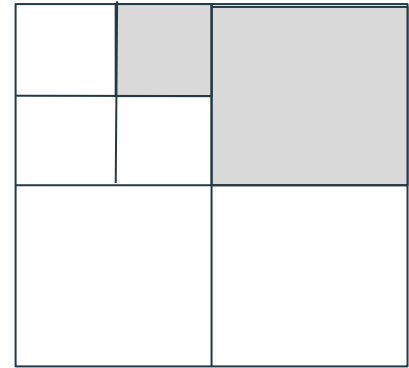
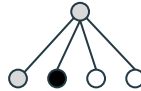
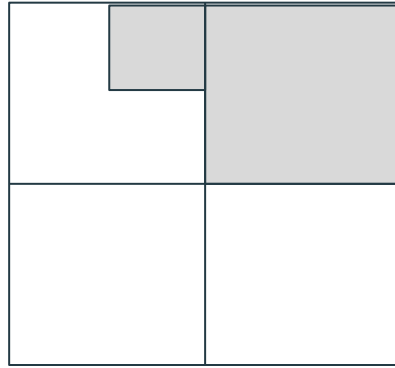
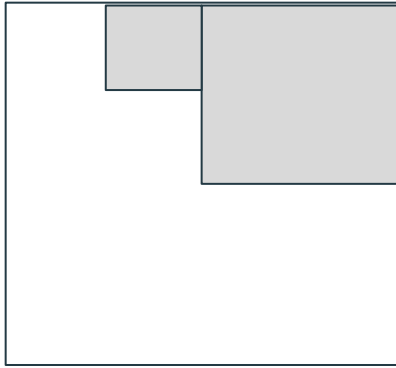
# Previous Research: Quadtrees

- Hierarchical data structure
  - Recursively subdivides a space
  - Other Applications:
    - Image processing
    - Cartography



Example quadtree mapping of the config space

## Config space

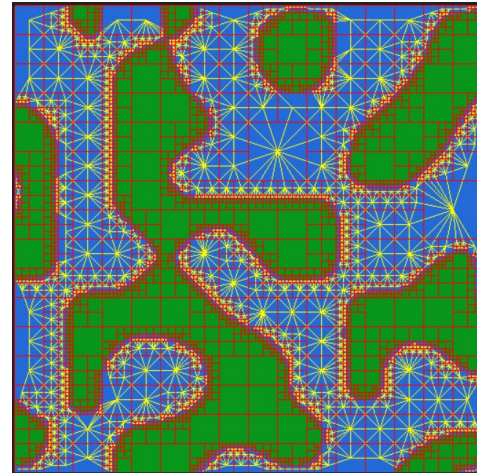
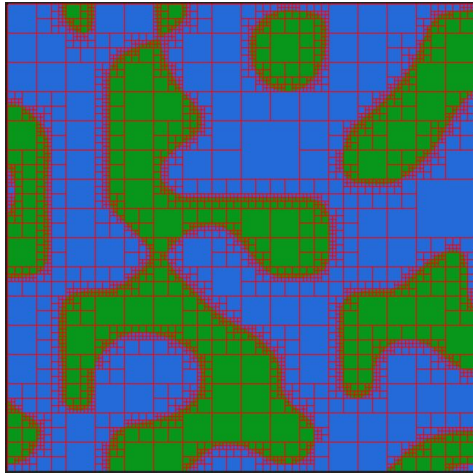


- : free space and obstacle
- : all obstacle
- : all free space

Split when node is gray

# Neighbor finding technique for Quadtrees

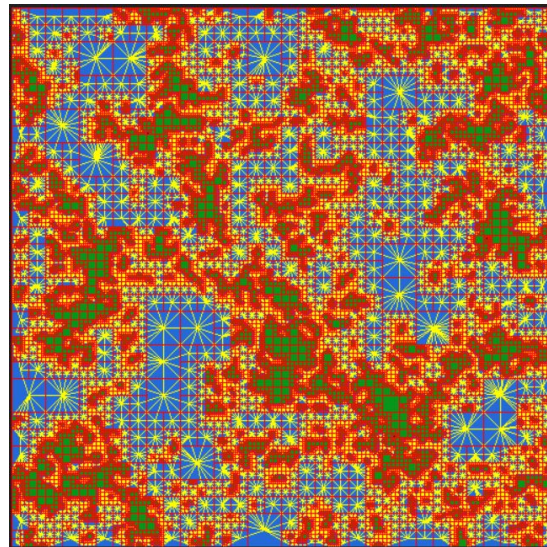
Use techniques from [10] to find neighbors in quadtree





