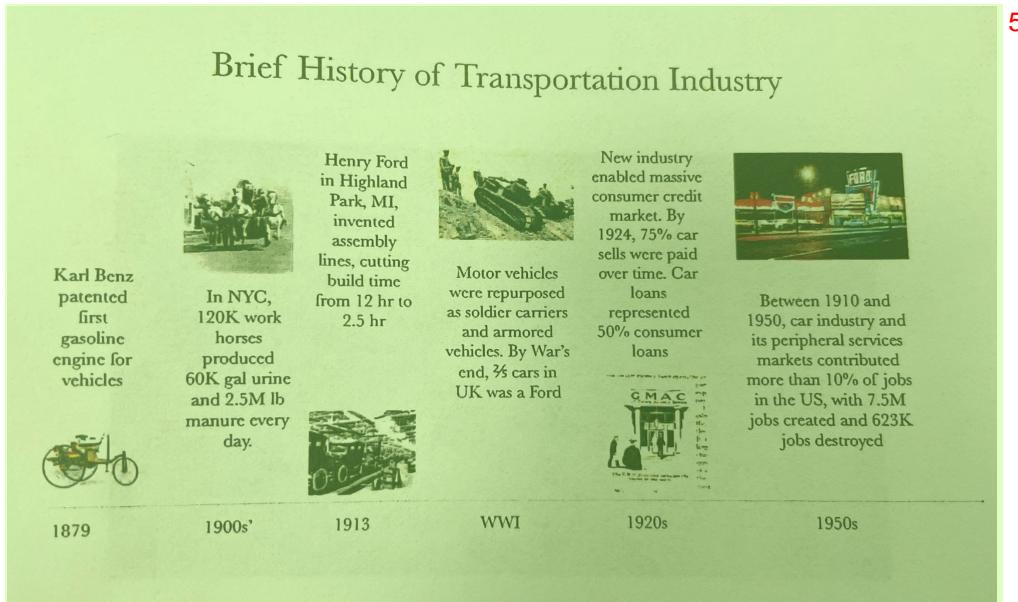


# Autonomous Driving<sup>1</sup>

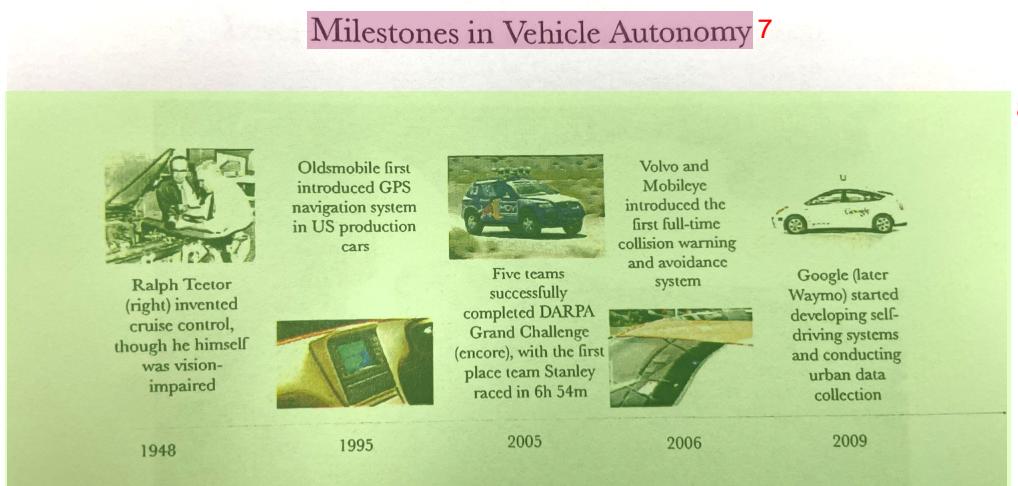
## Intro to Autonomous Driving<sup>2</sup>

(See slides for History of the Transportation Industry + Milestones in Vehicle Autonomy)<sup>3</sup>

