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In[93]:= sigma[x_] = ((2 * (muz + g x) * nu) / (K * (nu + muz + g x))) ^ 0.5
f[x_] = (T x / (2 * (nu + muz + g x))) +
  T (((2 / (K * nu)) ^ 0.5) * ((muz + g x) ^ 1.5 / (muz + nu + g x) ^ 0.5) *
    ((sinh[x / sigma[x]]) / (cosh[L / sigma[x]]))) / (muz + nu + g x)
f'[x_]
f''[x_]

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$$\text{Out[93]} = 1.41421 \left(\frac{\text{nu} (\text{muz} + \text{g x})}{K (\text{muz} + \text{nu} + \text{g x})} \right)^{0.5}$$

$$\text{Out[94]} = \frac{T x}{2 (\text{muz} + \text{nu} + \text{g x})} + \frac{1.41421 \left(\frac{1}{K \text{nu}} \right)^{0.5} T (\text{muz} + \text{g x})^{1.5} \sinh \left[\frac{0.707107 x}{\left(\frac{\text{nu} (\text{muz} + \text{g x})}{K (\text{muz} + \text{nu} + \text{g x})} \right)^{0.5}} \right]}{(\text{muz} + \text{nu} + \text{g x})^{1.5} \cosh \left[\frac{0.707107 L}{\left(\frac{\text{nu} (\text{muz} + \text{g x})}{K (\text{muz} + \text{nu} + \text{g x})} \right)^{0.5}} \right]}$$

$$\text{Out[95]} = -\frac{g T x_-}{2 (\text{muz} + \text{nu} + \text{g x}_-)^2} + \frac{T}{2 (\text{muz} + \text{nu} + \text{g x}_-)} - \frac{2.12132 g \left(\frac{1}{K \text{nu}} \right)^{0.5} T (\text{muz} + \text{g x}_-)^{1.5} \sinh \left[\frac{0.707107 x_-}{\left(\frac{\text{nu} (\text{muz} + \text{g x}_-)}{K (\text{muz} + \text{nu} + \text{g x}_-)} \right)^{0.5}} \right]}{\cosh \left[\frac{0.707107 L}{\left(\frac{\text{nu} (\text{muz} + \text{g x}_-)}{K (\text{muz} + \text{nu} + \text{g x}_-)} \right)^{0.5}} \right] (\text{muz} + \text{nu} + \text{g x}_-)^{2.5}} +$$

$$\frac{2.12132 g \left(\frac{1}{K \text{nu}} \right)^{0.5} T (\text{muz} + \text{g x}_-)^{0.5} \sinh \left[\frac{0.707107 x_-}{\left(\frac{\text{nu} (\text{muz} + \text{g x}_-)}{K (\text{muz} + \text{nu} + \text{g x}_-)} \right)^{0.5}} \right]}{\cosh \left[\frac{0.707107 L}{\left(\frac{\text{nu} (\text{muz} + \text{g x}_-)}{K (\text{muz} + \text{nu} + \text{g x}_-)} \right)^{0.5}} \right] (\text{muz} + \text{nu} + \text{g x}_-)^{1.5}} +$$

$$\left(0.5 L \left(\frac{1}{K \text{nu}} \right)^{0.5} T (\text{muz} + \text{g x}_-)^{1.5} \left(-\frac{g \text{nu} (\text{muz} + \text{g x}_-)}{K (\text{muz} + \text{nu} + \text{g x}_-)^2} + \frac{g \text{nu}}{K (\text{muz} + \text{nu} + \text{g x}_-)} \right) \right)$$

$$\sinh \left[\frac{0.707107 x_-}{\left(\frac{\text{nu} (\text{muz} + \text{g x}_-)}{K (\text{muz} + \text{nu} + \text{g x}_-)} \right)^{0.5}} \right] \cosh' \left[\frac{0.707107 L}{\left(\frac{\text{nu} (\text{muz} + \text{g x}_-)}{K (\text{muz} + \text{nu} + \text{g x}_-)} \right)^{0.5}} \right] \Bigg/$$

$$\left(\cosh \left[\frac{0.707107 L}{\left(\frac{\text{nu} (\text{muz} + \text{g x}_-)}{K (\text{muz} + \text{nu} + \text{g x}_-)} \right)^{0.5}} \right]^2 \left(\frac{\text{nu} (\text{muz} + \text{g x}_-)}{K (\text{muz} + \text{nu} + \text{g x}_-)} \right)^{1.5} (\text{muz} + \text{nu} + \text{g x}_-)^{1.5} \right) +$$