# Shortcomings of Previous Work

- Main Issue:
  - Allocation of quadtree nodes in configuration space
- Other shortcomings:
  - Representing vast unstructured environments
  - Configuration spaces of 3D spaces
  - Handling Dynamic obstacles
  - Quadtrees require more memory



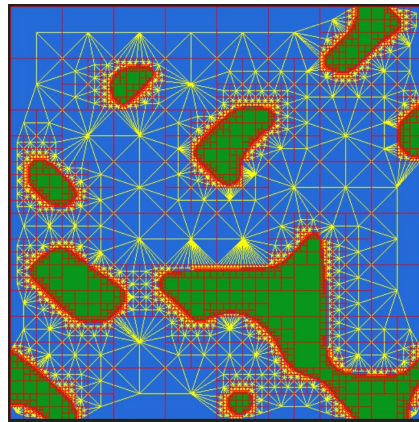
Quadtrees on dense environment  
~26000 nodes

# Problem Statement

Goal: Create a more **efficient quadtree representation** of the configuration space assuming a holonomic robot

Scenario: Combination of large obstacles and small but dense obstacles

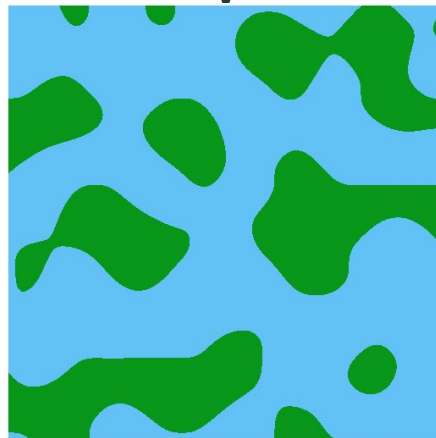
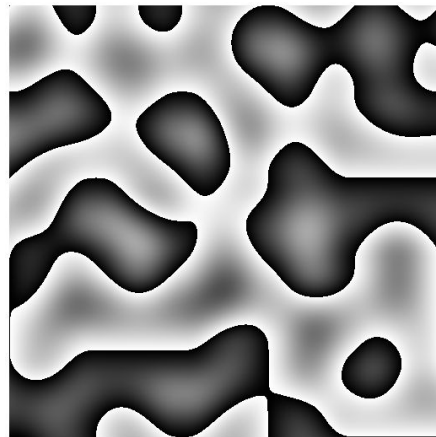
Task: Starting node  $\longrightarrow$  Goal node



Quadtree mapping of the config space

# Procedural Map Generation

- Perlin Noise to randomly generate configuration space
  - Gradient noise by Ken Perlin
  - Common in map generation for games
  - Binary threshold is used to generate islands
  - Realistically simulates a naval path planning problem



