## Math 10350 - Example Set 02A Quadratic Functions: Section 1.6 Basic Exponential Equations: Section 1.6

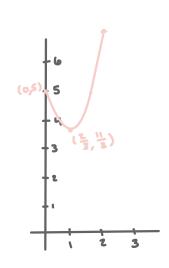
1. (Completing the Square Review) A particle moving in a straight line has position in meters, measured from a fixed point **O** on the straight line, at time t seconds is given by

$$s(t) = 5 - 4t + 3t^2$$

- (i) Sketch the graph of s(t). (ii) Find the time at which the particle is **closest** to the point **O**. (iii) How far can the particle be from the point **O**?
- **2.** (Sect 1.6) Solve the following equations: (a)  $4^x = \frac{1}{8}$ ; (b)  $3 \cdot 9^{x+1} = 81^x$ .
- 1. s(t) is the distance from the point 0, there is no gaurantee that the particle goes through O i.e. sits may never be 0

(i) Sketch  

$$s(t) = A(x-h)^2 + K$$
  
 $s(t) = 3t^2 - 4t + 5$   
 $s(t) = 3(t^2 - \frac{4}{3}t) + 5$   
 $b = -\frac{4}{3}; (\frac{1}{2}b)^2 = (-\frac{4}{6})^2 = (-\frac{2}{3})^2$   
 $s(t) = 3(t^2 - \frac{4}{3}t + \frac{4}{9} - \frac{4}{9}) + 5$   
 $= 3(t^2 - \frac{4}{3}t + \frac{4}{9}) - \frac{4}{3} + \frac{15}{3}$   
 $s(t) = 3(t - \frac{2}{3})^2 + \frac{11}{3}$   
 $(h, K) = (\frac{2}{3}, \frac{11}{3})$ 



(ii) minimum distance <1+>= distance minimum = vertex I meters away from 0 at time 3 seconds

(iii) maximum distance there is no maximum

note: parabolas have a min or a max not both

2. Solve the following equations:

(a) 
$$4^{x} = \frac{1}{8}$$
  
 $(2^{2})^{x} = (2)^{-3}$   
 $2^{2x} = 2^{-3}$   
 $2x = -3$   
 $x = -\frac{3}{2}$ 

eventually: (b)  $3 \cdot q^{x+1} = 81^x$  eventually:  $(2^2)^x = (2)^{-3}$   $\log_4 4^x = \log_4 \frac{1}{8}$   $3 \cdot (3^2)^{x+1} = (3^4)^x$   $\log_9 (3 \cdot q^{x+1}) = (3^4)^x$   $\log_$ 

eventually: loga(3.9x+1)= loga(92x) loga(3)+loga(9x+1)=loga(92x)