$$\left(1.41421 \left(\frac{1}{K \text{nu}} \right)^{0.5} T (\text{muz} + \text{g x}_-)^{1.5} \right)$$

$$\left(\frac{0.707107}{\left(\frac{\text{nu} (\text{muz} + \text{g x}_-)}{K (\text{muz} + \text{nu} + \text{g x}_-)} \right)^{0.5}} - \frac{0.353553 x_- \left(-\frac{g \text{nu} (\text{muz} + \text{g x}_-)}{K (\text{muz} + \text{nu} + \text{g x}_-)^2} + \frac{g \text{nu}}{K (\text{muz} + \text{nu} + \text{g x}_-)} \right)}{\left(\frac{\text{nu} (\text{muz} + \text{g x}_-)}{K (\text{muz} + \text{nu} + \text{g x}_-)} \right)^{1.5}} \right) \sinh' \left[\frac{0.707107 x_-}{\left(\frac{\text{nu} (\text{muz} + \text{g x}_-)}{K (\text{muz} + \text{nu} + \text{g x}_-)} \right)^{0.5}} \right] \Bigg/$$

$$\left(\cosh \left[\frac{0.707107 L}{\left(\frac{\text{nu} (\text{muz} + \text{g x}_-)}{K (\text{muz} + \text{nu} + \text{g x}_-)} \right)^{0.5}} \right] (\text{muz} + \text{nu} + \text{g x}_-)^{1.5} \right)$$