# Pruning Algorithm Heuristics

## Quadtrees Characterization and Properties

### Splitting rules:

- Minimum Resolution
- Pruning Distance Thresholds  $t_1, t_2$ , and  $t_3$

## Heuristic Considerations

### Optimal path close to:

- Straight line from start to goal

### Obstacles considerations:

- Only around starting node, goal node and optimal path

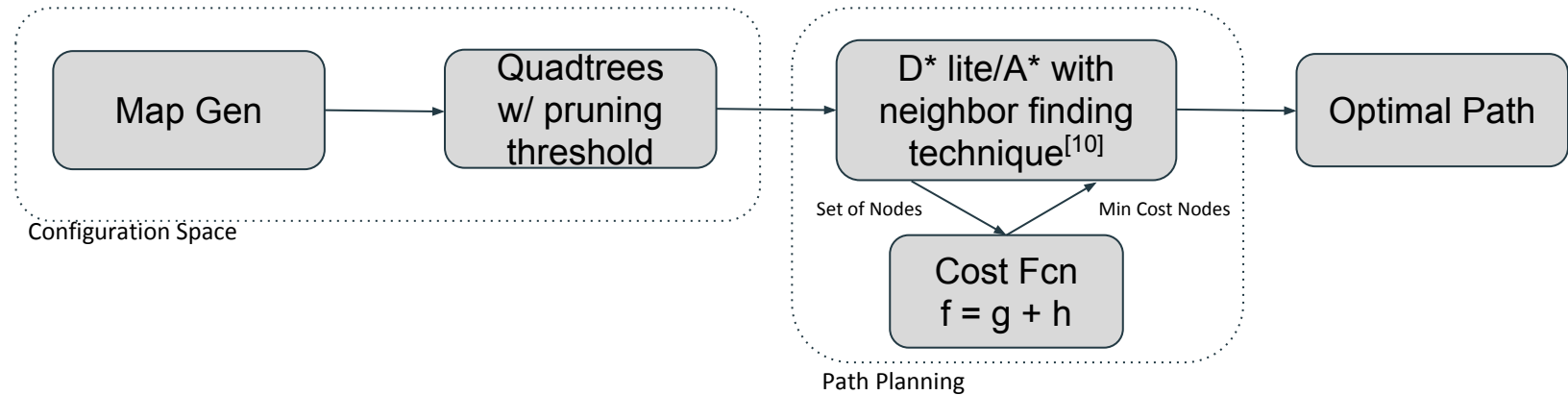
### Quadtree Resolution considerations:

- Size of smallest chokepoint

### Split if:

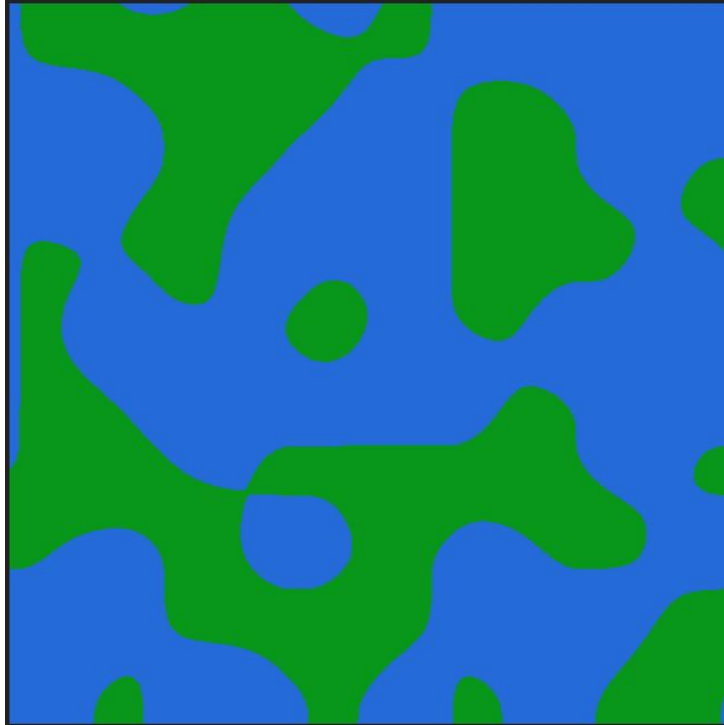
$\text{dist}(\text{node}, \text{start}) \leq t_1$  OR  $\text{dist}(\text{node}, \text{goal}) \leq t_2$  OR  $\text{dist}(\text{node}, \text{start}) + \text{dist}(\text{node}, \text{goal}) \leq t_3$

