

# Regular Operations and Closure Proofs

Sipser 1.2 (pages 47-63)

# Regular languages are closed under:

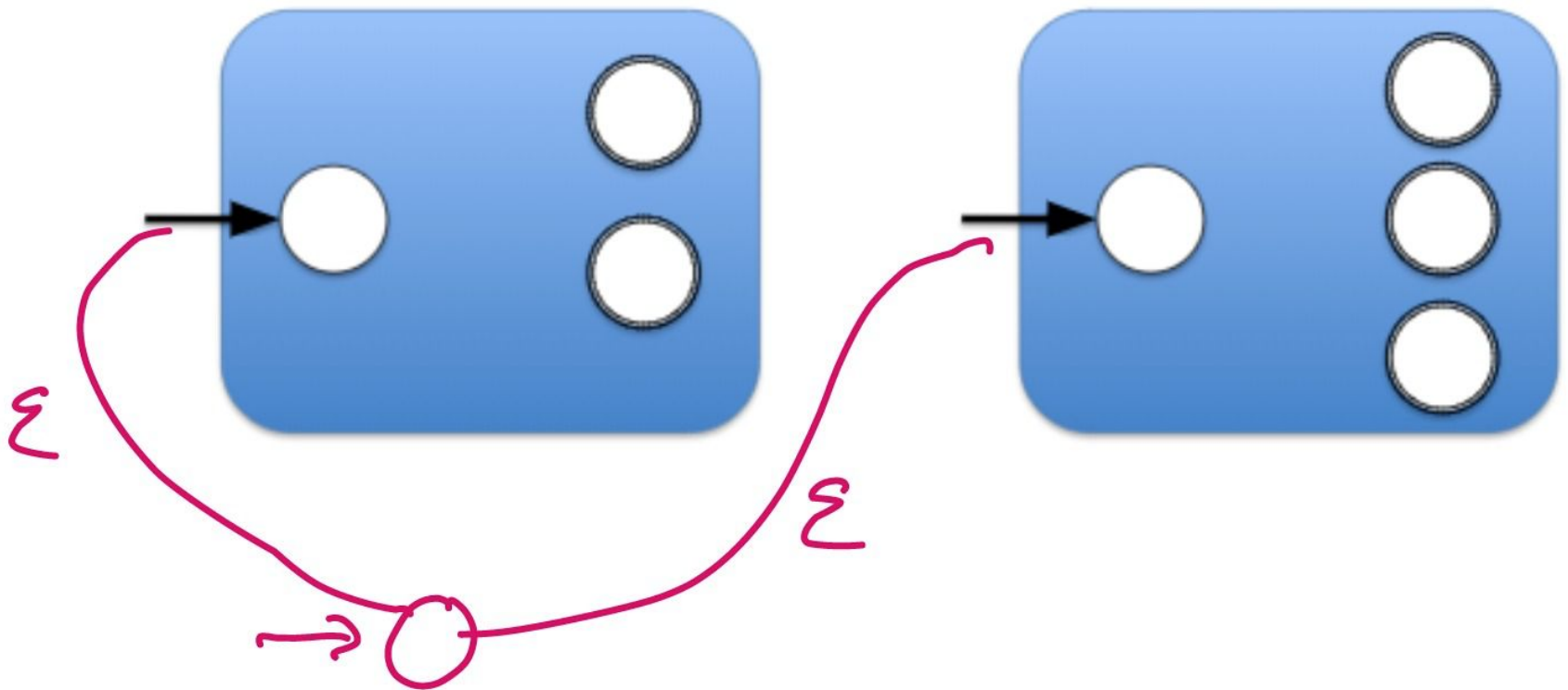
- complement
- **union**
- intersection
- **concatenation**
- **star**

# a sample proof

LaTeX files on the web site

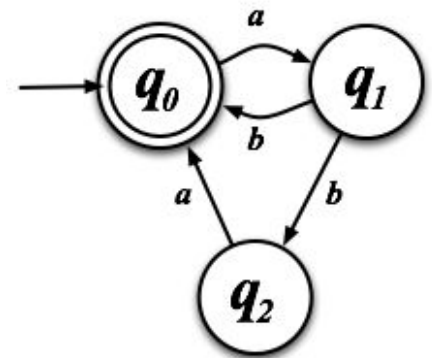
# Your turn...

closure under union!



# NFA

- A **nondeterministic finite automaton (NFA)** is a 5-tuple  $(Q, \Sigma, \delta, q_0, F)$ , where
  - $Q$  is a finite set called the **states**
  - $\Sigma$  is a finite set called the **alphabet**
  - $\delta: Q \times \Sigma^* \rightarrow P(Q)$  is the **transition function**
  - $q_0 \in Q$  is the **start state**
  - $F \subseteq Q$  is a set of **accept states**
- In-class exercise:



# NFA computation

- Let  $N=(Q, \Sigma, \delta, q_0, F)$  be a NFA and let  $w$  be a string over the alphabet  $\Sigma$
- Then  $N$  **accepts**  $w$  if
  - $w$  can be written as  $w_1w_2w_3...w_m$  with each  $w_i \in \Sigma$  and
  - There exists a sequence of states  $s_0, s_1, s_2, \dots, s_m$  exists in  $Q$  with the following conditions:

1.  $s_0 = q_0$
2.  $s_{i+1} \in \delta(s_i, w_{i+1})$  for  $i = 0, \dots, m-1$
3.  $s_m \in F$