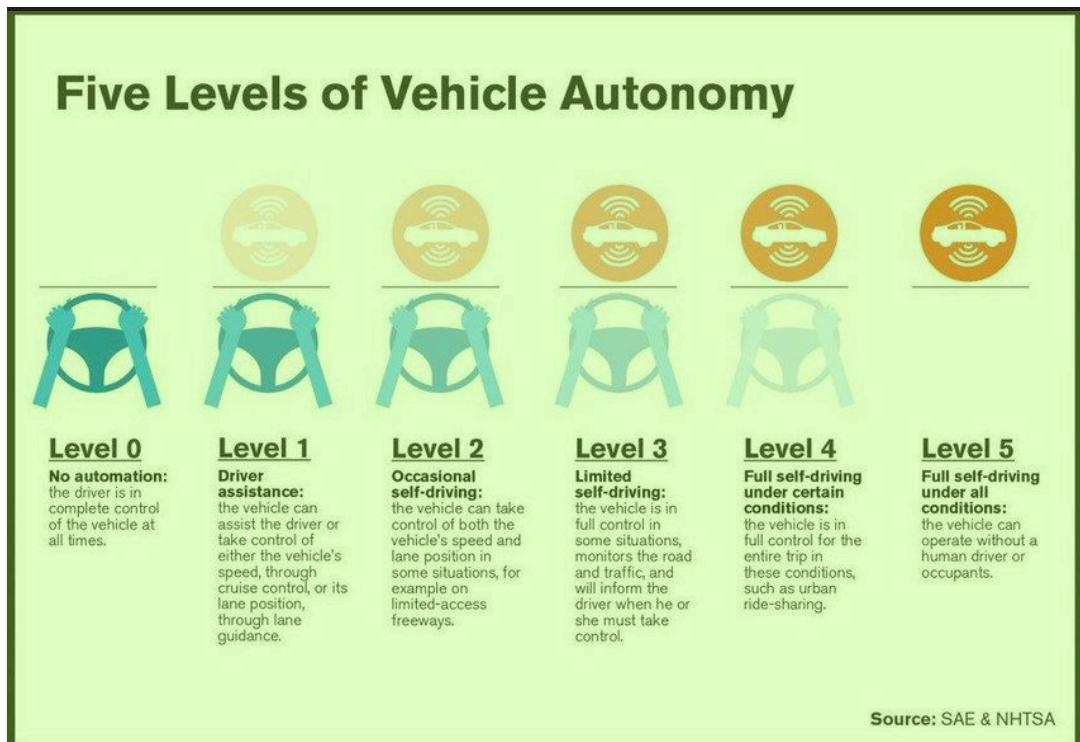
## Brief History of the Transportation Industry<sup>4</sup>