$$\begin{aligned}
\text{Out[96]} = & \frac{g^2 T x_-}{(\text{muz} + \text{nu} + g x_-)^3} - \frac{g T}{(\text{muz} + \text{nu} + g x_-)^2} + \frac{5.3033 g^2 \left(\frac{1}{K \text{nu}} \right)^{0.5} T (\text{muz} + g x_-)^{1.5} \sinh \left[\frac{0.707107 x_-}{\left(\frac{\text{nu} (\text{muz} + g x_-)}{K (\text{muz} + \text{nu} + g x_-)} \right)^{0.5}} \right]}{\cosh \left[\frac{0.707107 L}{\left(\frac{\text{nu} (\text{muz} + g x_-)}{K (\text{muz} + \text{nu} + g x_-)} \right)^{0.5}} \right] (\text{muz} + \text{nu} + g x_-)^{3.5}} - \\
& \frac{6.36396 g^2 \left(\frac{1}{K \text{nu}} \right)^{0.5} T (\text{muz} + g x_-)^{0.5} \sinh \left[\frac{0.707107 x_-}{\left(\frac{\text{nu} (\text{muz} + g x_-)}{K (\text{muz} + \text{nu} + g x_-)} \right)^{0.5}} \right]}{\cosh \left[\frac{0.707107 L}{\left(\frac{\text{nu} (\text{muz} + g x_-)}{K (\text{muz} + \text{nu} + g x_-)} \right)^{0.5}} \right] (\text{muz} + \text{nu} + g x_-)^{2.5}} + \\
& \frac{1.06066 g^2 \left(\frac{1}{K \text{nu}} \right)^{0.5} T \sinh \left[\frac{0.707107 x_-}{\left(\frac{\text{nu} (\text{muz} + g x_-)}{K (\text{muz} + \text{nu} + g x_-)} \right)^{0.5}} \right]}{\cosh \left[\frac{0.707107 L}{\left(\frac{\text{nu} (\text{muz} + g x_-)}{K (\text{muz} + \text{nu} + g x_-)} \right)^{0.5}} \right] (\text{muz} + g x_-)^{0.5} (\text{muz} + \text{nu} + g x_-)^{1.5}} + \\
& \left(0.5 L \left(\frac{1}{K \text{nu}} \right)^{0.5} T (\text{muz} + g x_-)^{1.5} \left(\frac{2 g^2 \text{nu} (\text{muz} + g x_-)}{K (\text{muz} + \text{nu} + g x_-)^3} - \frac{2 g^2 \text{nu}}{K (\text{muz} + \text{nu} + g x_-)^2} \right) \right. \\
& \left. \sinh \left[\frac{0.707107 x_-}{\left(\frac{\text{nu} (\text{muz} + g x_-)}{K (\text{muz} + \text{nu} + g x_-)} \right)^{0.5}} \right] \cosh' \left[\frac{0.707107 L}{\left(\frac{\text{nu} (\text{muz} + g x_-)}{K (\text{muz} + \text{nu} + g x_-)} \right)^{0.5}} \right] \right) / \\
& \left(\cosh \left[\frac{0.707107 L}{\left(\frac{\text{nu} (\text{muz} + g x_-)}{K (\text{muz} + \text{nu} + g x_-)} \right)^{0.5}} \right]^2 \left(\frac{\text{nu} (\text{muz} + g x_-)}{K (\text{muz} + \text{nu} + g x_-)} \right)^{1.5} (\text{muz} + \text{nu} + g x_-)^{1.5} \right) - \\
& \left(1.5 g L \left(\frac{1}{K \text{nu}} \right)^{0.5} T (\text{muz} + g x_-)^{1.5} \left(- \frac{g \text{nu} (\text{muz} + g x_-)}{K (\text{muz} + \text{nu} + g x_-)^2} + \frac{g \text{nu}}{K (\text{muz} + \text{nu} + g x_-)} \right) \right. \\
& \left. \sinh \left[\frac{0.707107 x_-}{\left(\frac{\text{nu} (\text{muz} + g x_-)}{K (\text{muz} + \text{nu} + g x_-)} \right)^{0.5}} \right] \cosh' \left[\frac{0.707107 L}{\left(\frac{\text{nu} (\text{muz} + g x_-)}{K (\text{muz} + \text{nu} + g x_-)} \right)^{0.5}} \right] \right) / \\
& \left(\cosh \left[\frac{0.707107 L}{\left(\frac{\text{nu} (\text{muz} + g x_-)}{K (\text{muz} + \text{nu} + g x_-)} \right)^{0.5}} \right]^2 \left(\frac{\text{nu} (\text{muz} + g x_-)}{K (\text{muz} + \text{nu} + g x_-)} \right)^{1.5} (\text{muz} + \text{nu} + g x_-)^{2.5} \right) + \\
& \left(1.5 g L \left(\frac{1}{K \text{nu}} \right)^{0.5} T (\text{muz} + g x_-)^{0.5} \left(- \frac{g \text{nu} (\text{muz} + g x_-)}{K (\text{muz} + \text{nu} + g x_-)^2} + \frac{g \text{nu}}{K (\text{muz} + \text{nu} + g x_-)} \right) \right. \\
& \left. \sinh \left[\frac{0.707107 x_-}{\left(\frac{\text{nu} (\text{muz} + g x_-)}{K (\text{muz} + \text{nu} + g x_-)} \right)^{0.5}} \right] \cosh' \left[\frac{0.707107 L}{\left(\frac{\text{nu} (\text{muz} + g x_-)}{K (\text{muz} + \text{nu} + g x_-)} \right)^{0.5}} \right] \right) / \\
& \left(\cosh \left[\frac{0.707107 L}{\left(\frac{\text{nu} (\text{muz} + g x_-)}{K (\text{muz} + \text{nu} + g x_-)} \right)^{0.5}} \right]^2 \left(\frac{\text{nu} (\text{muz} + g x_-)}{K (\text{muz} + \text{nu} + g x_-)} \right)^{1.5} (\text{muz} + \text{nu} + g x_-)^{1.5} \right) -
\end{aligned}$$