# Dynamic Path Planning Implementation



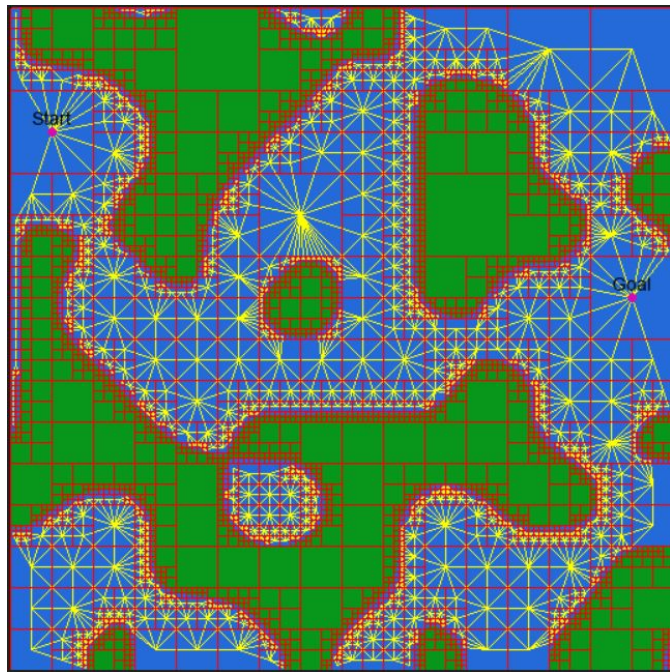
# Preliminary Results

# Initial Map

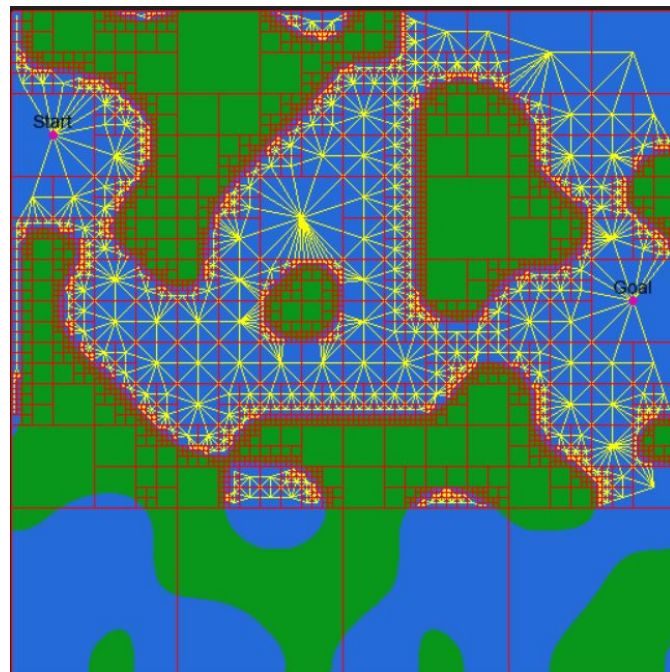


Map Generation Output

# Pruned Quadtree Results



Quad Tree Without Pruning Output (1054 nodes)

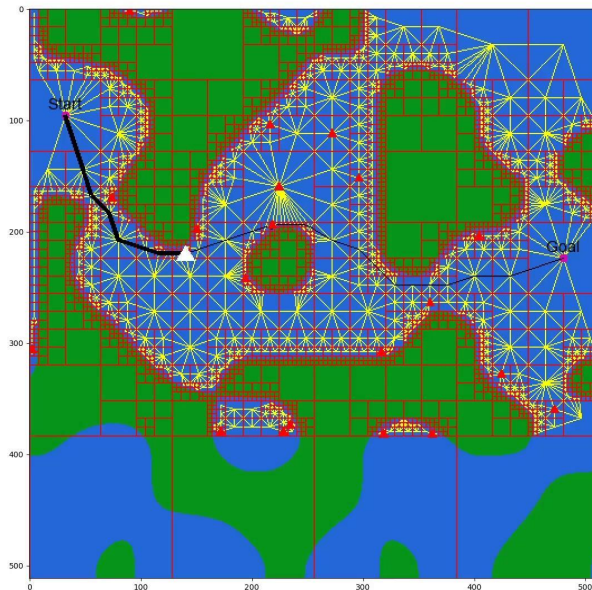


Quad Tree With Pruning Output (492 nodes)