## Milestones in Vehicle Autonomy<sup>6</sup>



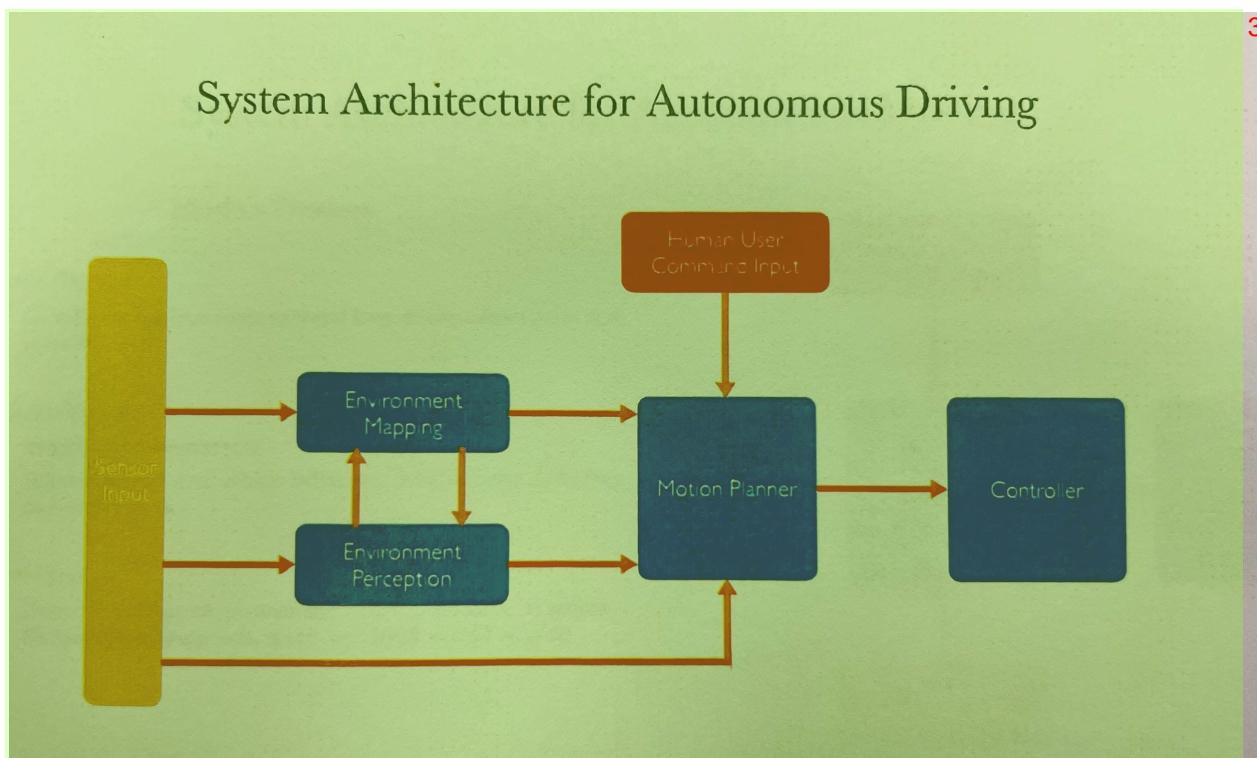
# Five Levels of Vehicle Autonomy



- **Lvl 0: no automation** 2
  - The human driver is fully in control
- **Lvl 1: driver assistance** 3
  - Alerts the driver to dangers, or intervenes briefly by performing simple maneuver 4
  - E.g. cruise control
  - E.g. automatic reverse braking
- **Lvl 2: supervised occasional self-driving** 5
  - The human still has to sit in the car
  - Most of the time the human driver is in control
  - In some cases the car can take control and drive autonomously
  - E.g. it parks the car while you are in the driver's seat
- **Lvl 3: limited self-driving** 6
  - → The vehicle is in full control in some situations
  - Most of the time the car can drive autonomously
  - BUT the driver will have to take control of the car at some point
  - E.g. the car can go park
- **Lvl 4: full self-driving under certain conditions** 7
  - Conditions → usually = approved driving within certain areas
  - There is no wheel, since there does not have to be a driver
  - BUT it is geofenced → the car can only do autonomous driving in an approved area
  - E.g. waymo
- **Lvl 5: full self-driving** 9

- The car can use autonomous driving to travel anywhere with no human intervention 1

## System Architecture for Autonomous Driving 2



For ROAR competition

- NO environment perception + NO human user command input 4

### Sensor Input 5

#### - Spatial Sensing: 6

- Short distance: ultrasound 7
- Midrange distance: 3D depth camera + LIDAR
- Long Distance: RGB Camera

#### - Global Position: GPS System 8

#### - Vehicle State Sensing: 9

- Motor speed sensor 10
- Wheel speed sensor
- Steering servo sensor
- Inertial measurement unit (IMU)

### Environment Mapping and Perception 11

- Environment Mapping: 12
  - 3D localization

- Road condition mapping: road, scenes, lanes 1
- Environment Perception: 2
  - Object detection & recognition 3
  - Object tracking

## Motion Planner 4

- Mission Planner 5
  - Calculating the best route to travel long distance from point A to point B 6
  - E.g. Turn to get to destination
- Behavior Planner 7
  - Vehicle safety monitoring
  - Determines real-time vehicle behaviors: overtake, stop, following, on/off ramp, etc.
  - E.g. How the vehicle will turn (slow down, steer, etc.)
- Local Planner 9
  - Based on the mission planner and behavior planner – Sets targets for immediate waypoints, speed, acceleration, and steering
  - E.g. Step by step how to turn from the vehicle's current position

## Controller 11

- Longitudinal (Speed) Control 12
  - Control vehicle motor's speed and acceleration
  - Equivalent to driver adjusting acceleration and braking
- Lateral (Steering) Control
  - Control vehicle steering and orientation
  - Equivalent to driver adjusting the steering wheel
- Popular control algorithms 13
  - Pure Pursuit Control 14
  - PID (Proportional-Integral-Derivative) Control
  - MPC (Model-Predictive Control)

## PID Control 15

A PID (Proportional-Integral-Derivative) controller is a control system that uses feedback to 16 regulate process variables by continuously adjusting the output to match a desired setpoint.

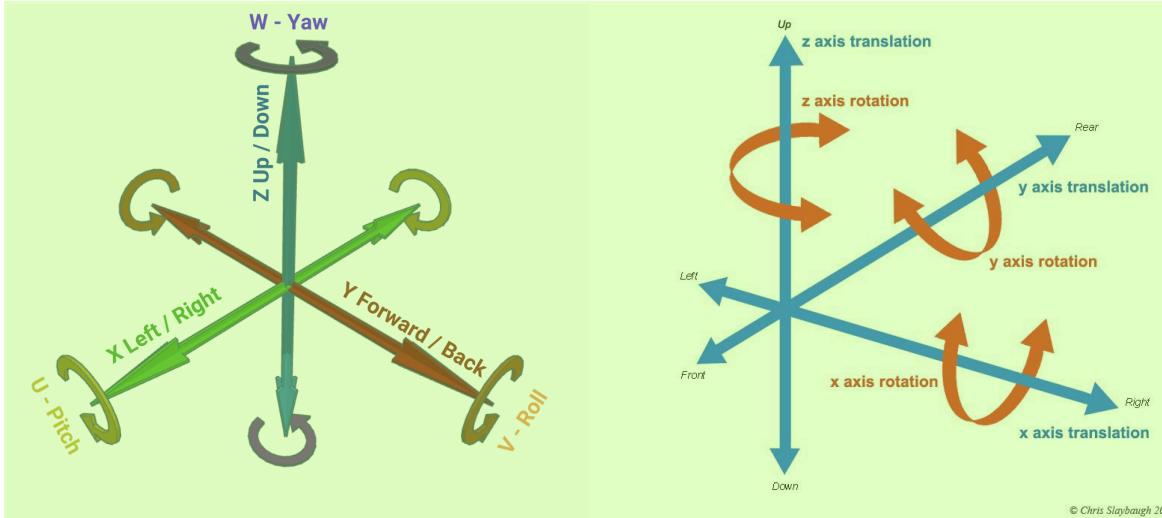
- Drive → just means to change the **state** of some system 17