$$\begin{aligned}
& \left(0.75 L \left(\frac{1}{K \nu} \right)^{0.5} T (\text{muz} + g x_-)^{1.5} \left(-\frac{g \nu (\text{muz} + g x_-)}{K (\text{muz} + \nu + g x_-)^2} + \frac{g \nu}{K (\text{muz} + \nu + g x_-)} \right)^2 \right. \\
& \quad \left. \sinh \left[\frac{0.707107 x_-}{\left(\frac{\nu (\text{muz} + g x_-)}{K (\text{muz} + \nu + g x_-)} \right)^{0.5}} \right] \cosh' \left[\frac{0.707107 L}{\left(\frac{\nu (\text{muz} + g x_-)}{K (\text{muz} + \nu + g x_-)} \right)^{0.5}} \right] \right) / \\
& \quad \left(\cosh \left[\frac{0.707107 L}{\left(\frac{\nu (\text{muz} + g x_-)}{K (\text{muz} + \nu + g x_-)} \right)^{0.5}} \right]^2 \left(\frac{\nu (\text{muz} + g x_-)}{K (\text{muz} + \nu + g x_-)} \right)^{2.5} (\text{muz} + \nu + g x_-)^{1.5} \right) + \\
& \quad \left(0.353553 L^2 \left(\frac{1}{K \nu} \right)^{0.5} T (\text{muz} + g x_-)^{1.5} \left(-\frac{g \nu (\text{muz} + g x_-)}{K (\text{muz} + \nu + g x_-)^2} + \frac{g \nu}{K (\text{muz} + \nu + g x_-)} \right)^2 \right. \\
& \quad \left. \sinh \left[\frac{0.707107 x_-}{\left(\frac{\nu (\text{muz} + g x_-)}{K (\text{muz} + \nu + g x_-)} \right)^{0.5}} \right] \cosh' \left[\frac{0.707107 L}{\left(\frac{\nu (\text{muz} + g x_-)}{K (\text{muz} + \nu + g x_-)} \right)^{0.5}} \right]^2 \right) / \\
& \quad \left(\cosh \left[\frac{0.707107 L}{\left(\frac{\nu (\text{muz} + g x_-)}{K (\text{muz} + \nu + g x_-)} \right)^{0.5}} \right]^3 \left(\frac{\nu (\text{muz} + g x_-)}{K (\text{muz} + \nu + g x_-)} \right)^{3.5} (\text{muz} + \nu + g x_-)^{1.5} \right) - \\
& \quad \left(4.24264 g \left(\frac{1}{K \nu} \right)^{0.5} T (\text{muz} + g x_-)^{1.5} \right. \\
& \quad \left(\frac{0.707107}{\left(\frac{\nu (\text{muz} + g x_-)}{K (\text{muz} + \nu + g x_-)} \right)^{0.5}} - \frac{0.353553 x_- \left(-\frac{g \nu (\text{muz} + g x_-)}{K (\text{muz} + \nu + g x_-)^2} + \frac{g \nu}{K (\text{muz} + \nu + g x_-)} \right)}{\left(\frac{\nu (\text{muz} + g x_-)}{K (\text{muz} + \nu + g x_-)} \right)^{1.5}} \right) \sinh' \left[\frac{0.707107 x_-}{\left(\frac{\nu (\text{muz} + g x_-)}{K (\text{muz} + \nu + g x_-)} \right)^{0.5}} \right] \right) / \\
& \quad \left(\cosh \left[\frac{0.707107 L}{\left(\frac{\nu (\text{muz} + g x_-)}{K (\text{muz} + \nu + g x_-)} \right)^{0.5}} \right] (\text{muz} + \nu + g x_-)^{2.5} \right) + \left(4.24264 g \left(\frac{1}{K \nu} \right)^{0.5} T (\text{muz} + g x_-)^{0.5} \right. \\
& \quad \left(\frac{0.707107}{\left(\frac{\nu (\text{muz} + g x_-)}{K (\text{muz} + \nu + g x_-)} \right)^{0.5}} - \frac{0.353553 x_- \left(-\frac{g \nu (\text{muz} + g x_-)}{K (\text{muz} + \nu + g x_-)^2} + \frac{g \nu}{K (\text{muz} + \nu + g x_-)} \right)}{\left(\frac{\nu (\text{muz} + g x_-)}{K (\text{muz} + \nu + g x_-)} \right)^{1.5}} \right) \sinh' \left[\frac{0.707107 x_-}{\left(\frac{\nu (\text{muz} + g x_-)}{K (\text{muz} + \nu + g x_-)} \right)^{0.5}} \right] \right) / \\
& \quad \left(\cosh \left[\frac{0.707107 L}{\left(\frac{\nu (\text{muz} + g x_-)}{K (\text{muz} + \nu + g x_-)} \right)^{0.5}} \right] (\text{muz} + \nu + g x_-)^{1.5} \right) + \\