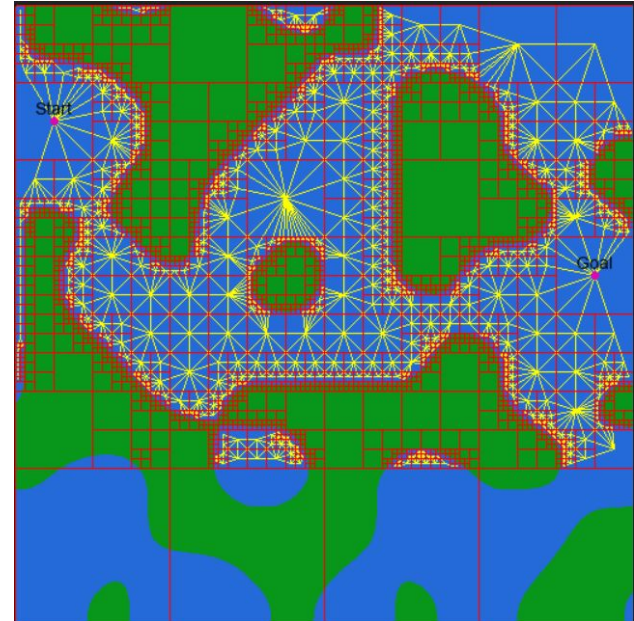
# Pruned Path Planning with Dynamic Obstacles (Preliminary Results)

- Moving obstacles (Red triangles) are added to the map
- A\* is used every time step to completely recalculate the path



# Conclusion

- More efficient representation of configuration space
  - Less memory needed
  - Possibly faster planning
- Pruned Quadtrees Approach
  - Remove unneeded nodes
  - Focus on nodes needed for the path



# Future Works

- Applying a better pruning heuristic to be more generalizable to new maps
- Using ALT algorithm<sup>[11]</sup> to further increase path planning speed
- Use D\* Lite to optimize path planning with dynamic obstacles
- K-framed Quadtrees<sup>[6]</sup> with pruning?
- Testing on larger environments

# Contacts

Akhil Avula, Aidan Cookson, Calvin Chang, Daniel Truong  
[aavula@g.ucla.edu](mailto:aavula@g.ucla.edu), [aucookson@g.ucla.edu](mailto:aucookson@g.ucla.edu), [calvinchang33@g.ucla.edu](mailto:calvinchang33@g.ucla.edu), [dktruong@g.ucla.edu](mailto:dktruong@g.ucla.edu)

# References

- [1] [Probabilistic Roadmaps for Path Planning in High-Dimensional Configuration Spaces - Robotics and Automation](#)
- [2] <https://link.springer.com/article/10.1007/BF00288933>
- [3] <https://dl.acm.org/doi/10.1145/359156.359164>
- [4] <https://citeseerx.ist.psu.edu/viewdoc/download?doi=10.1.1.83.1711&rep=rep1&type=pdf>
- [5] <http://msl.cs.uiuc.edu/~lavalle/papers/Lav98c.pdf>
- [6] [https://link.springer.com/chapter/10.1007/978-3-319-70833-1\\_5](https://link.springer.com/chapter/10.1007/978-3-319-70833-1_5)
- [7] <https://ieeexplore.ieee.org/stamp/stamp.jsp?tp=&arnumber=8703890>
- [8] <https://www.nssga.org/making-case-infrastructure-investment/cars-in-traffic/>
- [9] [https://en.wikipedia.org/wiki/Cargo\\_aircraft#/media/File:An-124\\_ready.jpg](https://en.wikipedia.org/wiki/Cargo_aircraft#/media/File:An-124_ready.jpg)
- [10] <https://citeseerx.ist.psu.edu/viewdoc/download?doi=10.1.1.445.7785&rep=rep1&type=pdf>
- [11] <https://www.cs.princeton.edu/courses/archive/spring06/cos423/Handouts/GH05.pdf>