## Modeling Robot Kinematics in DoF 18

- A rigid-body motion has 6 **degrees of freedom** in 3D space 19
  - $(x, y, z, \alpha, \beta, \gamma)$

- Note: going back & forth → only 1 degree of freedom (bc its moving along one axis) 1
- $\alpha, \beta, \gamma \rightarrow$  represent turning along each x, y, z axis 2
  - Represents: pan, tilt, roll
- Note: turning right & left is similarly only 1 degree of freedom (bc its turning along one axis) 3

#### Six axes of translation and rotation 4



5

- Robots that are modeled as rigid body and have 6 DoF: 6

- Quad-rotor helicopters 7
- Fixed-wing airplanes
- Underwater vehicles

- Q: How many DoF does BB-8 or R2D2 have? → 5 (everything except flying/jumping up) 8
- A rolling ball on the surface has five DoF

- Planar Movement: (x, y) 9
- Planar Rotation:  $\gamma$
- Body Pitch:  $\beta$
- Body Roll:  $\alpha$

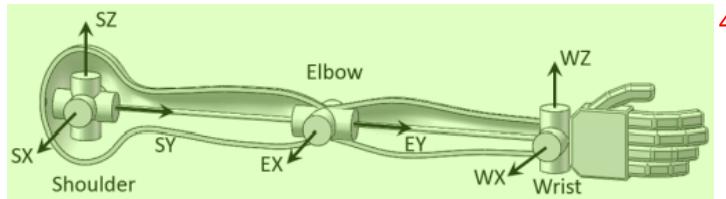


1

- Q: How many DoF of the human arm? 2

- 3 DoF at the Shoulder 3
- 2 DoF at the Elbow
- 2 DoF at the Wrist

-  $\Rightarrow$  Total 7 DoF



4

Figure 1. The DOF configuration of the humanoid arm 5

TABLE I. THE RANGE OF MOTION OF EACH DOF

## Four-Wheel Ground Vehicle Model<sup>6</sup>

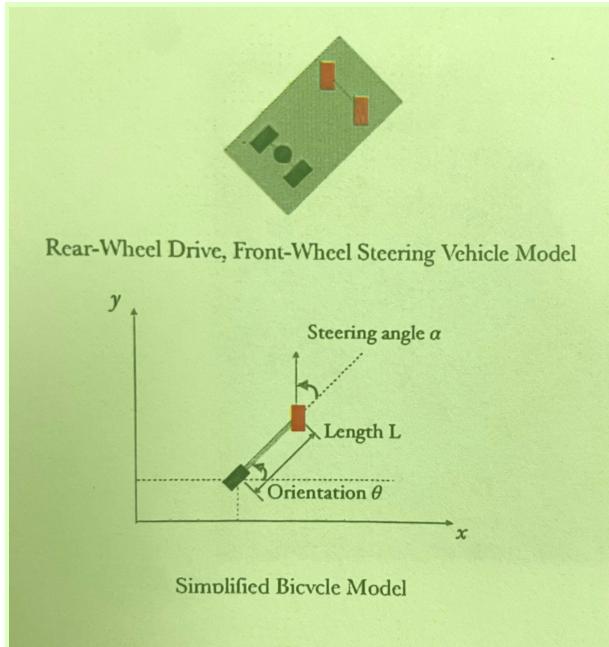
### Basic Four-Wheel Vehicle Model 7

- Driving wheels at the rear 8
- Steering wheels at the front
- 3 DoF constrained on the ground surface:  $(x, y, \theta)$ 
  - Can only pan right & left
- Having full control of all these DoF  $\rightarrow$  means we have achieved autonomous driving 9  
(Even tho the vehicle can tilt, like when going up a hill  $\rightarrow$  the vehicle itself isn't exactly controlling the tilt )

### Simplified Bicycle Model (simple way to think of vehicles' DoF) 10

- Four wheels simplified to two bicycle

- Vehicle center of mass at the center of the rear wheel:  $(x, y)$  1
- Wheel-to-wheel length:  $L$
- Orientation along the length- $L$  body:  $\theta$
- Steering angle:  $\alpha$



Note: 3

- Center of mass → at the rear wheel → so that's where we measure  $\theta$  from
    - $\alpha$  just represents where we steer from (unlike  $\theta$ , it's not a state/DoF)
  - Rear-wheel drive, front-wheel steering
    - → Bc the acc path of the turn is followed by the rear wheels, while the front wheels are free to turn (bc of steering angle  $\alpha$ )
- 4