& \quad \left(1.41421 \left(\frac{1}{K \nu} \right)^{0.5} T (\text{muz} + g x_-)^{1.5} \left(-\frac{0.353553 x_- \left(\frac{2 g^2 \nu (\text{muz} + g x_-)}{K (\text{muz} + \nu + g x_-)^3} - \frac{2 g^2 \nu}{K (\text{muz} + \nu + g x_-)^2} \right)}{\left(\frac{\nu (\text{muz} + g x_-)}{K (\text{muz} + \nu + g x_-)} \right)^{1.5}} - \right. \right. \\
& \quad \left. \frac{0.707107 \left(-\frac{g \nu (\text{muz} + g x_-)}{K (\text{muz} + \nu + g x_-)^2} + \frac{g \nu}{K (\text{muz} + \nu + g x_-)} \right)}{\left(\frac{\nu (\text{muz} + g x_-)}{K (\text{muz} + \nu + g x_-)} \right)^{1.5}} + \frac{0.53033 x_- \left(-\frac{g \nu (\text{muz} + g x_-)}{K (\text{muz} + \nu + g x_-)^2} + \frac{g \nu}{K (\text{muz} + \nu + g x_-)} \right)^2}{\left(\frac{\nu (\text{muz} + g x_-)}{K (\text{muz} + \nu + g x_-)} \right)^{2.5}} \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \sinh' \left[\frac{0.707107 x_-}{\left(\frac{nu (muz+g x_-)}{K (muz+nu+g x_-)} \right)^{0.5}} \right] \Bigg/ \left(\cosh \left[\frac{0.707107 L}{\left(\frac{nu (muz+g x_-)}{K (muz+nu+g x_-)} \right)^{0.5}} \right] (muz + nu + g x_-)^{1.5} \right) + \\
& \left(1. L \left(\frac{1}{K nu} \right)^{0.5} T (muz + g x_-)^{1.5} \left(- \frac{g nu (muz + g x_-)}{K (muz + nu + g x_-)^2} + \frac{g nu}{K (muz + nu + g x_-)} \right) \right. \\
& \left. \left(\frac{0.707107}{\left(\frac{nu (muz+g x_-)}{K (muz+nu+g x_-)} \right)^{0.5}} - \frac{0.353553 x_- \left(- \frac{g nu (muz+g x_-)}{K (muz+nu+g x_-)^2} + \frac{g nu}{K (muz+nu+g x_-)} \right)}{\left(\frac{nu (muz+g x_-)}{K (muz+nu+g x_-)} \right)^{1.5}} \right) \right. \\
& \left. \cosh' \left[\frac{0.707107 L}{\left(\frac{nu (muz+g x_-)}{K (muz+nu+g x_-)} \right)^{0.5}} \right] \sinh' \left[\frac{0.707107 x_-}{\left(\frac{nu (muz+g x_-)}{K (muz+nu+g x_-)} \right)^{0.5}} \right] \right) \Bigg/ \\
& \left(\cosh \left[\frac{0.707107 L}{\left(\frac{nu (muz+g x_-)}{K (muz+nu+g x_-)} \right)^{0.5}} \right]^2 \left(\frac{nu (muz + g x_-)}{K (muz + nu + g x_-)} \right)^{1.5} (muz + nu + g x_-)^{1.5} \right) - \\
& \left(0.176777 L^2 \left(\frac{1}{K nu} \right)^{0.5} T (muz + g x_-)^{1.5} \left(- \frac{g nu (muz + g x_-)}{K (muz + nu + g x_-)^2} + \frac{g nu}{K (muz + nu + g x_-)} \right) \right)^2 \\
& \sinh \left[\frac{0.707107 x_-}{\left(\frac{nu (muz+g x_-)}{K (muz+nu+g x_-)} \right)^{0.5}} \right] \cosh'' \left[\frac{0.707107 L}{\left(\frac{nu (muz+g x_-)}{K (muz+nu+g x_-)} \right)^{0.5}} \right] \Bigg/ \\
& \left(\cosh \left[\frac{0.707107 L}{\left(\frac{nu (muz+g x_-)}{K (muz+nu+g x_-)} \right)^{0.5}} \right]^2 \left(\frac{nu (muz + g x_-)}{K (muz + nu + g x_-)} \right)^3 (muz + nu + g x_-)^{1.5} \right) + \\
& \left(1.41421 \left(\frac{1}{K nu} \right)^{0.5} T (muz + g x_-)^{1.5} \right. \\
& \left. \left(\frac{0.707107}{\left(\frac{nu (muz+g x_-)}{K (muz+nu+g x_-)} \right)^{0.5}} - \frac{0.353553 x_- \left(- \frac{g nu (muz+g x_-)}{K (muz+nu+g x_-)^2} + \frac{g nu}{K (muz+nu+g x_-)} \right)}{\left(\frac{nu (muz+g x_-)}{K (muz+nu+g x_-)} \right)^{1.5}} \right)^2 \right. \\
& \left. \sinh'' \left[\frac{0.707107 x_-}{\left(\frac{nu (muz+g x_-)}{K (muz+nu+g x_-)} \right)^{0.5}} \right] \right) \Bigg/ \left(\cosh \left[\frac{0.707107 L}{\left(\frac{nu (muz+g x_-)}{K (muz+nu+g x_-)} \right)^{0.5}} \right] (muz + nu + g x_-)^{1.5} \right)
\end{aligned}$$

In[56]:=