## Kinematic Equations for Simplified Bicycle Model 5

Moving forward:

1

## Kinematic Equations for Simplified Bicycle Model

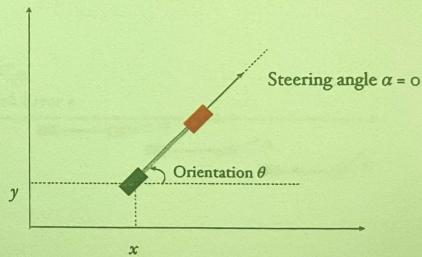
Assume steering angle  $\alpha$  and forward moving distance  $d$ ,  
solve new vehicle position:  $(x', y', \theta')$

- When  $\alpha$  is zero or very small

$$x' = x + d \cos \theta$$

$$y' = y + d \sin \theta$$

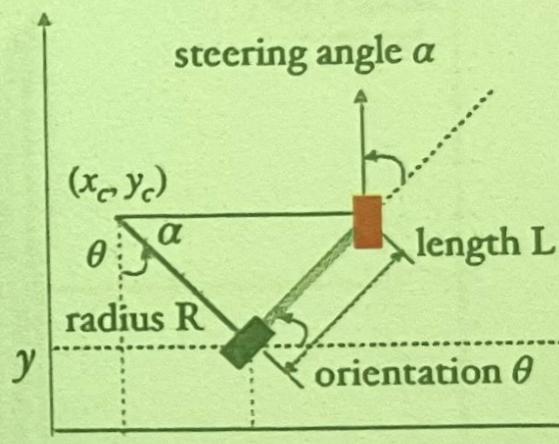
$$\theta' = \theta \% 2\pi$$



- $d$  is total distance ( $d = vt$ ) 2
- When  $\alpha$  is zero or very small: 3
  - $x' = x + d \cos \theta$  4
  - $y' = y + d \sin \theta$
  - $\theta' = \theta \% 2\pi$
- The red front wheels → shows new position  $x', y', \theta'$  5

## Turning: 6

7



• When  $\alpha$  is significant <sup>1</sup>

- Turning radius:  $R = \frac{L}{\tan \alpha}$  <sup>2</sup>
- Angular velocity:  $\dot{\theta} = \frac{v}{R}$
- Turn (radian):  $\beta = \frac{vt}{R} = \frac{d}{R}$

- Bc of the turning radius equation → longer vehicles → have to move their wheels further away to make a big turn
  - If  $\alpha$  is big (you turn ur wheel a lot) → you can make a small turn
- $\alpha \rightarrow$  static
- $\beta \rightarrow$  represents how much you turn (not static, increases as you keep traveling through the turn)
  - $\beta$  is the total travel distance/R

• Rotation center  $(x_c, y_c)$ : <sup>4</sup>

$$x_c = x - R \sin \theta$$

$$y_c = y + R \cos \theta$$

- Just use trig <sup>5</sup>

• New coordinates  $(x', y', \theta')$  <sup>6</sup>

$$x' = x_c + R \sin(\theta + \beta)$$

$$y' = y_c - R \cos(\theta + \beta)$$

$$\theta' = (\theta + \beta) \% 2\pi$$

- Add  $\beta$  to  $\theta \rightarrow$  bc we are turning  $\beta$  (radians) <sup>7</sup>

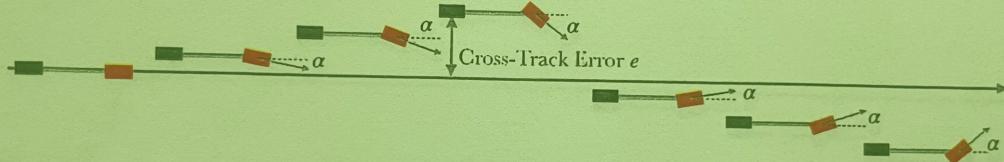
## PID Controller: Tracking Preset Trajectories <sup>8</sup>

- $K_p \rightarrow$  coefficient you choose

## Controller for Steering P<sup>1</sup>

2

### Controller for Steering: P



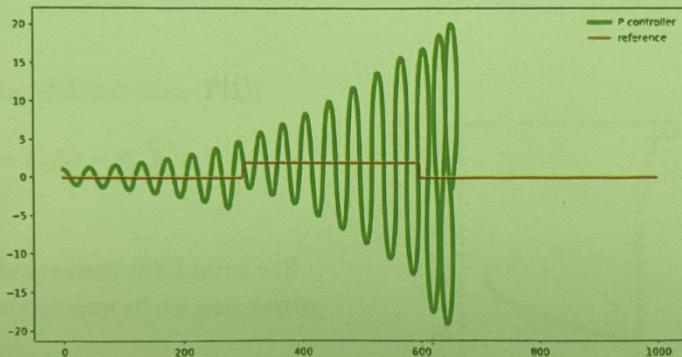
**Proportional (P):**  $\alpha = -K_p e$ , where  $e$  is also called the cross-track error (CTE)

- Multiply the error (the difference from where u want to be) → by a coefficient you choose (K<sub>p</sub>) to reduce the error

BUT problem: 4

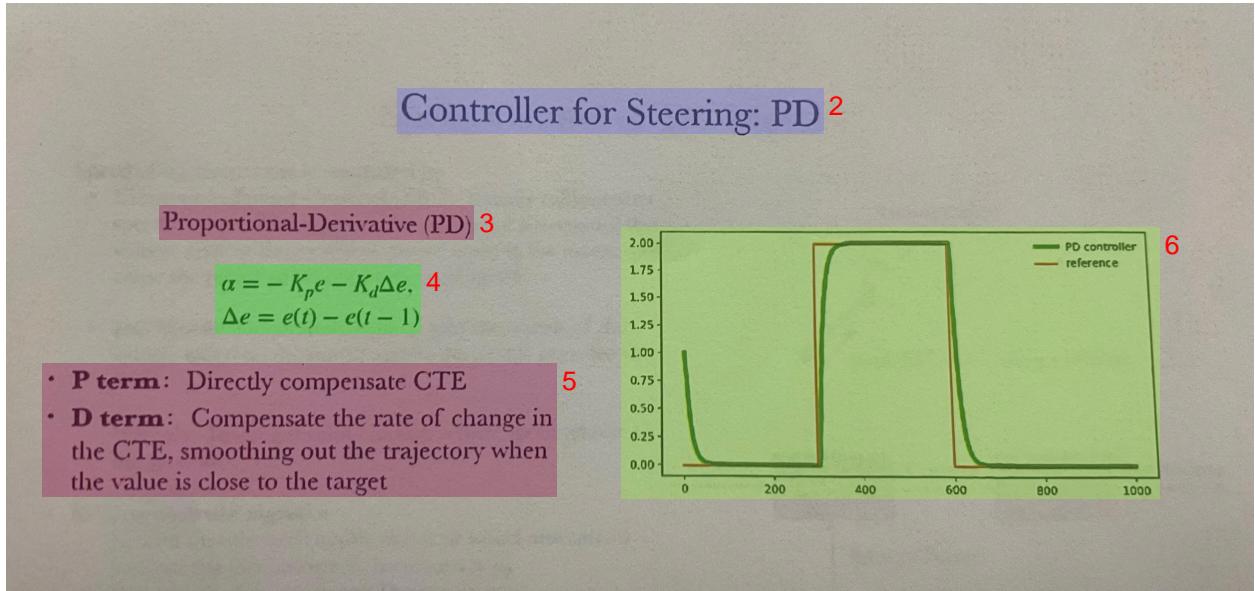
5

### Simulation Demo



P controller for tracking a trajectory leads to oscillation

## Controller for Steering PD<sup>1</sup>



- D for derivative <sup>7</sup>
- $\alpha \rightarrow$  takes into account the change in the  $K_p e$
  - **P term:** Directly compensates CTE (cross track error)
  - **D term:** Compensates the rate of change in the CTE, smoothing out the trajectory when the value is close to the target
    - I.e. If the error is decreasing rapidly, D control will reduce the corrective action, preventing overshoot.

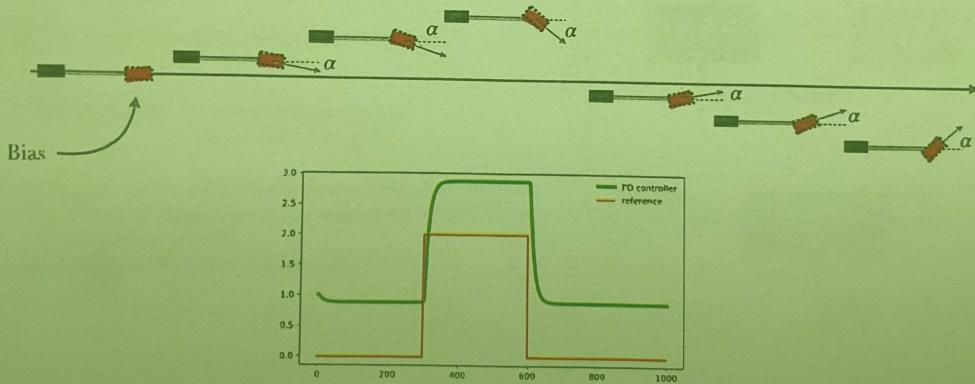
## Controller for Steering PID<sup>8</sup>

Problem: <sup>9</sup>

1

## Controller for Steering: PID

When estimating CTE, possible that systematic error exists



- Systematic errors (like car misalignment) arise → shown by the bias 2
- If the car is slightly misaligned → the error will accumulate over time

SO:

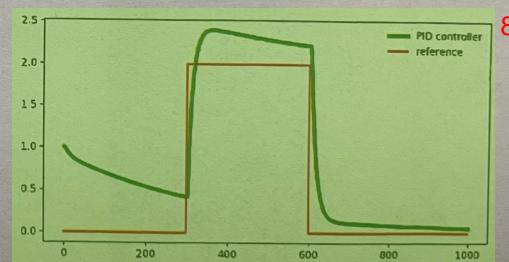
## Controller for Steering: PID 3

Proportional-Integral-Derivative (PID) 4

$$\alpha = -K_p e - K_d \Delta e - K_i \sum e \quad 5$$

• **I term:** If system bias exists, the I term will 6 compensate based on the sum of all past errors

• PID Controller Summary: 7  
 • Input: error signal  $e$   
 • Control coefficients:  $K_p$ ,  $K_d$ ,  $K_i$



- I for integral
- Mechanism: The integral term accumulates the error over time, meaning that even a small, persistent error will add up.
- As the integral of the error grows (i.e. if we've been going to the wrong dir for a long time), it produces an increasing corrective action until the error is driven to zero.

9

- Result: This helps to eliminate the steady-state error that remains with PD control alone.

## Speed Control of DC Motor<sup>1</sup>

2

### Speed Control of DC Motor

- Speed of an electric car is controlled by
  - **Electronic Speed Control (ESC):** Usually calibrated to specific motor, ESC converts throttle signal  $u$  to control the voltage and/or duty-cycle of power input to the motor, and cause the motor to output torque and speed.
- **DC Motor:** Generates torque to spin the wheels of the vehicle based on the power and its duty-cycle provided by ESC
- **Wheels:** Turning revolutions into vehicle speed relative to the ground
- **Setting throttle signal  $u$** 
  - Neutral throttle level:  $u_0$  (No motor or wheel movement)
  - Increase the forward speed: Increase  $u > u_0$
  - Decrease the forward speed: Decrease  $u < u_0$
  - Reverse the car: Decrease  $u < u_0$

## Cruise Control using PID Algorithm<sup>3</sup>

4

### Cruise Control using PID Algorithm

- Assume there exists systematic error in ESC calibration or environmental error caused by slippery ground conditions:<sup>5</sup>
  - Given a reference speed  $v_0$  and measured speed  $v'$ :<sup>6</sup>  
 $e = v_0 - v'$
  - A PID controller for maintaining speed  $v_0$ :<sup>7</sup>  
 $u = K_p e + K_d \Delta e + K_i \sum e$

**P:** Reduce the response time for error magnitude in speed  
**I:** Reduce the steady state error, making motor speed close to the reference speed  
**D:** Reduce settling time and overshoot

- PID can applied to controlling anything<sup>10</sup>
- Very simple calculations

## PID\_Control.py<sup>1</sup>

```
## This is course material for Introduction to Modern Artificial Intelligence  
## Example code: PID_control.py  
## Author: Allen Y. Yang  
##  
## (c) Copyright 2020. Intelligent Racing Inc. Not permitted for commercial use
```

```
import random  
import numpy as np  
import matplotlib.pyplot as plt  
  
class Vehicle2D(object):  
    def __init__(self, length=10.0):  
        """  
        Creates 2D vehicle model and initializes location (0,0) & orientation 0.  
        """  
        self.x = 0.0  
        self.y = 0.0  
        self.orientation = 0.0  
        self.length = length  
        self.steering_noise = 0.0  
        self.distance_noise = 0.0  
        self.steering_drift = 0.0  
  
    def set(self, x, y, orientation):  
        """  
        Sets the vehicle coordinates and orientation.  
        """  
        self.x = x  
        self.y = y  
        self.orientation = orientation % (2.0 * np.pi)  
  
    def set_noise(self, steering_noise, distance_noise):  
        """  
        Sets the noise parameters.  
        """  
        # makes it possible to change the noise parameters  
        self.steering_noise = steering_noise  
        self.distance_noise = distance_noise  
  
    def set_steering_drift(self, drift):  
        """
```

2

3

```

Sets the systematical steering drift parameter
"""

self.steering_drift = drift

def move(self, steering, distance, tolerance=0.001, max_steering_angle=np.pi /
4.0):
    """
    steering = front wheel steering angle, limited by max_steering_angle(max 90
degree)
    distance = total distance driven, most be non-negative
    """

    if max_steering_angle > np.pi/2:
        raise ValueError("Max steering angle cannot be greater than 90-degree.")

    if steering > max_steering_angle:
        steering = max_steering_angle
    if steering < -max_steering_angle:
        steering = -max_steering_angle
    if distance < 0.0:
        distance = 0.0

    # apply noise
    steering2 = random.gauss(steering, self.steering_noise)
    distance2 = random.gauss(distance, self.distance_noise)

    # apply steering drift
    steering2 += self.steering_drift

    # Execute motion
    turn = np.tan(steering2) * distance2 / self.length

    if abs(turn) < tolerance:
        # approximate by straight line motion
        self.x += distance2 * np.cos(self.orientation)
        self.y += distance2 * np.sin(self.orientation)
        self.orientation = (self.orientation + turn) % (2.0 * np.pi)
    else:
        # approximate bicycle model for motion
        radius = distance2 / turn
        cx = self.x - (np.sin(self.orientation) * radius)
        cy = self.y + (np.cos(self.orientation) * radius)
        self.orientation = (self.orientation + turn) % (2.0 * np.pi)

```

```

        self.x = cx + (np.sin(self.orientation) * radius)
        self.y = cy - (np.cos(self.orientation) * radius)

    def compute_error(self, track):
        min_distance = float('inf')
        for i in range(len(track)):
            distance = np.linalg.norm(np.array([self.x, self.y]) - np.array(track[i]))
            if distance < min_distance:
                min_distance = distance
            error = self.y - track[i][1] # This error only assumes cte based on
y-axis. Further extension is possible

        return error

    def run_PID(self, track, K_p, K_d, K_i, n=500, speed=1.0):
        x_trajectory = []
        y_trajectory = []

        prev_error = self.compute_error(track)
        cumulative_error = 0
        for _ in range(n):
            current_error = self.compute_error(track)
            cumulative_error += current_error
            diff = current_error - prev_error
            prev_error = current_error
            steer = -K_p * current_error - K_d * diff - K_i*cumulative_error
            self.move(steer, speed)
            x_trajectory.append(self.x)
            y_trajectory.append(self.y)

        return x_trajectory, y_trajectory

    def __repr__(self):
        return '[x=%.5f y=%.5f orient=%.5f]' % (self.x, self.y, self.orientation)

vehicle = Vehicle2D()
vehicle.set(0, 1, 0)
vehicle.set_steering_drift(10/180.*np.pi)

track_length = 1000
targets = []; track_x = []; track_y = []
for i in range(300):

```

```

targets.append([i, 0]); track_x.append(i); track_y.append(0)
for i in range(300,600):
    targets.append([i, 2]); track_x.append(i); track_y.append(2)
for i in range(600,track_length):
    targets.append([i, 0]); track_x.append(i); track_y.append(0)

# Set the parameters for K_p, K_d, and K_i
K_p = 0.2; K_d = 3; K_i = 0.0005
x_trajectory, y_trajectory = vehicle.run_PID(targets, K_p, K_d, K_i, track_length)
n = len(x_trajectory)

controller_legend = 'PID controller' if K_p!=0 and K_d!=0 and K_i!=0 else 'PD
controller'\
    if K_p!=0 and K_d!=0 else 'P controller' if K_p!=0 else 'unknown controller'
fig, ax1 = plt.subplots(1, 1, figsize=(8, 4))
ax1.plot(x_trajectory, y_trajectory, 'g', linewidth=4, label=controller_legend)
ax1.plot(track_x, track_y, 'r', label='target')
plt.legend()
plt.show()

```

## Example Cartpole Exercise<sup>2</sup>

```

## This is course material for Introduction to Modern Artificial Intelligence
## Example code: cartpole_dqn.py
## Author: Allen Y. Yang
##
## (c) Copyright 2020-2024. Intelligent Racing Inc. Not permitted for commercial use

```

```

# Please make sure to install openAI gym module 4
# pip install gym==0.17.3
# pip install pyglet==1.5.29

```

```

import gym 5
import time

# PID control parameters 6
Kp = 1.0 # Proportional gain
Ki = 0.0 # Integral gain
Kd = 0.5 # Derivative gain

# Environment settings

```

```

EPISODES = 10 # Number of episodes

done = False
while not done:
    env = gym.make('CartPole-v1')
    batch_size = 32

    # env.step(1) goes right
    # env.step(0) goes left
    K_p = 1; K_i = 0; K_d = 0.5; n=500; speed=1.0; cumulative_error = 0

    for e in range(EPISODES):
        state = env.reset()
        i, previous_state = 0, 0

        for _ in range(n):
            env.render()
            current_error = state[2]
            cumulative_error += current_error
            prev_error = previous_state
            diff = current_error - prev_error

            action = K_p * current_error + K_d * diff + K_i*cumulative_error

            control_signal = K_p * current_error + K_d * diff + K_i*cumulative_error

            # if control_signal > 0:
            #     action = 1
            # else:
            #     action = 0
            action = 1 if control_signal > 0 else 0

            next_state, _, done, _ = env.step(action)
            # env.step(action) returns four values: next state, reward, a boolean
            indicating if the episode has ended, and some extra info
            # here we just use "_" placeholders to ignore the reward and extra info and
            unpack the next_state and the done boolean
            env.render()

            previous_state = current_error
            state = next_state

```

```
if done:  
    done = False  
    break
```